

**Exercise 1.** Every identity arrow is iso.

*Proof.* Let  $\mathbf{1}_a$  be the identity arrow for an object  $a$ . The identity laws applied to arrows  $f, g: a \rightarrow a$  give:

$$\mathbf{1}_a \circ f = \mathbf{1}_a \quad g \circ \mathbf{1}_a = \mathbf{1}_a$$

Setting  $g = \mathbf{1}_a$  in the first equality and  $f = \mathbf{1}_a$  in the second yields

$$g \circ f = \mathbf{1}_a \quad g \circ f = \mathbf{1}_a$$

which is the definition of  $f$  and  $g$  being iso from  $a$  to  $a$ . Since  $f = g = \mathbf{1}_a$ , we conclude that  $\mathbf{1}_a$  is iso.

□