# CS 211 Notes

Introduction to Programming

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*Last modified October 22, 2021*

# 0 Course Overview

September 10, 2021

## 0.1 Objectives

The course is intended to teach how to develop a computer program to solve a problem. C++ is a tools that will be used to develop these skills and logical thinking. These skills will be transferable to other languages.

# 1 Computer Organization

## 1.1 Hardware

September 11, 2021

### 1.1.1 Components

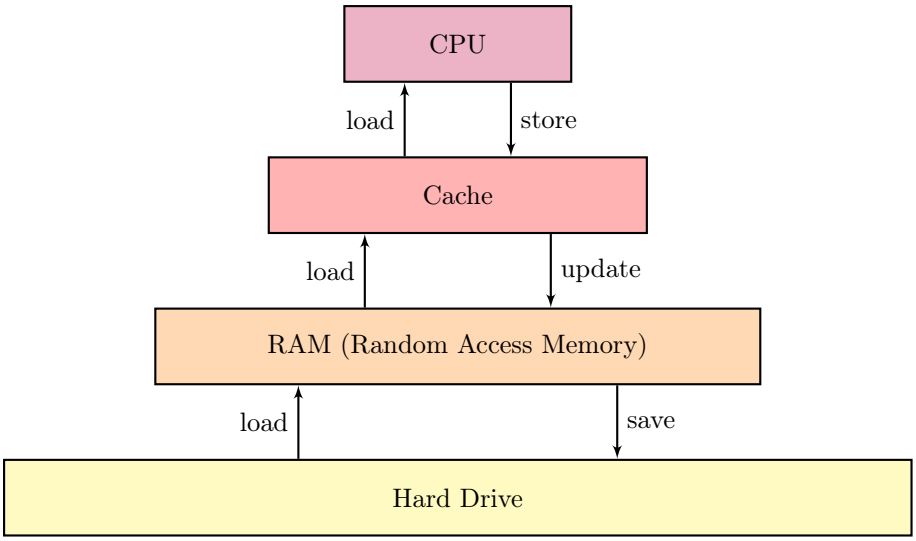
Modern computers are built using the **Von Neumann machine**. There are three aspects:

- **Architecture**: **I/O** (User interaction) + **Memory** (Storage) + **CPU** ($CU$: Control Unit, $ALU$: Arithmetic and Logic Unit). These are all connected by a shared bus.
- **Stored Programs**: All programs and data are stored in memory (binary).
- **Sequential Execution**: Also called the **fetch-decode-execute** cycle. Instructions are **fetched** from memory, **decoded** by the CU and then **executed** by the ALU. If there is a result, it is stored back in memory.

## 1.2 Memory

September 11, 2021

The memory is organized in a **hierarchy**. At the bottom of the hierarchy is the Hard Drive (in TB). At the top is the CPU. Since the hard drive is slow, when some data from the hard drive is needed, it is first loaded into **RAM (Random Access Memory)** (in GB). The RAM is still too slow for the RAM, so the data is stored in **cache** (in KB or MB). Yet still, this is not fast enough for the CPU, so **registers** (in Bytes) in the CPU itself are used to store variables.




As you **go up** the hierarchy, the **speed increases**, but the **size decreases** and the **cost increases**.

### 1.2.1 RAM

Random access memory is organized in an array of Bytes ("words").

Words in RAM are addressed with a byte themselves (e.g. 01101101 is an address). These are typically written in hexadecimal (e.g. 6D).

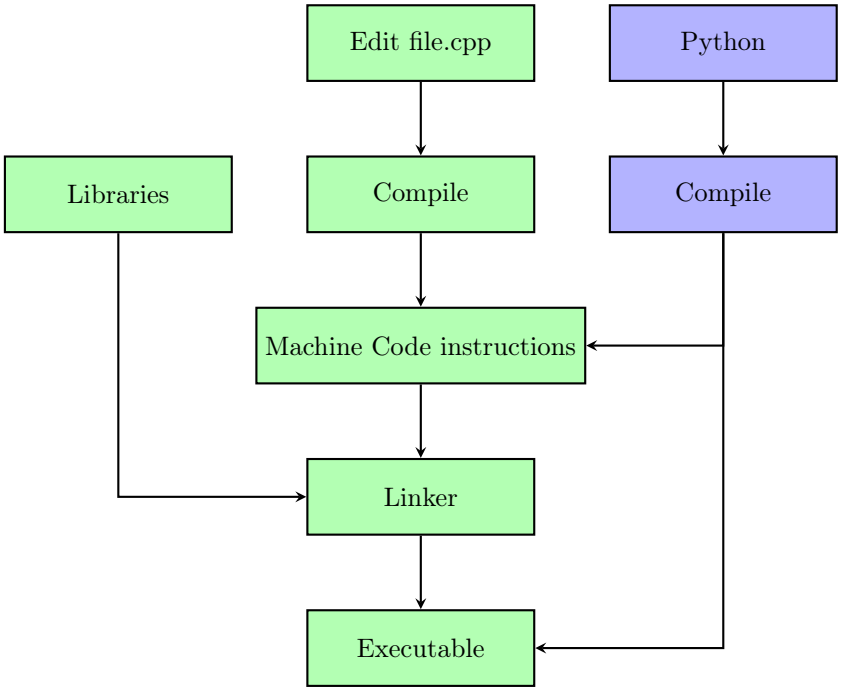
Words in RAM can be data or machine code instructions. Instructions contain a binary code for each operation (for example, addition). Instructions codes are dependent on the CPU.

# 2 Computer Organization

## 2.1 A Flow Chart: Program to Binary

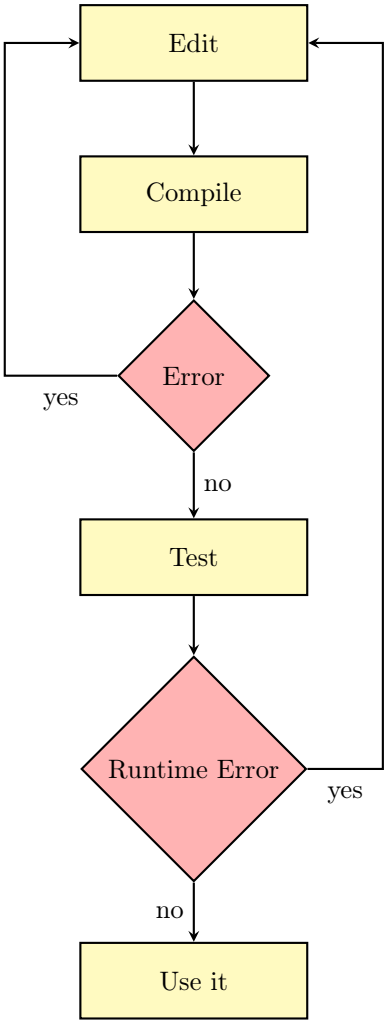
September 12, 2021

This is a flow chart of what is done by the computer when compiling a C++ file. In blue is the Python equivalent.



Note that the bottom of the flow chart is the same for all programming languages, because in all languages, CPU-specific machine code is needed to execute code.

The process of catching errors is as according to the following flow chart.




In this context, **errors** are caught by the compiler. This is opposed to **runtime errors**, which are not caught by the compiler. These can be something like division by zero or infinite loops.

## 2.2 First C++ Code

September 12, 2021

The following code is a hello world program in C++.

```
// helloworld.cpp
#include <iostream>   // include statement allows the use of C++ libraries
#include <stdio.h>    // this library contains getchar()

using namespace std; // a standard environment (input from keyboard, output is the screen)

int main() {

   cout << "Hello world!" << endl;  // Prints "Hello world!" to the screen

   getchar();     // wait for user to type a character

   return 0;     // 0 means that the execution was successful
}
```

## 2.3 Data types

September 12, 2021

Variables are referred to as identifiers. Identifiers are memory locations accessed and modified.

Inside a main function (as above), the following code declares a variable of integer type in C++.

```
int numYears;     // allocated space in memory to contain num of years
```

You can also initialize the variable with a value on declaration:

```
int number = 5;   // declare and initialize (give a value too)
```

Some rules to follow when naming variables are:

- Names have meanings
- Must be case sensitive (e.g. numYears is not numyears)
- Consists of letters, numbers and underscores
- First character cannot be a number

Some types of variables are:

- Integers (e.g. -5, 0, +2) [int]
- Real numbers (floating point numbers or doubles, e.g. 2.453, -4.1987e7) [float or double]
- Booleans (e.g. true, false) [bool]
- Characters [char]

You can assign a value to a variable after declaring it:

```
int width, height;
int area;

width = 5;
height = 3;

area = width * height;
```

Constants (denoted with the keyword "const") cannot be changed throughout the program. The convention is to use capital letters for constants.

```
const double PI = 3.14159265;

int radius = 6;
double area = PI * radius * radius;
```

You would get an error if you were to try to reassign a constant.

```
const double PI = 3.14159265;
PI = 3.14;  /// ERROR
```

## 2.4 Arithmetic operations

September 22, 2021

There are 5 basic arithmetic operations supported by C++

- Addition (+)
- Subtraction (-)
- Multiplication (*)
- Division (/)
- Modulus or "Remainder" (%)

For example,

```
int a = 5;
int b = 2;

cout << a + b / 2 << endl;    /// 6
cout << (a + b) / 2 << endl;  /// 3
cout << a / 2 + 3 << endl;    /// 5
cout << a / b / 3 << endl;    /// 0
```

This is done with integer operations since both arguments of each operation are integers (round down if the result of a division is a decimal). If one argument is a double/float, the result is a double/float. For example,

```
int a = 5;
int b = 2;

cout << a + b / 2 << endl;    /// 6
cout << (a + b) / 2 << endl;  /// 3.5
cout << a / 2 + 3 << endl;    /// 5
cout << a / b / 3 << endl;    /// 0.83333333
```

### 2.4.1 Assigning and operations

When you are assigning a variable and performing an operation to it at the same time you can do the following:

```
int x = 25;

x += 1     // equivalent to x = x + 1 (or x++)
x -= 2;    // equivalent to x = x - 2
x *= 3;    // equivalent to x = x * 3
x /= 4;    // equivalent to x = x / 4
x %= 5;    // equivalent to x = x / 5
```

### 2.4.2 Division when initializing or assigning a variable

Naively, to initialize a variable to the result of a division, you could try

```
int div = 7/3;  /// 2
```

However, this results in 2, not the desired result of 2.3333. You could also try changing the variable type

```
double div = 7/3;  /// 2
```

This does not work either, since the integer division happens before the result is assigned to the variable div. Instead, you have to force the compiler to recognize an argument as a float.

```
double div = 7.0/3;   /// 2.333333
```

If instead you had decided to make the variable type of div and integer and run it

```
int div = 7.0/3;   /// 2
```

It will perform the double operation, but save it in var as an integer.

A way of doing the float operation with two integers is by **casting** types. This can be done as follows.

```
double div = (double) 7/3;  /// 2.333333
double div2 = 7/(double)3;  /// 2.333333

int c = 7
double div3 = (double) c/3;   /// 2.333333
// Note, this does not change the type of c.
```

The remainder (%) operation returns the remainder of the division between two integers:

```
cout << 7 % 3 << endl;   /// 1
cout << 10 % 6 << endl;  /// 4
cout << 13 % 4 << endl;  /// 1
```

### 2.4.3 Type conversion

We can also convert types from doubles to integers by truncation or rounding:

```
double price = 2.55;

int sum = price;   /// truncate
int sum2 = price + 0.5  /// round to the nearest int
```

## 2.5 I/Os

September 22, 2021

To do this, we will use the iostream library and standard namespace.

```
#include <iostream>
using namespace std;
```

### 2.5.1 Reading inputs

You can get input from the keyboard using cin. For example,

```
int number;

cout << "Please enter a value between 0 and 10." << endl;

cin >> number;  // reads integer

cout << "The entered number is " << number;
```

You can also get multiple variables with the same cin.

```
int length, width;

cout << "Please enter the length and width of the rectangle: ";

cin >> length >> width;

int area = length * width;
cout << "The area is " << area
```

### 2.5.2 Formatting outputs

When outputting the result of a float, we inevitably run into an issue:

```
double result = 123456789.1284567;  /// 1.23457e+008

cout << result << endl;
```

This returns 1.23457e+008. To see all the digits, we must first pass result to fixed before cout.

```
double result = 123456789.1284567;

cout << fixed << result << endl;  /// 123456789.128457
```

To properly format the output of doubles, we must include the iomanip library and use the setprecision(n) function.

```
#include <iomanip>

double result = 123456789.1284567;

cout << fixed << setprecision(2) << result << endl;  /// 123456789.13
cout << result << endl;                    /// 123456789.13
```

This rounds the double to the nearest nth decimal. Note that result will now format that way if outputted without the fixed and setprecision call. However, this does not actually change the value of the result variable.

```
double result2 = result + 1;

cout << setprecision(3) << result2 << endl;   /// 123456790.128
```

Finally, to set a limit to the number of characters that are displayed to an integer n, we can use the setw(n) function from the iomanip library like this

```
cout << fixed << setprecision(2) << setw(15) << left << result << "End of line" << endl;
```

The result is "123456789.13  End of line". Note the exactly 15 characters until "End of line".

## 2.6 Strings

September 22, 2021

To use strings, you have to include the string library:

```
#include <string>
```

### 2.6.1 Declaration

You can declare, initialize, assign, and output strings as such

```
string lname;
string fname = "Jaeden";
lname = "Bardati";

cout << fname << " " << lname;   /// Jaeden Bardati
```

### 2.6.2 Concatenation

To combine strings together, we must use **concatenation**.

```
string name = fname + " " + lname;  /// Jaeden Bardati
```

This method does not work for constants

```
string greeting = "Hello" + " " + " World";  /// ERROR
```

An error occurs because we are trying to add the string " " to the constant string "Hello". A way to get around this is by adding a dummy variable before the concatenation.

```
string empt;     // empt = ""
string greeting = empt + "Hello" + " " + " World";  /// Hello World
```

### 2.6.3 Inputting strings

To read in a string, we can naively try

```
string myname;

cin >> myname;  /// Jaeden Bardati

cout << myname;    /// Jaeden
```

Only one word at a time is read in because cin treats things separated by spaces as distinct.

```
string myname;
string myfname, mylname;

cin >> myfname >> mylname;       /// Jaeden Bardati

myname = myfname + " " + mylname;

cout << myname << endl;          /// Jaeden Bardati
```

To get a full sentence (string) with cin, use the function getline(cin, sentence); This will get the whole line and put it in the variable sentence.

### 2.6.4 String functions

A useful quantity to know for a given string could be its length. You can get it as follows

```
int n = myname.length();

cout << "Your name has " << n-1 << " characters" << endl;
```

Here the number of characters is $n - 1$ since the space is not included.

You can also get substrings using substr($i$, $n$) to get the $n$ characters proceeding the character at location $i$. If only $i$ in entered, it will extract all characters preceding the character at location $i$.

```
string sub = myname.substr(0, 6);  /// Jaeden
string sub2 = myname.substr(7);    /// Bardati
```

### 2.6.5 Characters

Characters are strings of length 1, however, they can be declared explicitly with the char keyword and are expressed using single quotes.

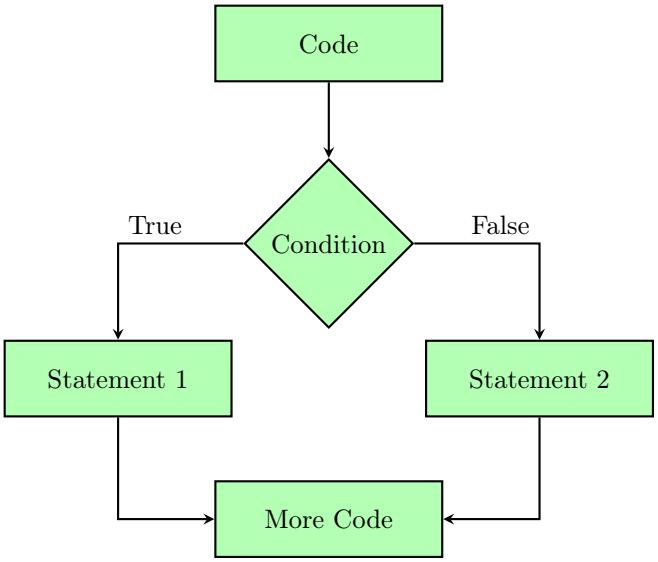
```
char c = 'Y';
```

## 2.7 The If Statement

September 23, 2021

We can also use conditional statements.

### 2.7.1 Flow Chart




### 2.7.2 Syntax

The if statement has the syntax

```
if (condition)
   statement1;
else
   statement2;
```

For multiple statements, we can use parentheses

```
if (condition) {
   statement;
   statement;
   ...
}
```

```
else {
   statement;
   statement;
   ...
}
```

### 2.7.3 The condition

A condition is a **boolean expression**. A boolean type can be **true** or **false**.

Boolean expressions are written using **relational operators**:

| | |
|---|---|
| < | Less than |
| > | Greater than |
| <= | Less than or equal |
| >= | Greater than or equal |
| == | Equal to |
| != | Not equal to |

You can also chain relational operators with **logic operators**:

| | |
|---|---|
| \|\| | OR |
| && | AND |
| ! | NOT |

For example,

```
if (num < 20 || num % 3 == 1) // if num is < 20 or if the remainder of num / 3 is 1
   num = num * 2
else
   num = num / 2
```

### 2.7.4 Floating point precision error

Let us show an example of a floating point precision error. Note that here we are including the cmath library.

```
double root, number;

root = sqrt(3);
number = pow(root, 2);

cout << setprecision(18) << "Number is : " << number << endl; // 2.999999999999999956, not 3

if (number == 3)
   cout << "sqrt(3) * sqrt(3) = 3" << endl;
else
   cout << "What just happened?" << endl;
```

When running this in a main function, we obtain the "What just happened?" result. What just happened indeed? The issue is that floating point numbers are only precise to a certain number of digits. To account for this, we must set our own precision as follows:

```
double precision = 1E-14;

if (abs(number - 3) < precision)
   cout << "sqrt(3) * sqrt(3) = 3" << endl;
else
   cout << "What just happened?" << endl;
```

This returns the desired result of "sqrt(3) * sqrt(3) = 3".

### 2.7.5 String comparison (alphabetical order)

We can also use comparison operators for strings. For example,

```
string name1, name2;

cin >> name1 >> name 2;

if (name1 < name2)
   cout << name1 << endl << name2;
else
   cout << name2 << endl << name1;
```

This will return two entered strings in alphabetical order.

### 2.7.6 Nested ifs

Sometimes there are more than one options. To do this we can use nested ifs. You check conditions within conditions for multiple branchings.
For example, we can assign a letter grade for a given percentage grade.

| | |
|---|---|
| A | 80 <= grade <= 100 |
| B | 65 <= grade < 80 |
| C | 50 <= grade < 65 |
| F | 0 <= grade < 50 |

The implementation of this in code is

```
int grade;
char letter;

cout << "Please enter a numeric grade: ";
cin >> grade;

if (grade >= 50)
   if (grade >= 65)
      if (grade >= 80)
         letter = 'A';
      else
         letter = 'B';
   else
      letter = 'C';
else
   letter = 'F';

cout << "The letter grade is " << letter << endl;
```

## 2.8 The Switch Statement

September 30, 2021

The **switch statement** is an alternative to nested ifs. This statement can be used if it compares a boolean, integer or character against a constant of the same type. Each constant creates an **alternative** or **branch**.

The syntax is as follows:

```
int n;
cin >> n;

switch (n) {
   case 1: cout << "ONE"; break;
   case 2: cout << "TWO"; break;
   case 3: cout << "THREE"; break;
   case 4: cout << "FOUR"; break;
   case 5: cout << "FIVE"; break;
   default: cout << "Not a number between 1 and 5";
}
```

The general process of the switch statement is that it will check each "case" until it finds a match, then it will run what comes next. The "default" will run if no other case has run. Remember to put breaks after each case! No break is needed after the default case.

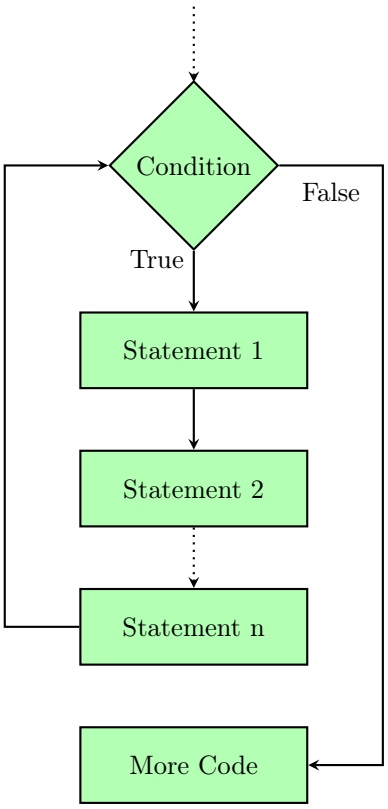
You can also stack cases as follows:

```
char c;
cin >> c;

switch (c) {
   case 'y': case 'Y': cout << "YES"; break;
   case 'n': case 'N': cout << "NO"; break;
   default: cout << "Not y or n";
}
```

## 2.9 The While Loop

September 30, 2021

The **while loop** can be used when a sequence of statements must be repeated multiple times so long as a condition is true. The following is a flow chart of the process.



The syntax for a while loop of *one statement* is

```
while (condition)
   statement;
```

Similarly, a while loop of *multiple statements* is made possible using parenthesis

```
while (condition) {
   statement;
   statement;
   ...
}
```

There are a few consideration we need to take into account:

- The condition must be initially true, other wise the loop will never execute
- If the condition is initially true, the loop executes at least once
- The loop executes until the condition becomes false
- The condition becomes false as a results of a statement in the loop
- If the condition never becomes false, the loop will be infinite

The following code is an example program using a while loop, to calculate how many years it takes for a bank account balance to double with a given rate:

```
#include <iostream>
using namespace std;

int main() {
   // Calculates the number of years to double the balance of a bank account.
   const double RATE = 0.03;

   double bal;

   cout << "Please enter an initial balance: ";
   cin >> bal;

   double target = 2 * bal;
   int years = 0;

   while(bal < target){
      bal += (bal * RATE);
      years++;
   }

   cout << "You require " << years << " years to double your balance.";

   return 0;
}
```

**Quick Aside:** In order to get the last number of a digit, you can use mod 10. For example, to get the last number of 729, we find that $729 \% 10 = 9$. We can use integer division by 10 to make 729 become 72 and then get the last number of that in order to get the second number form the right (here, 2).

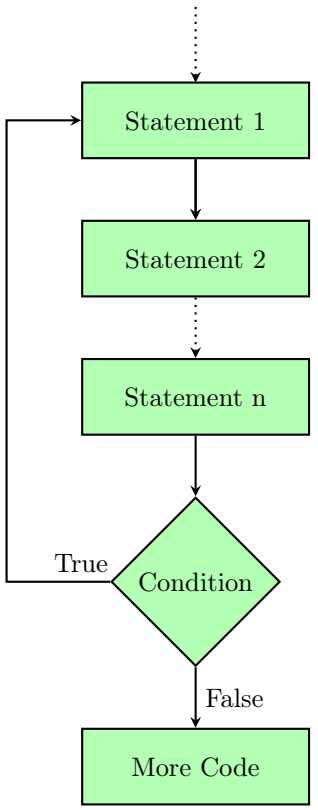
**Another Quick Aside:** If a variable is entered that is not of the right type in cin, it will fail. There is a function that checks if it fails: cin.fail(). It will return false if cin has not failed, and true if it has. After a cin fails, all the subsequent cins will fail. To allow for subsequent cins after failure, we can use cin.clear(). However, since the failed character is still in the buffer, you cin will fail again. Therefore, we need to also call cin.ignore(n, lastchar) after cin.clear() to ignore what is in the buffer that caused it to fail (up to n characters or up to lastchar). The following code demonstrates this.

```
#include <iostream>
using namespace std;

int main(){

   int input;

   cout << "Enter an integer value: " << endl;

   cin >> input;
   cout << "You have entered: " << input << " Status of cin: " << cin.fail() << endl;

   cin.clear();
   cin.ignore(10000, '\n');

   cout << "The cin status is now : " << cin.fail() << endl;

   cin >> input;
   cout << "You have entered: " << input << " Status of cin: " << cin.fail() << endl;

   return 0;
}
```

## 2.10 The Do-While Loop

October 6, 2021

The **do-while loop** can be used when a sequence of statements must be repeated multiple times so long as a condition is true. The following is a flow chart of the process.




This is different form the regular while loop because it always executes at least once. If the condition is initially false, there is one one execution. If the condition is initial true, the body of the loop is executed until the condition becomes false. The minimum number of iterations of a do-while loop is 1, whereas

the minimum number of iterations for a while-loop is 0.

The syntax in C++ for one statement is

```
do
   statement;
while(condition);
```

For many statements, you need curly braces as usual.

```
do {
   statement1;
   statement2;
   ...
}
while(condition);
```

An example application of a do-while loop is in input validation:

```
/// input validation using a do-while
do {
   cout << "Please enter a value for 0 < n < 100 ";
   cin >> n;
} while(n <= 0 || n >= 100);
```

## 2.11 The For Loop

October 6, 2021

The for loop is yet another iterative statement. For loops are based on the use of counters. It has the syntax:

```
for(statement1;statement2;statement3)
   statement;
```

Or, for multiple statement loops

```
for(statement1;statement2;statement3) {
...
statement;
...
}
```

The statement1 is for counter initialization.
The statement2 is for the loop condition.
The statement3 is to update the counter.

To demonstrate this we will compare it to the while loop.

```
int i = 1;
while (i <= n) {
   sum = sum + i;
   i = i + 1;
}
```

```
for (int i=1; i<=n; i++)
   sum = sum + i
```

We can see that the for loop is much more compact. It is preferred to use a for loop when you are using counters.

### 2.11.1 Nested For Loops

Just as if statements can be nested, so can loops. Nested loops are usuful since sometimes it is necessary to loop over loops (or repeat loops a certain number of times).

For example, if we wanted to draw an $n$ by $n$ square of *s. We could use a nested loop:

```
int n = 4;

for(int i = 1; i <= n; i++) {
   for (int j = 1; j <= n; j++)
      cout << "*";
   cout << endl;
}
```

You can even change the number of iterations in the inner loop via nested loops. For example, if we wanted the pattern

```
*
**
***
****
```

Then, we could use the following code.

```
int n = 4;

for(int i = 1; i <= n; i++) {
   for (int j = 1; j <= i; j++)
   cout << "*";
   cout << endl;
}
```

## 2.12 Random Variables
October 6, 2021

Sometimes it is useful to have (pseudo)random numbers to use in a program. The library that we need to include is

```
#include <cstdlib>
```

Then, to get two random numbers, we can do

```
int r1, r2;

r1 = rand();
r2 = rand();

cout << r1 << endl << r2 << endl;
```

Running it again though, you can notice that it gives you the same numbers as before!

This is because the the number is not truly random, only pseudo-random (random-looking). They are really just values that are generated from a mathematical sequence.

This sequence has to start somewhere and that number is called the "seed". We can set the seed value using

```
srand(765); // 765 is some arbituary number
```

If we want this to change with time, we need to input the computer time. To do this we will import the following library:

```
#include <ctime>
```

We can get the time in seconds since January 1st 1970 using

```
cout << time(0);
```

We can use this as the seed to make the starting random numbers change over time.

```
srand(time(0));
```

What is the range of the outputted randome numbers by rand()? It is between 0 and RAND_MAX. This is a constant defined in the cstdlib library. We can get this value ourselves:

```
cout << RAND_MAX << endl;
```

If we want doubles instead, we can do

```
int r = rand();
double x = r*1.0/RAND_MAX;
```

The variable x is a random variable between 0 and 1.

What if we want to generate random variables between and arbitrary a and b? To do this, we need to follow this procedure:

- Generate r between 0 and RAND_MAX (via rand())
- Generate x between 0 and 1 (via x = r*1.0/RAND_MAX))
- Generate y = a + (b-a)*x

So, if x = 0, y = a + (b-a)*0 = a. If x = 1, y = a + (b-a)*1 = a + b - a = b.

In code, this is

```
int r = rand();
double x = r*1.0/RAND_MAX;
double y = -1 + 2 * x;

cout << y << endl;
```

## 2.13 Functions

### 2.13.1 Introduction

A function is a sequence of instructions with a name. It is almost like a mini-program.

Why do we use functions?

- Convenient for splitting the work into modules
- Hiding details from the main() and making main() easier to understand (e.g. library function)
- Avoid repetitions, when portions of the code have to be used more than once

A function can either

- Calculate and return a value
- Perform a task

### 2.13.2 Declaration and Call

The function is **declared**, **defined** and **called** with a statement, just like any library function.

For example,

```
#include <cmath>
double x = 50.75;
double y = sqrt(x);
double z = pow(x, 3);
double cube(x); //but cube is not declared
int n = incr_by_value(n, value) //same as above
```

To declare a function, we need a **function heading**. We also should comment and explain what the function does. Something like

```
return_type fnct_name*(type ident, type ident, ...) {
   \\ function b ody
   Local declaration
   Calculations
   Return statement
}
```

For example, a function that calculates the cube of a value for a given variable of type double could be

```
#include <iostream>
using namespace std;

/*******************************************
Function cube calculates the volume of a cube.
Parameter side: The side of the cube.
*******************************************/

double cube(double s){
   double v = s*s*s;
   return v;
}


int main(){
   double side;
   cout << "Please enter the value of side: ";
   cin >> side;

   double volume = cube(side);

   cout << "The volume is : " << volume;

   return 0;
}
```

The parameter of the call are called the *actual parameters* (e.g. volume). The parameters of the function are called the *formal parameters* (e.g. s). It is important that the actual parameters match the formal parameters the formal parameters in type and number. The formal parameters and the actual parameters might have different names.

You must declare the function before it is called. For example, cube() must be before the function.

There is an exception to this, if you use **function prototyping**. This is where you first declare the function before it is used and then assign it later. In prototyping it is not necessary to put the parameter names. For example,

```
#include <iostream>
using namespace std;

/*******************************************
Function cube calculates the volume of a cube.
Parameter side: The side of the cube.
*******************************************/

double cube(double); // prototyping

int main(){
   double side;
   cout << "Please enter the value of side: ";
   cin >> side;

   double volume = cube(side);

   cout << "The volume is : " << volume;

   return 0;
}

 double cube(double s){
   return s*s*s;
}
```

Another example of a function is

```
#include <iostream>
using namespace std;


/***********************************
The function incr_by_val() increments
an integer v1 by another integer v2.
***********************************/

int incr_by_val(int v1, int v2){
   return v1 + v2;
}

int main(){
   int n = 4;
   int increment = 3;

   n = incr_by_val(n,2);
   cout << n << endl;
}
```

We can also make functions that only perform a task, which does not return a value. We can use **void** in the place of the return type. For example,

```
void printline(int length) {
   if (length >= 1) {
      for (int i=1; i<=length; i++) {
         cout << "-";
      }
   }
   else {
      return;
   }
```

```
    cout << "I am done with the function." << endl;
}
```

The following is a function that reads an integer between two values and keeps asking if it is not within that range.

```
int read_between(string what, int low, int high){
    int input;

    do{
        cout << "Please enter " << what << " between " << low << " and " << high << " :";
        cin >> input;
    } while(input < low || input > high);

    return input;
}
```

### 2.13.3 The scope of a variable

The scope of a variable is the portion fo the program where the variable is defined and can be used. These variables are **local**. For example,

```
int main() {
    int var = 5;  // scope of var is the main
    printline(var);
}

void printline(int n) { // the scope of n is printline()
    int index;    // The scope of index is printline()
}
```

You can only access variables in their scope. This is why you can use the same name in different scopes and the values of the variables can be different.

A variable declared in a block  is visible in all the block, unless a var with the same name is declared in a n inner block.

```
int main() {
    int n = 25;
    if (choice == 'D') {
        int n = 0;
        cout << n; // This prints 0
    }
    cout << n; // This prints 25
}
```

### 2.13.4 Global Variables
October 22, 2021

Global variables are defined *outside of the main and all other functions in the program.*

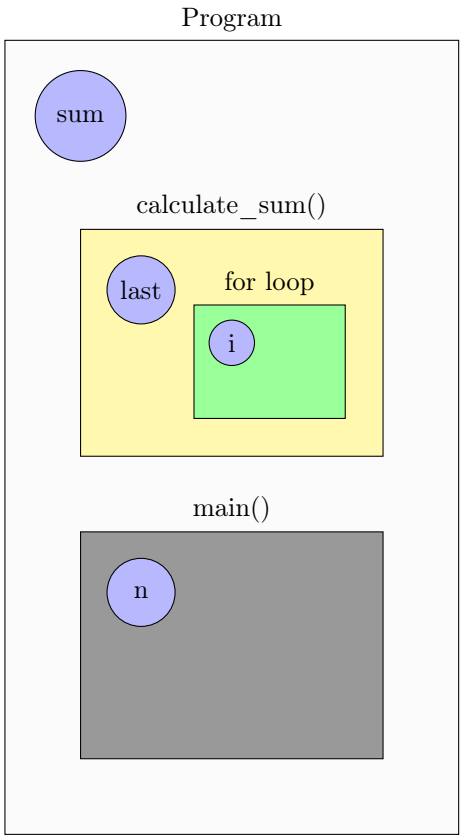
Their scope extends to all functions **defined after**. That is to say, they can be accessed and modified (read/write) from all functions (including the main) defined after.

Global variables are not recommended and are regarded as bad programming practice.

For example, the following program uses a global variable (passing by value) to calculate a Gauss sum.

```
#include <iostream>
using namespace std;

int sum = 0;  // Global variable

void calculate_sum(int last) {
   for (int i=0;i<=last;i++) {
      sum += i;
   }
}

int main() {
   calculate_sum(5);

   cout << sum;
}
```

The following is the **scope diagram** for the variables in the above program.




If the above program were written using local variables (passing by value) instead, one could write:

```
#include <iostream>
using namespace std;

int calculate_sum(int last){
   int result = 0;    // local variable
```

```
   for(int i = 0; i <= last; i++) {
      result += i;
   }

   return result;
}

int main(){
   int sum;   // local variable

   sum = calculate_sum(5);

   cout << sum;
}
```

### 2.13.5 Reference parameters

The parameters we've used so far are called **value parameters**. When a function is called, the **value** of the actual parameter **is copied** into the formal parameter. In that case, we say that parameters are **passed by value**.

When we passing by value, formal and actual parameters are **physically different** and only values can be passed. That is to say, both the formal and actual parameters have different locations in memory. Therefore, *changes to the formal parameter in the function will not affect the actual parameter.* For example,

```
void foo(int last){
   last = 2;
}

int main(){
   int n = 5;

   foo(n);

   // n is still 5, it has not been changed by foo()
}
```

An alternative solution is to pass parameters **by reference**. These are called **reference parameters**. In this case, the formal parameter (in the function header) *is not a local variable* within the function.

The function will instead have access to the *actual parameter* within the main. The function can use the value of the actual parameter from the main (a local variable to main) and change it directly.

To pass a parameter by reference in C++, we use the & symbol. For example,

```
void foo(int &last){
   last = 2;
}

int main(){
   int n = 5;

   foo(n);

   // n is now 2, it has been changed by foo()
}
```

Any change to last will affect n because of the use of the & character. We would say that the variable last is a **pointer** for the variable n. There is *no new variable physically* (in memory), last is simply another name for n.

When passing by value, a function can only calculate one value and return to the main. However, all parameters passed by reference can be changed by the function within the main. Therefore, *if we want to return multiple values*, we can use a function of type void and pass parameters by reference if we need to calculate multiple values by a function.

We will now repeat the local and global variable (passing by value) example, now adjusted to pass by parameter.

```
#include <iostream>
using namespace std;

void calculate_sum(int &result, int last) {
   for(int i = 0; i <= last; i++) {
      result += i;
   }
}

int main(){
   int sum = 0;

   calculate_sum(sum, 5);

   cout << sum;
}
```

Note that the parameter result is passed by reference, but the parameter last is passed by value.

Note also that we can not pass a constant by reference, since it has no location in memory.

## 2.14 Arrays

An array is a **structure** for storing **multiple values** of the **same type**.

For example, suppose we are reading the numbers 5, 10, 3, 12, and 1.

We could find the largest of the values and print the result and it's index in the list (here, 12 fourth position). This is much more convenient for large data, when, for instance, reading each input in a different integer variable (a=5, b=10, etc.).

Instead, we could store all the values in one structure that is an array. The type of the array is int and the size is 5. All elemetns in the array are associateed with an incremental index that starts from zero.

| index | 0 | 1 | 2 | 3 | 4 |
|---|---|---|---|---|---|
| element | 5 | 10 | 3 | 12 | 1 |

### 2.14.1 Defining arrays

We can define an array of type int with size 34 as follows:

```
int marks[34]; // define but not initialized
```

Often it is useful to create a constant variable for the size of the array.

```
int SIZE = 34
int marks[SIZE]; // define but not initialized
```

We can also initialize arrays.

```
int numbers[5] = {6, 3, -2, 0, 10}; // defined and initialized
```

There is no need to put the size of the array if we initialize it.

```
int numbers[] = {6, 3, -2, 0, 10}; // defined and initialized
```

If we give a size that is different from what is initialized. If the given size is greater than the size of the array passed to be initialized, it will fill the rest with zeros. Otherwise, if the given size is less than the size of the array passed to be initialized, it will give an error.

```
int special[5] = {6, 3};         // special = [6, 3, 0, 0, 0]
int error[2] = {6, 3, -2, 0, 10};  // This results in a compile error
```

If we want an array of size 5 to be initialized with all 0s, we can do

```
int grades[5] = {};
```

You can also declare an array of other types.

```
string names[34];                      // names = ["", "", ...]
char vowels[] = {'a', 'e', 'i', 'o', 'u'};
```

### 2.14.2 Accessing array elements

We can access arrays using square brackets as follows. We can read/write as with regular variables.

```
int A[5];

A[3] = 25;            \\ set value at index 3 to 25
A[4] = A[3] + 1;      \\ set value at index 4 to the value at index 3 plus one
```

If we want to print the contents of an array, we must iterate through each of the elements and print them individually.

```
for (int i=0;i<5;i++){
   cout << A[i] << endl;
}
```

Since we have not initialized A[0], A[1], and A[2], they contain **garbage** (arbitrary, meaningless values).

The following is an example code to enter a sequence of grades using an array and calculate various properties of the set.

```
#include <iostream>
using namespace std;

int main(){
```

```
int Grades[5] = {};  // initialized with zeros
int grade;
int size = 0;


// Get grades
for(int i=0;i<5;i++){

   cout << "Please enter a grade or -1 to quit: ";
   cin >> grade;

   if(grade == -1){
      break;     \\ exits for loop
   } else {
      Grades[i] = grade;
      size++;
   }
}


// Calculate average of grades
int sum = 0;

for(int i=0; i<size; i++) {
   sum = sum + Grades[i];
}

double average = sum/(double)size;

cout << "Average is: " << average;


/// Find the maximum and minimum grades

int max = Grades[0];
int min = Grades[0];

for(int i=1; i<size; i++) {
   if(Grades[i] > max) {
      max = Grades[i];
   }
   if(Grades[i] < min) {
      min = Grades[i];
   }
}

cout << "Max is: " << Max << endl;
cout << "Min is: " << Min << endl;
```