

**Exercise 2.** If  $f$  is iso, so is  $f^{-1}$ .

*Proof.* An arrow  $a \xrightarrow{F} b$  is iso iff there exists an arrow  $b \xrightarrow{G} a$  such that

$$F \circ G = \mathbf{1}_b \quad G \circ F = \mathbf{1}_a \quad (1)$$

For  $a \xrightarrow{f} b$  an iso arrow, the above equations are satisfied if we set  $F = f$  and  $G = f^{-1}$ . But they are also satisfied if we set  $F = f^{-1}$  and  $G = f$ , so that  $f^{-1}$  is an iso arrow  $b \rightarrow a$  with  $f$  as its inverse.

□