

CS4495/6495

Introduction to Computer Vision

3B-L2 *Epipolar geometry*

Depth from disparity

image $I(x,y)$

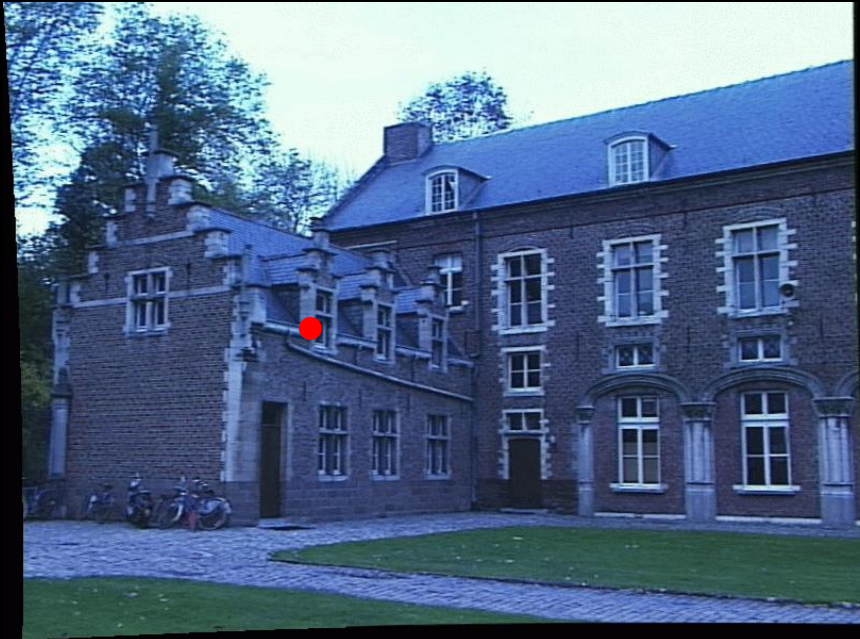


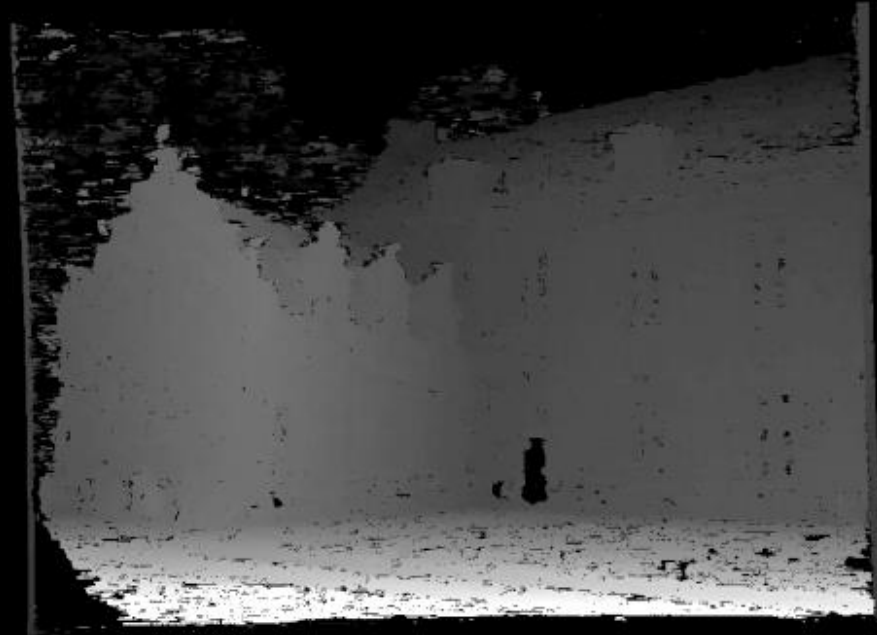
image $I'(x,y)$



Depth from disparity

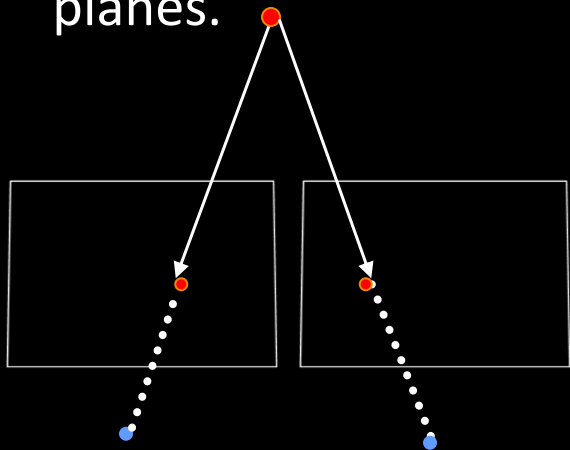
image $I(x,y)$

Disparity map $D(x,y)$

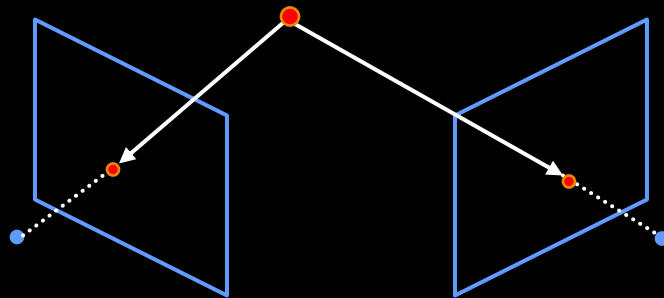


General case, with calibrated cameras

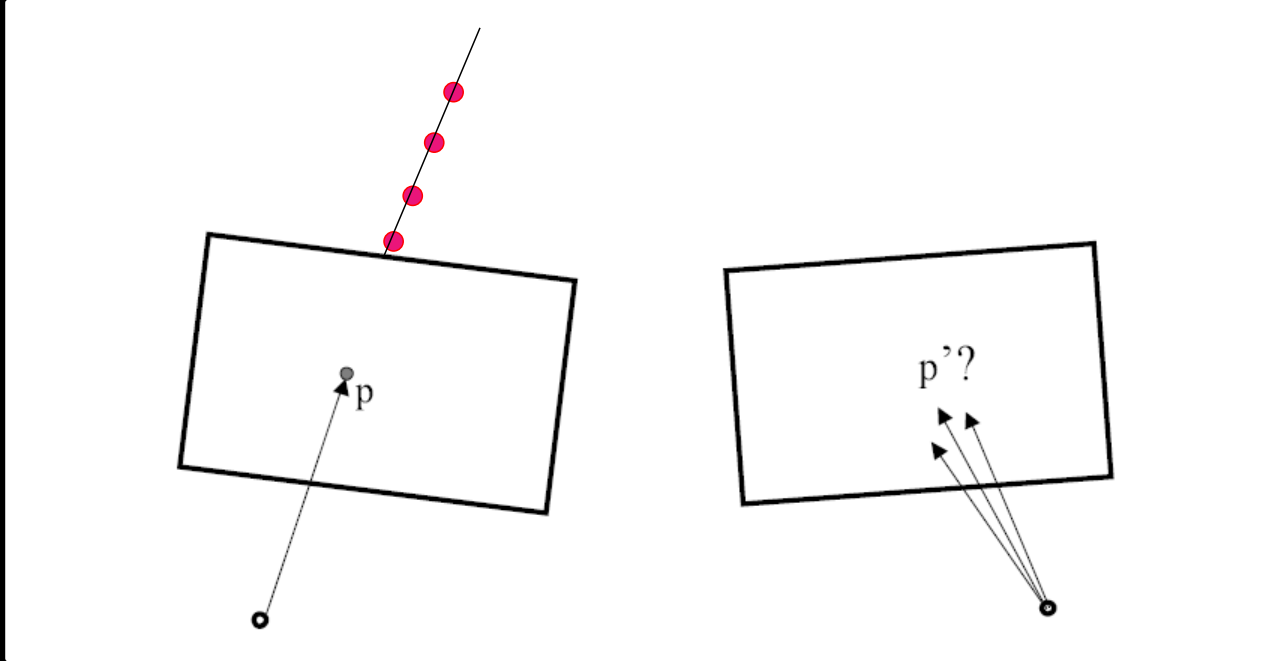
- The two cameras need not have parallel optical axes and image planes.



vs.



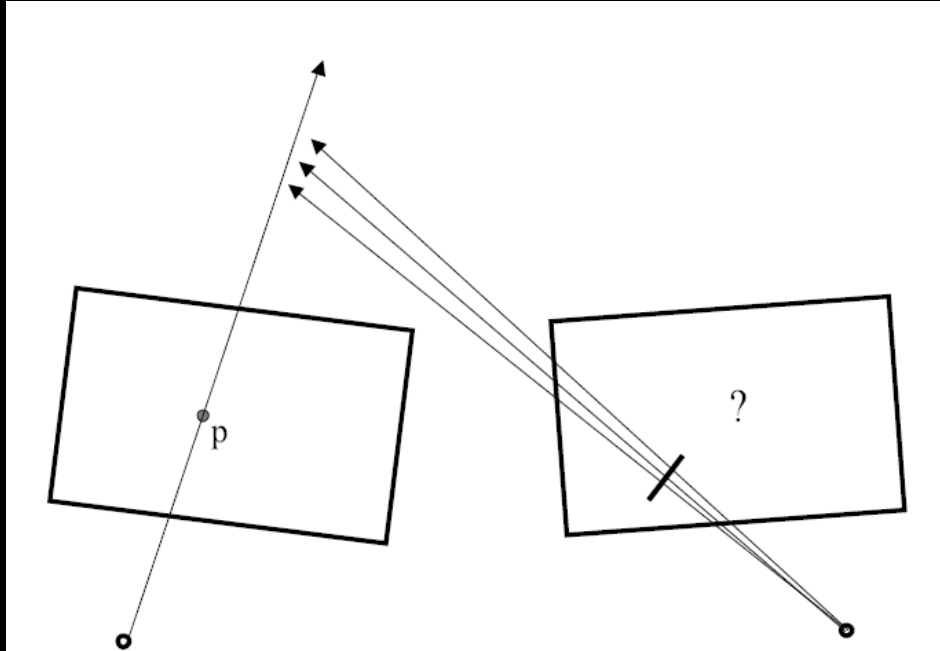
Stereo correspondence constraints



Given p in left image, where can corresponding point p' be?

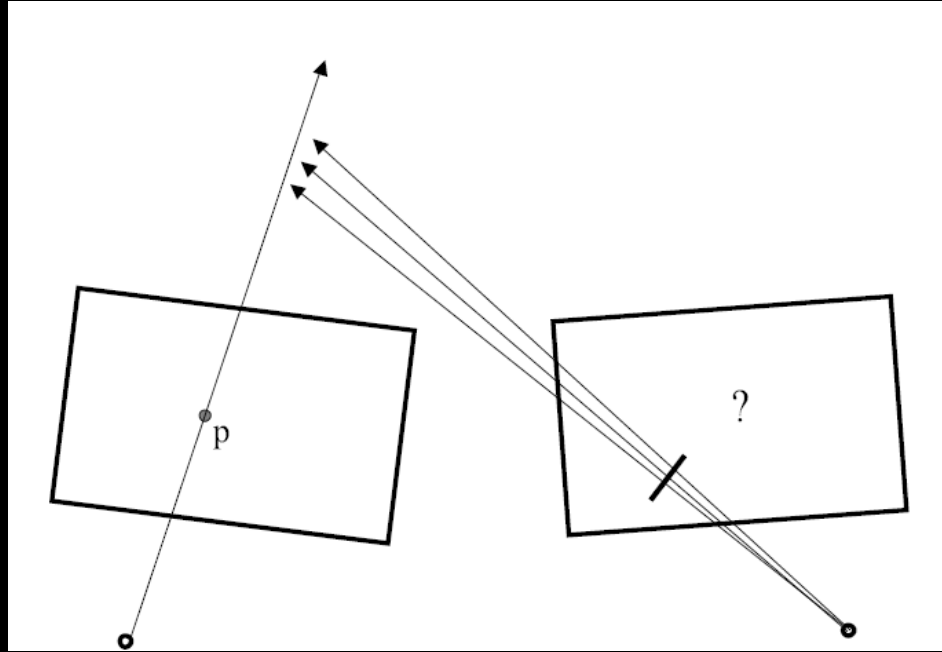
Stereo correspondence constraints

Remember: in perspective projection, lines project into lines.

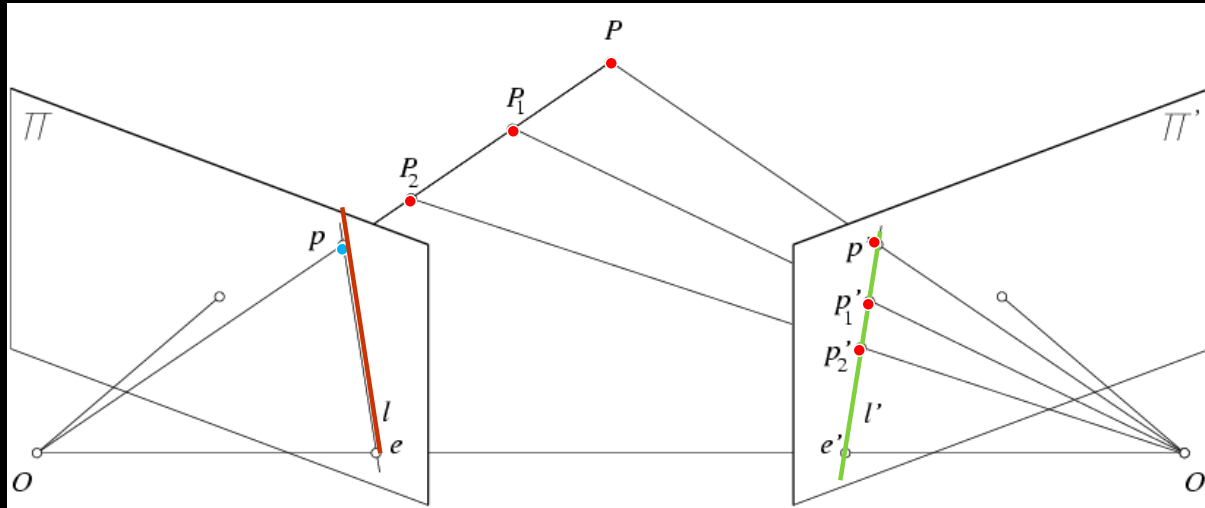


Stereo correspondence constraints

So the **line** containing the center of projection and the point P in the left image must project to a **line** in the right image.



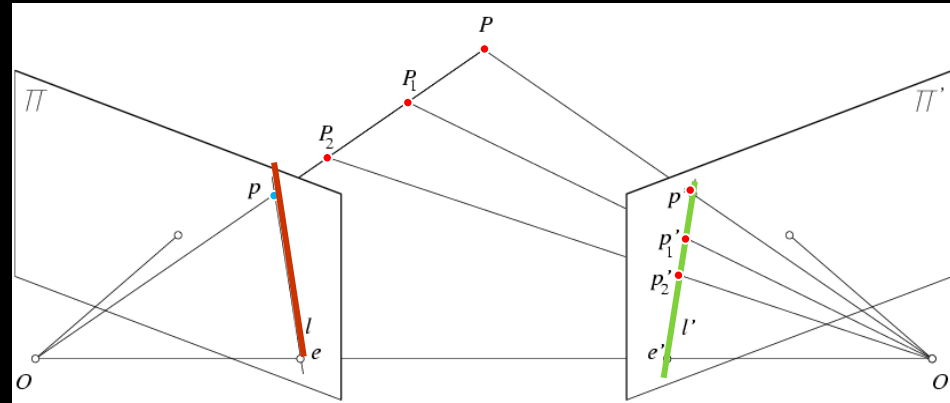
Epipolar constraint



Geometry of two views constrains where the corresponding pixel for some image point in the first view must occur in the second view.

Epipolar geometry: Terms

- **Baseline**: line joining the camera centers
- **Epipolar plane**: plane containing baseline and world point
- **Epipolar line**: intersection of epipolar plane with the image plane – come in pairs
- **Epipole**: point of intersection of baseline with image plane



Why is the epipolar constraint useful?

Epipolar constraint

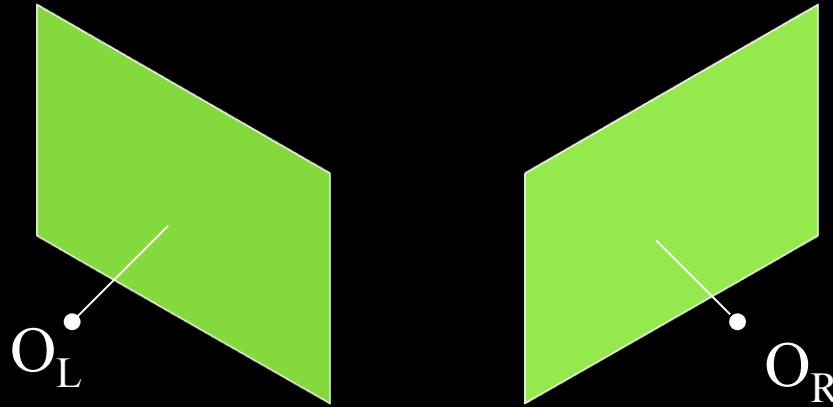


The *epipolar constraint* reduces the correspondence problem to a 1D search along an epipolar line.

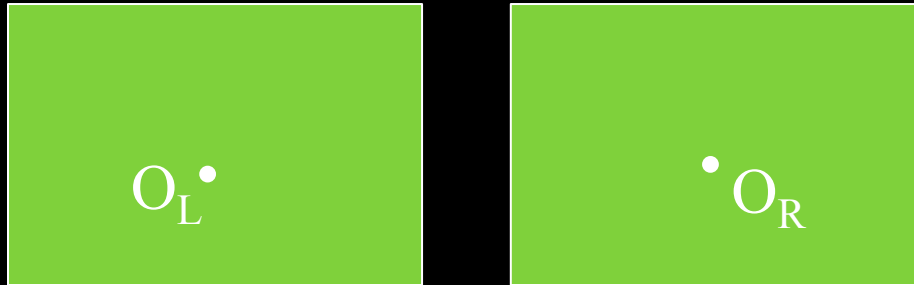
Image from Andrew Zisserman

What do the epipolar lines look like?

1.



2.



Example: converging cameras

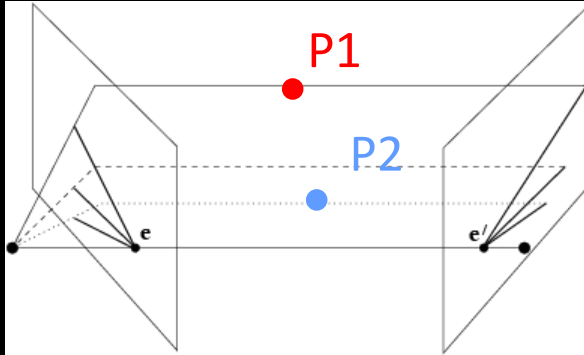
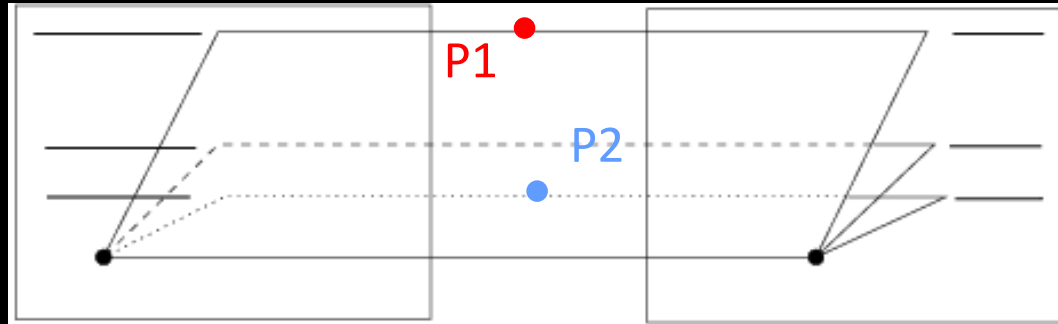


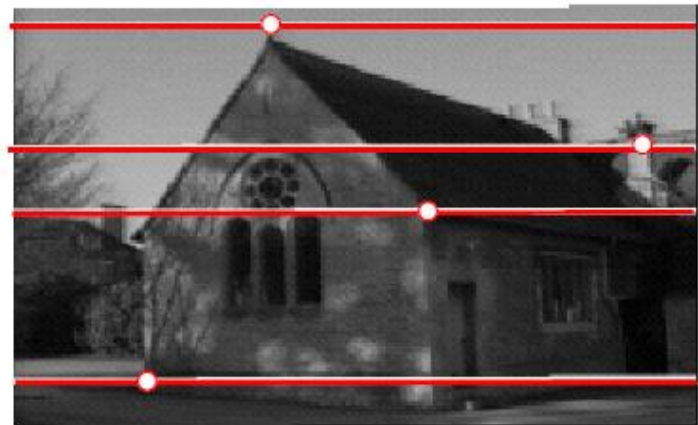
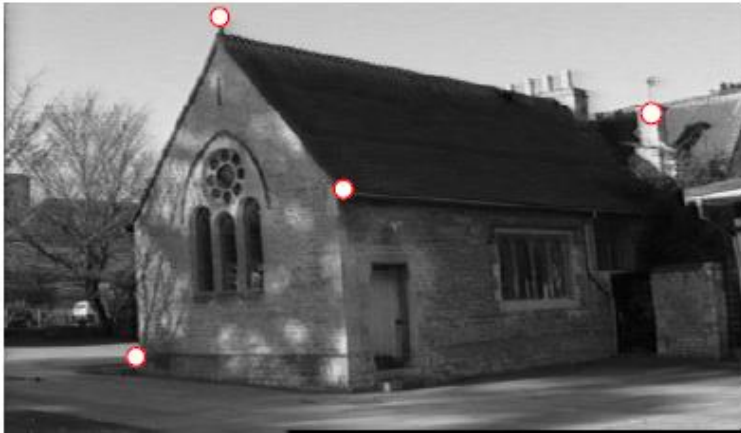
Figure from Hartley & Zisserman



Example: parallel image planes

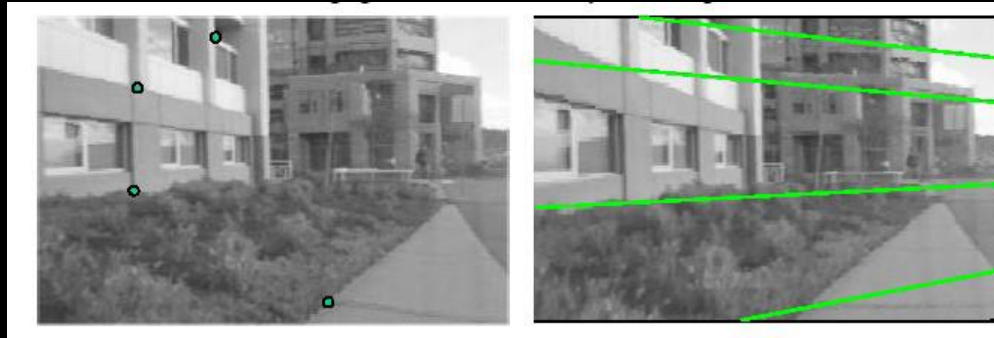


Where are the epipoles?



Quiz: two stereo pairs

a)



b)



Quiz:

How do we know that (B) has parallel image planes

- a) The epipolar lines are horizontal
- b) The epipolar lines are parallel
- c) Because I just said (B) had parallel image planes