$$\dot{x} = x + e^{-y}$$
 can't be represented as $\dot{y} = -y$ $\dot{x} = ax + by$ $\dot{y} = cx + dy$

Step 1: Find fixed points

Fixed points (also called stationary points) are those points where the time-derivative of each coordinate is zero. $\dot{x} = 0$ and $\dot{y} = 0$
 $0 = x + e^{-y} \implies -x = e^{-y} = 1$
 $0 = -y \implies y = 0$

Thus, one fixed point at $(x, y) = (-1,0)$