$$\max_{\{S_t\}_{t=1}^T} p(\{S_t\}_{t=1}^T, \{O_t\}_{t=1}^T) = \max_k V_T^k$$
 Compute probability V_t^k recursively over t

 $V_t^k := \max_{S_1, \dots, S_{t-1}} p(S_t = k, S_1, \dots, S_{t-1}, O_1, \dots, O_t)$

. Bayes rule
$$O_{t-1} O_{t}$$