SICP

God's Programming Book

Lecture-18 Composition

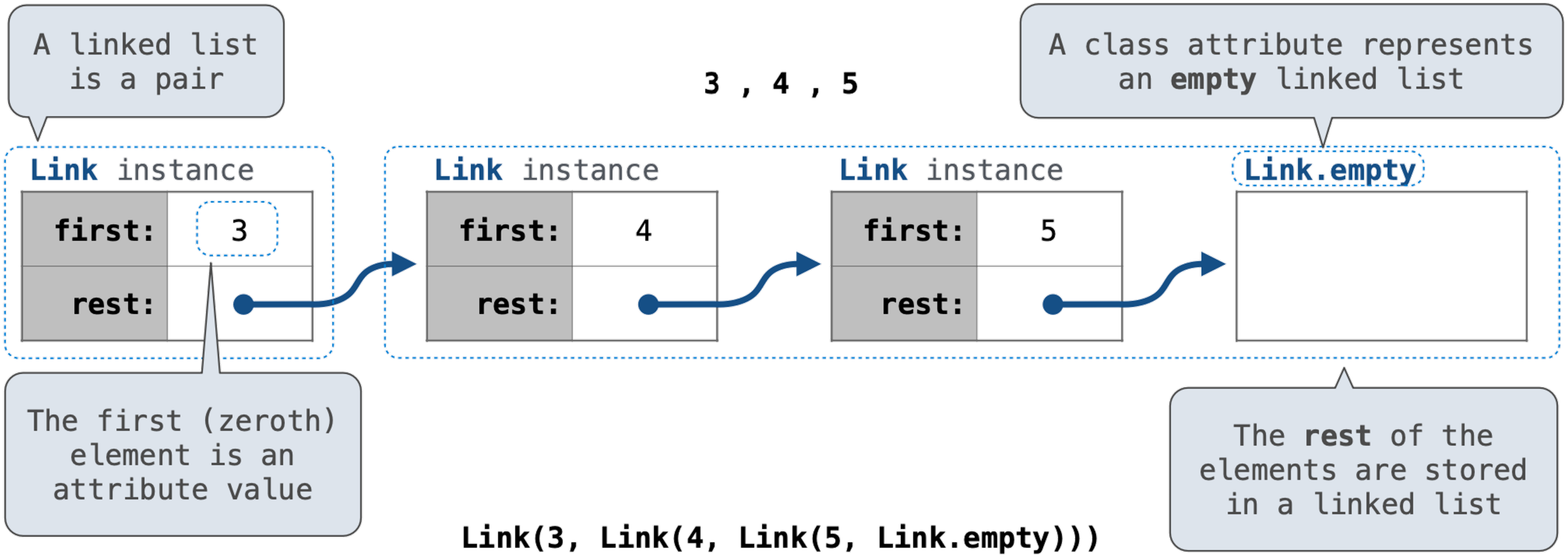
Composition

Slides Adapted from cs61a of UC Berkeley

Linked Lists

Linked List Structure

A linked list is either empty **or** a first value and the rest of the linked list



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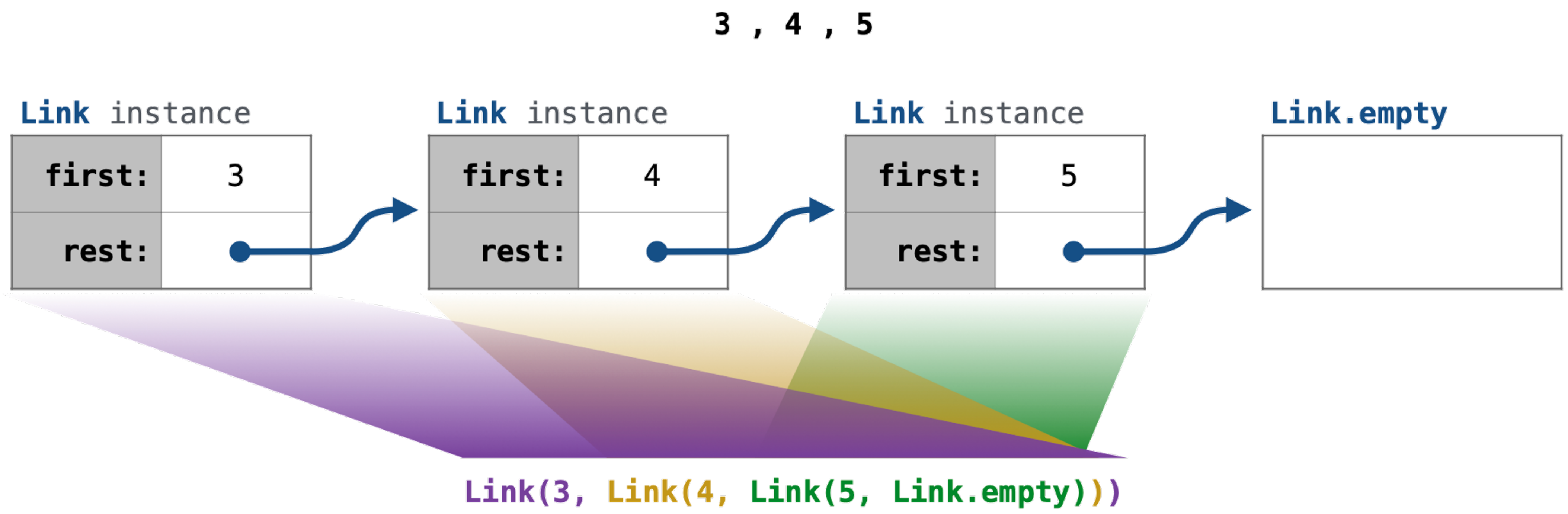

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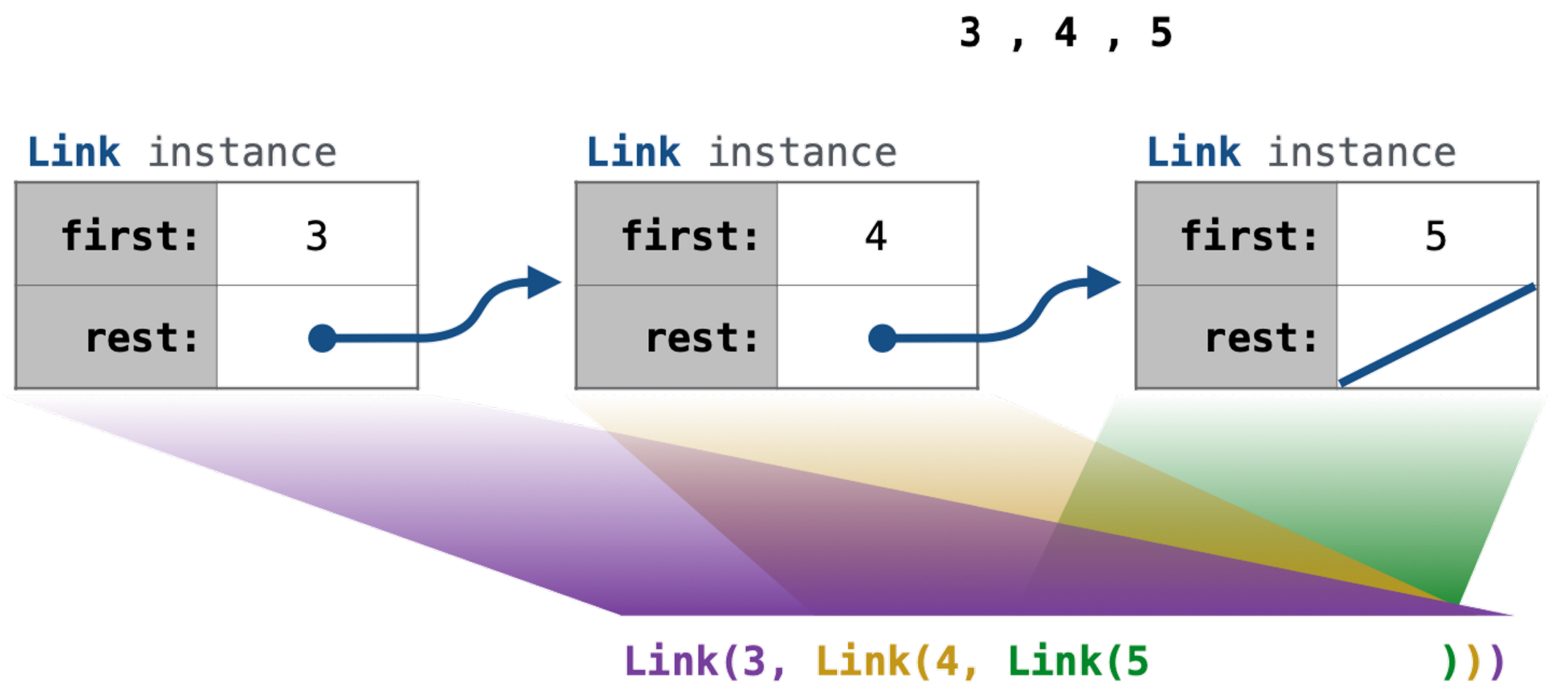


Linked List Class

Linked list class: attributes are passed to __init__

```
class Link:

    empty = ()

    def __init__(self, first, rest=empty):
        assert rest is Link.empty or isinstance(rest, Link)
        self.first = first
        self.rest = rest
```

Some zero-length sequence

Returns whether rest is a Link

help(isinstance): Return whether an object is an instance of a class or of a subclass thereof.

`Link(3, Link(4, Link(5          )))`

Linked List Processing

Example: Range, Map, and Filter for Linked Lists

```
square, odd = lambda x: x * x, lambda x: x % 2 == 1
list(map(square, filter(odd, range(1, 6))))          # [1, 9, 25]
map_link(square, filter_link(odd, range_link(1, 6)))  # Link(1, Link(9, Link(25)))

def range_link(start, end):
    """Return a Link containing consecutive integers from start to end.

    >>> range_link(3, 6)
    Link(3, Link(4, Link(5)))
    """


def map_link(f, s):
    """Return a Link that contains f(x) for each x in Link s.

    >>> map_link(square, range_link(3, 6))
    Link(9, Link(16, Link(25)))
    """


def filter_link(f, s):
    """Return a Link that contains only the elements x of Link s for which f(x)
    is a true value.

    >>> filter_link(odd, range_link(3, 6))
    Link(3, Link(5))
    """
```

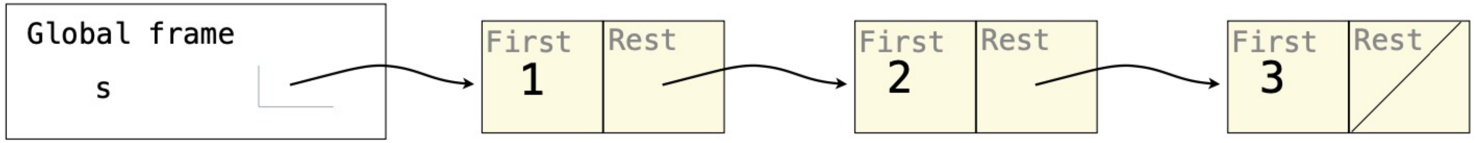
Linked Lists Mutation

Linked Lists Can Change

Attribute assignment statements can change first and rest attributes of a Link

The rest of a linked list can contain the linked list as a sub-list

```
>>> s = Link(1, Link(2, Link(3)))
```



Note: The actual environment diagram is much more complicated.

Linked Lists Can Change

Attribute assignment statements can change first and rest attributes of a Link

The rest of a linked list can contain the linked list as a sub-list

```
>>> s = Link(1, Link(2, Link(3)))
>>> s.first = 5
>>> t = s.rest
>>> t.rest = s
>>> s.first
5
>>> s.rest.rest.rest.rest.rest.first
2
```

```
Note: The actual
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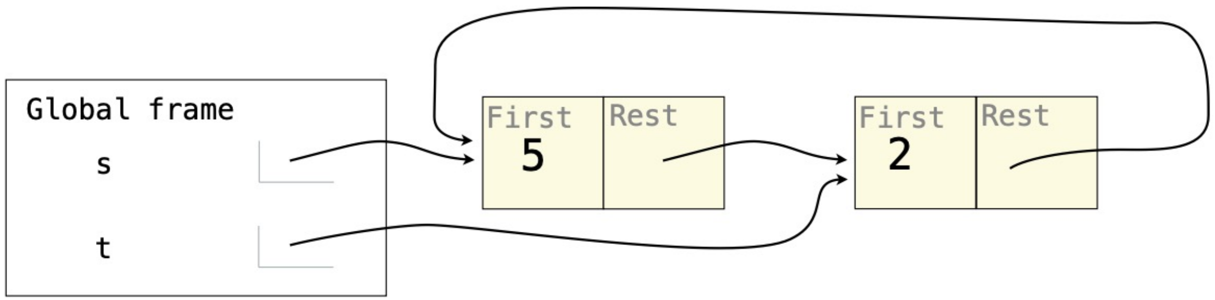

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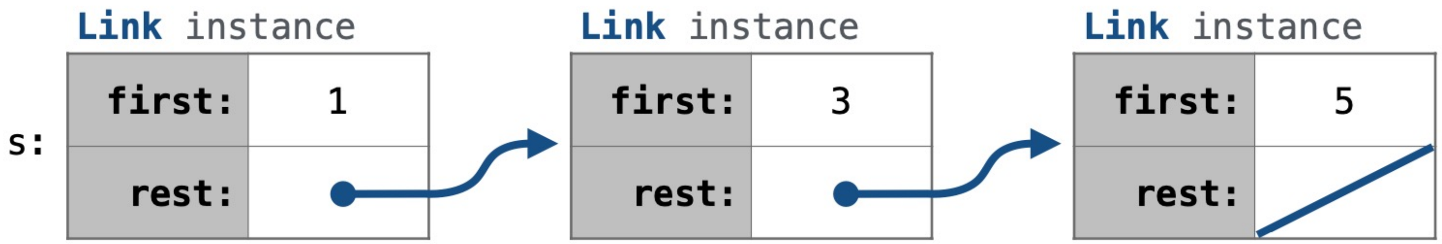
Linked List Mutation Example

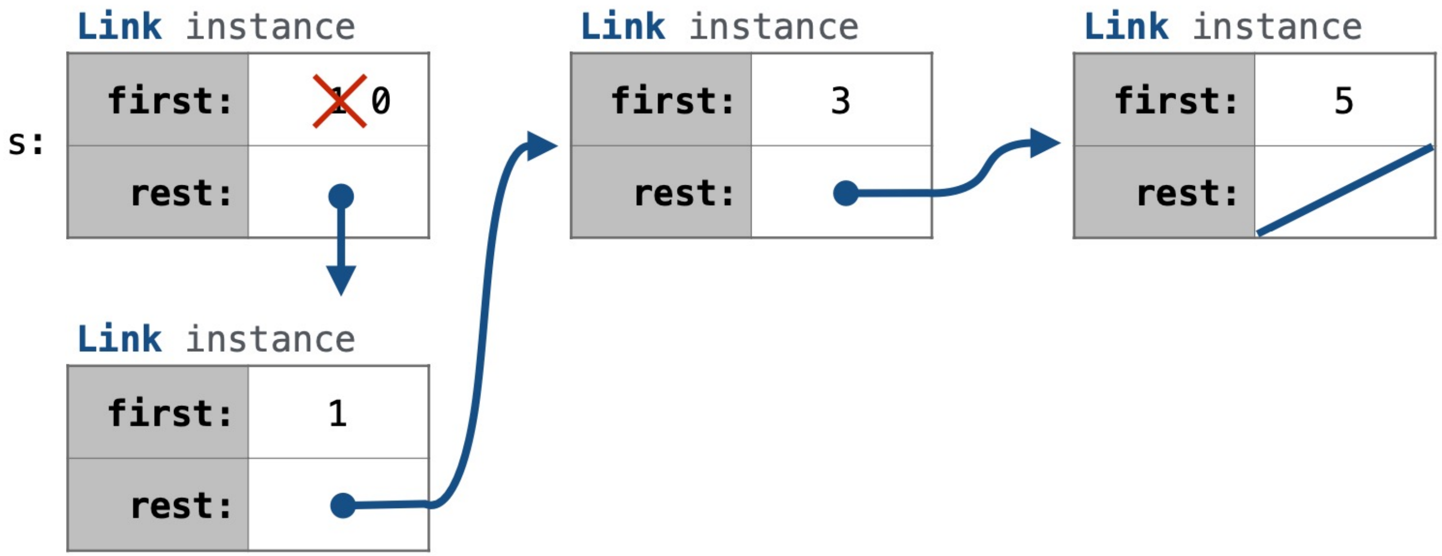
Adding to an Ordered List




```
def add(s, v):
    """Add v to an ordered list s with no repeats, returning modified s."""
    (Note: If v is already in s, then don't modify s, but still return it.)

        add(s, 0)
```

Adding to an Ordered List

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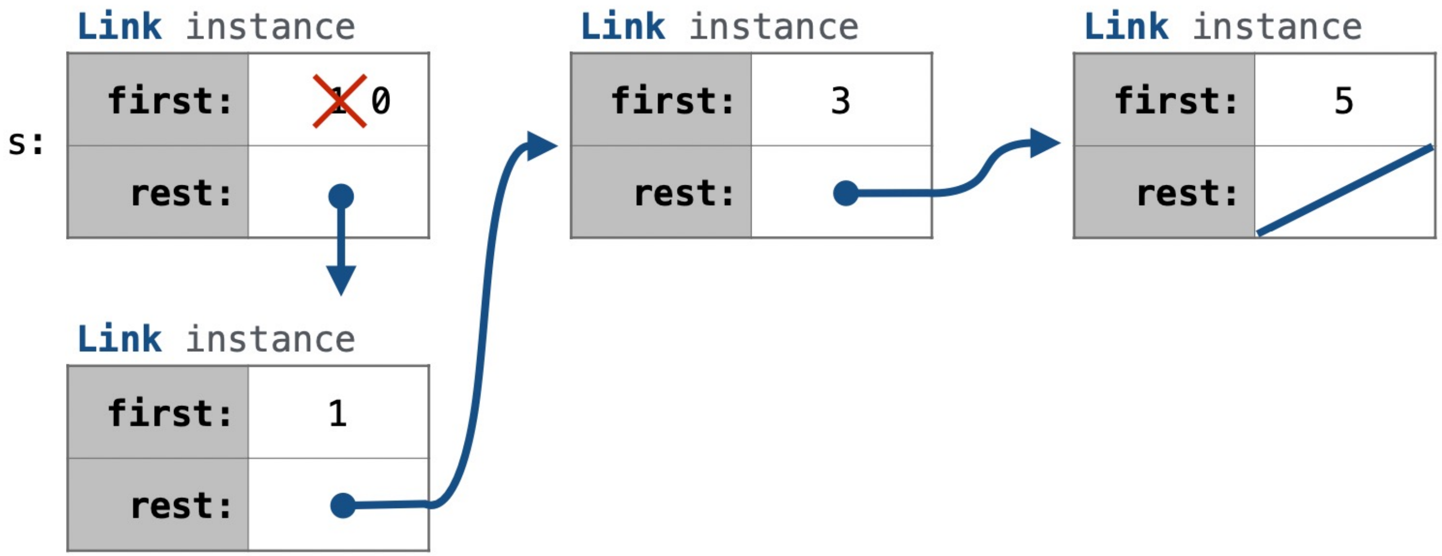
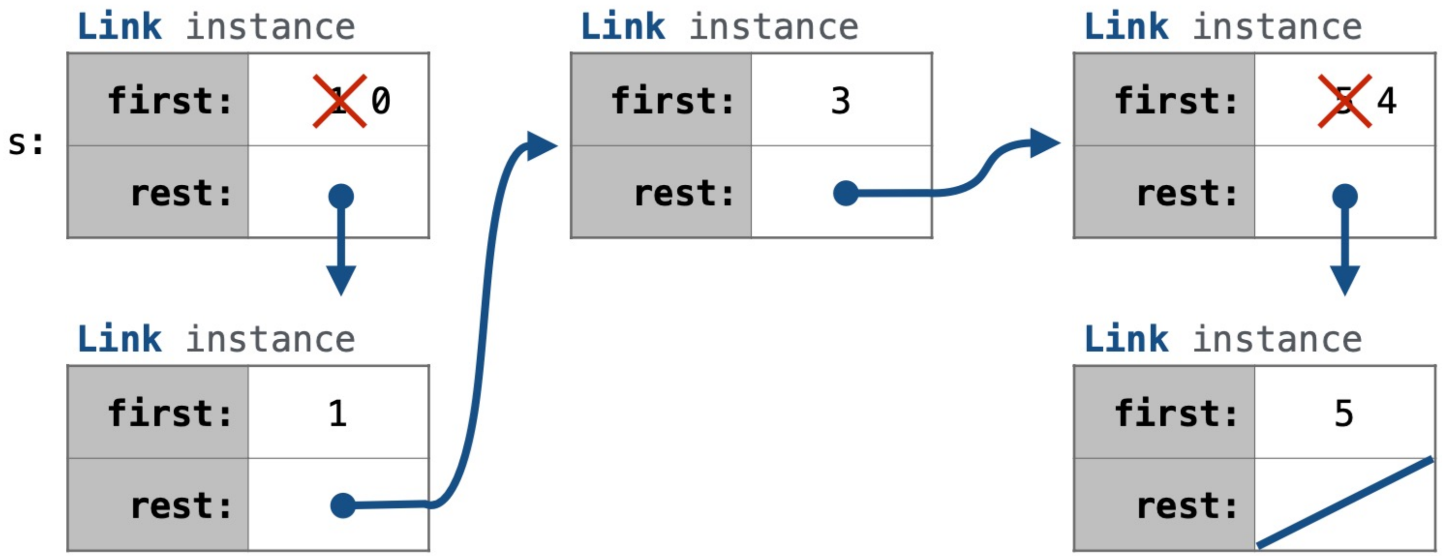



```
def add(s, v):
    """Add v to an ordered list s with no repeats, returning modified s."""
    (Note: If v is already in s, then don't modify s, but still return it.)

        add(s, 0)      add(s, 3)      add(s, 4)
```

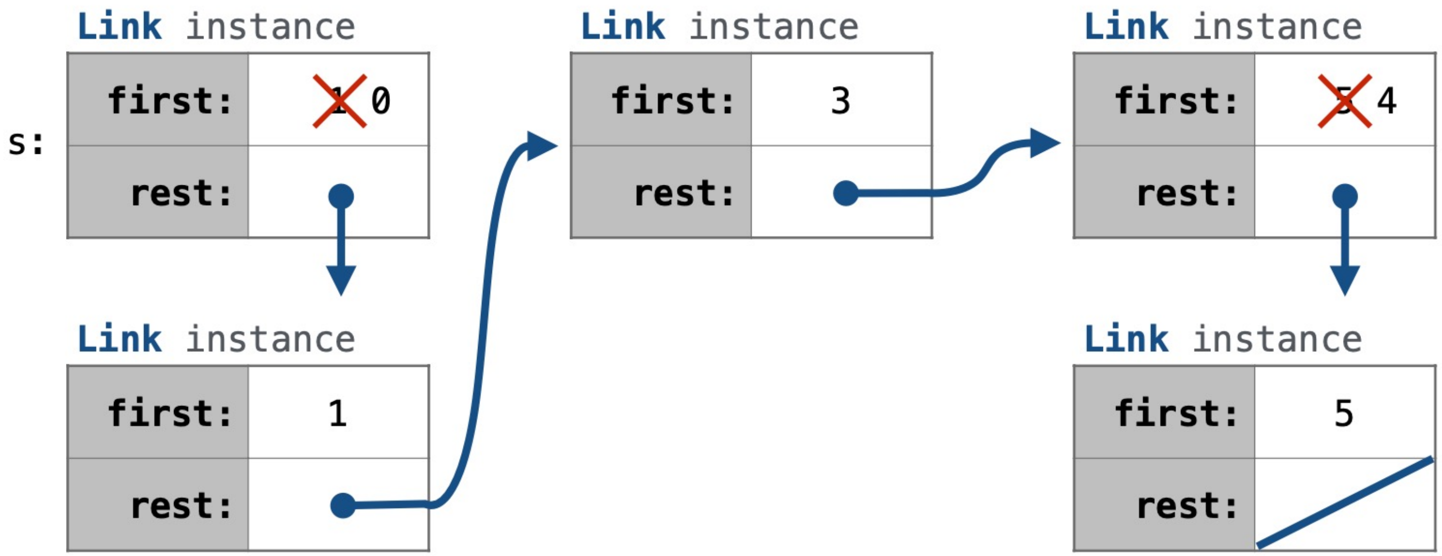
Adding to an Ordered List




```
def add(s, v):
    """Add v to an ordered list s with no repeats..."""
```

```
add(s, 0)      add(s, 3)      add(s, 4)
```

Adding to an Ordered List

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def add(s, v):
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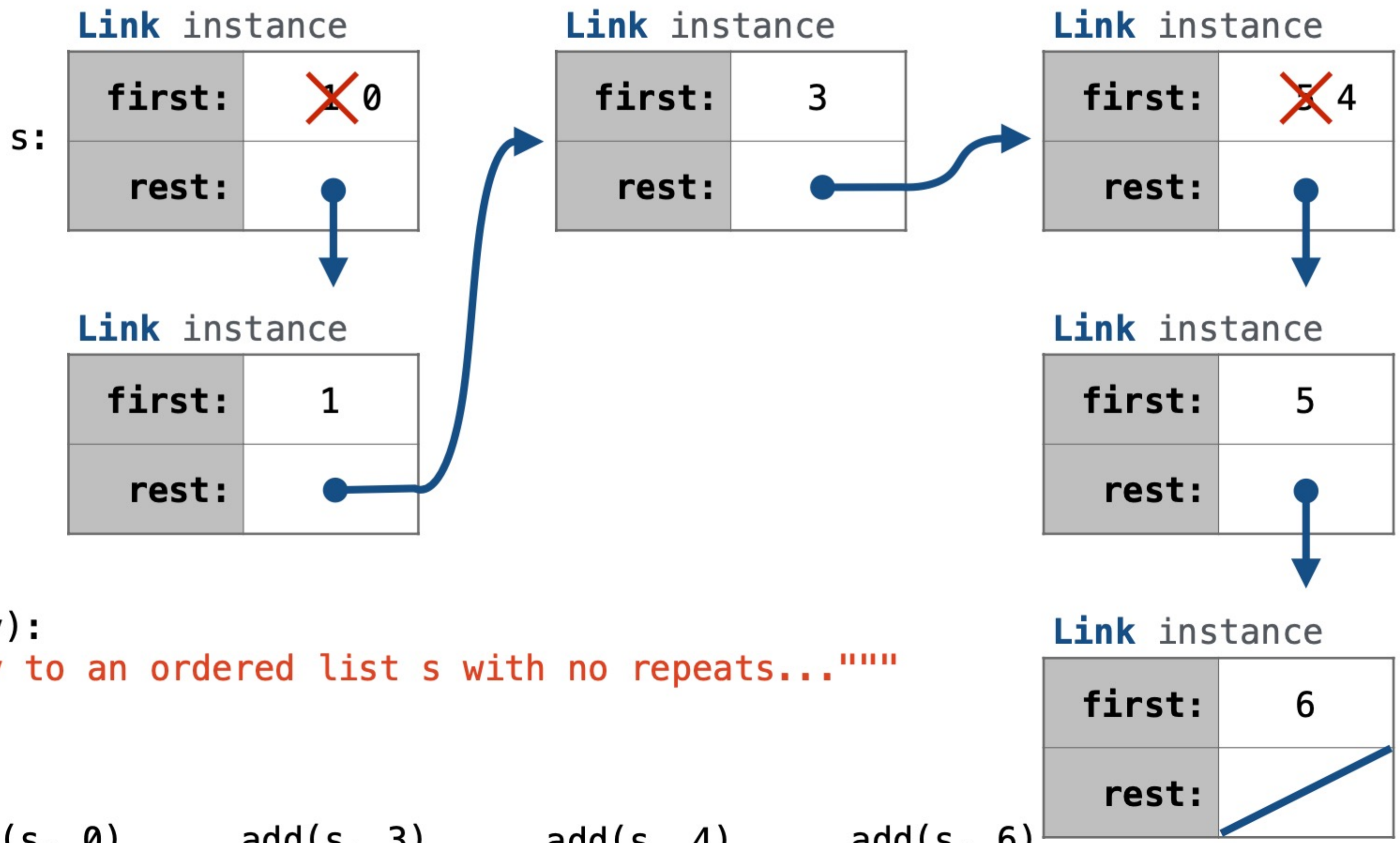
```
add(s, 0)    add(s, 3)    add(s, 4)    add(s, 6)
```

Adding to an Ordered List



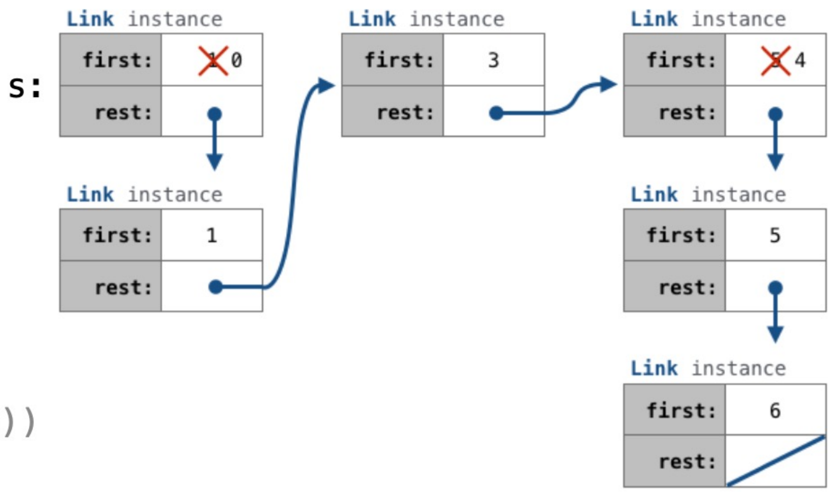

```
def add(s, v):
    """Add v to an ordered list s with no repeats..."""
```

```
add(s, 0)      add(s, 3)      add(s, 4)      add(s, 6)
```

Adding to a Set Represented as an Ordered List

```
def add(s, v):
    """Add v to s, returning modified s."""

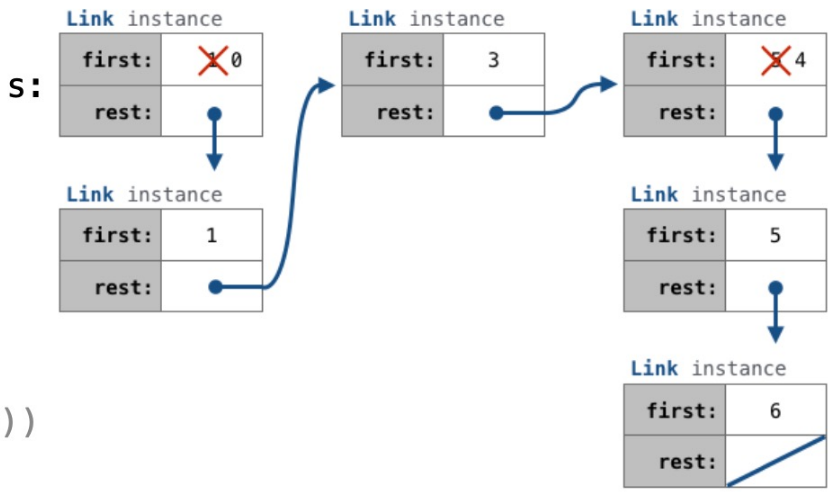
    >>> s = Link(1, Link(3, Link(5)))
    >>> add(s, 0)
    Link(0, Link(1, Link(3, Link(5))))
    >>> add(s, 3)
    Link(0, Link(1, Link(3, Link(5))))
    >>> add(s, 4)
    Link(0, Link(1, Link(3, Link(4, Link(5)))))
    >>> add(s, 6)
    Link(0, Link(1, Link(3, Link(4, Link(5, Link(6))
    """
    assert s is not List.empty
    if s.first > v:
        s.first, s.rest = __________________________ , ____________________________
    elif s.first < v and empty(s.rest):
        s.rest = ___________________________________________________________________
    elif s.first < v:
        ____________________________________________________________________________
    return s
```



Adding to a Set Represented as an Ordered List

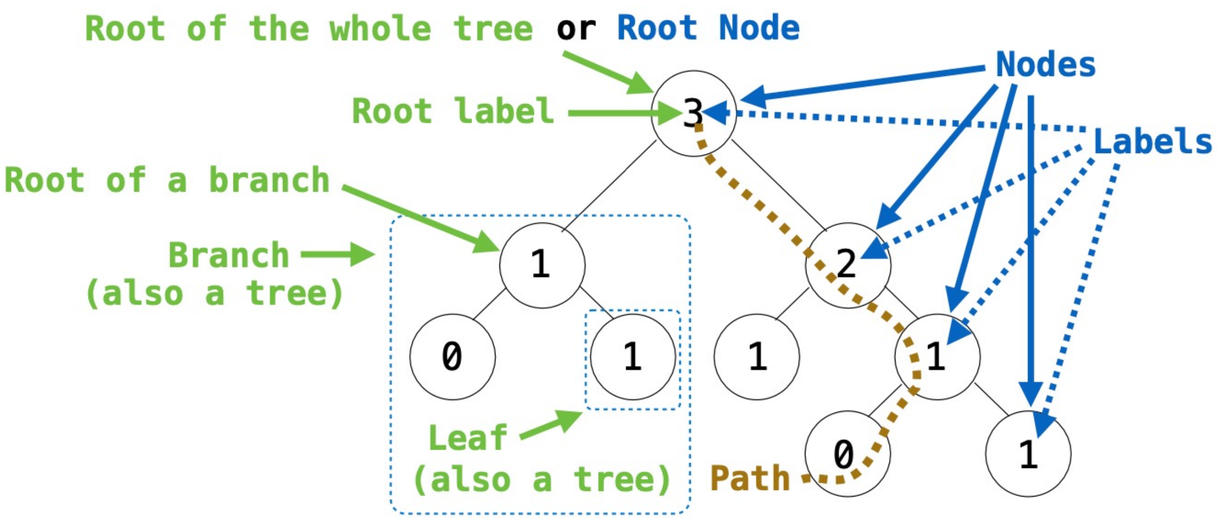
```
def add(s, v):
    """Add v to s, returning modified s."""

    >>> s = Link(1, Link(3, Link(5)))
    >>> add(s, 0)
    Link(0, Link(1, Link(3, Link(5))))
    >>> add(s, 3)
    Link(0, Link(1, Link(3, Link(5))))
    >>> add(s, 4)
    Link(0, Link(1, Link(3, Link(4, Link(5)))))
    >>> add(s, 6)
    Link(0, Link(1, Link(3, Link(4, Link(5, Link(6))
    """
    assert s is not List.empty
    if s.first > v:
        s.first, s.rest = ____v____ , ____Link(s.first, s.rest)____
    elif s.first < v and empty(s.rest):
        s.rest = ____Link(v)____
    elif s.first < v:
        ____add(s.rest, v)____
    return s
```



Tree Class

Tree Abstraction (Review)



Recursive description (wooden trees):

A **tree** has a **root label** and a list of **branches**

Each **branch** is a **tree**

A **tree** with zero **branches** is called a **leaf**

A **tree** starts at the **root**

Relative description (family trees):

Each location in a tree is called a **node**

Each **node** has a **label** that can be any value

One node can be the **parent/child** of another

The top node is the **root node**

People often refer to labels by their locations: "each parent is the sum of its children"

Tree Class

A Tree has a label and a list of branches; each branch is a Tree

```
class Tree:
    def __init__(self, label, branches=[]):
        self.label = label
        for branch in branches:
            assert isinstance(branch, Tree)
        self.branches = list(branches)
```

```
def tree(label, branches=[]):
    for branch in branches:
        assert is_tree(branch)
    return [label] + list(branches)
def label(tree):
    return tree[0]
def branches(tree):
    return tree[1:]
```

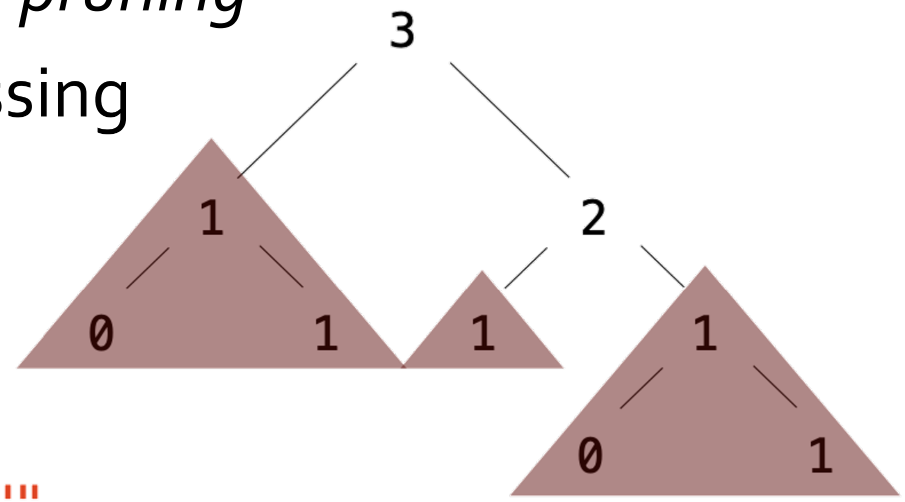
```
def fib_tree(n):
    if n == 0 or n == 1:
        return Tree(n)
    else:
        left = fib_tree(n-2)
        right = fib_tree(n-1)
        fib_n = left.label + right.label
        return Tree(fib_n, [left, right])
```

```
def fib_tree(n):
    if n == 0 or n == 1:
        return tree(n)
    else:
        left = fib_tree(n-2)
        right = fib_tree(n-1)
        fib_n = label(left) + label(right)
        return tree(fib_n, [left, right])
```

Tree Mutation

Example: Pruning Trees

- Removing subtrees from a tree is called *pruning*
- Prune branches before recursive processing




```
def prune(t, n):
    """Prune all sub-trees whose label is n."""
    t.branches = [______________ for b in t.branches if _____________________]
    for b in t.branches:
        prune(_______________________________, _______________________________)
```

Example: Pruning Trees

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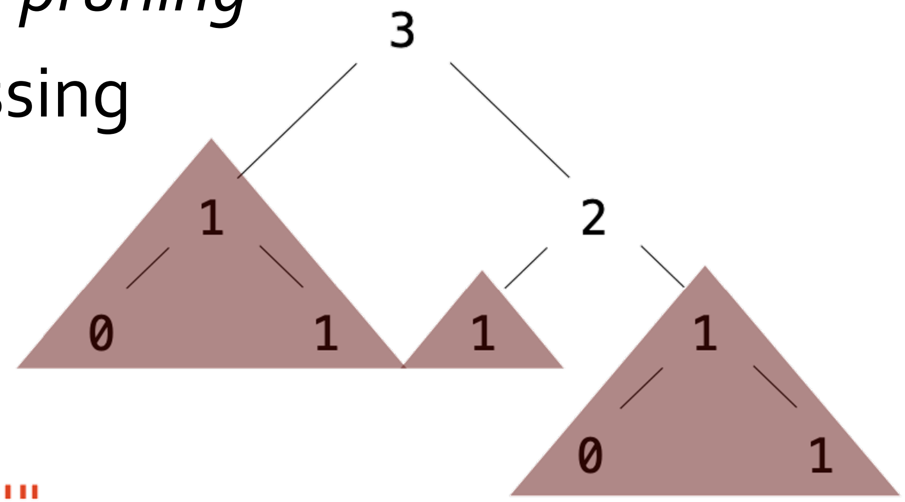


```
def prune(t, n):
    """Prune all sub-trees whose label is n."""
    t.branches = [b for b in t.branches if b.label != n]
    for b in t.branches:
        prune(b, n)
```

Thanks for Listening