

**B.Tech.-3<sup>rd</sup> Semester-CE/IT/CSE/EC/CIVIL/METALLURGY/ICT/Cyber Security**

**Subject: Probability, Statistics & Numerical Analysis**

**Subject Code- MA0314**

**Unit-1 Basics of Probability & Probability Distributions.**

### **Tutorial-1**

- 1) Three unbiased coins are tossed. Find the probability of getting (i) exactly two heads, (ii) at least one tail, (iii) at most two heads, (iv) a head on the second coin, and (v) exactly two heads in succession.
- 2) From a collection of 10 bulbs, of which 4 are defective, 3 bulbs are selected at random and fitted into lamps. Find the probability that (i) all three bulbs glow, and (ii) the room is lit.
- 3) A card is drawn from a pack of 52 cards. Find the probability of getting a king or a heart or a red card.
- 4) A bag contains 3 red and 4 white balls. Two draws are made without replacement. What is the probability that both the balls are red?
- 5) A businessman goes to hotels X, Y, Z for 20%, 50%, 30% of the time respectively. It is known that 5%, 4%, 8% of the rooms in X, Y, Z hotels have faulty plumbings. What is the probability that the businessman's room having faulty plumbing is assigned to Hotel Z?
- 6) A fair die is tossed once. If the random variable is getting an even number, find the probability distribution of X.

7) A fair dice is tossed. Let the random variable  $X$  denote the twice the number appearing on the dice. Write the probability distribution of  $X$ .

8) Two unbiased dice are thrown at random. Find the probability distribution of the sum of the numbers on them.

9) Show that the function  $f(x)$  defined by

$$f(x) = \begin{cases} \frac{1}{7} & 1 < x < 8 \\ 0 & \text{otherwise} \end{cases}$$

is a Probability Density Function for a random variable. Hence, find  $P(3 < x < 10)$

10) An unbiased coin is tossed 6 times. Find the probability of getting (i) exactly 4 tails; (ii) at least 4 tails.

11) The probability that a pen manufactured by a company will be defective is  $1/10$ . If 12 such pens are manufactured, find the probability that

- 1) Exactly two will be defective
- 2) At least two will be defective
- 3) None will be defective

12) Let  $X$  be a Poisson variate with  $P(X=2)=0.25$  and  $P(X=3)=0.125$ . Find  $P(X=0)$ ,  $P(X=1)$  and  $P(X < 3)$ .

13) 100 electric bulbs are found to be defective in a lot of 500 bulbs. Use Poisson distribution to find the probability that at most 3 bulbs are defective in a box of 100 bulbs. [Use  $e^{-2} = 0.1353$ ]

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