Netflix intro



In machine learning, clustering can be used to group similar data for prediction and recommendation. For example, each Netflix user's viewing history can be represented as a n-tuple indicating their preferences about movies in the database, where n is the number of movies in the database. People with similar tastes in movies can then be clustered to provide recommendations of movies for one another. Mathematically, clustering is based on a notion of distance between pairs of n-tuples.

Set operations

To define a set we can use the roster method, set builder notation, a recursive definition, and also we can apply a set operation to other sets.

New! Cartesian product of sets and set-wise concatenation of sets of strings

Definition: Let A and B be sets. The **Cartesian product** of A and B, denoted $A \times B$, is the set of all ordered pairs (a, b) where $a \in A$ and $b \in B$

$$A\times B=\{(a,b)\mid a\in A \text{ and } b\in B\}$$

Definition: Let A and B be sets of strings over the same alphabet. The **set-wise concatenation** of A and B, denoted $A \circ B$, is the set of all results of string concatenation ab where $a \in A$ and $b \in B$

$$A \circ B = \{ab \mid a \in A \text{ and } b \in B\}$$

Fill in the missing entries in the table:

Set	Example elements in this set:
В	A C G U
	(A,C) (U,U)
$B \times \{-1, 0, 1\}$	
$\{-1,0,1\} \times B$	
	(0, 0, 0)
$\{\mathtt{A},\mathtt{C},\mathtt{G},\mathtt{U}\}\circ\{\mathtt{A},\mathtt{C},\mathtt{G},\mathtt{U}\}$	
	GGGG

Defining functions

New! Defining functions A function is defined by its (1) domain, (2) codomain, and (3) rule assigning each element in the domain exactly one element in the codomain.

The domain and codomain are nonempty sets.

The rule can be depicted as a table, formula, or English description.

Examples:

Definition (Of a function, recursively) A function rnalen that computes the length of RNA strands in S is defined by:

The domain of *rnalen* is ______. The codomain of *rnalen* is ______.

$$rnalen(\mathtt{ACU}) = _$$

 $Extra\ example$: A function basecount that computes the number of a given base b appearing in a RNA strand s is defined recursively: $fill\ in\ codomain\ and\ sample\ function\ applications$

$$basecount: S \times B \rightarrow \\ Basis \ \text{Step:} \qquad \text{If} \ b_1 \in B, b_2 \in B \qquad basecount(b_1,b_2) \qquad = \begin{cases} 1 & \text{when} \ b_1 = b_2 \\ 0 & \text{when} \ b_1 \neq b_2 \end{cases}$$

$$Recursive \ \text{Step:} \quad \text{If} \ s \in S, b_1 \in B, b_2 \in B \quad basecount(sb_1,b_2) \qquad = \begin{cases} 1 & \text{when} \ b_1 = b_2 \\ 0 & \text{when} \ b_1 \neq b_2 \end{cases}$$

$$basecount(ACU,A) =$$

basecount(ACU, G) =

Defining functions recursively

Definition (Of a function, recursively) A function rnalen that computes the length of RNA strands in S is defined by:

Basis Step: If $b \in B$ then rnalen(s) = 1Recursive Step: If $s \in S$ and $b \in B$, then rnalen(sb) = 1 + rnalen(s)

The domain of rnalen is _____. The codomain of rnalen is _____.

 $rnalen(\mathtt{ACU}) = \underline{\hspace{1cm}}$

Extra example: A function basecount that computes the number of a given base b appearing in a RNA strand s is defined recursively: fill in codomain and sample function applications

 $basecount(\mathtt{ACU},\mathtt{G}) = \underline{\hspace{1cm}}$