

```

dt = 0.001;
tmax = 20;
Nn = Evaluate[tmax / dt] // Round;

In[*]:= tT = Table[i dt, {i, 0, Nn}];

In[*]:= ξ1 = RandomVariate[NormalDistribution[0, Sqrt[dt]], Nn];
ξ2 = RandomVariate[NormalDistribution[0, Sqrt[dt]], Nn];
ξ3 = RandomVariate[NormalDistribution[0, Sqrt[dt]], Nn];
ξ4 = RandomVariate[NormalDistribution[0, Sqrt[dt]], Nn];
ξ5 = RandomVariate[NormalDistribution[0, Sqrt[dt]], Nn];
ξ6 = RandomVariate[NormalDistribution[0, Sqrt[dt]], Nn];
ξ7 = RandomVariate[NormalDistribution[0, Sqrt[dt]], Nn];
ξ8 = RandomVariate[NormalDistribution[0, Sqrt[dt]], Nn];
ξ9 = RandomVariate[NormalDistribution[0, Sqrt[dt]], Nn];
ξ10 = RandomVariate[NormalDistribution[0, Sqrt[dt]], Nn];
ξ11 = RandomVariate[NormalDistribution[0, Sqrt[dt]], Nn];
ξ12 = RandomVariate[NormalDistribution[0, Sqrt[dt]], Nn];

In[*]:= x = ConstantArray[1, Nn + 1];
y = ConstantArray[1, Nn + 1];
z = ConstantArray[1, Nn + 1];

In[*]:= V = 1000;

```

Steady State

```
In[ ]:= VvalsSS = {V0 -> 2, V1 -> 2, V4 -> 5, kf -> 1, k -> 10, β -> 0.01, ε -> 0.1, VM2 -> 6, k2 -> 0.1,
  VM3 -> 20, m -> 2, kx -> 0.5, ky -> 0.2, kz -> 0.2, VM5 -> 30, k5 -> 0.3, kd -> 0.5, p -> 2, n -> 4};
```

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For[i = 1, i ≤ Nn, i++,
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x[[i + 1]] =
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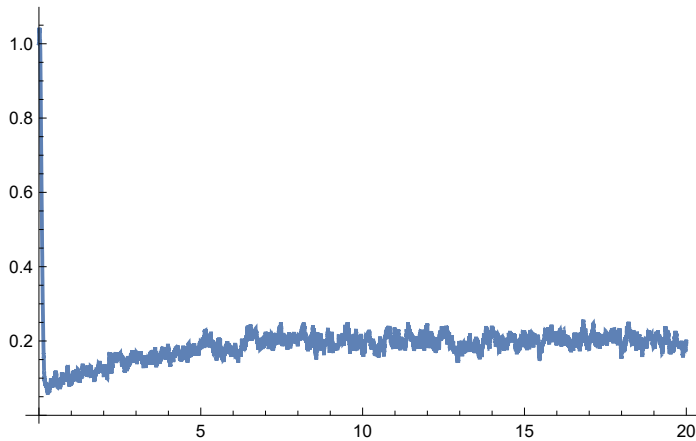
$$\left(x[[i]] + \left(V0 + V1 \beta - k x[[i]] - \frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2} + kf y[[i]] + \frac{VM3 x[[i]]^m y[[i]]^2 z[[i]]^4}{(kx^m + x[[i]]^m) (ky^2 + y[[i]]^2) (kz^4 + z[[i]]^4)} \right) dt + \frac{1}{\sqrt{V}} \left(\sqrt{V0} \xi1[[i]] + \sqrt{V1} \xi2[[i]] - \sqrt{\frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2}} \xi3[[i]] + \sqrt{\frac{VM3 x[[i]]^m y[[i]]^2 z[[i]]^4}{kx^m + x[[i]]^m ky^2 + y[[i]]^2 kz^4 + z[[i]]^4}} \xi4[[i]] + \sqrt{kf y[[i]]} \xi5[[i]] - \sqrt{kx} \xi6[[i]] \right) /. VvalsSS \right);$$

$$y[[i + 1]] = \left(y[[i]] + \left(\frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2} - kf y[[i]] - \frac{VM3 x[[i]]^m y[[i]]^2 z[[i]]^4}{(kx^m + x[[i]]^m) (ky^2 + y[[i]]^2) (kz^4 + z[[i]]^4)} \right) dt + \frac{1}{\sqrt{V}} \left(\sqrt{\frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2}} \xi7[[i]] - \sqrt{\frac{VM3 x[[i]]^m y[[i]]^2 z[[i]]^4}{kx^m + x[[i]]^m}} \xi8[[i]] - \sqrt{kf y[[i]]} \xi9[[i]] \right) /. VvalsSS \right);$$

$$z[[i + 1]] = \left(z[[i]] + \left(V4 \beta - \epsilon z[[i]] - \frac{VM5 x[[i]]^n z[[i]]^p}{(kd^n + x[[i]]^n) (k5^p + z[[i]]^p)} \right) dt + \frac{1}{\sqrt{V}} \left(\sqrt{V4 \beta} \xi10[[i]] - \sqrt{\frac{VM5 x[[i]]^n z[[i]]^p}{kd^n + x[[i]]^n}} \xi11[[i]] - \sqrt{\epsilon z[[i]]} \xi12[[i]] \right) /. VvalsSS \right);$$

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ListLinePlot[Transpose[{tT, x}], PlotRange -> All]
```

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Out[ ]:=
```



Simple Periodic Oscillations

```

In[ ]:= VvalsSPO = {V0 → 2, V1 → 2, V4 → 2, kf → 1, k → 10, β → 0.5, ε → 0.1, VM2 → 6, k2 → 0.1,
  VM3 → 20, m → 2, kx → 0.5, ky → 0.2, kz → 0.2, VM5 → 5, k5 → 1, kd → 0.4, p → 2, n → 4};
For[i = 1, i ≤ Nn, i++,
  x[[i + 1]] =
    
$$\left( x[[i]] + \left( V0 + V1 \beta - k x[[i]] - \frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2} + kf y[[i]] + \frac{VM3 x[[i]]^m y[[i]]^2 z[[i]]^4}{(kx^m + x[[i]]^m) (ky^2 + y[[i]]^2) (kz^4 + z[[i]]^4)} \right) \right. \\
    dt + \frac{1}{\sqrt{V}} \left( \sqrt{V0} \xi1[[i]] + \sqrt{V1 \beta} \xi2[[i]] - \sqrt{\frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2}} \xi3[[i]] + \right. \\
    \sqrt{\frac{VM3 x[[i]]^m y[[i]]^2 z[[i]]^4}{kx^m + x[[i]]^m ky^2 + y[[i]]^2 kz^4 + z[[i]]^4}} \xi4[[i]] + \\
    \left. \left. \sqrt{kf y[[i]]} \xi5[[i]] - \sqrt{kx} \xi6[[i]] \right) /. VvalsSPO \right);$$

    y[[i + 1]] = 
$$\left( y[[i]] + \left( \frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2} - kf y[[i]] - \frac{VM3 x[[i]]^m y[[i]]^2 z[[i]]^4}{(kx^m + x[[i]]^m) (ky^2 + y[[i]]^2) (kz^4 + z[[i]]^4)} \right) dt + \frac{1}{\sqrt{V}} \right. \\
    \left( \sqrt{\frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2}} \xi7[[i]] - \sqrt{\frac{VM3 x[[i]]^m}{kx^m + x[[i]]^m}} \xi8[[i]] - \sqrt{kf y[[i]]} \xi9[[i]] \right) /. VvalsSPO \right);$$

    z[[i + 1]] = 
$$\left( z[[i]] + \left( V4 \beta - \epsilon z[[i]] - \frac{VM5 x[[i]]^n z[[i]]^p}{(kd^n + x[[i]]^n) (k5^p + z[[i]]^p)} \right) dt + \frac{1}{\sqrt{V}} \left( \sqrt{V4 \beta} \xi10[[i]] - \right. \right. \\
    \left. \left. \sqrt{\frac{VM5 z[[i]]^p}{k5^p + z[[i]]^p} \frac{x[[i]]^n}{kd^n + x[[i]]^n}} \xi11[[i]] - \sqrt{\epsilon z[[i]]} \xi12[[i]] \right) /. VvalsSPO \right);$$


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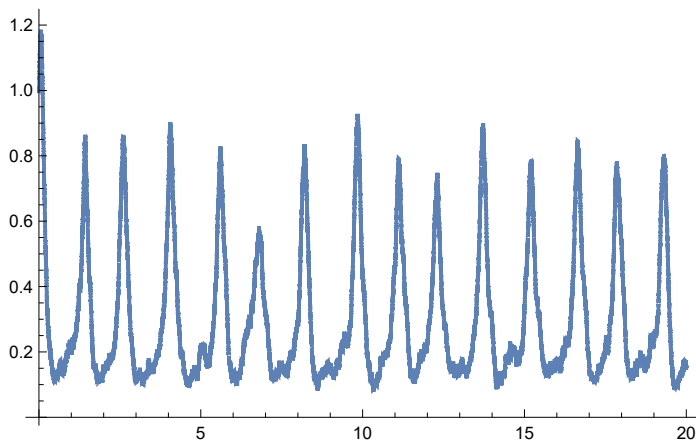
In[ ]:= ListLinePlot[Transpose[{tT, x}], PlotRange → All]

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Out[ ]:=

```



Bursting

```
In[ ]:= VvalsB = {V0 -> 2, V1 -> 2, V4 -> 2.5, kf -> 1, k -> 10, beta -> 0.46, epsilon -> 0.1, VM2 -> 6, k2 -> 0.1,
  VM3 -> 20, m -> 4, kx -> 0.3, ky -> 0.2, kz -> 0.1, VM5 -> 30, k5 -> 1, kd -> 0.6, p -> 1, n -> 2};
```

```
For[i = 1, i ≤ Nn, i++,
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```
x[[i + 1]] =
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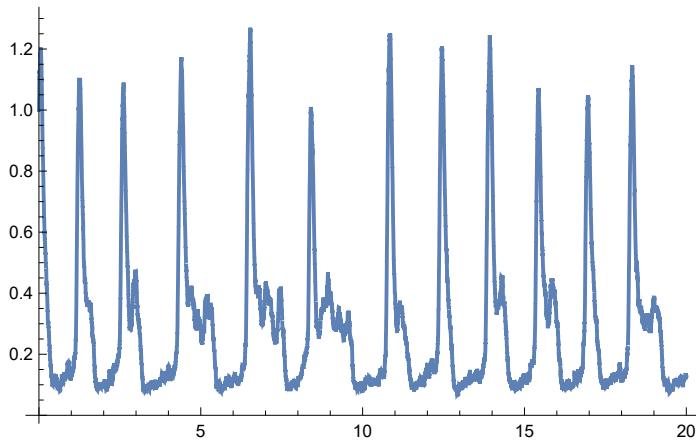
$$\left(x[[i]] + \left(V0 + V1 \beta - k x[[i]] - \frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2} + kf y[[i]] + \frac{VM3 x[[i]]^m y[[i]]^2 z[[i]]^4}{(kx^m + x[[i]]^m) (ky^2 + y[[i]]^2) (kz^4 + z[[i]]^4)} \right) dt + \frac{1}{\sqrt{V}} \left(\sqrt{V0} \xi1[[i]] + \sqrt{V1 \beta} \xi2[[i]] - \sqrt{\frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2}} \xi3[[i]] + \sqrt{\frac{VM3 x[[i]]^m y[[i]]^2 z[[i]]^4}{kx^m + x[[i]]^m ky^2 + y[[i]]^2 kz^4 + z[[i]]^4}} \xi4[[i]] + \sqrt{kf y[[i]]} \xi5[[i]] - \sqrt{kx} \xi6[[i]] \right) /. VvalsB \right);$$

$$y[[i + 1]] = \left(y[[i]] + \left(\frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2} - kf y[[i]] - \frac{VM3 x[[i]]^m y[[i]]^2 z[[i]]^4}{(kx^m + x[[i]]^m) (ky^2 + y[[i]]^2) (kz^4 + z[[i]]^4)} \right) dt + \frac{1}{\sqrt{V}} \left(\sqrt{\frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2}} \xi7[[i]] - \sqrt{\frac{VM3 x[[i]]^m}{kx^m + x[[i]]^m}} \xi8[[i]] - \sqrt{kf y[[i]]} \xi9[[i]] \right) /. VvalsB \right);$$

$$z[[i + 1]] = \left(z[[i]] + \left(V4 \beta - \epsilon z[[i]] - \frac{VM5 x[[i]]^n z[[i]]^p}{(kd^n + x[[i]]^n) (k5^p + z[[i]]^p)} \right) dt + \frac{1}{\sqrt{V}} \left(\sqrt{V4 \beta} \xi10[[i]] - \sqrt{\frac{VM5 z[[i]]^p}{k5^p + z[[i]]^p} \frac{x[[i]]^n}{kd^n + x[[i]]^n}} \xi11[[i]] - \sqrt{\epsilon z[[i]]} \xi12[[i]] \right) /. VvalsB \right);$$

```
ListLinePlot[Transpose[{tT, x}], PlotRange -> All]
```

```
Out[ ]:=
```



Chaos

`In[]:= VvalsC = {V0 → 2, V1 → 2, V4 → 3, kf → 1, k → 10, β → 0.65, ε → 13, VM2 → 6, k2 → 0.1, VM3 → 30, m → 2, kx → 0.6, ky → 0.3, kz → 0.1, VM5 → 50, k5 → 0.3194, kd → 1, p → 1, n → 4};`

`For[i = 1, i ≤ Nn, i++,`

`x[[i + 1]] =`

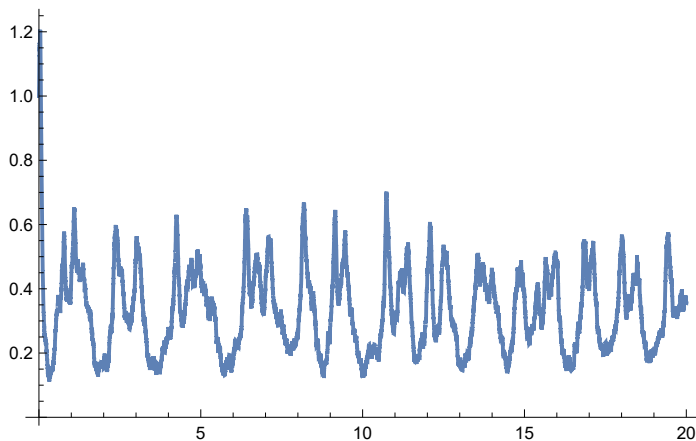
$$\left(x[[i]] + \left(V0 + V1 \beta - k x[[i]] - \frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2} + kf y[[i]] + \frac{VM3 x[[i]]^m y[[i]]^2 z[[i]]^4}{(kx^m + x[[i]]^m) (ky^2 + y[[i]]^2) (kz^4 + z[[i]]^4)} \right) \right) * \\ dt + \frac{1}{\sqrt{V}} \left(\sqrt{V0} \xi1[[i]] + \sqrt{V1 \beta} \xi2[[i]] - \sqrt{VM2 \frac{x[[i]]^2}{k2^2 + x[[i]]^2}} \xi3[[i]] + \right. \\ \left. \sqrt{VM3 \frac{x[[i]]^m}{kx^m + x[[i]]^m} \frac{y[[i]]^2}{ky^2 + y[[i]]^2} \frac{z[[i]]^4}{kz^4 + z[[i]]^4}} \xi4[[i]] + \right. \\ \left. \sqrt{kf y[[i]]} \xi5[[i]] - \sqrt{kx} \xi6[[i]] \right) /. VvalsC];$$

$$y[[i + 1]] = \left(y[[i]] + \left(\frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2} - kf y[[i]] - \frac{VM3 x[[i]]^m y[[i]]^2 z[[i]]^4}{(kx^m + x[[i]]^m) (ky^2 + y[[i]]^2) (kz^4 + z[[i]]^4)} \right) dt + \right. \\ \left. \frac{1}{\sqrt{V}} \left(\sqrt{VM2 \frac{x[[i]]^2}{k2^2 + x[[i]]^2}} \xi7[[i]] - \sqrt{VM3 \frac{x[[i]]^m}{kx^m + x[[i]]^m}} \xi8[[i]] - \sqrt{kf y[[i]]} \xi9[[i]] \right) \right) /. VvalsC];$$

$$z[[i + 1]] = \left(z[[i]] + \left(V4 \beta - \epsilon z[[i]] - \frac{VM5 x[[i]]^n z[[i]]^p}{(kd^n + x[[i]]^n) (k5^p + z[[i]]^p)} \right) dt + \frac{1}{\sqrt{V}} \right. \\ \left. \left(\sqrt{V4 \beta} \xi10[[i]] - \sqrt{VM5 \frac{z[[i]]^p}{k5^p + z[[i]]^p} \frac{x[[i]]^n}{kd^n + x[[i]]^n}} \xi11[[i]] - \sqrt{\epsilon z[[i]]} \xi12[[i]] \right) \right) /. VvalsC];$$

`In[]:= ListLinePlot[Transpose[{tT, x}], PlotRange → All]`

`Out[]:=`



Period Doubling Sequences

```

In[ ]:= VvalsPDS = {V0 → 2, V1 → 2, V4 → 3, kf → 1, k → 10, β → 0.7, ε → 13, VM2 → 6, k2 → 0.1,
  VM3 → 30, m → 2, kx → 0.6, ky → 0.3, kz → 0.1, VM5 → 50, k5 → 0.3194, kd → 1, p → 1, n → 4};
For[i = 1, i ≤ Nn, i++,
  x[[i + 1]] =
    
$$\left( x[[i]] + \left( V0 + V1 \beta - k x[[i]] - \frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2} + kf y[[i]] + \frac{VM3 x[[i]]^m y[[i]]^2 z[[i]]^4}{(kx^m + x[[i]]^m) (ky^2 + y[[i]]^2) (kz^4 + z[[i]]^4)} \right) \right. \\
    dt + \frac{1}{\sqrt{V}} \left( \sqrt{V0} \xi1[[i]] + \sqrt{V1 \beta} \xi2[[i]] - \sqrt{\frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2}} \xi3[[i]] + \right. \\
    \sqrt{\frac{VM3 x[[i]]^m y[[i]]^2 z[[i]]^4}{kx^m + x[[i]]^m ky^2 + y[[i]]^2 kz^4 + z[[i]]^4}} \xi4[[i]] + \\
    \left. \left. \sqrt{kf y[[i]]} \xi5[[i]] - \sqrt{kx} \xi6[[i]] \right) /. VvalsPDS \right);$$

    y[[i + 1]] = 
$$\left( y[[i]] + \left( \frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2} - kf y[[i]] - \frac{VM3 x[[i]]^m y[[i]]^2 z[[i]]^4}{(kx^m + x[[i]]^m) (ky^2 + y[[i]]^2) (kz^4 + z[[i]]^4)} \right) dt + \frac{1}{\sqrt{V}} \right. \\
    \left( \sqrt{\frac{VM2 x[[i]]^2}{k2^2 + x[[i]]^2}} \xi7[[i]] - \sqrt{\frac{VM3 x[[i]]^m}{kx^m + x[[i]]^m}} \xi8[[i]] - \sqrt{kf y[[i]]} \xi9[[i]] \right) /. VvalsPDS \right);$$

    z[[i + 1]] = 
$$\left( z[[i]] + \left( V4 \beta - \epsilon z[[i]] - \frac{VM5 x[[i]]^n z[[i]]^p}{(kd^n + x[[i]]^n) (k5^p + z[[i]]^p)} \right) dt + \frac{1}{\sqrt{V}} \left( \sqrt{V4 \beta} \xi10[[i]] - \right. \right. \\
    \left. \left. \sqrt{\frac{VM5 z[[i]]^p}{k5^p + z[[i]]^p} \frac{x[[i]]^n}{kd^n + x[[i]]^n}} \xi11[[i]] - \sqrt{\epsilon z[[i]]} \xi12[[i]] \right) /. VvalsPDS \right);$$


```

```

In[ ]:= ListLinePlot[Transpose[{tT, x}], PlotRange → All]

```

```

Out[ ]:=

```

