Exercise 1: Ap Part a) Basic Op et's have two lists of word a = ["spark", "rdd", "pyth b = ["operation", "apache	Syed Pache Spark Perations on R ds as follows: hon", "context", "create	Exercise Sh Wasif Murtaza Basics Resilient Dist ", "class"]		
from operator import from pyspark.sql im from collections im from pyspark.sql.fu import matplotlib.g from pyspark.sql.fu from datetime import from datetime import import dateutil from pyspark.sql.tg from pyspark.sql.tg from collections im	rt add mport functions as mport Counter unctions import ud pyplot as plt unctions import me rt date rt date rt datetime ypes import * mport Window	s F	uld be remained in the results of join operated as _stddev, col	tions.
<pre>import statistics from itertools impo # storing session of sc= SparkContext.ge sc SparkContext Spark UI /ersion //aster AppName</pre>	<pre>ort chain context in variabl etOrCreate() v2.3.0 local[*] PySparkShell</pre>			
<pre>print('a_tuple:',a_ b = ["operation", ' for rdd converting for rd</pre>	uterJoin and full(and b. Then I converted both be list. Then I created two RI ", "python", "conting list to tuple (a, list(range(1, luple)) "apache", "scala", and list to tuple	OuterJoin operate but hist into list of tuple DDs with both tuple list. Document of tuple list. Document of tuple list. Document of tuple list. Document of tuple list.		number a
	_tuple) th rdds lize(a_tuple) ize(b_tuple)), ('rdd', 2), ('pyth', 1), ('apache', 2), er join of a_rdd w a_rdd.rightOuterJo Join:',right_oute to list	non', 3), ('contex , ('scala', 3), (' with b_rdd pin(b_rdd) er_join.collect(
print('Right Outer Right Outer Join: [('p 1)), ('apache', (None, Right Outer Join List: # taking full outer full_outer_join= (a print('Full Outer of # converting back to full_outer_join_lis print('Full Outer of Full Outer Join: [('py ('parallel', (None, 5) ('operation', (None, 1)	Join List:', right parallel', (None, 5)) ('partition', ['parallel', 'lambo r join of a_rdd wi a_rdd.fullOuterJoi Join:', full_outer_ to list st = full_outer_jo Join List:', full_o ython', (3, None), (), ('lambda', (None, 1)), ('apache', (None	couter_join_lis ('lambda', (Nor (None, 6))] da', 'scala', 'ope th b_rdd (n(b_rdd)) join.collect()) vin.map(lambda x outer_join_list. ('spark', (1, None (4)), ('class', (6, 2)), ('partition	<pre>st.collect()) ne, 4)), ('scala', (None, 3)), ('oper eration', 'apache', 'partition'] st:x[0]) collect()) e)), ('context', (4, None)), ('create (6, None)), ('rdd', (2, None)), ('scalar) on', (None, 6))]</pre>	e', (5, ala', (N
'operation', 'apache', 2. Using map and rall a and b.	reduce functions haracter in both rdd with h st a and b lize(a) ize(b) dds n(b_rdd)	to count how	many times the character "s" aand then taking union of count Rdds. Reduce	appea
a', 'parallel', 'parti Count of s in all a an Total count of s: 4 B. Using aggregate and b.	<pre>imap(lambda x:x.cou in all a and b:',c ith reduce t_rdd.reduce(add) of s: ',total_cou ', 'rdd', 'python', ' ition'] nd b: [1, 0, 0, 0, 0, 0, 0]</pre>	ent('s')) count_rdd.collec	e', 'class', 'operation', 'apache', '	rs in al
# parallelizing list a_rdd = sc.parallelit b_rdd = sc.parallelit # combining both recordd = a_rdd.union print('Combined RDI # defining seqOp and	st a and b lize(a) ize(b) dds n(b_rdd) D:',c_rdd.collect(rgument which calc cal_result, list_e)) culates count in element: (local_	result + list_element.count('s')	
another_local_resulted rdd_c_agg = rdd_c. print('Count of s v Combined RDD: ['spark'a', 'parallel', 'particount of s with aggreger Part b) Basic Op	.aggregate(0, seq with aggregate:',r ', 'rdd', 'python', ' ition'] gate: 4	[Op, combOp) dd_c_agg) context', 'create DataFrames	result: (some_local_result + e', 'class', 'operation', 'apache', ' First creating DataFrames from the dataset	
course	on(sc.parallelize(dob fin October 14, 1983 eptember 26, 1980 June 12, 1982 April 5, 1987 November 1, 1978 17 February 1981 Ch 1 January 1984 January 13, 1978 26 December 1989 30 December 1989 30 December 1987 June 12, 1975 July 2, 1985 July 22, 1980 7 February 1986 May 18, 1987	data)) rst_name last_name Alan Joe Martin Genberg Athur Watsor Anabelle Sanberg Kira Schommer	e points s_id -++ e 10 1 g 17 2 n 16 3 g 12 4 r 11 5 m 10 6 d 14 7 1 10 8 n 15 9 s 11 10 z 12 11 k null 12 y 13 13 r 12 14	
Business Machine Learning Data Analytics Business Data Analytics Calculating mean	August 10, 1984 16 December 1990 null 7 March 1980 June 2, 1985 Value(s) in colur lect (_mean(col('po	Martin Steele Colin Martinez Bridget Twair Darlene Mills Zachary null mn points by the control of the colon of the co	e 7 16 z 9 17 n 6 18 s 19 19 1 10 20	
df.printSchema Mean: 11.7368421052631	dob fir October 14, 1983 eptember 26, 1980 June 12, 1982 April 5, 1987 7 November 1, 1978 17 February 1981 Ch 1 January 1984 January 13, 1978 26 December 1989 30 December 1987 June 12, 1975 July 2, 1985 July 22, 1980 7 February 1986 May 18, 1987	Alan Joe Martin Genberg Athur Watsor Anabelle Sanberg Kira Schommer Aristian Kiriam Barbara Ballarg John null Marcus Carsor Marta Brooks Holly Schwartz April Black Irene Bradley Mark Weber Rosie Normar	e points s_id -++ e 10 1 g 17 2 n 16 3 g 12 4 r 11 5 m 10 6 d 14 7 1 10 8 n 15 9 s 11 10 z 12 11 k 11 12 y 13 13 r 12 14 n 9 15	
Data Analytics Business Data Analytics Data Analytics Cound method DataFramering, points: bigint, oint column is bigint that	16 December 1990 null 7 March 1980 June 2, 1985 me.printSchema of Dat s_id: bigint]> ts why 11.7 is converted value(s) in colur alue in dob column e="unknown", subset	taFrame[course: st to 11. mn dob and co nn with unknown =["dob"])		
df=df.na.fill(value df.show() +	e="", subset=["la dob fin dob fin October 14, 1983 eptember 26, 1980 June 12, 1982 April 5, 1987 November 1, 1978 17 February 1981 Ch 1 January 1984 January 13, 1978 26 December 1989 30 December 1989 30 December 1987 June 12, 1975 July 2, 1985 July 22, 1980 7 February 1986 May 18, 1987	st_name"]) Alan Joe Martin Genberg Athur Watsor Anabelle Sanberg Kira Schommer nristian Kiriam Barbara Ballarg John Marcus Carsor Marta Brooks Holly Schwartz April Black Irene Bradley Mark Weber Rosie Normar	-++ e points s_id -++ e 10 1 g 17 2 n 16 3 g 12 4 r 11 5 m 10 6 d 14 7 - 10 8 n 15 9 s 11 10 z 12 11 k 11 12 y 13 13 r 12 14 n 9 15	
Business Machine Learning Data Analytics Business Data Analytics Business Data Analytics Machine Learning Business	August 10, 1984 16 December 1990	Martin Steele Colin Martinez Bridget Twair Darlene Mills Zachary	of dates, e.g. October 14, 198 OD-MM-YYYY format where DI as and four digits for year resp	D, MM
date = date # converting formatedDate return form else: # if unknow return 'unk # updating dob colu df=df.withColumn("column("	eutil.parser.parse ng datetime to str teStr = date.strft matedDateStr wn value comes it known' umn with udf dob", changeFormat(c(date) ring of required rime("%d-%m-%Y") returns unknown df.dob)) +	++ s_id	
Computer Science 26 Graphic Design 12 Graphic Design 05 Psychology 01 Business 17 Machine Learning 01 Deep Learning 13 Machine Learning 26 Physics 30 Data Analytics 12 Computer Science 02 Computer Science 02 Psychology 07 Informatics 18 Business 10 Machine Learning 16 Data Analytics Business 07 Data Analytics 02 Data Analytics 02	6-09-1980 Martin 2-06-1982 Athur 5-04-1987 Anabelle 1-11-1978 Kira 7-02-1981 Christian 1-01-1984 Barbara 3-01-1978 John 6-12-1989 Marcus 0-12-1987 Marta 2-06-1975 Holly 2-07-1985 April 2-07-1986 Mark 3-05-1987 Rosie 0-08-1984 Martin 6-12-1990 Colin unknown Bridget 7-03-1980 Darlene 2-06-1985 Zachary	Genberg 17 Watson 16 Sanberg 12 Schommer 11 Kiriam 10 Ballard 14 10 Carson 15 Brooks 11 Schwartz 12 Black 11 Bradley 13 Weber 12 Norman 9 Steele 7 Martinez 9 Twain 6 Mills 19 10	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 10 11 15 16 17 18 19 20	
<pre># creating a udf for @udf("int") def calculateAge(bit if(birthDateStr today = dat # convertin birthDate = # if todays age = today birthDate.day)) else: age = 0</pre>	<pre>irthDateStr): r!='unknown'): te.today() ng string to date = datetime.strptim</pre> s month and date i	e from dob for e		
return age # creating age colu df=df.withColumn("a df.show() course Lumanities and Art 14 Computer Science 26 Graphic Design 12 Graphic Design 05 Psychology 01 Business 17 Machine Learning 01 Deep Learning 13 Machine Learning 26 Physics 30 Data Analytics 12 Computer Science 02 Computer Science 02	age", calculateAge (dob first_name dob firs		s_id age ++ 1 38 2 41 3 40 4 35 5 43 6 41	
Computer Science 22 Psychology 07 Informatics 18 Business 10 Machine Learning 16 Data Analytics Business 07 Data Analytics 02 10 10 10 10 10 10 10	Trene	Bradley 13 Weber 12 Norman 9 Steele 7 Martinez 9 Twain 6 Mills 19 10 Horse for good part of the standard deviation of the standard deviat	13 41 14 36 15 35 16 37 17 31 18 0 19 42 20 37 +++ performed students in the clas ation of all points, then we upon Annex 1 for a tutorial on how the	date h
<pre>df = df.withColumn # calculating mean meanPoints = df.sel print('mean of poin # adding points to df = df.withColumn std of points: 3.24605 mean of points: 11.7 # defining udf for @udf("int") def updatePoints(points) > mean</pre>	<pre>("std",F.lit(stdPo and adding in a c lect(_mean(col('po nts:',meanPoints) df ("mean",F.lit(mean 502314756554 updating points oints,std,mean): ean + std :</pre>	column ints')).alias(':	mean')).collect()[0]['mean']	
# removing extra codd=df.drop("std","mdf.show() t	points and passing points", updatePoin olumns mean") dob first_name	ts(df.points,df	++ s_id age +++ 1 38 2 41 3 40 4 35 5 43 6 41	
Business 17 Machine Learning 01 Deep Learning 13 Machine Learning 26 Physics 30 Data Analytics 12 Computer Science 02 Computer Science 22 Psychology 07 Informatics 18 Business 10 Machine Learning 16 Data Analytics Business 07 Data Analytics 02 Create a histogra	7-02-1981 Christian 1-01-1984 Barbara 3-01-1978 John 6-12-1989 Marcus 0-12-1987 Marta 2-06-1975 Holly 2-07-1985 April 2-07-1980 Irene 7-02-1986 Mark 8-05-1987 Rosie 0-08-1984 Martin 6-12-1990 Colin unknown Bridget 7-03-1980 Darlene 2-06-1985 Zachary	Kiriam 10 Ballard 14 10 Carson 20 Brooks 11 Schwartz 12 Black 11 Bradley 13 Weber 12 Norman 9 Steele 7 Martinez 9 Twain 6 Mills 20 10 Held of the created of the country of the created of the country of the co	6 41 7 38 8 44 9 32 10 34 11 47 12 37 13 41 14 36 15 35 16 37 17 31 18 0 19 42 20 37	
<pre># Plotting the hist plt.hist(points_arr plt.xlabel('Points' plt.ylabel('BinCour plt.title(r'Histogr plt.show()</pre>	<pre>togram. ray, bins=5, densi ') nts')</pre>			
Exercise 2: Ma Spark For this exercise you will us	on dataset with ratings contains data in the forn ormations and actions.	Recommel et available at https:/	nder Dataset with Apa //grouplens.org/datasets/ movielens/10m/ to 5. Specifically, you will be working with Tag::Timestamp". You have to solve following	. The mo
schema = StructType().add("U tags=spark.read.opt tags.show() ++	UserID", IntegerTyp tions (delimiter=': Tag Time excellent! 12151 politics 11882 satire 11882 hanks 11882 ryan 11882 action 11882 spoof 11882 star wars 11882	').schema(schem+ estamp + 184630 263867 263867 263835 263835 263835 263755 263756 263880 263880	'MovieID", IntegerType(), True).add ha).csv("tags.dat")	("Tag"
20 3033 20 7438 20 7438 20 7438 21 55247 21 55253 25 50 25 6709 31 65 31 546 strang 31 1091 1091	star wars 11882 bloody 11882 kung fu 11882 R 12050 NC-17 12050 Kevin Spacey 11661 Johnny Depp 11621 buddy comedy 11882 gely compelling 11882 catastrophe 11882 ows On for a user can Typically, an inaction. Your task is	263880 263801 263801 263801 281506 081488 101426 147221 263759 263741 + be defined as a continuous description to separate out		termir
<pre># creating new data # collect_list is of merge same userID if session_list_df = t F.collect_list('Time # ordering dataframe</pre>	aframe and adding collecting timesta rows tags.withColumn('tmestamp').over(w)) me with userIds session_list_df.or ow() + mp_list + 184630]	userIds and cor amps of each use imestamp_list', .groupBy('UserI	rresponding timestamps in one rower in the window, then grouped by	userI.
15 [12151	184630] 1188 1205 1166 1188 1215 1188 1215 1188 160415] 691425] 1165 1188 1148 1188 1148 1148 1148 1140 1140			
<pre>previous one and as @udf(returnType=Arr def createSession(t session_list=[] for i in range(</pre>	<pre>ssign session rayType(IntegerTyp timeStampList):] (len(timeStampList)</pre>	<pre>de())) de())): de is less than deStampList[i-1] desion</pre>	and for each user , compare time 1800 seconds then session is not) < 1800):	
session_list_previous_session_list_df=session_list_df=session_list_df.shoots	st.append(session) ession=session _list dding session_list ssion_list_df.with ow() mp_list session_list 184630 1188 [1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1	column which had a column ("session of the column c	nas session ids for each tag n_list",createSession(session_lis	t_df.t
21 [1205081488, 1 25 [1162147221, 1 31 [1188263644, 1 32 [11647 39 [1188263764, 1 48 [1215135517, 1 49 [1188264095, 1 75 [11621 78 [11766 109 [1165554764, 1 127 [1188265347, 1 133 [1188265347, 1 133 [1188265375, 1 146 [1147948639, 1 147 [1162188631, 1 170 [11622 175 [1188441420, 1 181 [1188266123, 1 190 [1140031954, 1 190 1140031954, 1	1205 1166 1188 [1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1	[1, 1] [1, 2] 1, 1, 1] [1, 1, 1] 1, 1, 1] 1, 1 [1, 1] 1, 1 1, 1 1, 1, 1] 4, 4 [1, 1] [1, 2] 1, 1, 1] 2, 2 +		
session_list_df.fil [1, 1, 1, 1, 1, 1, 1, 1, 2]. Once you have a or each user session # creating udf for @udf (returnType=Arm def CountFrequency # count each set	lter(session_list_ 1, 1, 1, 1, 2, 2, 3, all the tagging secon calculating frequerayType(IntegerType) (sessionList): ession id in list ssionList) values()) creating new column	df.UserID==109) , 3, 3, 4, 5, 6, 7 essions for each ency from sessione()))	h user, calculate the frequency	
session_list_df=session_list_df.sho +	ssion_list_df.with ow() +	[1] 1, 1, 1] [1] 1, 1 [1] [1] 1, 1 [1] [1] 1, 1 [1] [1] 1, 1 [1] [1] 1, 1 [1]		ession_I
133 [1188265375, 1 146 [1147948639, 1 147 [1162188631, 1 170 [11622 175 [1188441420, 1 181 [1188266123, 1 190 [1140031954, 1 ++	1188 [1, 1, 1, 1, 1, 1, 1, 2, 3, 3, 3, 1, 1, 1, 2, 2, 3, 3, 1, 1, 1, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,	1, 1, 1] 4, 4 [1, 1, 2, [1, 1] [1], [2] 1, 1, 1] 2, 2 [3] c each session f df.UserID==109)	[5] , 12, 2, [2] [1] [1, 1] [4] 3, 3, 17, 3]	
<pre>@udf(FloatType()) def CalculateMean(f sum= 0 for i in range() sum += free return sum/(ler session_list_df=ses</pre>	<pre>freqList): (len(freqList)): qList[i] n(freqList)) ssion_list_df.with calculating std of reqList):</pre>	.Column("mean_Fr	requency_each_user",CalculateMean	(session
<pre>if (len (freqList</pre>	istics.stdev(freqL ssion_list_df.with lect(['UserID','fr tagging mean_Frequence [1] [12] [2] [1, 1] [5] [1] [5]	Column("std_Fre requence_of_tagg	Frequency_each_user	-
39 48 49 75 78 109 [11, 2, 3, 1, 127 133 146 [1, 1, 2, 12, 147 170 175 181 190 [3, 3, 12] 190 [3, 3, 13] 4 showing mean of 19	[5] [2] [15] [1] [1] 1, [26] [5] 2, [2] [1] [1, 1] [4] 17, 3]	5.0 2.0 15.0 1.0 1.0 2.7777777 26.0 5.0 4.948949 2.0 1.0 1.0 4.0 6.5	0.0 0.0 0.0 0.0 0.0 3.2702363 0.0 0.0	.ch_use
<pre># showing std of r session_list_df.fil 3.2702362537384033 4. Find a mean and # converting freque frequency_list = list(chain.from_ite x).collect())) # calculating std a stdPoints = statist</pre>	d standard deviate ence_of_tagging to erable (session_lise and adding in a contics.stdev(frequenter)	df.UserID==109) tion of the tag 2d list and th t_df.select('fr	.collect()[0]['std_Frequency_eac ging frequency for across user men converting it to ID requence_of_tagging').rdd.flatMap	rs.
<pre># calculating mean meanPoints = statis session_list_df = s</pre>		thColumn("std_a	across_user",F.lit(stdPoints))	
UserID mean Frequency	stics.mean(frequen session_list_df.wi lect(['UserID','me	cy_list) thColumn("mean_ ean_Frequency_ea	_across_user",F.lit(meanPoints)) ach_user','std_Frequency_each_use	er','mea

++	Select(['UserID', 'mean_Frequency_each_user', 'st	+ wo_std_from_mean
<pre># showing users w session_list_df.f</pre>	26.0 22.07944597647594 7.17114764172684 5.0 22.07944597647594 7.17114764172684 4.948949 22.07944597647594 7.17114764172684 2.0 22.07944597647594 7.17114764172684 1.0 22.07944597647594 7.17114764172684 4.0 22.07944597647594 7.17114764172684 6.5 22.07944597647594 7.17114764172684 6.5 22.07944597647594 7.17114764172684 7.0 22.07944597647594 7.17114764172684 8.20 22.07944597647594 7.17114764172684 12.0 22.07944597647594 7.17114764172684 12.0 22.07944597647594 7.17114764172684 12.0 22.07944597647594 7.17114764172684 10.0 22.07944597647594 7.17114764172684	.select(['UserID','mean_Fred
133 146 147 170 175 181 190 +	5.0 22.07944597647594 7.17114764172684 4.948949 22.07944597647594 7.17114764172684 2.0 22.07944597647594 7.17114764172684 1.0 22.07944597647594 7.17114764172684 4.0 22.07944597647594 7.17114764172684 6.5 22.07944597647594 7.17114764172684 6.5 22.07944597647594 7.17114764172684 7.0 22.07944597647594 7.17114764172684 8.5 22.07944597647594 7.17114764172684 8.5 22.07944597647594 7.17114764172684 8.5 22.07944597647594 7.17114764172684 8.5 22.07944597647594 7.17114764172684 8.5 22.07944597647594 7.17114764172684 8.5 22.07944597647594 7.17114764172684	1 1 1 1 1 1 1

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1988, 2000, 2014, 2024, 2039, 2040, 2053, 2075, 2098, 2102, 2108,	
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