

Software Requirements Specification for Solar Water Heating Systems Incorporating PCM

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1 Reference Material

This section records information for easy reference.

1.1 Table of Units

The unit system used throughout is SI (Système International d'Unités). In addition to the basic units, several derived units are also used. For each unit, the [Table of Units](#) lists the symbol, a description, and the SI name.

Table 1: Table of Units

Symbol	Description	SI Name
°C	temperature	centigrade
J	energy	joule
kg	mass	kilogram
m	length	metre
s	time	second
W	power	watt

1.2 Table of Symbols

The symbols used in this document are summarized in the [Table of Symbols](#) along with their units. The choice of symbols was made to be consistent with the heat transfer literature and with existing documentation for solar water heating systems. The symbols are listed in alphabetical order. For vector quantities, the units shown are for each component of the vector.

Table 2: Table of Symbols

Symbol	Description	Units
A_C	Heating coil surface area	m^2
A_C^{\max}	Maximum surface area of coil	m^2
A_{in}	Surface area over which heat is transferred in	m^2
A_{out}	Surface area over which heat is transferred out	m^2
A_P	Phase change material surface area	m^2
A_{tol}	Absolute tolerance	—
AR	Aspect ratio	—

Continued on next page

Table 2: Table of Symbols (Continued)

Symbol	Description	Units
AR_{\max}	Maximum aspect ratio	—
AR_{\min}	Minimum aspect ratio	—
C	Specific heat capacity	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
C^{L}	Specific heat capacity of a liquid	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
C^{S}	Specific heat capacity of a solid	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
C^{V}	Specific heat capacity of a vapour	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
C_{P}^{L}	Specific heat capacity of PCM as a liquid	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
C_{P}^{S}	Specific heat capacity of PCM as a solid	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
C_{tol}	Relative tolerance for conservation of energy	—
C_{W}	Specific heat capacity of water	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
C_{W}^{\max}	Maximum specific heat capacity of water	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
C_{W}^{\min}	Minimum specific heat capacity of water	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
$C_{\text{P}}^{\text{L}}_{\max}$	Maximum specific heat capacity of PCM as a liquid	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
$C_{\text{P}}^{\text{L}}_{\min}$	Minimum specific heat capacity of PCM as a liquid	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
$C_{\text{P}}^{\text{S}}_{\max}$	Maximum specific heat capacity of PCM as a solid	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
$C_{\text{P}}^{\text{S}}_{\min}$	Minimum specific heat capacity of PCM as a solid	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
D	Diameter of tank	m
E	Sensible heat	J
E_{P}	Change in heat energy in the PCM	J
E_{W}	Change in heat energy in the water	J
$E_{\text{P}_{\text{melt}}}^{\text{init}}$	Change in heat energy in the PCM at the instant when melting begins	J
g	Volumetric heat generation per unit volume	$\frac{\text{W}}{\text{m}^3}$
H_{f}	Specific latent heat of fusion	$\frac{\text{J}}{\text{kg}}$
$H_{\text{f}_{\max}}$	Maximum specific latent heat of fusion	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
$H_{\text{f}_{\min}}$	Minimum specific latent heat of fusion	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
h	Convective heat transfer coefficient	$\frac{\text{W}}{\text{m}^2^\circ\text{C}}$
h_{C}	Convective heat transfer coefficient between coil and water	$\frac{\text{W}}{\text{m}^2^\circ\text{C}}$

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Table 2: Table of Symbols (Continued)

Symbol	Description	Units
h_C^{\max}	Maximum convective heat transfer coefficient between coil and water	$\frac{W}{m^2 \cdot ^\circ C}$
h_C^{\min}	Minimum convective heat transfer coefficient between coil and water	$\frac{W}{m^2 \cdot ^\circ C}$
h_{\min}	Minimum thickness of a sheet of PCM	m
h_P	Convective heat transfer coefficient between PCM and water	$\frac{W}{m^2 \cdot ^\circ C}$
h_P^{\max}	Maximum convective heat transfer coefficient between PCM and water	$\frac{W}{m^2 \cdot ^\circ C}$
h_P^{\min}	Minimum convective heat transfer coefficient between PCM and water	$\frac{W}{m^2 \cdot ^\circ C}$
L	Length of tank	m
L_{\max}	Maximum length of tank	m
L_{\min}	Minimum length of tank	m
m	Mass	kg
m_P	Mass of phase change material	kg
m_W	Mass of water	kg
$MINFRACT$	Minimum fraction of the tank volume taken up by the PCM	—
$\hat{\mathbf{n}}$	Unit outward normal vector for a surface	—
Q	Latent heat	J
Q_P	Latent heat energy added to PCM	J
q	Heat flux	$\frac{W}{m^2}$
q_C	Heat flux into the water from the coil	$\frac{W}{m^2}$
q_{in}	Heat flux input	$\frac{W}{m^2}$
q_{out}	Heat flux output	$\frac{W}{m^2}$
q_P	Heat flux into the PCM from water	$\frac{W}{m^2}$
\mathbf{q}	Thermal flux vector	$\frac{W}{m^2}$
R_{tol}	Relative tolerance	—
S	Surface	m^2
T	Temperature	$^\circ C$
ΔT	Change in temperature	$^\circ C$
T_{boil}	Boiling point temperature	$^\circ C$

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Table 2: Table of Symbols (Continued)

Symbol	Description	Units
T_C	Temperature of the heating coil	$^{\circ}\text{C}$
T_{env}	Temperature of the environment	$^{\circ}\text{C}$
T_{init}	Initial temperature	$^{\circ}\text{C}$
T_{melt}	Melting point temperature	$^{\circ}\text{C}$
$T_{\text{melt}}^{\text{P}}$	Melting point temperature for PCM	$^{\circ}\text{C}$
T_{P}	Temperature of the phase change material	$^{\circ}\text{C}$
T_{W}	Temperature of the water	$^{\circ}\text{C}$
t	Time	s
t_{final}	Final time	s
$t_{\text{final}}^{\text{max}}$	Maximum final time	s
$t_{\text{melt}}^{\text{final}}$	Time at which melting of PCM ends	s
$t_{\text{melt}}^{\text{init}}$	Time at which melting of PCM begins	s
t_{step}	Time step for simulation	s
V	Volume	m^3
V_{P}	Volume of PCM	m^3
V_{tank}	Volume of the cylindrical tank	m^3
V_{W}	Volume of water	m^3
η	ODE parameter related to decay rate	—
π	Ratio of circumference to diameter for any circle	—
ρ	Density	$\frac{\text{kg}}{\text{m}^3}$
ρ_{P}	Density of PCM	$\frac{\text{kg}}{\text{m}^3}$
$\rho_{\text{P}}^{\text{max}}$	Maximum density of PCM	$\frac{\text{kg}}{\text{m}^3}$
$\rho_{\text{P}}^{\text{min}}$	Minimum density of PCM	$\frac{\text{kg}}{\text{m}^3}$
ρ_{W}	Density of water	$\frac{\text{kg}}{\text{m}^3}$
$\rho_{\text{W}}^{\text{max}}$	Maximum density of water	$\frac{\text{kg}}{\text{m}^3}$
$\rho_{\text{W}}^{\text{min}}$	Minimum density of water	$\frac{\text{kg}}{\text{m}^3}$
τ	Dummy variable for integration over time	s
$\tau_{\text{P}}^{\text{L}}$	ODE parameter for liquid PCM	s
$\tau_{\text{P}}^{\text{S}}$	ODE parameter for solid PCM	s
τ_{W}	ODE parameter for water related to decay time	s

Continued on next page

Table 2: Table of Symbols (Continued)

Symbol	Description	Units
ϕ	Melt fraction	–
∇	Gradient	–

1.3 Abbreviations and Acronyms

Table 3: Abbreviations and Acronyms

Abbreviation	Full Form
A	Assumption
DD	Data Definition
GD	General Definition
GS	Goal Statement
IM	Instance Model
LC	Likely Change
ODE	Ordinary Differential Equation
PCM	Phase Change Material
PS	Physical System Description
R	Requirement
RHS	Right-Hand Side
RefBy	Referenced by
Refname	Reference Name
SRS	Software Requirements Specification
SWHS	Solar Water Heating System
TM	Theoretical Model
UC	Unlikely Change
Uncert.	Typical Uncertainty

2 Introduction

Due to increasing costs, diminishing availability, and negative environmental impact of fossil fuels, the demand is high for renewable energy sources and energy storage technology. Solar water heating systems incorporating phase change material (PCM) use a renewable energy source and provide a novel way of storing energy. Solar water heating systems incorporating

PCM improve over the traditional solar water heating systems because of their smaller size. The smaller size is possible because of the ability of PCM to store thermal energy as latent heat, which allows higher thermal energy storage capacity per unit weight.

The following section provides an overview of the Software Requirements Specification (SRS) for solar water heating systems incorporating PCM. The developed program will be referred to as Solar Water Heating System (SWHS) based on the original, manually created version of [SWHS](#). This section explains the purpose of this document, the scope of the requirements, the characteristics of the intended reader, and the organization of the document.

2.1 Purpose of Document

The primary purpose of this document is to record the requirements of SWHS. Goals, assumptions, theoretical models, definitions, and other model derivation information are specified, allowing the reader to fully understand and verify the purpose and scientific basis of SWHS. With the exception of [system constraints](#), this SRS will remain abstract, describing what problem is being solved, but not how to solve it.

This document will be used as a starting point for subsequent development phases, including writing the design specification and the software verification and validation plan. The design document will show how the requirements are to be realized, including decisions on the numerical algorithms and programming environment. The verification and validation plan will show the steps that will be used to increase confidence in the software documentation and the implementation. Although the SRS fits in a series of documents that follow the so-called waterfall model, the actual development process is not constrained in any way. Even when the waterfall model is not followed, as Parnas and Clements point out [5], the most logical way to present the documentation is still to “fake” a rational design process.

2.2 Scope of Requirements

The scope of the requirements includes thermal analysis of a single solar water heating tank incorporating PCM. This entire document is written assuming that the substances inside the solar water heating tank are water and PCM.

2.3 Characteristics of Intended Reader

Reviewers of this documentation should have an understanding of heat transfer theory from level 3 or 4 mechanical engineering and differential equations from level 1 and 2 calculus. The users of SWHS can have a lower level of expertise, as explained in [Sec:User Characteristics](#).

2.4 Organization of Document

The organization of this document follows the template for an SRS for scientific computing software proposed by [3], [7], [8], and [6]. The presentation follows the standard pattern of

presenting goals, theories, definitions, and assumptions. For readers that would like a more bottom up approach, they can start reading the **instance models** and trace back to find any additional information they require.

The **goal statements** are refined to the theoretical models and the **theoretical models** to the **instance models**. The instance models to be solved are referred to as **IM:eBalanceOnWtr**, **IM:eBalanceOnPCM**, **IM:heatEInWtr**, and **IM:heatEInPCM**. The instance models provide the ordinary differential equations (ODEs) and algebraic equations that model the solar water heating systems incorporating PCM. SWHS solves these ODEs.

3 General System Description

This section provides general information about the system. It identifies the interfaces between the system and its environment, describes the user characteristics, and lists the system constraints.

3.1 System Context

Fig:SysCon shows the system context. A circle represents an external entity outside the software, the user in this case. A rectangle represents the software system itself (SWHS). Arrows are used to show the data flow between the system and its environment.

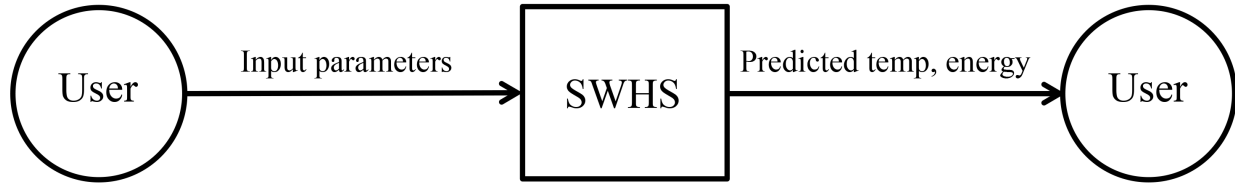


Figure 1: System Context

SWHS is mostly self-contained. The only external interaction is through the user interface. The responsibilities of the user and the system are as follows:

- User Responsibilities:
 - Provide the input data to the system, ensuring no errors in the data entry
 - Take care that consistent units are used for input variables
- SWHS Responsibilities:
 - Detect data type mismatch, such as a string of characters instead of a floating point number

- Determine if the inputs satisfy the required physical and software constraints
- Calculate the required outputs

3.2 User Characteristics

The end user of SWHS should have an understanding of undergraduate Level 1 Calculus and Physics.

3.3 System Constraints

There are no system constraints.

4 Specific System Description

This section first presents the problem description, which gives a high-level view of the problem to be solved. This is followed by the solution characteristics specification, which presents the assumptions, theories, and definitions that are used.

4.1 Problem Description

A system is needed to investigate the effect of employing PCM within a solar water heating tank.

4.1.1 Terminology and Definitions

This subsection provides a list of terms that are used in the subsequent sections and their meaning, with the purpose of reducing ambiguity and making it easier to correctly understand the requirements.

- Heat flux: The rate of thermal energy transfer through a given surface per unit time.
- Phase change material: A substance that uses phase changes (such as melting) to absorb or release large amounts of heat at a constant temperature.
- Specific heat capacity: The amount of energy required to raise the temperature of the unit mass of a given substance by a given amount.
- Thermal conduction: The transfer of heat energy through a substance.
- Transient: Changing with time.

4.1.2 Physical System Description

The physical system of SWHS, as shown in Fig:Tank, includes the following elements:

PS1: Tank containing water.

PS2: Heating coil at bottom of tank. (q_C represents the heat flux into the water from the coil.)

PS3: PCM suspended in tank. (q_P represents the heat flux into the PCM from water.)

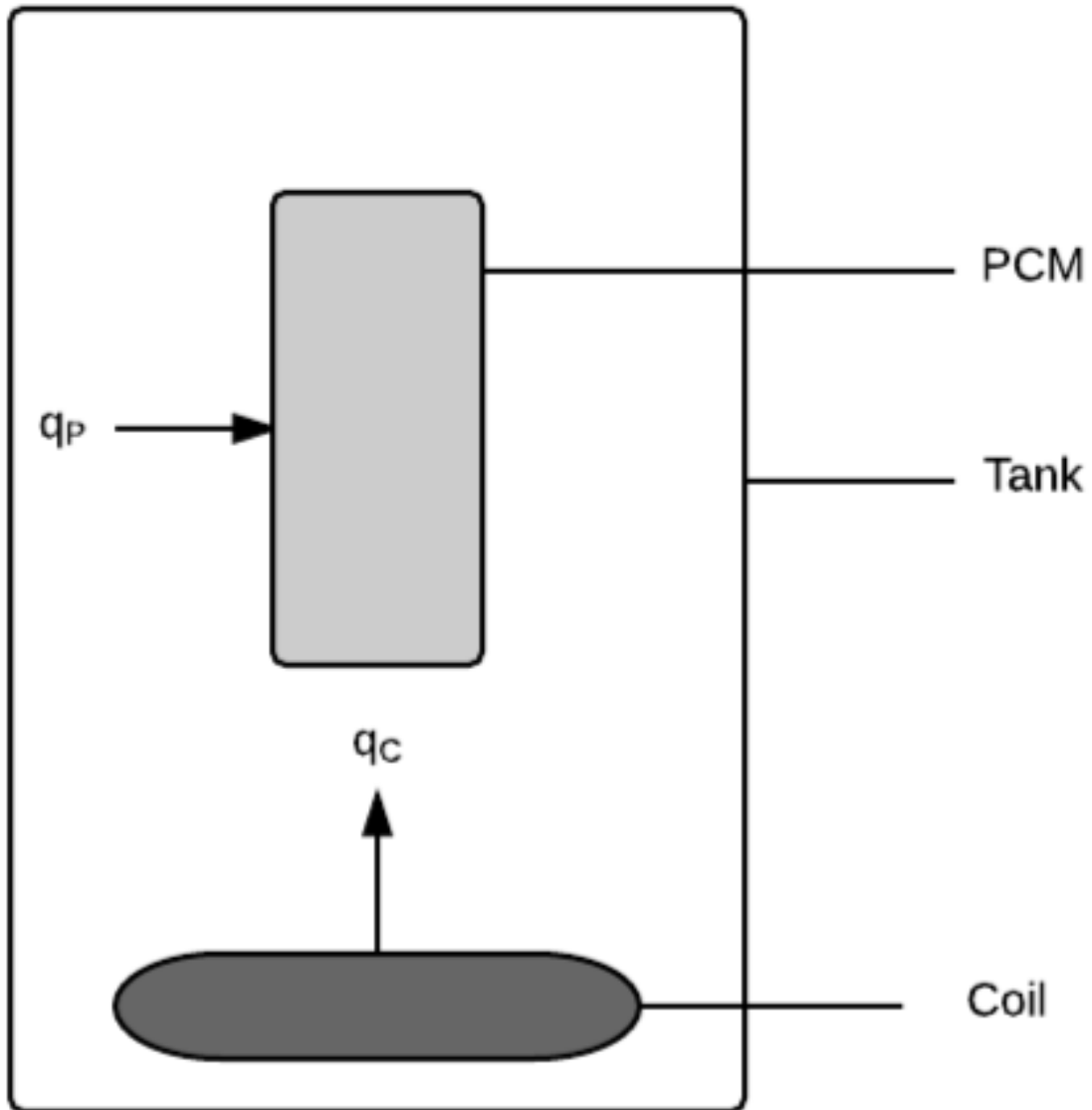


Figure 2: Solar water heating tank, with heat flux into the water from the coil of q_C and heat flux into the PCM from water of q_P

4.1.3 Goal Statements

Given the temperature of the heating coil, the initial conditions for the temperature of the water and the temperature of the phase change material, and the material properties, the goal statements are:

Predict-Water-Temperature: Predict the temperature of the water over time.

Predict-PCM-Temperature: Predict the temperature of the phase change material over time.

Predict-Water-Energy: Predict the change in heat energy in the water over time.

Predict-PCM-Energy: Predict the change in heat energy in the PCM over time.

4.2 Solution Characteristics Specification

The instance models that govern SWHS are presented in the [Instance Model Section](#). The information to understand the meaning of the instance models and their derivation is also presented, so that the instance models can be verified.

4.2.1 Assumptions

This section simplifies the original problem and helps in developing the theoretical models by filling in the missing information for the physical system. The assumptions refine the scope by providing more detail.

Thermal-Energy-Only: The only form of energy that is relevant for this problem is thermal energy. All other forms of energy, such as mechanical energy, are assumed to be negligible. (RefBy: [TM:consThermE](#).)

Heat-Transfer-Coeffs-Constant: All heat transfer coefficients are constant over time. (RefBy: [TM:nwtnCooling](#).)

Constant-Water-Temp-Across-Tank: The water in the tank is fully mixed, so the temperature of the water is the same throughout the entire tank. (RefBy: [GD:rocTempSimp](#), [IM:eBalanceOnWtr](#), and [IM:eBalanceOnPCM](#).)

Temp-PCM-Constant-Across-Volume: The temperature of the phase change material is the same throughout the volume of PCM. (RefBy: [GD:rocTempSimp](#), [IM:eBalanceOnWtr](#), [IM:eBalanceOnPCM](#), and [LC:Uniform-Temperature-PCM](#).)

Density-Water-PCM-Constant-over-Volume: The density of water and density of PCM have no spatial variation; that is, they are each constant over their entire volume. (RefBy: [GD:rocTempSimp](#).)

Specific-Heat-Energy-Constant-over-Volume: The specific heat capacity of water, specific heat capacity of PCM as a solid, and specific heat capacity of PCM as a liquid have no spatial variation; that is, they are each constant over their entire volume. (RefBy: [GD:rocTempSimp](#).)

Newton-Law-Convective-Cooling-Coil-Water: Newton's law of convective cooling applies between the heating coil and the water. (RefBy: [GD:htFluxWaterFromCoil](#).)

Temp-Heating-Coil-Constant-over-Time: The temperature of the heating coil is constant over time. (RefBy: [GD:htFluxWaterFromCoil](#) and [LC:Temperature-Coil-Variable-Over-Day](#).)

Temp-Heating-Coil-Constant-over-Length: The temperature of the heating coil does not vary along its length. (RefBy: [IM:eBalanceOnWtr](#) and [LC:Temperature-Coil-Variable-Over-Length](#).)

Law-Convective-Cooling-Water-PCM: Newton's law of convective cooling applies between the water and the PCM. (RefBy: [GD:htFluxPCMFromWater](#).)

Charging-Tank-No-Temp-Discharge: The model only accounts for charging of the tank, not discharging. The temperature of the water and temperature of the phase change material can only increase, or remain constant; they do not decrease. This implies that the initial temperature [A:Same-Initial-Temp-Water-PCM](#) is less than (or equal) to the temperature of the heating coil. (RefBy: [IM:eBalanceOnWtr](#) and [LC:Discharging-Tank](#).)

Same-Initial-Temp-Water-PCM: The initial temperature of the water and the PCM is the same. (RefBy: [IM:eBalanceOnWtr](#), [IM:eBalanceOnPCM](#), [LC:Different-Initial-Temps-PCM-Water](#), and [A:Charging-Tank-No-Temp-Discharge](#).)

PCM-Initially-Solid: The simulation will start with the PCM in a solid state. (RefBy: [IM:heatEInPCM](#) and [IM:eBalanceOnPCM](#).)

Water-Always-Liquid: The operating temperature range of the system is such that the water is always in liquid state. That is, the temperature will not drop below the melting point temperature of water, or rise above its boiling point temperature. (RefBy: [IM:heatEInWtr](#), [IM:eBalanceOnWtr](#), and [UC:Water-PCM-Fixed-States](#).)

Perfect-Insulation-Tank: The tank is perfectly insulated so that there is no heat loss from the tank. (RefBy: [IM:eBalanceOnWtr](#) and [LC:Tank-Lose-Heat](#).)

No-Internal-Heat-Generation-By-Water-PCM: No internal heat is generated by either the water or the PCM; therefore, the volumetric heat generation per unit volume is zero. (RefBy: [IM:eBalanceOnWtr](#), [IM:eBalanceOnPCM](#), and [UC:No-Internal-Heat-Generation](#).)

Volume-Change-Melting-PCM-Negligible: The volume change of the PCM due to melting is negligible. (RefBy: [IM:eBalanceOnPCM](#).)

No-Gaseous-State-PCM: The PCM is either in a liquid state or a solid state but not a gaseous state. (RefBy: [IM:heatEInPCM](#), [IM:eBalanceOnPCM](#), [UC:Water-PCM-Fixed-States](#), and [UC:No-Gaseous-State](#).)

Atmospheric-Pressure-Tank: The pressure in the tank is atmospheric, so the melting point temperature and boiling point temperature are 0°C and 100°C, respectively. (RefBy: [IM:heatEInWtr](#) and [IM:eBalanceOnWtr](#).)

Volume-Coil-Negligible: When considering the volume of water in the tank, the volume of the heating coil is assumed to be negligible. (RefBy: [DD:waterVolume_pcm](#).)

4.2.2 Theoretical Models

This section focuses on the general equations and laws that SWHS is based on.

Refname	TM:consThermE
Label	Conservation of thermal energy
Equation	$-\nabla \cdot \mathbf{q} + g = \rho C \frac{\partial T}{\partial t}$
Description	<p>∇ is the gradient (Unitless)</p> <p>\mathbf{q} is the thermal flux vector ($\frac{\text{W}}{\text{m}^2}$)</p> <p>$g$ is the volumetric heat generation per unit volume ($\frac{\text{W}}{\text{m}^3}$)</p> <p>$\rho$ is the density ($\frac{\text{kg}}{\text{m}^3}$)</p> <p>$C$ is the specific heat capacity ($\frac{\text{J}}{\text{kg}^\circ\text{C}}$)</p> <p>$t$ is the time (s)</p> <p>T is the temperature ($^\circ\text{C}$)</p>
Notes	<p>The above equation gives the law of conservation of energy for transient heat transfer in a given material.</p> <p>For this equation to apply, other forms of energy, such as mechanical energy, are assumed to be negligible in the system (A:Thermal-Energy-Only).</p>
Source	Fourier Law of Heat Conduction and Heat Equation
RefBy	GD:rocTempSimp

Refname	TM:sensHtE
Label	Sensible heat energy
Equation	$E = \begin{cases} C^S m \Delta T, & T < T_{\text{melt}} \\ C^L m \Delta T, & T_{\text{melt}} < T < T_{\text{boil}} \\ C^V m \Delta T, & T_{\text{boil}} < T \end{cases}$
Description	<p>E is the sensible heat (J)</p> <p>C^S is the specific heat capacity of a solid ($\frac{\text{J}}{\text{kg}^\circ\text{C}}$)</p> <p>$m$ is the mass (kg)</p> <p>ΔT is the change in temperature ($^\circ\text{C}$)</p> <p>C^L is the specific heat capacity of a liquid ($\frac{\text{J}}{\text{kg}^\circ\text{C}}$)</p> <p>$C^V$ is the specific heat capacity of a vapour ($\frac{\text{J}}{\text{kg}^\circ\text{C}}$)</p> <p>$T$ is the temperature ($^\circ\text{C}$)</p> <p>T_{melt} is the melting point temperature ($^\circ\text{C}$)</p> <p>T_{boil} is the boiling point temperature ($^\circ\text{C}$)</p>
Notes	<p>Sensible heating occurs as long as the material does not reach a temperature where a phase change occurs. A phase change occurs if $T = T_{\text{boil}}$ or $T = T_{\text{melt}}$. If this is the case, refer to TM:latentHtE.</p>
Source	Definition of Sensible Heat
RefBy	IM:heatEInWtr and IM:heatEInPCM

Refname	TM:latentHtE
Label	Latent heat energy
Equation	$Q(t) = \int_0^t \frac{dQ(\tau)}{d\tau} d\tau$
Description	<p>Q is the latent heat (J)</p> <p>t is the time (s)</p> <p>τ is the dummy variable for integration over time (s)</p>
Notes	<p>Q is the change in thermal energy (latent heat energy).</p> <p>$Q(t) = \int_0^t \frac{dQ(\tau)}{d\tau} d\tau$ is the rate of change of Q with respect to time τ.</p> <p>t is the time elapsed, as long as the phase change is not complete.</p> <p>The status of the phase change depends on the melt fraction (from DD:meltFrac).</p> <p>Latent heating stops when all material has changed to the new phase.</p>
Source	Definition of Latent Heat
RefBy	TM:sensHtE and IM:heatEInPCM

Refname	TM:nwtnCooling
Label	Newton's law of cooling
Equation	$q(t) = h \Delta T(t)$
Description	<p>q is the heat flux ($\frac{\text{W}}{\text{m}^2}$)</p> <p>$t$ is the time (s)</p> <p>h is the convective heat transfer coefficient ($\frac{\text{W}}{\text{m}^2\text{°C}}$)</p> <p>$\Delta T$ is the change in temperature (°C)</p>
Notes	<p>Newton's law of cooling describes convective cooling from a surface. The law is stated as: the rate of heat loss from a body is proportional to the difference in temperatures between the body and its surroundings.</p> <p>h is assumed to be independent of T (from A:Heat-Transfer-Coeffs-Constant).</p> <p>$\Delta T(t) = T(t) - T_{\text{env}}(t)$ is the time-dependant thermal gradient between the environment and the object.</p>
Source	[2, (pg. 8)]
RefBy	GD:htFluxPCMFromWater and GD:htFluxWaterFromCoil

4.2.3 General Definitions

This section collects the laws and equations that will be used to build the instance models.

Refname	GD:rocTempSimp
Label	Simplified rate of change of temperature
Equation	$m C \frac{dT}{dt} = q_{\text{in}} A_{\text{in}} - q_{\text{out}} A_{\text{out}} + g V$
Description	<p> m is the mass (kg) C is the specific heat capacity ($\frac{\text{J}}{\text{kg}^\circ\text{C}}$) t is the time (s) T is the temperature ($^\circ\text{C}$) q_{in} is the heat flux input ($\frac{\text{W}}{\text{m}^2}$) A_{in} is the surface area over which heat is transferred in (m^2) q_{out} is the heat flux output ($\frac{\text{W}}{\text{m}^2}$) A_{out} is the surface area over which heat is transferred out (m^2) g is the volumetric heat generation per unit volume ($\frac{\text{W}}{\text{m}^3}$) V is the volume (m^3) </p>
Source	–
RefBy	GD:rocTempSimp, IM:eBalanceOnWtr, and IM:eBalanceOnPCM

Detailed derivation of simplified rate of change of temperature: Integrating **TM:consThermE** over a volume (V), we have:

$$-\int_V \nabla \cdot \mathbf{q} dV + \int_V g dV = \int_V \rho C \frac{\partial T}{\partial t} dV$$

Applying Gauss's Divergence Theorem to the first term over the surface S of the volume, with \mathbf{q} as the thermal flux vector for the surface and $\hat{\mathbf{n}}$ as a unit outward normal vector for a surface:

$$-\int_S \mathbf{q} \cdot \hat{\mathbf{n}} dS + \int_V g dV = \int_V \rho C \frac{\partial T}{\partial t} dV$$

We consider an arbitrary volume. The volumetric heat generation per unit volume is assumed constant. Then Equation (1) can be written as:

$$q_{\text{in}} A_{\text{in}} - q_{\text{out}} A_{\text{out}} + g V = \int_V \rho C \frac{\partial T}{\partial t} dV$$

Where q_{in} , q_{out} , A_{in} , and A_{out} are explained in **GD:rocTempSimp**. The integral over the surface could be simplified because the thermal flux is assumed constant over A_{in} and A_{out}

and 0 on all other surfaces. Outward flux is considered positive. Assuming ρ , C , and T are constant over the volume, which is true in our case by [A:Constant-Water-Temp-Across-Tank](#), [A:Temp-PCM-Constant-Across-Volume](#), [A:Density-Water-PCM-Constant-over-Volume](#), and [A:Specific-Heat-Energy-Constant-over-Volume](#), we have:

$$\rho C V \frac{dT}{dt} = q_{\text{in}} A_{\text{in}} - q_{\text{out}} A_{\text{out}} + g V$$

Using the fact that $\rho = m/V$, Equation (2) can be written as:

$$m C \frac{dT}{dt} = q_{\text{in}} A_{\text{in}} - q_{\text{out}} A_{\text{out}} + g V$$

Refname	GD:htFluxWaterFromCoil
Label	Heat flux into the water from the coil
Units	$\frac{\text{W}}{\text{m}^2}$
Equation	$q_C = h_C (T_C - T_W(t))$
Description	<p>q_C is the heat flux into the water from the coil ($\frac{\text{W}}{\text{m}^2}$)</p> <p>$h_C$ is the convective heat transfer coefficient between coil and water ($\frac{\text{W}}{\text{m}^2 \cdot ^\circ\text{C}}$)</p> <p>$T_C$ is the temperature of the heating coil ($^\circ\text{C}$)</p> <p>T_W is the temperature of the water ($^\circ\text{C}$)</p> <p>t is the time (s)</p>
Notes	<p>q_C is found by assuming that Newton's law of cooling applies (A:Newton-Law-Convective-Cooling-Coil-Water). This law (defined in TM:nwtnCooling) is used on the surface of the heating coil.</p> <p>A:Temp-Heating-Coil-Constant-over-Time</p>
Source	[3]
RefBy	IM:eBalanceOnWtr

Refname	GD:htFluxPCMFromWater
Label	Heat flux into the PCM from water
Units	$\frac{W}{m^2}$
Equation	$q_P = h_P (T_W(t) - T_P(t))$
Description	<p>q_P is the heat flux into the PCM from water ($\frac{W}{m^2}$)</p> <p>h_P is the convective heat transfer coefficient between PCM and water ($\frac{W}{m^2 \cdot ^\circ C}$)</p> <p>$T_W$ is the temperature of the water ($^\circ C$)</p> <p>t is the time (s)</p> <p>T_P is the temperature of the phase change material ($^\circ C$)</p>
Notes	<p>q_P is found by assuming that Newton's law of cooling applies (A:Law-Convective-Cooling-Water-PCM). This law (defined in TM:nwtnCooling) is used on the surface of the phase change material.</p>
Source	[3]
RefBy	IM:eBalanceOnWtr and IM:eBalanceOnPCM

4.2.4 Data Definitions

This section collects and defines all the data needed to build the instance models.

Refname	DD:waterMass
Label	Mass of water
Symbol	m_W
Units	kg
Equation	$m_W = V_W \rho_W$
Description	m_W is the mass of water (kg) V_W is the volume of water (m ³) ρ_W is the density of water ($\frac{\text{kg}}{\text{m}^3}$)
Source	–
RefBy	FR:Find-Mass

Refname	DD:waterVolume.pcm
Label	Volume of water
Symbol	V_W
Units	m^3
Equation	$V_W = V_{\text{tank}} - V_P$
Description	<p>V_W is the volume of water (m^3)</p> <p>V_{tank} is the volume of the cylindrical tank (m^3)</p> <p>V_P is the volume of PCM (m^3)</p>
Notes	Based on A:Volume-Coil-Negligible . V_{tank} is defined in DD:tankVolume .
Source	–
RefBy	FR:Find-Mass

Refname	DD:tankVolume
Label	Volume of the cylindrical tank
Symbol	V_{tank}
Units	m^3
Equation	$V_{\text{tank}} = \pi \left(\frac{D}{2}\right)^2 L$
Description	<p>V_{tank} is the volume of the cylindrical tank (m^3)</p> <p>π is the ratio of circumference to diameter for any circle (Unitless)</p> <p>D is the diameter of tank (m)</p> <p>L is the length of tank (m)</p>
Source	—
RefBy	FR:Find-Mass and DD:waterVolume_pcm

Refname	DD:balanceDecayRate
Label	ODE parameter for water related to decay time
Symbol	τ_W
Units	s
Equation	$\tau_W = \frac{m_W C_W}{h_C A_C}$
Description	<p> τ_W is the ODE parameter for water related to decay time (s) m_W is the mass of water (kg) C_W is the specific heat capacity of water ($\frac{J}{kg^\circ C}$) h_C is the convective heat transfer coefficient between coil and water $(\frac{W}{m^2 \cdot ^\circ C})$ A_C is the heating coil surface area (m²) </p>
Source	[3]
RefBy	IM:eBalanceOnWtr and FR:Output-Input-Derived-Values

Refname	DD:balanceDecayTime
Label	ODE parameter related to decay rate
Symbol	η
Units	Unitless
Equation	$\eta = \frac{h_P A_P}{h_C A_C}$
Description	<p>η is the ODE parameter related to decay rate (Unitless)</p> <p>h_P is the convective heat transfer coefficient between PCM and water $(\frac{W}{m^2 \cdot ^\circ C})$</p> <p>$A_P$ is the phase change material surface area (m^2)</p> <p>h_C is the convective heat transfer coefficient between coil and water $(\frac{W}{m^2 \cdot ^\circ C})$</p> <p>$A_C$ is the heating coil surface area (m^2)</p>
Source	[3]
RefBy	IM:eBalanceOnWtr and FR:Output-Input-Derived-Values

Refname	DD:balanceSolidPCM
Label	ODE parameter for solid PCM
Symbol	τ_P^S
Units	s
Equation	$\tau_P^S = \frac{m_P C_P^S}{h_P A_P}$
Description	<p>τ_P^S is the ODE parameter for solid PCM (s)</p> <p>m_P is the mass of phase change material (kg)</p> <p>C_P^S is the specific heat capacity of PCM as a solid ($\frac{J}{kg \cdot C}$)</p> <p>h_P is the convective heat transfer coefficient between PCM and water ($\frac{W}{m^2 \cdot C}$)</p> <p>A_P is the phase change material surface area (m²)</p>
Source	[4]
RefBy	IM:eBalanceOnPCM and FR:Output-Input-Derived-Values

Refname	DD:balanceLiquidPCM
Label	ODE parameter for liquid PCM
Symbol	τ_P^L
Units	s
Equation	$\tau_P^L = \frac{m_P C_P^L}{h_P A_P}$
Description	<p>τ_P^L is the ODE parameter for liquid PCM (s)</p> <p>m_P is the mass of phase change material (kg)</p> <p>C_P^L is the specific heat capacity of PCM as a liquid ($\frac{J}{kg^{\circ}C}$)</p> <p>h_P is the convective heat transfer coefficient between PCM and water ($\frac{W}{m^2^{\circ}C}$)</p> <p>A_P is the phase change material surface area (m²)</p>
Source	[4]
RefBy	IM:eBalanceOnPCM and FR:Output-Input-Derived-Values

Refname	DD:htFusion
Label	Specific latent heat of fusion
Symbol	H_f
Units	$\frac{\text{J}}{\text{kg}}$
Equation	$H_f = \frac{Q}{m}$
Description	<p>H_f is the specific latent heat of fusion ($\frac{\text{J}}{\text{kg}}$)</p> <p>$Q$ is the latent heat (J)</p> <p>m is the mass (kg)</p>
Notes	The specific latent heat of fusion (also known as the enthalpy of fusion) of a substance is the heat energy required (Q) to change the state of a unit of the mass (m) of the substance from solid to liquid, at constant pressure.
Source	[1, (pg. 282)]
RefBy	IM:heatEInPCM and DD:meltFrac

Refname	DD:meltFrac
Label	Melt fraction
Symbol	ϕ
Units	Unitless
Equation	$\phi = \frac{Q_P}{H_f m_P}$
Description	<p>ϕ is the melt fraction (Unitless)</p> <p>Q_P is the latent heat energy added to PCM (J)</p> <p>H_f is the specific latent heat of fusion ($\frac{J}{kg}$)</p> <p>m_P is the mass of phase change material (kg)</p>
Notes	<p>The value of ϕ is constrained to $0 \leq \phi \leq 1$.</p> <p>DD:htFusion</p>
Source	[3]
RefBy	TM:latentHtE and IM:eBalanceOnPCM

Refname	DD:aspectRatio
Label	Aspect ratio
Symbol	AR
Units	Unitless
Equation	$AR = \frac{D}{L}$
Description	AR is the aspect ratio (Unitless) D is the diameter of tank (m) L is the length of tank (m)
Source	–
RefBy	

4.2.5 Instance Models

This section transforms the problem defined in the [problem description](#) into one which is expressed in mathematical terms. It uses concrete symbols defined in the [data definitions](#) to replace the abstract symbols in the models identified in [theoretical models](#) and [general definitions](#).

The goals [GS:Predict-Water-Temperature](#), [GS:Predict-PCM-Temperature](#), [GS:Predict-Water-Energy](#), and [GS:Predict-PCM-Energy](#) are solved by [IM:eBalanceOnWtr](#), [IM:eBalanceOnPCM](#), [IM:heatEInWtr](#), and [IM:heatEInPCM](#). The solutions for [IM:eBalanceOnWtr](#) and [IM:eBalanceOnPCM](#) are coupled since the solutions for T_W and T_P depend on one another. [IM:heatEInWtr](#) can be solved once [IM:eBalanceOnWtr](#) has been solved. The solutions of [IM:eBalanceOnPCM](#) and [IM:heatEInPCM](#) are also coupled, since the temperature of the phase change material and the change in heat energy in the PCM depend on the phase change.

Refname	IM:eBalanceOnWtr
Label	Energy balance on water to find the temperature of the water
Input	$m_W, C_W, h_C, A_P, h_P, A_C, T_P, t_{\text{final}}, T_C, T_{\text{init}}$
Output	T_W
Input Constraints	$T_C > T_{\text{init}}$
Output Constraints	
Equation	$\frac{dT_W}{dt} = \frac{1}{\tau_W} (T_C - T_W(t) + \eta (T_P(t) - T_W(t)))$
Description	<p>t is the time (s)</p> <p>T_W is the temperature of the water ($^{\circ}\text{C}$)</p> <p>τ_W is the ODE parameter for water related to decay time (s)</p> <p>T_C is the temperature of the heating coil ($^{\circ}\text{C}$)</p> <p>η is the ODE parameter related to decay rate (Unitless)</p> <p>T_P is the temperature of the phase change material ($^{\circ}\text{C}$)</p>
Notes	<p>T_P is defined by IM:eBalanceOnPCM.</p> <p>The input constraint $T_{\text{init}} \leq T_C$ comes from A:Charging-Tank-No-Temp-Discharge.</p> <p>τ_W is calculated from DD:balanceDecayRate.</p> <p>η is calculated from DD:balanceDecayTime.</p> <p>The initial conditions for the ODE are $T_W(0) = T_P(0) = T_{\text{init}}$ following A:Same-Initial-Temp-Water-PCM.</p> <p>The ODE applies as long as the water is in liquid form, $0 < T_W < 100$ ($^{\circ}\text{C}$) where 0 ($^{\circ}\text{C}$) and 100 ($^{\circ}\text{C}$) are the melting and boiling point temperatures of water, respectively (from A:Water-Always-Liquid and A:Atmospheric-Pressure-Tank).</p>
Source	[3]
RefBy	IM:eBalanceOnWtr , IM:eBalanceOnPCM , UC:No-Internal-Heat-Generation , FR:Output-Values , FR:Find-Mass , and FR:Calculate-Values

Detailed derivation of the energy balance on water: To find the rate of change of T_W , we look at the energy balance on water. The volume being considered is the volume of water in the tank V_W , which has mass m_W and specific heat capacity, C_W . Heat transfer occurs in the water from the heating coil as q_C (**GD:htFluxWaterFromCoil**) and from the water into the PCM as q_P (**GD:htFluxPCMFromWater**), over areas A_C and A_P , respectively. The thermal flux is constant over A_C , since the temperature of the heating coil is assumed to not vary along its length (**A:Temp-Heating-Coil-Constant-over-Length**), and the thermal flux is constant over A_P , since the temperature of the PCM is the same throughout its volume (**A:Temp-PCM-Constant-Across-Volume**) and the water is fully mixed (**A:Constant-Water-Temp-Across-Tank**). No heat transfer occurs to the outside of the tank, since it has been assumed to be perfectly insulated (**A:Perfect-Insulation-Tank**). Since the assumption is made that no internal heat is generated (**A:No-Internal-Heat-Generation-By-Water-PCM**), $g = 0$. Therefore, the equation for **GD:rocTempSimp** can be written as:

$$m_W C_W \frac{dT_W}{dt} = q_C A_C - q_P A_P$$

Using **GD:htFluxWaterFromCoil** for q_C and **GD:htFluxPCMFromWater** for q_P , this can be written as:

$$m_W C_W \frac{dT_W}{dt} = h_C A_C (T_C - T_W) - h_P A_P (T_W - T_P)$$

Dividing Equation (2) by $m_W C_W$, we obtain:

$$\frac{dT_W}{dt} = \frac{h_C A_C}{m_W C_W} (T_C - T_W) - \frac{h_P A_P}{m_W C_W} (T_W - T_P)$$

Factoring the negative sign out of the second term of the right-hand side (RHS) of Equation (3) and multiplying it by $h_C A_C / h_C A_C$ yields:

$$\frac{dT_W}{dt} = \frac{h_C A_C}{m_W C_W} (T_C - T_W) + \frac{h_C A_C}{h_C A_C} \frac{h_P A_P}{m_W C_W} (T_P - T_W)$$

Rearranging this equation gives us:

$$\frac{dT_W}{dt} = \frac{h_C A_C}{m_W C_W} (T_C - T_W) + \frac{h_P A_P}{h_C A_C} \frac{h_C A_C}{m_W C_W} (T_P - T_W)$$

By substituting τ_W (from **DD:balanceDecayRate**) and η (from **DD:balanceDecayTime**), this can be written as:

$$\frac{dT_W}{dt} = \frac{1}{\tau_W} (T_C - T_W) + \frac{\eta}{\tau_W} (T_P - T_W)$$

Finally, factoring out $\frac{1}{\tau_W}$, we are left with the governing ODE for **IM:eBalanceOnWtr**:

$$\frac{dT_W}{dt} = \frac{1}{\tau_W} (T_C - T_W + \eta (T_P - T_W))$$

Refname	IM:eBalanceOnPCM
Label	Energy Balance on PCM to find temperature of PCM
Input	$T_{\text{melt}}^{\text{P}}, t_{\text{final}}, T_{\text{init}}, A_{\text{P}}, h_{\text{P}}, m_{\text{P}}, C_{\text{P}}^{\text{S}}, C_{\text{P}}^{\text{L}}$
Output	T_{P}
Input Constraints	$T_{\text{melt}}^{\text{P}} > T_{\text{init}}$
Output Constraints	
Equation	$\frac{dT_{\text{P}}}{dt} = \begin{cases} \frac{1}{\tau_{\text{P}}^{\text{S}}} (T_{\text{W}}(t) - T_{\text{P}}(t)), & T_{\text{P}} < T_{\text{melt}}^{\text{P}} \\ \frac{1}{\tau_{\text{P}}^{\text{L}}} (T_{\text{W}}(t) - T_{\text{P}}(t)), & T_{\text{P}} > T_{\text{melt}}^{\text{P}} \\ 0, & T_{\text{P}} = T_{\text{melt}}^{\text{P}} \wedge 0 < \phi < 1 \end{cases}$
Description	<p>t is the time (s)</p> <p>T_{P} is the temperature of the phase change material ($^{\circ}\text{C}$)</p> <p>$\tau_{\text{P}}^{\text{S}}$ is the ODE parameter for solid PCM (s)</p> <p>T_{W} is the temperature of the water ($^{\circ}\text{C}$)</p> <p>$\tau_{\text{P}}^{\text{L}}$ is the ODE parameter for liquid PCM (s)</p> <p>$T_{\text{melt}}^{\text{P}}$ is the melting point temperature for PCM ($^{\circ}\text{C}$)</p> <p>ϕ is the melt fraction (Unitless)</p>
Notes	<p>T_{W} is defined by IM:eBalanceOnWtr.</p> <p>The input constraint $T_{\text{init}} \leq T_{\text{melt}}^{\text{P}}$ comes from A:PCM-Initially-Solid.</p> <p>The temperature remains constant at $T_{\text{melt}}^{\text{P}}$, even with the heating (or cooling), until the phase change has occurred for all of the material; that is as long as $0 < \phi < 1$. ϕ (from DD:meltFrac) is determined as part of the heat energy in the PCM, as given in (IM:heatEInPCM).</p> <p>$\tau_{\text{P}}^{\text{S}}$ is calculated in DD:balanceSolidPCM.</p> <p>$\tau_{\text{P}}^{\text{L}}$ is calculated in DD:balanceLiquidPCM.</p> <p>The initial conditions for the ODE are $T_{\text{W}}(0) = T_{\text{P}}(0) = T_{\text{init}}$ following A:Same-Initial-Temp-Water-PCM.</p>
Source	[3]
RefBy	IM:eBalanceOnWtr , UC:No-Internal-Heat-Generation , UC:No-Gaseous-State , FR:Output-Values , FR:Find-Mass , FR:Calculate-Values , FR:Calculate-PCM-Melt-End-Time , and FR:Calculate-PCM-Melt-Begin-Time

Detailed derivation of the energy balance on the PCM during sensible heating phase: To find the rate of change of T_P , we look at the energy balance on the PCM. The volume being considered is the volume of PCM (V_P). The derivation that follows is initially for the solid PCM. The mass of phase change material is m_P and the specific heat capacity of PCM as a solid is C_P^S . The heat flux into the PCM from water is q_P (**GD:htFluxPCMFromWater**) over phase change material surface area A_P . The thermal flux is constant over A_P , since the temperature of the PCM is the same throughout its volume (**A:Temp-PCM-Constant-Across-Volume**) and the water is fully mixed (**A:Constant-Water-Temp-Across-Tank**). There is no heat flux output from the PCM. Assuming no volumetric heat generation per unit volume (**A:No-Internal-Heat-Generation-By-Water-PCM**), $g = 0$, the equation for **GD:rocTempSimp** can be written as:

$$m_P C_P^S \frac{dT_P}{dt} = q_P A_P$$

Using **GD:htFluxPCMFromWater** for q_P , this equation can be written as:

$$m_P C_P^S \frac{dT_P}{dt} = h_P A_P (T_W - T_P)$$

Dividing by $m_P C_P^S$ we obtain:

$$\frac{dT_P}{dt} = \frac{h_P A_P}{m_P C_P^S} (T_W - T_P)$$

By substituting τ_P^S (from **DD:balanceSolidPCM**), this can be written as:

$$\frac{dT_P}{dt} = \frac{1}{\tau_P^S} (T_W - T_P)$$

Equation (4) applies for the solid PCM. In the case where all of the PCM is melted, the same derivation applies, except that C_P^S is replaced by C_P^L , and thus τ_P^S is replaced by τ_P^L . Although a small change in surface area would be expected with melting, this is not included, since the volume change of the PCM with melting is assumed to be negligible (**A:Volume-Change-Melting-PCM-Negligible**).

In the case where $T_P = T_{\text{melt}}^P$ and not all of the PCM is melted, the temperature of the phase change material does not change. Therefore, $d T_P / d t = 0$.

This derivation does not consider the boiling of the PCM, as the PCM is assumed to either be in a solid state or a liquid state (**A:No-Gaseous-State-PCM**).

Refname	IM:heatEInWtr
Label	Heat energy in the water
Input	$T_{\text{init}}, m_{\text{W}}, C_{\text{W}}, m_{\text{W}}$
Output	E_{W}
Input Constraints	
Output Constraints	
Equation	$E_{\text{W}}(t) = C_{\text{W}} m_{\text{W}} (T_{\text{W}}(t) - T_{\text{init}})$
Description	<p>E_{W} is the change in heat energy in the water (J)</p> <p>t is the time (s)</p> <p>C_{W} is the specific heat capacity of water ($\frac{\text{J}}{\text{kg}^\circ\text{C}}$)</p> <p>$m_{\text{W}}$ is the mass of water (kg)</p> <p>T_{W} is the temperature of the water ($^\circ\text{C}$)</p> <p>T_{init} is the initial temperature ($^\circ\text{C}$)</p>
Notes	<p>The above equation is derived using TM:sensHtE.</p> <p>The change in temperature is the difference between the temperature at time t (s), T_{W} and the initial temperature, T_{init} ($^\circ\text{C}$).</p> <p>This equation applies as long as $0 < T_{\text{W}} < 100^\circ\text{C}$ (A:Water-Always-Liquid, A:Atmospheric-Pressure-Tank).</p>
Source	[3]
RefBy	FR:Output-Values , FR:Find-Mass , and FR:Calculate-Values

Refname	IM:heatEInPCM
Label	Heat energy in the PCM
Input	$T_{\text{melt}}^{\text{P}}, t_{\text{final}}, T_{\text{init}}, A_{\text{P}}, h_{\text{P}}, m_{\text{P}}, C_{\text{P}}^{\text{S}}, C_{\text{P}}^{\text{L}}, T_{\text{P}}, H_{\text{f}}, t_{\text{melt}}^{\text{init}}$
Output	E_{P}
Input Constraints	$T_{\text{melt}}^{\text{P}} > T_{\text{init}}$
Output Constraints	
Equation	$E_{\text{P}} = \begin{cases} C_{\text{P}}^{\text{S}} m_{\text{P}} (T_{\text{P}}(t) - T_{\text{init}}), & T_{\text{P}} < T_{\text{melt}}^{\text{P}} \\ E_{\text{P}_{\text{melt}}}^{\text{init}} + H_{\text{f}} m_{\text{P}} + C_{\text{P}}^{\text{L}} m_{\text{P}} (T_{\text{P}}(t) - T_{\text{melt}}^{\text{P}}), & T_{\text{P}} > T_{\text{melt}}^{\text{P}} \\ E_{\text{P}_{\text{melt}}}^{\text{init}} + Q_{\text{P}}(t), & T_{\text{P}} = T_{\text{melt}}^{\text{P}} \wedge 0 < \phi < 1 \end{cases}$
Description	<p>E_{P} is the change in heat energy in the PCM (J)</p> <p>C_{P}^{S} is the specific heat capacity of PCM as a solid ($\frac{\text{J}}{\text{kg}^{\circ}\text{C}}$)</p> <p>$m_{\text{P}}$ is the mass of phase change material (kg)</p> <p>T_{P} is the temperature of the phase change material ($^{\circ}\text{C}$)</p> <p>t is the time (s)</p> <p>T_{init} is the initial temperature ($^{\circ}\text{C}$)</p> <p>$E_{\text{P}_{\text{melt}}}^{\text{init}}$ is the change in heat energy in the PCM at the instant when melting begins (J)</p> <p>H_{f} is the specific latent heat of fusion ($\frac{\text{J}}{\text{kg}}$)</p> <p>$C_{\text{P}}^{\text{L}}$ is the specific heat capacity of PCM as a liquid ($\frac{\text{J}}{\text{kg}^{\circ}\text{C}}$)</p> <p>$T_{\text{melt}}^{\text{P}}$ is the melting point temperature for PCM ($^{\circ}\text{C}$)</p> <p>Q_{P} is the latent heat energy added to PCM (J)</p> <p>ϕ is the melt fraction (Unitless)</p>
Notes	<p>The above equation is derived using TM:sensHtE and TM:latentHtE. E_{P} for the solid PCM is found using TM:sensHtE for sensible heating, with the specific heat capacity of the solid PCM, C_{P}^{S} ($\frac{\text{J}}{\text{kg}^{\circ}\text{C}}$) and the change in the PCM temperature from the initial temperature ($^{\circ}\text{C}$).</p> <p>E_{P} for the melted PCM ($T_{\text{P}} > E_{\text{P}_{\text{melt}}}^{\text{init}}$) is found using TM:sensHtE for sensible heat of the liquid PCM plus the energy when melting starts, plus the energy required to melt all of the PCM.</p> <p>The energy required to melt all of the PCM is $H_{\text{f}} m_{\text{P}}$ (J) (from DD:htFusion).</p> <p>The change in temperature is $T_{\text{P}} - T_{\text{melt}}^{\text{P}}$ ($^{\circ}\text{C}$).</p> <p>E_{P} during melting of the PCM is found using the energy required at the instant melting of the PCM begins, $E_{\text{P}_{\text{melt}}}^{\text{init}}$ plus the latent heat energy added to the PCM, Q_{P} (J) and the change in temperature of the PCM, $T_{\text{P}} - T_{\text{melt}}^{\text{P}}$ ($^{\circ}\text{C}$).</p>

4.2.6 Data Constraints

The **Data Constraints Table** shows the data constraints on the input variables. The column for physical constraints gives the physical limitations on the range of values that can be taken by the variable. The uncertainty column provides an estimate of the confidence with which the physical quantities can be measured. This information would be part of the input if one were performing an uncertainty quantification exercise. The constraints are conservative to give the user of the model the flexibility to experiment with unusual situations. The column of typical values is intended to provide a feel for a common scenario. The column for software constraints restricts the range of inputs to reasonable values. (*) These quantities cannot be equal to zero, or there will be a divide by zero in the model. (+) These quantities cannot be zero, or there would be freezing (**A:PCM-Initially-Solid**). (++) The constraints on the surface area are calculated by considering the surface area to volume ratio. The assumption is that the lowest ratio is 1 and the highest possible is $\frac{2}{h_{\min}}$, where h_{\min} is the thickness of a “sheet” of PCM. A thin sheet has the greatest surface area to volume ratio. (**) The constraint on the maximum time at the end of the simulation is the total number of seconds in one day.

Table 4: Input Data Constraints

Var	Physical Constraints	Software Constraints	Typical Value	Uncert.
A_C	$A_C > 0$	$A_C \leq A_C^{\max}$	0.12 m ²	10%
A_P	$A_P > 0$	$V_P \leq A_P \leq \frac{2}{h_{\min}} V_{\text{tank}}$	1.2 m ²	10%
C_P^L	$C_P^L > 0$	$C_P^L_{\min} < C_P^L < C_P^L_{\max}$	2270 $\frac{\text{J}}{\text{kg}^\circ\text{C}}$	10%
C_P^S	$C_P^S > 0$	$C_P^S_{\min} < C_P^S < C_P^S_{\max}$	1760 $\frac{\text{J}}{\text{kg}^\circ\text{C}}$	10%
C_W	$C_W > 0$	$C_W^{\min} < C_W < C_W^{\max}$	4186 $\frac{\text{J}}{\text{kg}^\circ\text{C}}$	10%
D	$D > 0$	$AR_{\min} \leq D \leq AR_{\max}$	0.412 m	10%
H_f	$H_f > 0$	$H_{f\min} < H_f < H_{f\max}$	211600 $\frac{\text{J}}{\text{kg}}$	10%
h_C	$h_C > 0$	$h_C^{\min} \leq h_C \leq h_C^{\max}$	1000 $\frac{\text{W}}{\text{m}^2^\circ\text{C}}$	10%
h_P	$h_P > 0$	$h_P^{\min} \leq h_P \leq h_P^{\max}$	1000 $\frac{\text{W}}{\text{m}^2^\circ\text{C}}$	10%
L	$L > 0$	$L_{\min} \leq L \leq L_{\max}$	1.5 m	10%
T_C	$0 < T_C < 100$	—	50 °C	10%
T_{init}	$0 < T_{\text{init}} < T_{\text{melt}}$	—	40 °C	10%
T_{melt}^P	$0 < T_{\text{melt}}^P < T_C$	—	44.2 °C	10%
t_{final}	$t_{\text{final}} > 0$	$t_{\text{final}} < t_{\text{final}}^{\max}$	50000 s	10%
t_{step}	$0 < t_{\text{step}} < t_{\text{final}}$	—	0.01 s	10%

Continued on next page

Table 4: Input Data Constraints (Continued)

Var	Physical Constraints	Software Constraints	Typical Value	Uncert.
V_P	$0 < V_P < V_{\text{tank}}$	$V_P \geq \text{MINFRAC}T V_{\text{tank}}$	0.05 m^3	10%
ρ_P	$\rho_P > 0$	$\rho_P^{\min} < \rho_P < \rho_P^{\max}$	$1007 \frac{\text{kg}}{\text{m}^3}$	10%
ρ_W	$\rho_W > 0$	$\rho_W^{\min} < \rho_W \leq \rho_W^{\max}$	$1000 \frac{\text{kg}}{\text{m}^3}$	10%

4.2.7 Properties of a Correct Solution

The **Data Constraints Table** shows the data constraints on the output variables. The column for physical constraints gives the physical limitations on the range of values that can be taken by the variable.

Table 5: Output Data Constraints

Var	Physical Constraints
T_W	$T_{\text{init}} \leq T_W \leq T_C$
T_P	$T_{\text{init}} \leq T_P \leq T_C$
E_W	$E_W \geq 0$
E_P	$E_P \geq 0$

A correct solution must exhibit the law of conservation of energy. This means that the change in heat energy in the water should equal the difference between the total energy input from the heating coil and the energy output to the PCM. This can be shown as an equation by taking **GD:htFluxWaterFromCoil** and **GD:htFluxPCMFromWater**, multiplying each by their respective surface area of heat transfer, and integrating each over the simulation time, as follows:

$$E_W = \int_0^t h_C A_C (T_C - T_W(t)) dt - \int_0^t h_P A_P (T_W(t) - T_P(t)) dt$$

In addition, the change in heat energy in the PCM should equal the energy input to the PCM from the water. This can be expressed as

$$E_P = \int_0^t h_P A_P (T_W(t) - T_P(t)) dt$$

Equations (FIXME: Equation 7) and (FIXME: Equation 8) can be used as “sanity” checks to gain confidence in any solution computed by SWHS. The relative error between the results computed by SWHS and the results calculated from the RHS of these equations should be less than C_{tol} **FR:Verify-Energy-Output-Follow-Conservation-of-Energy**.

5 Requirements

This section provides the functional requirements, the tasks and behaviours that the software is expected to complete, and the non-functional requirements, the qualities that the software is expected to exhibit.

5.1 Functional Requirements

This section provides the functional requirements, the tasks and behaviours that the software is expected to complete.

Input-Values: Input the values from **Tab:ReqInputs**, which define the tank parameters, material properties, and initial conditions.

Find-Mass: Use the inputs in **FR:Input-Values** to find the masses needed for **IM:eBalanceOnWtr**, **IM:eBalanceOnPCM**, **IM:heatEInWtr**, and **IM:heatEInPCM**, using **DD:waterMass**, **DD:waterVolume_pcm**, and **DD:tankVolume**.

Check-Input-with-Physical_Constraints: Verify that the inputs satisfy the required **physical constraints**.

Output-Input-Derived-Values: Output the input values and derived values in the following list: the values (from **FR:Input-Values**), the masses (from **FR:Find-Mass**), τ_W (from **DD:balanceDecayRate**), η (from **DD:balanceDecayTime**), τ_P^S (from **DD:balanceSolidPCM**), and τ_P^L (from **DD:balanceLiquidPCM**).

Calculate-Values: Calculate the following values: $T_W(t)$ (from **IM:eBalanceOnWtr**), $T_P(t)$ (from **IM:eBalanceOnPCM**), $E_W(t)$ (from **IM:heatEInWtr**), and $E_P(t)$ (from **IM:heatEInPCM**).

Verify-Energy-Output-Follow-Conservation-of-Energy: Verify that the energy outputs ($E_W(t)$ and $E_P(t)$) follow the law of conservation of energy, as outlined in **Properties of a Correct Solution**, with relative error no greater than C_{tol} .

Calculate-PCM-Melt-Begin-Time: Calculate and output the time at which the PCM begins to melt t_{melt}^{init} (from **IM:eBalanceOnPCM**).

Calculate-PCM-Melt-End-Time: Calculate and output the time at which the PCM stops melting t_{melt}^{final} (from **IM:eBalanceOnPCM**).

Output-Values: Output $T_W(t)$ (from **IM:eBalanceOnWtr**), $T_P(t)$ (from **IM:eBalanceOnPCM**), $E_W(t)$ (from **IM:heatEInWtr**), and $E_P(t)$ (from **IM:heatEInPCM**).

Table 6: Required Inputs

Symbol	Description	Units
A_C	Heating coil surface area	m^2
A_P	Phase change material surface area	m^2
A_{tol}	Absolute tolerance	—
C_P^L	Specific heat capacity of PCM as a liquid	$\frac{J}{kg^\circ C}$
C_P^S	Specific heat capacity of PCM as a solid	$\frac{J}{kg^\circ C}$
C_W	Specific heat capacity of water	$\frac{J}{kg^\circ C}$
D	Diameter of tank	m
H_f	Specific latent heat of fusion	$\frac{J}{kg}$
h_C	Convective heat transfer coefficient between coil and water	$\frac{W}{m^2 \cdot ^\circ C}$
h_P	Convective heat transfer coefficient between PCM and water	$\frac{W}{m^2 \cdot ^\circ C}$
L	Length of tank	m
R_{tol}	Relative tolerance	—
T_C	Temperature of the heating coil	$^\circ C$
T_{init}	Initial temperature	$^\circ C$
T_{melt}^P	Melting point temperature for PCM	$^\circ C$
t_{final}	Final time	s
t_{step}	Time step for simulation	s
V_P	Volume of PCM	m^3
ρ_P	Density of PCM	$\frac{kg}{m^3}$
ρ_W	Density of water	$\frac{kg}{m^3}$

5.2 Non-Functional Requirements

This section provides the non-functional requirements, the qualities that the software is expected to exhibit.

Correctness: The outputs of the code have the **properties of a correct solution**.

Verifiability: The code is tested with complete verification and validation plan.

Understandability: The code is modularized with complete module guide and module interface specification.

Reusability: The code is modularized.

Maintainability: If a likely change is made to the finished software, it will take at most 10% of the original development time, assuming the same development resources are available.

6 Likely Changes

This section lists the likely changes to be made to the software.

Uniform-Temperature-PCM: **A:Temp-PCM-Constant-Across-Volume** - PCM is actually a poor thermal conductor, so the assumption of uniform temperature of the phase change material is not likely.

Temperature-Coil-Variable-Over-Day: **A:Temp-Heating-Coil-Constant-over-Time** - The temperature of the heating coil will change over the course of the day, depending on the energy received from the sun.

Temperature-Coil-Variable-Over-Length: **A:Temp-Heating-Coil-Constant-over-Length** - The temperature of the heating coil will actually change along its length as the water within it cools.

Discharging-Tank: **A:Charging-Tank-No-Temp-Discharge** - The model currently only accounts for charging of the tank. A more complete model would also account for discharging of the tank.

Different-Initial-Temps-PCM-Water: **A:Same-Initial-Temp-Water-PCM** - To add more flexibility to the simulation, the initial temperature of the water and the PCM could be allowed to have different values.

Tank-Lose-Heat: **A:Perfect-Insulation-Tank** - Any real tank cannot be perfectly insulated and will lose heat.

7 Unlikely Changes

This section lists the unlikely changes to be made to the software.

Water-PCM-Fixed-States: **A:Water-Always-Liquid**, **A:No-Gaseous-State-PCM** - It is unlikely for the change of water from liquid to a solid or the state change of the phase change material from a liquid to a gas to be considered.

No-Internal-Heat-Generation: **A:No-Internal-Heat-Generation-By-Water-PCM** - Is used for the derivations of **IM:eBalanceOnWtr** and **IM:eBalanceOnPCM**.

No-Gaseous-State: **A:No-Gaseous-State-PCM** - Is used for the derivation of **IM:eBalanceOn-PCM** and for the equation given by **IM:heatEInPCM** to be valid.

8 Traceability Matrices and Graphs

The purpose of the traceability matrices is to provide easy references on what has to be additionally modified if a certain component is changed. Every time a component is changed, the items in the column of that component that are marked with an “X” should be modified as well. [Tab:TraceMatAvsA](#) shows the dependencies of the assumptions on each other. [Tab:TraceMatAvsAll](#) shows the dependencies of the data definitions, theoretical models, general definitions, instance models, requirements, likely changes, and unlikely changes on the assumptions. [Tab:TraceMatRefvsRef](#) shows the dependencies of the data definitions, theoretical models, general definitions, and instance models on each other. [Tab:TraceMatAllvsR](#) shows the dependencies of the requirements and goal statements on the data definitions, theoretical models, general definitions, and instance models.

	A:Thermal-Energy-Only	A:Heat-Transfer-Coe
A:Thermal-Energy-Only		
A:Heat-Transfer-Coeffs-Constant		
A:Constant-Water-Temp-Across-Tank		
A:Temp-PCM-Constant-Across-Volume		
A:Density-Water-PCM-Constant-over-Volume		
A:Specific-Heat-Energy-Constant-over-Volume		
A:Newton-Law-Convective-Cooling-Coil-Water		
A:Temp-Heating-Coil-Constant-over-Time		
A:Temp-Heating-Coil-Constant-over-Length		
A:Law-Convective-Cooling-Water-PCM		
A:Charging-Tank-No-Temp-Discharge		
A:Same-Initial-Temp-Water-PCM		
A:PCM-Initially-Solid		
A:Water-Always-Liquid		
A:Perfect-Insulation-Tank		
A:No-Internal-Heat-Generation-By-Water-PCM		
A:Volume-Change-Melting-PCM-Negligible		
A:No-Gaseous-State-PCM		
A:Atmospheric-Pressure-Tank		
A:Volume-Coil-Negligible		

	A:Thermal-Energy-Only	A:Heat-Tran
DD:waterMass		
DD:waterVolume_pcm		
DD:tankVolume		
DD:balanceDecayRate		
DD:balanceDecayTime		
DD:balanceSolidPCM		
DD:balanceLiquidPCM		
DD:htFusion		
DD:meltFrac		
DD:aspectRatio		
TM:consThermE	X	
TM:sensHtE		
TM:latentHtE		
TM:nwtnCooling		X
GD:rocTempSimp		
GD:htFluxWaterFromCoil		
GD:htFluxPCMFromWater		
IM:eBalanceOnWtr		
IM:eBalanceOnPCM		
IM:heatEInWtr		
IM:heatEInPCM		
FR:Input-Values		
FR:Find-Mass		
FR:Check-Input-with-Physical_Constraints		
FR:Output-Input-Derived-Values		
FR:Calculate-Values		
FR:Verify-Energy-Output-Follow-Conservation-of-Energy		
FR:Calculate-PCM-Melt-Begin-Time		
FR:Calculate-PCM-Melt-End-Time		
FR:Output-Values		

	A:Thermal-Energy-Only	A:Heat-Trans
NFR:Correctness		
NFR:Verifiability		
NFR:Understandability		
NFR:Reusability		
NFR:Maintainability		
LC:Uniform-Temperature-PCM		
LC:Temperature-Coil-Variable-Over-Day		
LC:Temperature-Coil-Variable-Over-Length		
LC:Discharging-Tank		
LC:Different-Initial-Temps-PCM-Water		
LC:Tank-Lose-Heat		
UC:Water-PCM-Fixed-States		
UC:No-Internal-Heat-Generation		
UC:No-Gaseous-State		

	DD:waterMass	DD:waterVolume_pcm	DD:tankVolume	DD:balanceDecayRate
DD:waterMass				
DD:waterVolume_pcm		X		
DD:tankVolume				
DD:balanceDecayRate				
DD:balanceDecayTime				
DD:balanceSolidPCM				
DD:balanceLiquidPCM				
DD:htFusion				
DD:meltFrac				
DD:aspectRatio				
TM:consThermE				
TM:sensHtE				

	DD:waterMass	DD:waterVolume_pcm	DD:tankVolume	DD:waterVolume_tank
TM:latentHtE				
TM:nwtnCooling				
GD:rocTempSimp				
GD:htFluxWaterFromCoil				
GD:htFluxPCMFromWater				
IM:eBalanceOnWtr				X
IM:eBalanceOnPCM				
IM:heatEInWtr				
IM:heatEInPCM				
	DD:waterMass	DD:waterVolume_pcm	DD:tankVolume	DD:waterVolume_tank
GS:Predict-Water-Temperature				
GS:Predict-PCM-Temperature				
GS:Predict-Water-Energy				
GS:Predict-PCM-Energy				
FR:Input-Values				
FR:Find-Mass	X		X	
FR:Check-Input-with-Physical_Constraints				
FR:Output-Input-Derived-Values				
FR:Calculate-Values				
FR:Verify-Energy-Output-Follow-Conservation-of-Energy				
FR:Calculate-PCM-Melt-Begin-Time				
FR:Calculate-PCM-Melt-End-Time				
FR:Output-Values				
NFR:Correctness				
NFR:Verifiability				
NFR:Understandability				
NFR:Reusability				

The purpose of the traceability graphs is also to provide easy references on what has to be additionally modified if a certain component is changed. The arrows in the graphs represent dependencies. The component at the tail of an arrow is depended on by the component at the head of that arrow. Therefore, if a component is changed, the components that it points to should also be changed. **Fig:TraceGraphAvsA** shows the dependencies of assumptions on each other. **Fig:TraceGraphAvsAll** shows the dependencies of data definitions, theoretical models, general definitions, instance models, requirements, likely changes, and unlikely changes on the assumptions. **Fig:TraceGraphRefsRef** shows the dependencies of data definitions, theoretical models, general definitions, and instance models on each other. **Fig:TraceGraphAllvsR** shows the dependencies of requirements and goal statements on the data definitions, theoretical models, general definitions, and instance models. **Fig:TraceGraphAllvsAll** shows the dependencies of dependencies of assumptions, models, definitions, requirements, goals, and changes with each other.

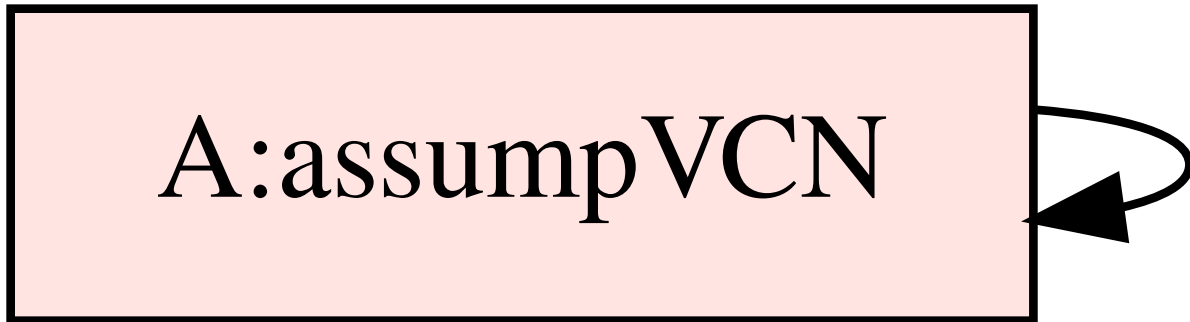


Figure 3: TraceGraphAvsA

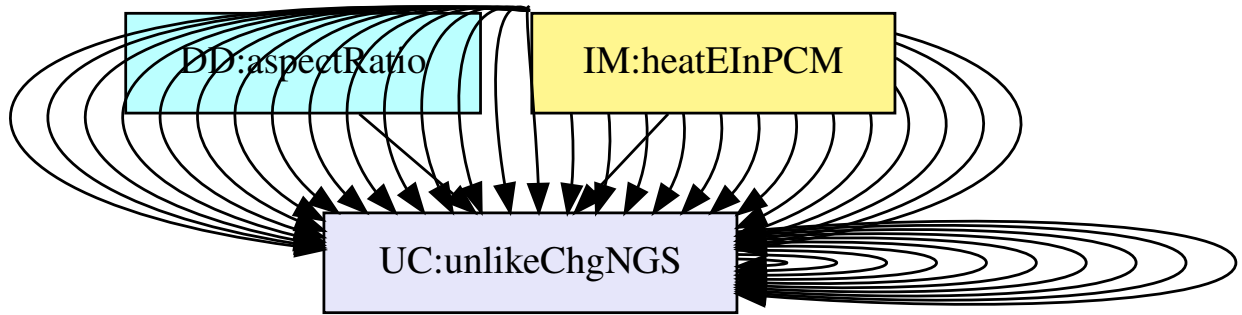


Figure 4: TraceGraphAvsAll

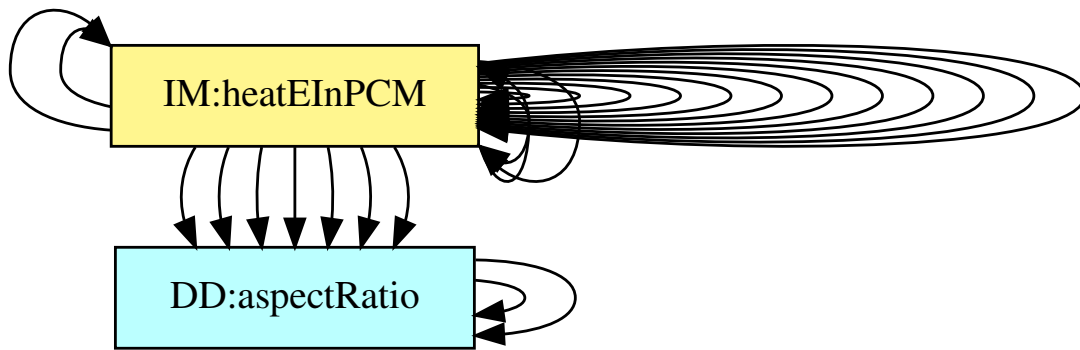


Figure 5: TraceGraphRefvsRef

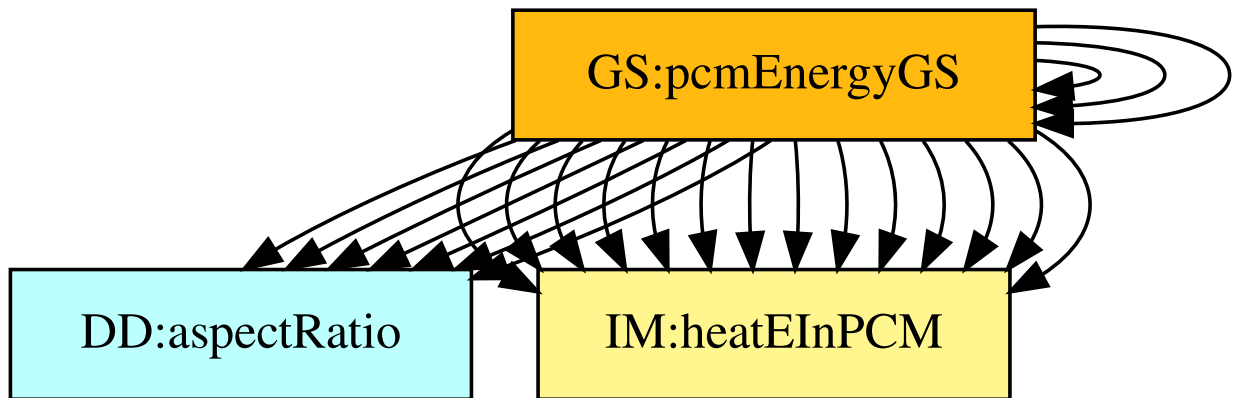


Figure 6: TraceGraphAllvsR

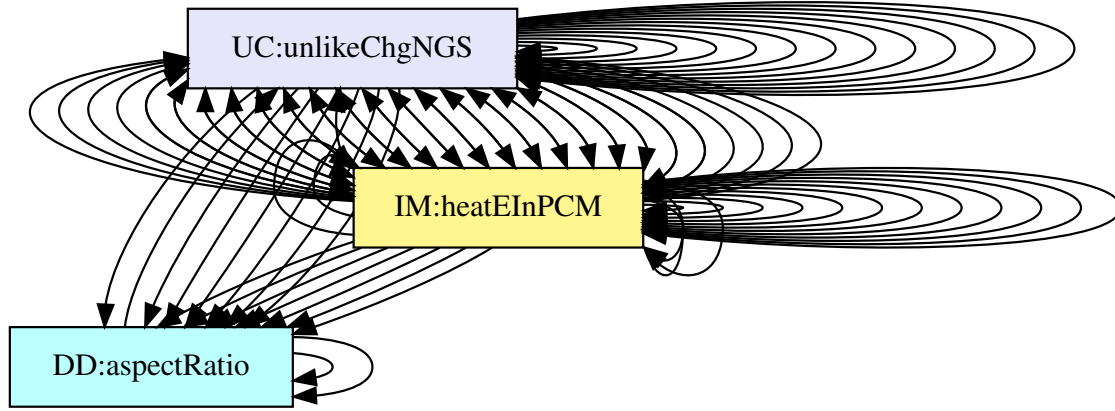


Figure 7: TraceGraphAllvsAll

For convenience, the following graphs can be found at the links below:

- [TraceGraphAvsA](#)
- [TraceGraphAvsAll](#)
- [TraceGraphRefvsRef](#)
- [TraceGraphAllvsR](#)
- [TraceGraphAllvsAll](#)

9 Values of Auxiliary Constants

This section contains the standard values that are used for calculations in SWHS.

Table 11: Auxiliary Constants

Symbol	Description	Value	Unit
A_C^{\max}	maximum surface area of coil	100000	m^2
AR_{\max}	maximum aspect ratio	100	—
AR_{\min}	minimum aspect ratio	0.01	—
C_{tol}	relative tolerance for conservation of energy	0.001%	—
C_W^{\max}	maximum specific heat capacity of water	4210	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$
C_W^{\min}	minimum specific heat capacity of water	4170	$\frac{\text{J}}{\text{kg}^\circ\text{C}}$

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Table 11: Auxiliary Constants (Continued)

Symbol	Description	Value	Unit
$C_{\text{P}}^{\text{L}}_{\text{max}}$	maximum specific heat capacity of PCM as a liquid	5000	$\frac{\text{J}}{\text{kg}^{\circ}\text{C}}$
$C_{\text{P}}^{\text{L}}_{\text{min}}$	minimum specific heat capacity of PCM as a liquid	100	$\frac{\text{J}}{\text{kg}^{\circ}\text{C}}$
$C_{\text{P}}^{\text{S}}_{\text{max}}$	maximum specific heat capacity of PCM as a solid	4000	$\frac{\text{J}}{\text{kg}^{\circ}\text{C}}$
$C_{\text{P}}^{\text{S}}_{\text{min}}$	minimum specific heat capacity of PCM as a solid	100	$\frac{\text{J}}{\text{kg}^{\circ}\text{C}}$
H_{fmax}	maximum specific latent heat of fusion	1000000	$\frac{\text{J}}{\text{kg}^{\circ}\text{C}}$
H_{fmin}	minimum specific latent heat of fusion	0	$\frac{\text{J}}{\text{kg}^{\circ}\text{C}}$
$h_{\text{C}}^{\text{max}}$	maximum convective heat transfer coefficient between coil and water	10000	$\frac{\text{W}}{\text{m}^2\text{C}}$
$h_{\text{C}}^{\text{min}}$	minimum convective heat transfer coefficient between coil and water	10	$\frac{\text{W}}{\text{m}^2\text{C}}$
$h_{\text{P}}^{\text{max}}$	maximum convective heat transfer coefficient between PCM and water	10000	$\frac{\text{W}}{\text{m}^2\text{C}}$
$h_{\text{P}}^{\text{min}}$	minimum convective heat transfer coefficient between PCM and water	10	$\frac{\text{W}}{\text{m}^2\text{C}}$
L_{max}	maximum length of tank	50	m
L_{min}	minimum length of tank	0.1	m
$MINFRACT$	minimum fraction of the tank volume taken up by the PCM	$1.0 \cdot 10^{-6}$	—
$t_{\text{final}}^{\text{max}}$	maximum final time	86400	s
$\rho_{\text{P}}^{\text{max}}$	maximum density of PCM	20000	$\frac{\text{kg}}{\text{m}^3}$
$\rho_{\text{P}}^{\text{min}}$	minimum density of PCM	500	$\frac{\text{kg}}{\text{m}^3}$
$\rho_{\text{W}}^{\text{max}}$	maximum density of water	1000	$\frac{\text{kg}}{\text{m}^3}$
$\rho_{\text{W}}^{\text{min}}$	minimum density of water	950	$\frac{\text{kg}}{\text{m}^3}$

10 References

- [1] J. Frederick Bueche. *Introduction to Physics for Scientists*. 4th ed. New York City, New York: McGraw Hill, 1986.
- [2] F. P. Incropera et al. *Fundamentals of Heat and Mass Transfer*. 6th ed. Hoboken, New Jersey: John Wiley and Sons, 2007.
- [3] Nirmitha Koothoor. “A Document Driven Approach to Certifying Scientific Computing Software”. MA thesis. Hamilton, ON, Canada: McMaster University, 2013.

- [4] Marilyn Lightstone. *Derivation of tank/pcm model*. From Marilyn Lightstone’s Personal Notes. 2012.
- [5] David L. Parnas and P. C. Clements. “A rational design process: How and why to fake it”. In: *IEEE Transactions on Software Engineering* 12.2 (Feb. 1986), pp. 251–257.
- [6] W. Spencer Smith and Nirmitha Koothoor. “A Document-Driven Method for Certifying Scientific Computing Software for Use in Nuclear Safety Analysis”. In: *Nuclear Engineering and Technology* 48.2 (Apr. 2016), pp. 404–418.
- [7] W. Spencer Smith and Lei Lai. “A new requirements template for scientific computing”. In: *Proceedings of the First International Workshop on Situational Requirements Engineering Processes - Methods, Techniques and Tools to Support Situation-Specific Requirements Engineering Processes, SREP’05*. Ed. by PJ Agerfalk, N. Kraiem, and J. Ralyte. In conjunction with 13th IEEE International Requirements Engineering Conference, Paris, France, 2005, pp. 107–121.
- [8] W. Spencer Smith, Lei Lai, and Ridha Khedri. “Requirements Analysis for Engineering Computation: A Systematic Approach for Improving Software Reliability”. In: *Reliable Computing, Special Issue on Reliable Engineering Computation* 13.1 (Feb. 2007), pp. 83–107.