CS4495/6495 Introduction to Computer Vision

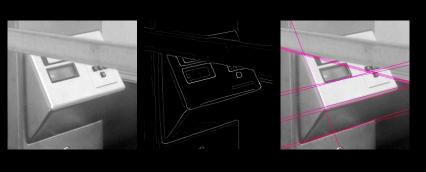
2B-L1 Hough transform: Lines

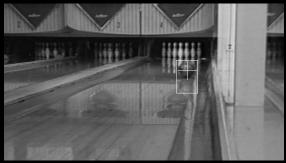
Now some "real" vision...

Image processing: $F: I(x, y) \longrightarrow I'(x, y)$

Real vision: $F: I(x, y) \longrightarrow \text{good stuff}$

Fitting a model











Parametric model

- A *parametric* model can represent a class of instances where each is defined by a value of the parameters.
- Examples include lines, or circles, or even a parameterized template.

Fitting a parametric model

- Choose a parametric model to represent a set of features
- Membership criterion is not local:
 Can't tell whether a point in the image belongs to a given model just by looking at that point
- Computational complexity is important
 Not feasible to examine possible parameter setting

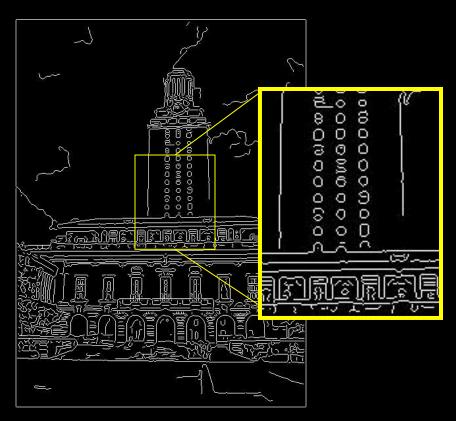
Example: Line fitting







Difficulty of line fitting



- Extra edge points (clutter), multiple models.
- Only some parts of each line detected, and some parts are missing.
- Noise in measured edge points, orientations.

Voting

It's not feasible to check all possible models or all combinations of features (e.g. edge pixels) by fitting a model to each possible subset.

Voting is a general technique where we let the features vote for all models that are compatible with it.

- 1. Cycle through features, each casting votes for model parameters.
- 2. Look for model parameters that receive a lot of votes.

Voting – why it works

- Noise & clutter features will cast votes too, but typically their votes should be inconsistent with the majority of "good" features.
- Ok if some features not observed, as model can span multiple fragments.

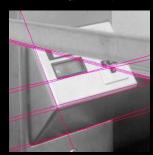
Fitting lines

To fit lines we need to answer a few questions:

- Given points that belong to a line, what is the line?
- How many lines are there?
- Which points belong to which lines?





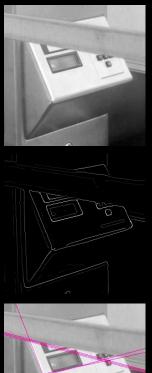


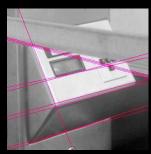
Fitting lines

Hough Transform is a voting technique that can be used to answer all of these

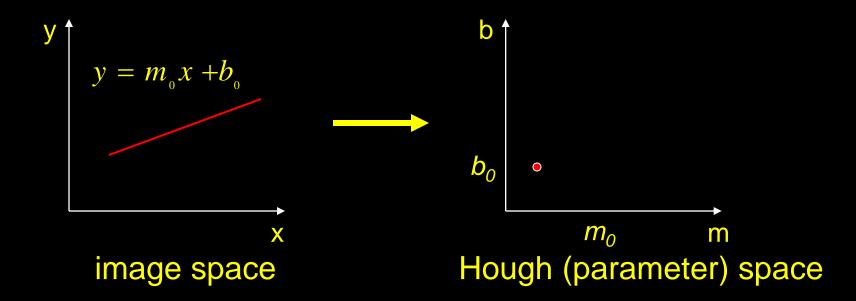
Main idea

- Each edge point votes for compatible lines.
- 2. Look for lines that get many votes.



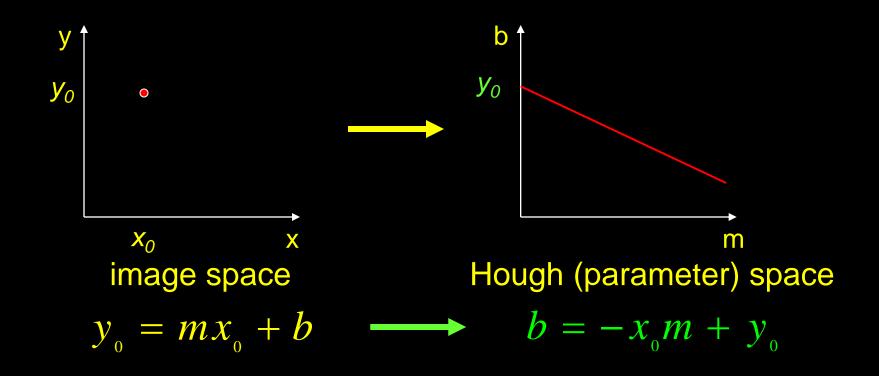


Hough space

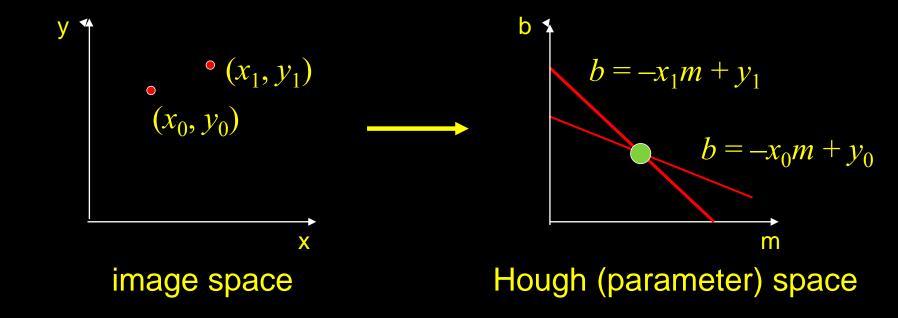


A line in the image corresponds to a point in Hough space

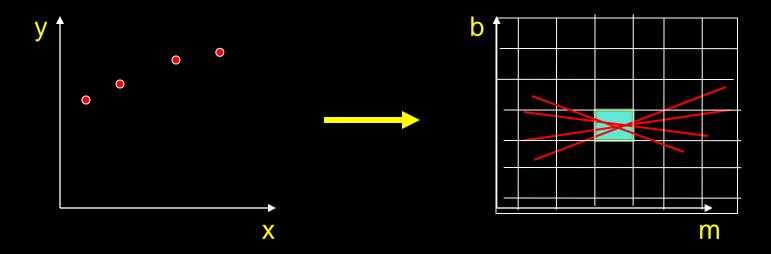
Hough space



Hough space



Hough algorithm

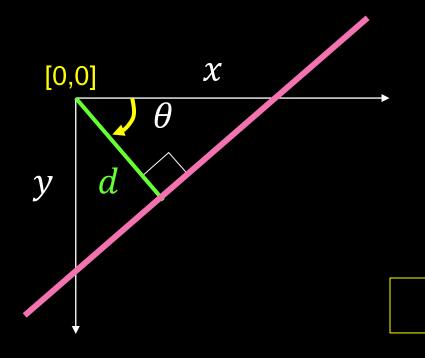


- Let each edge point in image space vote for a set of possible parameters in Hough space
- Accumulate votes in discrete set of bins; parameters with the most votes indicate line in image space.

Line representation issues

- Before we implement this we need to rethink our representations of lines.
- As you may remember, there are issues with the y – mx + b representation of line.
- In particular, undefined for vertical lines with m being infinity. So we use a more robust polar representation of lines.

Polar representation for lines

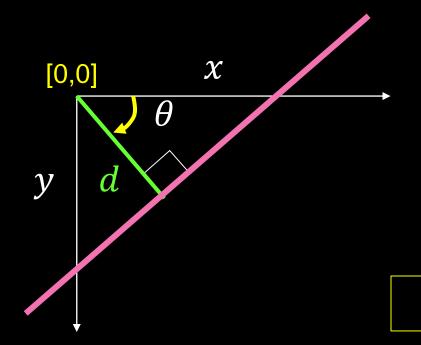


d: perpendicular distance from line to origin

 θ : angle the perpendicular makes with the x-axis

$$x\cos\theta + y\sin\theta = d$$

Polar representation for lines



d: perpendicular distance from line to origin

 θ : angle the perpendicular makes with the x-axis

$$x \cos\theta + y \sin\theta = d$$

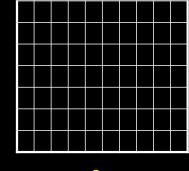
Point in image space is now sinusoid segment in Hough space

Hough transform algorithm

Using the polar parameterization:

$$x\cos\theta + y\sin\theta = d$$

And a Hough Accumulator Array (keeps the votes)



 θ

Source: Steve Seitz

Basic Hough transform algorithm

- 1. Initialize $H[d, \theta] = 0$
- 2. For each *edge* point in E(x,y) in the image for θ = -90 to +90 // some quantization; why not 2pi? $d = x\cos\theta + y\sin\theta \quad // \text{ maybe negative}$ $H[d, \theta] += 1$
- 3. Find the value(s) of (d, θ) where H[d, θ] is maximum
- 4. The detected line in the image is given by $\mathbf{d} = x \cos \theta + y \sin \theta$

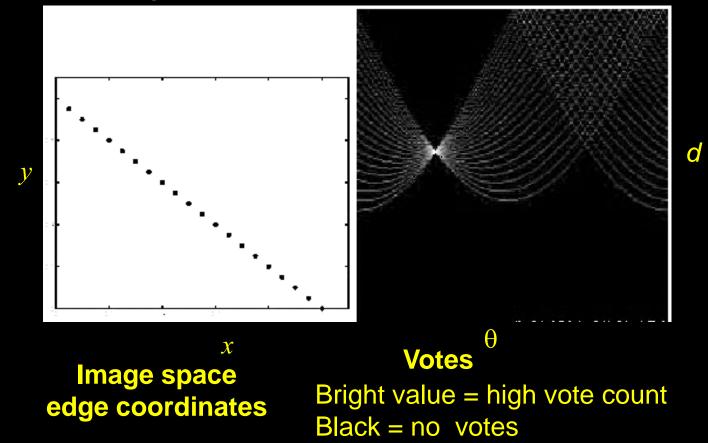
Source: Steve Seitz

Complexity of the Hough transform

Space complexity? k^n (n dimensions, k bins each)

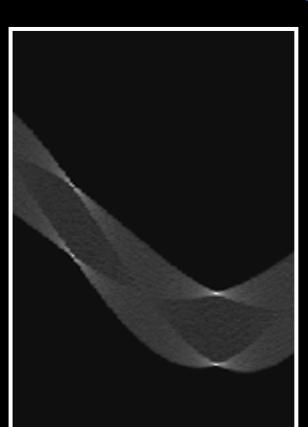
Time complexity (in terms of number of voting elements)?

Hough example

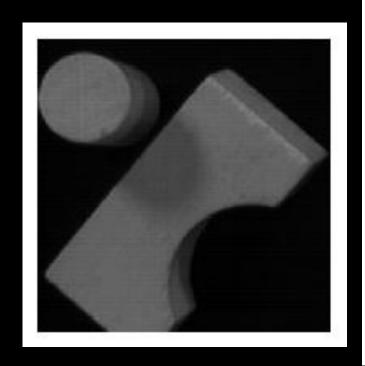


Example: Hough transform of a square

Square:



Hough transform of blocks scene





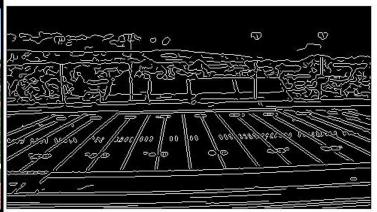
Hough Demo

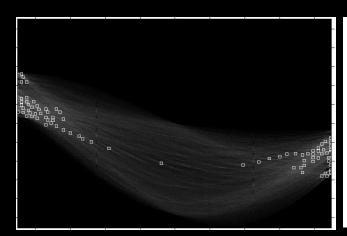
```
% Hough Demo
pkg load image; % Octave only
%% Load image, convert to grayscale and apply Canny operator to find edge pixels
img = imread('shapes.png');
grays = rgb2gray(img);
edges = edge(grays, 'canny');
%% Apply Hough transform to find candidate lines
[accum theta rho] = hough(edges); % Matlab (use houghtf in Octave)
figure, imagesc(accum, 'XData', theta, 'YData', rho), title('Hough accumulator');
%% Find peaks in the Hough accumulator matrix
peaks = houghpeaks(accum, 100); % Matlab (use immaximas in Octave)
hold on; plot(theta(peaks(:, 2)), rho(peaks(:, 1)), 'rs'); hold off;
```

Hough Demo (contd.)

```
%% Find lines (segments) in the image
line segs = houghlines(edges, theta, rho, peaks); % Matlab
figure, imshow(img), title('Line segments');
hold on:
for k = 1:length(line_segs)
   endpoints = [line segs(k).point1; line segs(k).point2];
   plot(endpoints(:, 1), endpoints(:, 2), 'LineWidth', 2, 'Color', 'green');
end
hold off;
%% Play with parameters to get more precise lines
peaks = houghpeaks(accum, 100, 'Threshold', ceil(0.6 * max(accum(:))), 'NHoodSize', [5 5]);
line_segs = houghlines(edges, theta, rho, peaks, 'FillGap', 50, 'MinLength', 100);
```



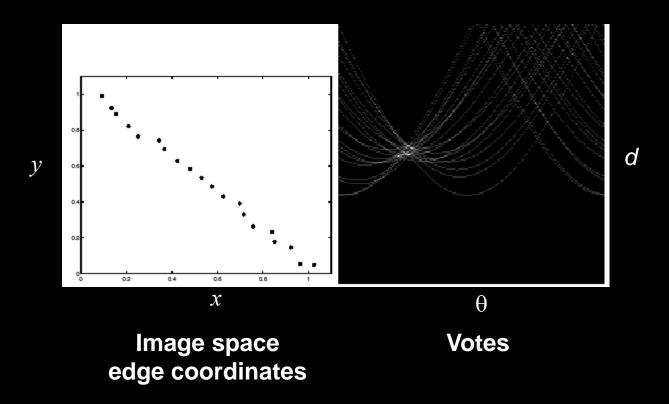




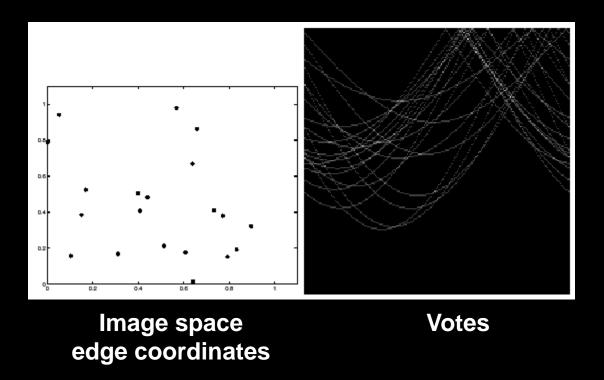


Showing longest segments found

Impact of noise on Hough



Impact of more noise on Hough



Extensions – using the gradient

1. Initialize H[d, θ]=0

 $H[d, \theta] += 1$

- 2. For each *edge* point in E(x, y) in the image $\theta = \text{gradient at } (x,y)$ $d = x \cos \theta + y \sin \theta$
- 3. Find the value(s) of (d, θ) where H[d, θ] is maximum
- 4. The detected line in the image is given by $d = x\cos\theta + y\sin\theta$



$$\nabla f = \left[\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}\right]$$

$$\theta = \tan^{-1}(\frac{\partial f}{\partial y} / \frac{\partial f}{\partial x})$$

Extensions

Extension 2

Give more votes for stronger edges

Extension 3

change the sampling of (d, θ) to give more/less resolution

Extension 4

The same procedure can be used with circles, squares, or any other shape