1 Tutorial 1: The simplest case.

This is the simplest example of using the GenCheck framework to test an implementation against a specification. This module contains a revList (reverse) function that reverses the order of the elements in a list, and two properties for this function: reversing a list twice returns the original list, and reversing a singleton list has no effect.

module TestReverseList where

```
import Test.SimpleCheck
```

The properties that the revList function must satisfy:

- propRevUnitEq the reverse of a singleton list is the original
- propRevRevEq reversing the reverse is the original list (involutive)

Note that the first is a property of individual values and the second is a property of lists, so different test suites and test case generators are required.

```
propRevUnitEq :: (Eq a) ⇒ Property a
propRevUnitEq x = (revList [x]) == [x]

propRevRevEq :: (Eq a) ⇒ Property [a]
propRevRevEq xs = (revList.revList) xs == xs

The implementation to test.

revList :: [a] → [a]
revList xs = rev xs []
where rev [] xs' = xs'
    rev (y:ys) xs' = rev ys (y:xs')
```

To evaluate whether the properties are satisfied, we need to generate a collection of test cases, evaluate them and report the results of the test. To do this, we pick one of the test programs provided by GenCheck, and the best place to start is the friendly sounding module SimpleCheck. There are a number of test programs here that provide variations on how test cases are generated and results are reported. The name of the test program consists of three parts:

testsuite Describes the kind of test suite generated: std, deep, base

reporting Defines whether the first failure (Check), all failures (Test) or all results (Report) are printed to the screen

arguments functions ending in Args have additional parameters; those not ending in Args provide default values for these parameters and default test case generators (so must be instances of Testable, more on this class coming up soon).

The first property takes a value, puts it in a list, and tests that reversing the list doesn't change the value. This value could be of any Haskell type, but we have to pick one to actually run the tests, so we'll start with Char. Char is a "base" type (as opposed to a structure) so all of the elements of this type are the same size. SimpleCheck's baseTest, baseCheck, and baseReport are all appropriate as they don't distinguish test elements by size. We'll pick baseTest so that all of the test cases are evaluated, but only the failure cases are reported. Char is an instance of the Testable class, so we don't need to use the parameterized versions (baseTestArgs, etc.) and will settle for the default settings for now.

Note that the GenCheck test programs generally request the desired number of test cases as input, but then only uses that as a guide in developing the test suite. The actual number of test cases will vary according to the number of possible test cases in the test domain.

```
testUnitEq_1 = baseTest (propRevUnitEq :: Property Char) 100
```

The next property requires a list of values to reverse, so baseTest is no longer appropriate as it is only for scalar values. The test suite must have lists of a variety of different lengths; in GenCheck parlance the size of a structure is referred to as it's "rank". stdTest and deepTest both generate test suites for structures, with deepTest including much higher ranked test cases, but fewer at each rank. For lists, there is only one list structure for each rank, so we'll use deepTest (deepReport and deepCheck would produce the same test cases).

Setting the property to a list of Ints seems a good starting point, but in order to use the SimpleCheck test functions we need an instance of Testable. Is —[Int]— an instance of Testable or do we need to do something? Lists are instances of the Structure class, which provides the method to populate a structure with elements from another generator, and also an instance of Testable, so there are standard generators available. A default instance of Testable is provided for lists of any Testable type, and Ints are Testable, so we don't have to worry about how lists are generated - yet.

```
testRevIdem_1 = deepTest (propRevRevEq :: Property [Int]) 100
```

The tests are passing, but somewhat unsatisfying that we can't see the test cases. So, we switch to the baseReport / deepReport functions that report all of the results, flagging any failed test cases with "FAILED:". These are the same cases that were used for baseTest / deepTest, so we already know they will be successful, but using the Report versions will allow an evaluation of the quality of the test suite. The report dumps a lot of data onto the screen, so it made sense to verify the properties worked first with the Test functions so we didn't miss any of the FAILED flags.

```
testUnitEq_2 = baseReport (propRevUnitEq :: Property Char) 100
testRevIdem_2 = deepReport (propRevRevEq :: Property [Int]) 100
```

What happens when one or more test cases fail? Let's create a failing property, such as comparing a reversed list with the original. The very first test case with two elements in the list fails.

```
propRevEqNot :: (Eq a) \Rightarrow Property [a]
propRevEqNot xs = revList xs == xs

testRevEqNot_1 = deepTest (propRevEqNot :: Property [Int]) 100 -- should fail
```

We also see that *every* other case failed too - maybe we shouldn't print out all the failures! This is where using deepCheck comes in handy - it stops after the first failure case.

```
-- isn't implemented yet, so this is redundant
testRevEqNot_2 = deepCheck (propRevEqNot :: Property [Int]) 100
```

The SimpleCheck module provides a useful collection of simple test programs that start with default test parameters and test case generators, but allow the tester to make a few simple choices to customize the testing if desired. The simpleTest, simpleReport and simpleCheck functions are the glue to connect the reporting, test execution and test suite options for a test program.

The examples in this module have properties over standard Haskell types, where the default generators were already available. How are test cases generated when the module contains a new type? How are the test cases chosen for inclusion in the test suite, and how can that be controlled? Surely there is a better way to display the results? These questions and more are answered in the next part of the tutorial.

2 Tutorial 2: Testing with New Data Types

The first tutorial covered testing properties over standard Haskell types. Default test case generators were already supplied by GenCheck as instances of the Testable class, but what about new data types? In this tutorial, we explain how to use the type constructor definition and GenCheck enumeration combinators to construct the standard test generators based on the type constructor definitions.

There are three steps in testing a module against a specification using the GenCheck framework:

- 1. define and code the properties that make up the specification
- 2. select the test system that provides the most appropriate test scheduling and reporting schema for the current phase of the development
- 3. define the test suite for those properties, including the test case generators for each.

In the previous section the details of the test system and test suite generation were hidden by the SimpleCheck API. In this section, we look at each of these steps in detail and discuss how to generate new data types and customize test suites for a particular set of properties.

For this tutorial, we'll look at a list zipper implementation, taken from the ListZipper package (1.2.0.2). Only snippets of the code will be provided as the

package is rather large (see tutorial/list_zipper/ListZipper.hs for the module source). The Zipper data type is

```
data Zipper a = Zip ![a] ![a] deriving (Eq,Show)
```

where the "current" element or "cursor" is the head of the second list. The specification for ListZipper includes empty, cursor, start, end, left, right, foldrz, foldlz, and many more functions. The example below shows how to test (some) of the specification for this module, with a focus on the generators for the new type.

2.1 Specifications and Properties

A GenCheck specification is the collection of properties that any implementation of the specification must satisfy. Properties are univariate Boolean valued Haskell functions; this is not a restriction as the input value may be of an arbitrarily complicated type to support uncurried predicates. The GenCheck test programs accept a single property and test it over the defined suite of test cases. Only one property is tested per call because different properties may have different input types or require different test suites The specification module would normally be separate from the implementation, but may include functions that test the properties using GenCheck.

2.1.1 List Zipper Properties

A small set of properties from the ListZipper package specification.

```
module PropListZip where
import Test.GenCheck (Property)
import ListZipper as Zipper
```

A ziplist is empty iff the cursor is both at the beginning and the end

```
propEmptyP :: Property (Zipper a)
propEmptyP z = emptyp z == beginp z && endp z
```

Folding an operation over the zipper with the cursor at the start should be identical to folding it over the unzipped list. Note that the zipper fold folds the cursor through the zipper, but always passes the zipper to the function. (cursor safety is supposed to be guaranteed by the foldz' functions)

```
propFoldrz :: (Eq b) \Rightarrow (a \rightarrow b \rightarrow b) \rightarrow b \rightarrow Property (Zipper a) propFoldrz f y0 zxs = let xs = Zipper.toList zxs in (foldr f y0 xs == foldrz f' y0 (start zxs)) where f' zs y = f (cursor zs) y
```

```
propFoldlz :: (Eq b) \Rightarrow (b \rightarrow a \rightarrow b) \rightarrow b \rightarrow Property [a] propFoldlz f y0 xs =

let zxs = Zipper.fromList xs

fval = foldl f y0 xs

zxs' = start zxs

in (fval == foldlz f' y0 zxs') && (fval == foldlz' f' y0 zxs')

where f' y zs = f y (cursor zs)
```

Replace is equivalent to deleting the current element and inserting a new one.

```
propInsDelRepl :: (Eq a) \Rightarrow Property (a, Zipper a)
propInsDelRepl (x, xs) = Zipper.insert x (Zipper.delete xs) == Zipper.replace x xs
```

2.2 Test Suites and Standard Generators

The module System. TestSuite contains functions that assemble test suites from one or more test case generators. These suite builders take a collection of "standard" generators and a set of "generator instructions", a list of rank, count pairs. The allocation of test cases to ranks through these instructions is called a "test strategy" and can be used independently of the type of data being generated, assuming that the standard generators are available for that type.

A GenCheck generator is any function from a rank (positive integer) to a list of values. Generators may be finite or infinite, may include duplicates of the same value, and may be missing values from the total population of the type. Generators can be manually coded or built from a GenCheck enumeration of the type using a sampling strategy called an "enumerative strategy". These strategies can be applied to any data type that can be enumerated, i.e. ordered, and indexed by a finite rank.

The so called standard generators are just four different sampling strategies that can be applied to an enumeration of the generated type. These are:

exhaustive Produces all of the values of the specified rank in a sequence,

extreme Alternating lowest and highest values in the enumeration,

uniform Select the specified number elements at uniform intervals through the enumeration,

random Use the random generator to pick an infinite list of values.

The basis for the test suites used by SimpleCheck test programs are the standard generator set described above. These are not the only valuable sampling strategies that could be used, but these were selected as the "standard" generator strategies to be used by the GenCheck API. A type is an instance of Testable if a set of standard generators is available for it; these generators can be constructed for any type that has an Enumeration associated with it.

A test suite is a collection of test cases selected from the ranks of one or more generators. Each test suite uses a sampling "strategy" to decide which generators and at what rank to select the test cases; this mix is called the test strategy. The SimpleCheck test strategies draw test cases from the four standard generator strategies to provide a good sampling of the test cases relative to the number of tests performed. The strategies are heuristic of course, and the optimal composition of a test strategy depends on the nature of the structures and properties being tested, so these provided test suite strategies are really just a starting point. The TestSuite module contains the test suite building functions:

stdSuite exhaustive testing for smaller structures, then the boundary elements and a mix of uniformly and randomly selected values to the specified maximum rank

deepSuite similar to standard but for "narrow" structures with fewer elements per rank (i.e. a binary tree or list), so the exhaustive testing goes to a much higher rank

baseSuite a test suite for base types, where the rank is always 1

The System.SimpleCheck module test suites are test cases stored in a Haskell map (as in Data.Map) indexed by rank, called a MapRankSuite.

2.2.1 Enumerating New Data Types

A GenCheck enumeration is a way of ordering the values of a type, and is used as the basis for the standard test case generators in GenCheck. A generator can be any function that produces a list of values of the generated type. Since the values are in a list, the generator must order those elements, and the GenCheck enumerations are one way to provide a consistent index over the values. Note that generators do not have to provide all of the possible values of the type, nor is there a restriction against providing multiple instances of a value in any given list, so the position of an element in a generator's output is not generally the same as an enumeration.

Haskell structure types can be recursively defined and therefore arbitrarily large, even infinitely large with lazy evaluation. To allow any sort of ordering of these infinite sets, the values are first partitioned into finite subsets by the number of elements in the structure, which is called the rank of the structure. The common sized elements in the subset are then ordered and indexed using a depth first, sum of products view of the values. This allows most (any regularly recursive polynomial) structure type to be enumerated using a two tiered (rank, integer index) pair. Structure types that are enumerated are instances of the Enumerated class, which provides methods to count and select (construct) values of the specified rank and index.

A base type, such as Int or Char, do not have a rank and are enumerated if there is a single ordering over all of the elements of that type. This is called a base enumeration (BaseEnum) and is effectively the same as the Haskell Enum class; the GenCheck class is called EnumGC to highlight that it is an extension of Enum.

A generator may be constructed from an enumeration by mapping the selector method over a sorted list of integer indices. The GenCheck standard generators are created by applying the four standard strategies - exhaustive, boundary (extreme), uniform and random - over an enumeration of the type. These sampling strategies abstract the test plan from the concrete construction of particular instances of the test values, leaving the details of the specified type being tested to the enumeration methods.

Enumerations for standard Haskell data types such as list and tuples are provided. For new data types, enumerations can be easily made using the enumeration combinators —eConst, eNode, eSum, eProd, etc.— in the Generator.Enumeration module. These combinators simply mirror the structure of the type constructors to produce the required enumerations, and can be constructed mechanically.

A pure structure enumeration / generator constructs structures that are over a constant value (i.e. unit), so some method is required for substituting other values into the data nodes. One approach is to define the structure over a particular kind of element, and have the enumeration count all of those element types as distinct values of the structure. From a testing perspective, this creates an unfortunate imbalance in the number of values for any given size of structure vs. the relevance of the values in the structures' nodes. For example, when testing a heap sort insert, it would be nice to exhaustively test all shapes of heaps up to a certain size, but not necessarily exhaustively test all possible integer node values in each of those heap shapes. A better solution is to create a structure generator and sample it using the appropriate strategies, and then populate each of those shapes with one or more sets of values, also chosen from an appropriately sampling generator. GenCheck supports this kind of substitution at the generator level; a generator of structures Fooa is created by applying one of the substitution functions over a Foo generator and an a generator. A collection of substitution functions is available in the Generator. Substitution module, and provides the ability to populate each structure with one or more sets of elements, using different strategies such as all permutations, all combinations, or just unique elements. Substitution allows a great deal of control over the generation of complex data structures by decoupling the sampling strategy of the structures, the elements, and their substitution; this is one of the most important benefits of GenCheck over QuickCheck and SmallCheck.

2.2.2 List Zipper Enumeration and Generators

The GenCheck class Structure and Enumeration instances for Zipper. It is typical of what would be mechanically generated for the type, but has been converted to literate Haskell and documented. There is no special significance to the $_{G}C$ suffix in the name, that is just a convention so the GenCheck instances module is easily found.

```
{-# LANGUAGE FlexibleInstances,FlexibleContexts #-}
module ListZipper_GC where
import Control.Monad (liftM2)
import Test.GenCheck
import Test.GenCheck.Generator.Enumeration
--import Test.GenCheck.Generator.Generator (Testable(..))
--import Test.GenCheck.Generator.StructureGens()
--import Test.GenCheck.Generator.Substitution (Structure(..))
import ListZipper
```

The Structure class has a single method called substitute. It replaces the elements in the structure with elements from a list and returns a newly populated instance of the structure and the remaining elements; if there are insufficient elements in the list to populate the structure Nothing is returned along with the original list of elements.

A default substitution method can be mechanically derived for algebraic data types, by interpreting the type as a sum of products, and using substitute methods for any substructures. Alternate substitutions could be provided instead.

```
instance Structure Zipper where
  substitute = substZipper

substZipper :: Zipper a → [b] → (Maybe (Zipper b), [b])
substZipper (Zip x1 x2) ys =
  let (mx1, ys') = substitute x1 ys
        (mx2, ys'') = substitute x2 ys'
        zip' = liftM2 Zip mx1 mx2
  in (zip', ys'')
```

The Zipper is just a product of two lists of like elements. The enumeration is built from the combinators eProd and eList (list gets a special combinator due to it's frequent appearance and special syntax).

The Enumeration consists of two functions that, given a rank, produce the number of structures and a selector function that generates a structure given an index. These functions are highly recursive, so are memoized using the Memoize Hackage (eMemoize just applies memoize to both the count and selector functions in the Enumeration records).

The selector function from the Enumeration creates instances of the structure. The Label type is used as a way to instantiate those structures and provide a label for the parametric type variables in the structure as a convenience.

```
instance Testable (Zipper Label) where
  stdTestGens = stdEnumGens
instance Enumerated Zipper where
```

```
enumeration = eZipper
eZipper :: Enumeration Zipper Label
eZipper = eMemoize e
  where
    e = eProd Zip (eList A) (eList A)

    Gordon says: This should be in Test.GenCheck.Generator.Enumeration ????
( ???)
eList :: a → Enumeration [] a
eList x = mkEnum c s
  where c _ = 1 -- there is only one list of any length
    s r k | k == 1 = take r $ repeat x
    s _ _ | otherwise = error "Selector error"
```

Generators are created from enumerations and enumerative strategies using Generator.enumGenerator for structure types and BaseGen.baseEnumGen for base types. The standard generator set, and therefore the Testable instance, is built using stdEnumGens.

2.3 The Testing Process

Typically a GenCheck user would start with the default test suites and only reporting failures during the development cycle. Nearing completion, s/he would switch to the test programs that provide more control over the test suite generation, and report all of the test cases in the results to ensure good coverage.

2.3.1 Testing the List Zipper Module

```
{\tt genValZip\_Char} \ :: \ {\tt Rank} \ \to \ {\tt [(Char, Zipper \ Char)]}
genValZip\_Char r =
  let gc = (genUpperCharRnd (mkStdGen 657985498)) -- random value generator
      gz = genAll genZip_Char -- exhaustive zipper generator
  in zip (gc 1) (gz r) -- (Char, Zipper Char) generator with random Char, exhaustive zippers
testFoldrz_1, testFoldrz_2 :: Rank \rightarrow Count \rightarrow IO (r)
testFoldrz_1 r n =
  let propFoldrz_str = propFoldrz (:) "" :: Property (Zipper Char)
      lbl = "Compare concatenating strings with right fold, up to rank " +\!+\!
(show r)
  in stdTestArgs genZip_Char lbl r propFoldrz_str n
testFoldrz_2 r n =
  let propFoldrz_str = propFoldrz (:) "" :: Property (Zipper Char)
      lbl = "Compare concatenating strings with right fold, up to rank " +\!+\!
(show r)
  in stdReportArgs genZip_Char lbl r propFoldrz_str n
\texttt{testFoldlz\_1, testFoldlz\_2} \ :: \ \texttt{Rank} \ \to \ \texttt{Count} \ \to \ \texttt{IO} \ \ (\texttt{r})
testFoldlz_1 r n =
  let propFoldlz_sum = propFoldlz (+) 0 :: Property [Int]
      lbl = "Compare sum over integer list to left fold, up to rank " ++ (show r)
  in stdTest propFoldlz_sum n
testFoldlz_2 r n =
  let propFoldlz_sum = propFoldlz (+) 0 :: Property [Int]
      lbl = "Compare sum over integer list to left fold, up to rank " ++ (show r)
  in stdReport propFoldlz_sum n
\texttt{testInsDelRepl\_1} \; :: \; \texttt{Rank} \; \rightarrow \; \texttt{IO} \; \; (\texttt{r})
testInsDelRepl_1 r =
  let lbl = "Compare insert/delete to replace, up to rank " ++ (show r)
      -- do up to maxr tests for zippers up to rank maxr
      instruct maxr = [(rk, toInteger maxr) | rk ← [1..maxr]]
      suite = genSuite genValZip_Char (instruct r)
  in simpleReport lbl propInsDelRepl suite
```