

Aye Jalili

HEAT AND THERMOMETRY

°C/Kelvin

ouchh

Topics

- Heat

Thermometry: process of measuring temperature
Measurement of heat

$$C^{\circ} = \frac{5}{9}(F - 32) + 32$$

$$F = \frac{9}{5}(C + 32) + 32$$

Freezing point of water (0°C)		
Fahrenheit	Kelvin	Celsius
32	273.15	0
212	373.15	100

1. Heat And Temperature

↓ form of energy. (measured in joules) ^{not}
(non-mechanical way of transfer of energy)

how energy is transferred?

before that:

temperature: measure of hotness or coldness of ^{a body} ~~matter~~
molecule or.

average vibrational kinetic energy of every molecule
temperature & vibration & kinetic energy.

Heat flows when difference in temperature...

(energy transfers when difference in temperature
(vibrational energy of molecules))

Thermometry: branch of science that deals with ~~the~~
measurement of heat

$$C^{\circ} = K^{\circ} - 273.15$$

$$K^{\circ} = C^{\circ} + 273.15$$

$$C^{\circ} = \frac{9}{5} (F - 32)$$

$$K^{\circ} = \frac{9}{5} (C^{\circ} + 273.15) + 273.15$$

$$F = \left(\frac{5}{9} C\right) + 32$$

$$F = \left(\frac{5}{9} K - 273.15\right) + 32$$

Scales

Ice point (Freezing) Steam point (Boiling)

Celsius	0	100
Kelvin	273.15	373.15
Fahrenheit	32	212

this derivation is excellently explained in
padike videos...

for any scale.

$$\frac{\text{Reading} - \text{Icepoint}}{\text{Steam point} - \text{Icepoint}} = \text{constant for any scale}$$

So,

$$\frac{R_c - IP_c}{SP_c - IP_c} = \frac{R_F - IP_F}{SP_F - IP_F} = \frac{R_K - IP_K}{SP_K - IP_K} = \text{constant}$$

(Celsius) (Fahrenheit) (Kelvin)

deriving the eq formula.

$$\frac{C - 0}{100 - 0} = \frac{F - 32}{212 - 32} \quad \frac{C - 0}{100 - 0} = \frac{K - 273.15}{373.15 - 273.15}$$

$$C = (F - 32) \frac{100}{180}$$

$$\frac{C - 0}{100} = \frac{K - 273.15}{100}$$

$$C = (F - 32) \frac{5}{9}$$

$$C = K - 273.15$$

Similarly for all...

Q Convert 50°C to Kelvin & Fahrenheit

Q on Reaumur scale of temperature the melting point of ice and the boiling point of water is 0R and 80R respectively. The freezing point and boiling point of mercury on Celsius are 39°C and 357°C respectively. Express them in Reaumur scale.

2. Thermal Expansion

tendency of a material to change its dimensions (length, height, area, volume) when its temperature is changed.

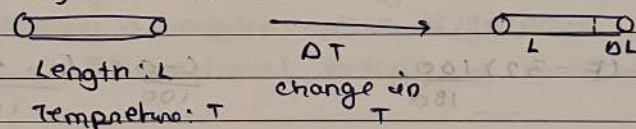
Why does it happen?

- Heating \uparrow atomic vibrations
- Average distance between atoms grows
- so material expands

* Linear Expansion

"Increase in the length of a solid material when its temperature rises"

Why it happens:



ΔT cause ΔL in L

so $\Delta L \propto \Delta T$ (proportionalities)

$\Delta L \propto L$

$\Delta L \propto \Delta T L$

$$\Delta L = \alpha L \Delta T$$

coefficient of linear thermal expansion

α = increase in length

per unit length

per unit rise in temperature.

$$\alpha = \frac{\Delta L}{L \Delta T}$$

so unit = $\frac{1}{^\circ\text{C}}$

$$\text{e.g. } \alpha_{\text{steel}} = 1.2 \times 10^{-5} \text{ } ^\circ\text{C}^{-1}$$

$$\alpha_{\text{copper}} = 1.7 \times 10^{-5} \text{ } ^\circ\text{C}^{-1}$$

* Volume Expansion

"Increase in the ^{volume} length of a solid material when its temperature is changed"

so,

Condition: works only till $T < 200\text{ K}$

$$\Delta V \propto \Delta T$$

$$\Delta V \propto V$$

$$\Delta V \propto V \Delta T$$

$$\Delta V = V \gamma \Delta T$$

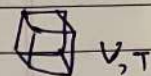
(gamma)

coefficient of volume expansion

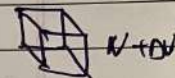
$$\gamma = \frac{\Delta V}{V \Delta T}, \text{ unit } \left[\frac{1}{^\circ\text{C}} \right]$$

γ is not always linearly proportional to ΔT or T
so many times relations are given.

e.g., $\gamma = T^4 + 2T^2$



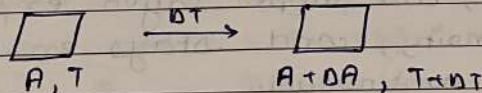
V, T



$V + \Delta V$

* Area Expansion

"Increase in the area of the solid material when its temperature is changed."



so, $\Delta A \propto \Delta T$

$$\Delta A \propto A$$

$$\Delta A \propto A \Delta T$$

$$\Delta A = A \beta \Delta T$$

(beta) coefficient of volume expansion (Beta)

* Relation Between α, β, γ ($\gamma = 3\alpha$) ($\beta = 2\alpha$)

simple hai bhai, γ is about volume

so d is about L , so $\gamma = 3\alpha$ (3)

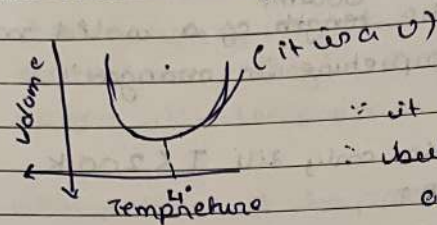
same area = L^2 , $\beta = 2\alpha$

(you can mathematically prove too)

$$\gamma = 3\alpha$$

$$\beta = 2\alpha$$

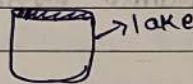
* Anomalous expansion of water



∴ it expands after 4°C
 ∴ but instead of being compressed at lower temp it expands too.

Most Example.

Imagine a lake, temp of $\text{H}_2\text{O} \rightarrow 10^{\circ}\text{C}$



1. when it goes to 9°C

the upper layer denser as volume decreases as ~~mass~~ temp decreases

$$\left(d \propto \frac{1}{V} \right)$$

then the second (which is at surface) cools and moves down and so on...

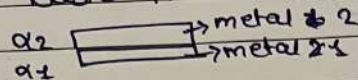
but at 4°C , when water expands on lower temperatures, the upper layer expands, so lighter density, and stays on top, and cools down continuously, so you always see the frozen lakes have water beneath and only surface is frozen...

moral: water expands below 4°C too
 and expands above 4°C too

* Bimetallic Strip,

when two metal strips of different expansion coefficient are joined together.

Basic mechanism



$$\alpha_2 > \alpha_1$$

so metal 2 expands more than metal 1

we heated metal 2

expands more and its increase in length (ΔL_2) is more but ΔL_1 is less, so ends up curled on heating



* Effect on density of liquid.

Simply $T \uparrow$ and $V \uparrow$

(density) $\propto \frac{1}{V}$

so high temperature \rightarrow low density

CALORIMETRY:

branch of science that deals with the measurement of heat exchanged during physical changes

* Specific Heat Capacity: (C, c , S)

$$\text{J/Kg}^\circ\text{C}$$

heat amount required to change 1°C (1K) temperature of 1kg of a material.

C of water: $4.184 \text{ J/kg}^\circ\text{C}$

$$C = \frac{Q}{m \Delta T}$$

Q = heat amount (J) ΔT = change in temperature (K)

So

$$Q = c m \Delta T$$

heat amount mass

Q Find the amount of heat required to raise the temp of 10g of water from 10°C to 50°C ($c = 4.2 \text{ J/g}^\circ\text{C}$)

Q A heater gives heat at the rate of 1000W. It is used to heat 40g of water from 10°C to 50°C . Find time taken to heat ($c = 4.2 \text{ J/g}^\circ\text{C}$)

power

Watt

$$P = \frac{\text{work done}}{\text{time}}$$

Q. A completely 100W heater is used for 5 min to heat some water from 20°C to 50°C . What is the mass. ($c = 4.2 \text{ J/g}^\circ\text{C}$)

* Principle of Calorimetry

"heat loss by = heat gain by"

hot body (in) cold body (in)

based on conservation of energy...

$$Q_{HB} = Q_{CB} \quad \therefore \Delta T_{HB} \neq \Delta T_{CB}$$

$$C_{HB} m_{HB} \Delta T_{HB} = C_{CB} m_{CB} \Delta T_{CB}$$

Q. 10g of water at 80°C mixed with 50g of copper at 10°C

Find final temp of mixture ($C_w = 4.2 \text{ J/g}^\circ\text{C}$, $C_c = 0.41 \text{ J/g}^\circ\text{C}$)

$$\therefore \Delta T_{HB} = \text{final temp} - \text{its } 80^\circ\text{C temp}$$

$$\Delta T_{CB} = \text{final temp} - \text{its } 10^\circ\text{C temp}$$

and confusing

In a copper vessel (mass 20g) of hot water at 80°C

Now 100g of cold water at 10°C is added. Find final

temp, if vessel weights 50g ($C_w = 4.2$, $C_c = 0.4$)

* Heat Capacity: (C)

[J/K]

"amount of heat to raise 1°C (1°K) of a body (whole)"

$$C = \frac{Q}{\Delta T} \rightarrow \text{amount of heat} \rightarrow \text{change in temp}$$

$$C = \frac{Q}{\Delta T} = \frac{C m \Delta T}{\Delta T} = C m \rightarrow \text{mass}$$

* Change of State

while changing state of a material Heat is required.

when a state is changed temperature remains same because, all the heat provided goes into ^{change} state. \uparrow inter molecular space, \downarrow molecular force

i.e. $\boxed{\text{ice}}$ $\xrightarrow{\text{heat}}$ $\boxed{\text{water}}$
 0°C 0°C

Solid \leftrightarrow liquid \leftrightarrow gas

Latent Heat $\boxed{\text{J}}$: amount of heat to change state of a material (no change in temperature)

(1) $\boxed{\text{J/kg}}$ Specific Heat Latent: amount of heat to change state of 1kg of material, at constant temperature

$$L_{\text{ice}} = 336 \text{ J/g or } 3.34 \times 10^5 \text{ J/kg}$$

(from ice \rightarrow water)

$$L_{\text{water}} = 2267 \text{ J/g or } 2.26 \times 10^5 \text{ J/kg}$$

$$Q = Q/m$$

$$Q = m L \rightarrow \text{specific latent heat}$$

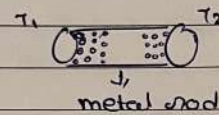
latent heat \downarrow mass

Heat Transfer:

process of transferring heat energy.

- ↳ conduction (solid)
- ↳ convection (liquid and gases)
- ↳ radiation (gases + light)

* Conduction



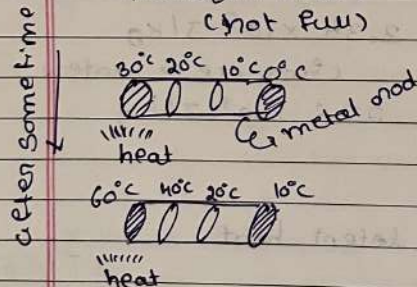
here ends of a metal (solid) have different temperatures, (energies) so vibrating at different rates so this vibration spreads to the side that has less temp vibration

∴ no flow of matter (molecules), just energy.

∴ heat transfer in solid is due to molecular collisions

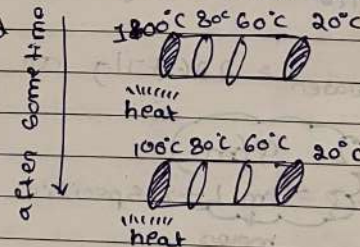
Variable State

(when solid can transfer heat)
(hot full)



Steady State

(when solid can't transfer heat, because they are full (max molecular vibration))



temp at every intersection remains constant with respect to time and do change bcoz because diff of temp

∴ For Steady States

K = thermal conductivity $\phi \propto A \rightarrow \text{area}$

$K \text{ unit} = \text{J/mK.s}$ $\phi \propto 1/L \rightarrow \text{length}$

$= \text{W/mK}$ ($\text{J/s} = \text{W}$) $\phi \propto t \rightarrow \text{time}$

$\phi \propto \Delta T$ (temp difference)

$\phi \propto \frac{A \Delta T t}{L}$

$$Q = K \frac{A \Delta T t}{L}$$

\rightarrow thermal conductivity of the substance...

Heat Current: rate of flow of heat

$(H) = H = Q/t$ (replacing ϕ from $Q = K \frac{A \Delta T t}{L}$)

$$H = K \frac{A \Delta T}{L}$$

*

HEAT AND THERMOMETRY

-From JA only :)

L1

Heat: Form of energy
can be converted from 1 form to another
unit SI: Joules (J)
cgs: erg
etc: calorie (cal)

Temperature: measure of hotness or coldness
"degree of intensity of heat present in a body"
Heat transfer: when temp difference
between body and surrounding

calorie heat required to raise 1°C / 1K temp of a body with mass 1g.

Kilocalorie heat required to raise 1°C / 1K of 1kg of mass of a body (1 kcal = 1000 cal)

!/? (JA includes wrong definitions of heat / cal / kcal)

Thermometer device to measure temperature using some measuring scales

L2 Modes of Heat Transfer:

1. Conduction: heat transfer between solids
(due to molecular vibrations)
(from higher temp to lower temp)
without actual molecular movement
 - ✓ heat transfer - require solid medium
 - ✗ molecule transfer

2. Convection: heat transfer in fluids (liquids, gases)

- ✓ heat transfer
 - ✓ molecular movement
 - require medium (fluid)
- types
- natural (sunlight)
 - forced (external force) (pump, etc)

13 3. Radiation: heat transfer (emission) through electromagnetic waves without requiring medium

thermal waves

- ✓ heat transfer
- x medium required
- x molecular movement

14 Temperature Measurement Scales

	* Celsius	* Kelvin	* Fahrenheit
freezing point	0°C	273.15 K	32°F
boiling point	100°C	373.15 K	212°F
Celsius		$C = K - 273.15$	$C = (F - 32) \frac{5}{9}$
Kelvin	$K = C + 273.15$		$K = (C - 32) \frac{5}{9} + 273.15$
Fahrenheit	$F = (9/5 \times C) + 32$	$F = (9/5 (K - 273.15)) + 32$	
Q	50°C to K & F	Q	-45°C to K & F
Q	temp at which $C = F$		
	$F = K$		

Heat Capacity and Specific Heat Capacity

amount of heat transferred to the body to cause unit (1) temperature change

amount of heat transferred to every Kg (unit mass) of a body to produce of unit temperature change

on H_c

Heat Capacity $C_{rep}: C$, unit: J/K
 $C = \frac{Q}{\Delta T} \rightarrow$ change in temperature
heat \downarrow amount of
capacity heat so, $Q = C \Delta T$

Specific heat Capacity $C_{rep}: c$, unit: $J/Kg K$
 $c = \frac{Q}{m \Delta T} \rightarrow$ amount of heat
specific \downarrow mass
heat capacity \downarrow change in temperature
so, $Q = c m \Delta T$
also $C = c m \rightarrow$ mass
heat capacity \downarrow specific heat capacity

\therefore Heat capacity depends on specific heat capacity and mass

$$H_c \propto c$$

$$H_c \propto m$$

\therefore Types of Specific Heat Capacity

\hookrightarrow Specific Heat at constant volume (C_v)

amount of heat required to change the temperature of 1 mole of gas by $1K$ keeping its volume constant, is called specific heat C_v of the gas at constant volume

\hookrightarrow Specific Heat at constant pressure (C_p)

amount of heat required to change the temperature of 1 mole of gas by $1K$ keeping its pressure constant, is called specific heat C_p of the gas at constant pressure

$$C_p - C_v = R$$

gas constant

$$PV = nR_0T$$

pressure ← P → temperature
 volume ← V →
 mole ↑ n ↓
 universal gas constant R_0
 (8.314 J/K mol K)

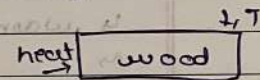
Coefficient of Thermal Conductivity E It's Thermal Applications

Thermal Conductivity: ability of the material to conduct heat (ability capacity to allow heat current)

materials properties

↳ low thermal conductivity

↳ high thermal conductivity



* depends on

heat being transferred

1. $\Phi \propto A$ (cross section area)

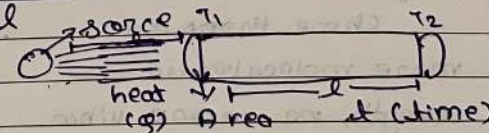
$\Phi \propto t$ (time)

$\Phi \propto \Delta T$ (temperature difference at both ends)

$\Phi \propto \frac{1}{l}$ (distance from the body to body) (length of the rod)

$$\Phi \propto \frac{A \Delta T}{l}$$

$$\Phi = \frac{k A \Delta T}{l}$$



Coefficient of thermal conductivity

k = unit: $W / K m$

Temperature Gradient
 the temperature difference per unit length
 of the rod is called temperature gradient


$$G = \frac{\Delta T}{d} \quad \left(\frac{\text{temp diff}}{\text{distance}} \right) \quad \frac{K}{m}$$

Applications

- ↳ pop at ceiling to reduce heat transfer
- ↳ pop in less thermal conductive
- ↳ metal handles of wood ($\downarrow TC$)
- ↳ vessel of metals ($\uparrow TC$)
- ↳ ice kept in wood ($\uparrow TC$) so no melting ($\times \uparrow T$)
- ↳ warm winter clothes

Expansion of Solids, Coefficient of Linear Expansion

when heat provided \rightarrow \uparrow molecular movement
 increase in size
 (molecules vibrate/move) equally in all
 directions, but longer dimension expands
 more because it has more molecules in
 its direction

Strip
 e.g. 

there there are
 more molecules in
 length, so more vib
 and movement, so length
 increases more, than
 width

metal sheet



here w, l are equal, but $\downarrow h$ more so
 so w, l increase all increa
 causing area so, volum
 expansion

Linear Expansion

Note Moral of the story:

There is always volume expansion in this 3D world, because molecules vibrate same in every direction.

but, sometimes movement in one direction is ignorable
→ we named it linear expansion for simplicity

when it is ignorable, we call it area expansion
(refer padhle notes/videos)

* Linear Expansion

when length of the object increases due to heat transfer

depends on ΔT , L ,

change in length ΔL depends on,

~~SL~~ $\Delta L \propto L$ (orig length)

$\Delta L \propto \Delta T$ (change in length)

$\Delta L \propto L \Delta T$

$\Delta L = K \Delta T L$

↓
coefficient of linear

expansion. unit: $1/K$

(constant (same) for every material)

$$K = \frac{\Delta L \times \Delta T}{L}$$