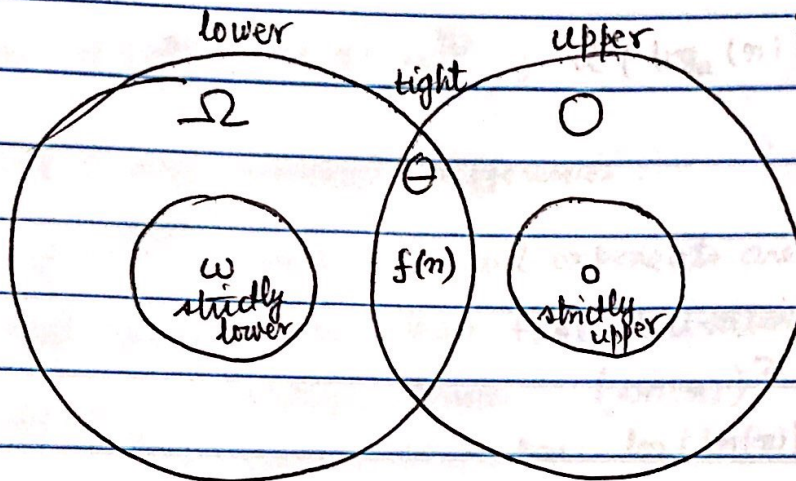


Asymptotic Growth of Functions

Def 1	O	upper	$\Leftarrow 0 \leq L < \infty$ (Th3) \nRightarrow Ex A
Def 2	Ω	lower	$\Leftarrow 0 < L \leq \infty$ (Th4) \nRightarrow Ex C
Def 3	Θ	tight	$\Leftarrow 0 < L < \infty$ (Ex B) \nRightarrow Ex B
Def 4	o	strictly upper	iff $L=0$ (Lemma 1)
Def 5	ω	strictly lower	iff $L=\infty$ (Exercise 5)

$$\lim_{n \rightarrow \infty} \frac{f(n)}{g(n)} = L$$



Reflexivity : $f(n) = \Theta(f(n))$; $f(n) = O(f(n))$; $f(n) = \Omega(f(n))$

Symmetry : $f(n) = \Theta(g(n))$ iff $g(n) = \Theta(f(n))$

Transpose symmetry : $f(n) = O(g(n))$ iff $g(n) = \Omega(f(n))$
 $f(n) = o(g(n))$ iff $g(n) = \omega(f(n))$

Transitivity $\Theta, O, \Omega, o, \omega$

$\underbrace{\dots, \ln \ln(n), \ln(n), \dots}_{\text{logarithms}}, \underbrace{n, n^2, \dots, n^{100}, \dots}_{\text{Polynomials}}, \underbrace{2^n, e^n, 10^n, \dots}_{\text{exponentials}}$