

- **E-step**

$$\gamma_i(t) = p(S_t = i | O, \theta)$$

$$\xi_{ij}(t) = p(S_{t-1} = i, S_t = j | O, \theta)$$

$$\sum_{t=1}^T \gamma_i(t) = \text{expected \# times} \\ \text{in state } i$$

$$\sum_{t=1}^{T-1} \gamma_i(t) = \text{expected \# transitions} \\ \text{from state } i$$

$$\sum_{t=1}^{T-1} \xi_{ij}(t) = \text{expected \# transitions} \\ \text{from state } i \text{ to } j$$

- **M-step**

$$\pi_i = \gamma_i(1)$$

$$p_{ij} = \frac{\sum_{t=1}^{T-1} \xi_{ij}(t)}{\sum_{t=1}^{T-1} \gamma_i(t)}$$

$$q_i^k = \frac{\sum_{t=1}^T \delta_{O_t=k} \gamma_i(t)}{\sum_{t=1}^T \gamma_i(t)}$$