Most likely state vs. Most likely sequence

Most likely state assignment at time t

$$\arg\max_{k} p(S_t = k | \{O_t\}_{t=1}^T) = \arg\max_{k} \alpha_t^k \beta_t^k$$

E.g. Which die was most likely used by the casino in the third roll given the observed sequence?

Most likely assignment of state sequence

$$\arg\max_{\{S_t\}_{t=1}^T} p(\{S_t\}_{t=1}^T | \{O_t\}_{t=1}^T)$$

E.g. What was the most likely sequence of die rolls used by the casino given the observed sequence?

Not the same solution!

MLA of x? MLA of (x,y)? P(x,y)

0.05

0.3

0.3