Binary expansions exist proof

Representing positive integers

Theorem: Every positive integer is a sum of (one or more) distinct powers of 2. *binary expansions exist!*

Proof by strong induction, with $b = 1$ and $j = 0$.

Basis step: WTS property is true about 1.

Recursive step: Consider an arbitrary integer $n \geq 1$. Assume (as the IH) that the property is true about each of $1, \ldots, n$. WTS that the property is true about $n + 1$.