

Lab Course Machine Learning

Exercise Sheet 7

December 22th 2021

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Exercise 0: Dataset Preprocessing

```
import numpy as np
import math
from sklearn.preprocessing import PolynomialFeatures
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
from matplotlib import cm
from matplotlib.ticker import MultipleLocator
from sympy import symbols, diff
import pandas as pd
import math
import warnings
import itertools
import matplotlib.colors as colors
from matplotlib.cm import ScalarMappable
from scipy.spatial.distance import pdist, odist
warnings.filterwarnings('ignore')
```

Reading datasets from archive

```
# for checking which dataset in dataset dictionary has missing values
def getNaNDataSets(datanDict):
    nanDataSets = {}
    for key in datanDict:
        data = np.array(datanDict.get(key))
        is_null = False
        for i in range(1, len(data)):
            array_sum = np.sum(data[i])
            # if sum is null then array as null values
            array_has_nan = np.isnan(array_sum)
            if (array_has_nan):
                is_null = True
        if (is_null):
            nanDataSets.append(key) # appending into list of dataset having missing values
    return nanDataSets
```

Below functions is used for getting dataframe from archive folders and merging train and test splits and finally creating a dictionary of all datasets.

```
def getDatanDict(direct):
    dataFrameDict = {}
    for dirpath, filenames in os.walk(direct):
        if len(filenames)>0:
            train = [f for f in filenames if "TRAIN" in f] # getting train file from folder
            test = [f for f in filenames if "TEST" in f] # getting test file from folder
            key = (train[0]*10 and len(test)>0):
                train[0].split('.')[0] # for the name of dataset
            #train
            dfTrain = os.path.abspath(os.path.join(dirpath, train[0])) # for complete reference of file
            dfTrain = pd.read_csv(absPathTrain, sep='\t', header=None)
            #test
            dfTest = os.path.abspath(os.path.join(dirpath, test[0])) # for complete reference of file
            dfTest = pd.read_csv(absPathTest, sep='\t', header=None)
            df = pd.concat([dfTrain, dfTest], ignore_index=True) # merging train and test dataframes
            df = df.rename(columns={'0': 'Y'})
            #normalizing
            df.loc[:, df.columns != 'Y'] = (df.loc[:, df.columns != 'Y']-df.loc[:, df.columns != 'Y'].mean())/(df.loc[:, df.columns != 'Y'].std())
            return dataFrameDict[key] = df
    return dataFrameDict
```

dframesDict = getDatanDict('Dataset')

2. Preprocess the datasets

```
nullDataSets=[]
for key in dframesDict:
    df= dframesDict.get(key)
    if (df.isnull().values.any()):
        nullDataSets.append(key)
```

Datasets with missing values.

```
nullDataSets
['AllGestureWiimoteX',
'AllGestureWiimoteY',
'DodgerLoopDay',
'DodgerLoopWeekend',
'GestureMidAirD1',
'GestureMidAirD3',
'GesturePebbleZ1',
'GesturePebbleZ2',
'MelbournePedestrian',
'PickupGestureWiimoteZ',
'ShakeGestureWiimoteZ',
'ShakeGestureWiimoteX',
'ShakeGestureWiimoteY']
```

Some timeseries in datasets have not equal length and has NAN in the end of rows. for these we have to pad zeros in. So i traversed each row from end and until i found nan i replaced it with zeros.

```
def paddingDataset(dataSetDict):
    paddedDict = dict()
    for key in dataSetDict:
        dataset = dataSetDict.get(key).to_numpy()
        indRow=0
        for row in dataset:
            if np.isnan(row):
                dataset[indRow][0]=0
            else:
                break # coming out of loop when finding non- null value
            indRow += 1
        paddedDict.update({key: dataset})
    return paddedDict
```

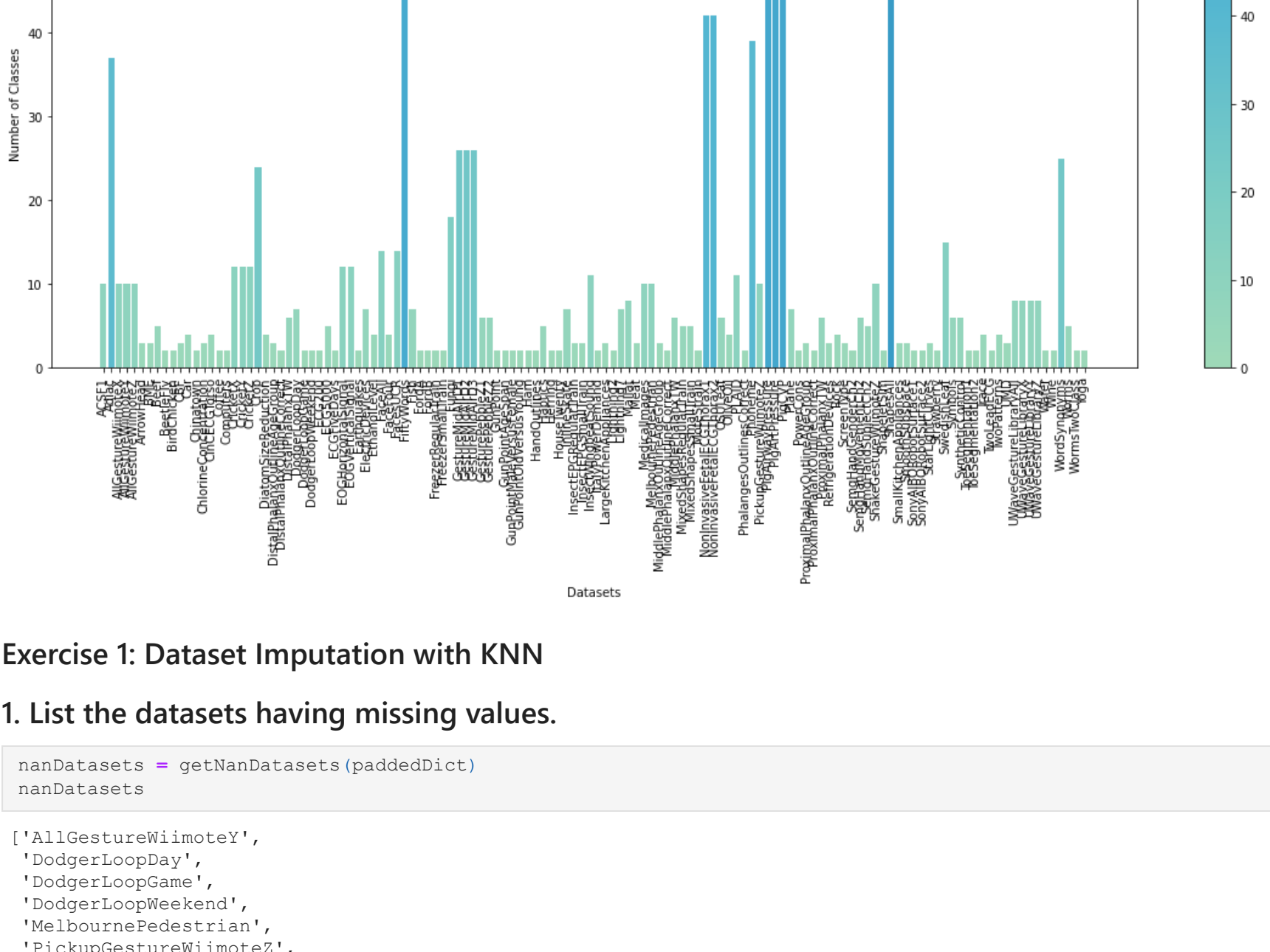
paddedDict = paddingDataset(dframesDict.copy())

Plot interesting statistics:

```
# for cmap values in range
def truncate_colormap(cmap, minval=0.0, maxval=1.0, n=100):
    new_cmap = colors.LinearSegmentedColormap.from_list(
        ('trunc({0},{1},{2},{3},{4})'.format(cmap.name, minval, maxval,
        cmap1=plt.cm.get_cmap('magma', n))
    return new_cmap
```

length of samples

```
sampleDict = {}
for key in dframesDict:
    data = dframesDict.get(key)
    sampleDict.update({key:len(data.columns)})
lists = sorted(sampleDict.items()) # sorted by key, return a list of tuples
x, y = zip(*lists) # unpack a list of pairs into two tuples
fig = plt.figure(figsize=(20,8))
ax = plt.axes()
# Reference for colormap: https://moonbooks.org/Articles/How-to-plot-a-bar-chart-with-a-colorbar-using-matplotlib
data_high_t_normalized = [x / max(y) for x in y]
my_cmap = plt.cm.get_cmap('GnBu')
new_cmap = truncate_colormap(my_cmap.copy(), 0.4, 0.7)
colorMap = new_cmap1(data_high_normalized)
sm = ScalarMappable(cmap=new_cmap1, norm=plt.Normalize(0,max(y)))
sm.set_array([])
char = plt.colorbar(sm)
char.set_label('Color', rotation=270, labelpad=25)
ax.bar(x, y, color=colorMap)
ax.set_xlabel('Datasets')
ax.set_ylabel('Length Of Samples')
plt.xticks(rotation=90)
plt.show()
```



Number of samples

```
sampleDict = {}
for key in dframesDict:
    data = dframesDict.get(key)
    sampleDict.update({key:len(data)})
lists = sorted(sampleDict.items()) # sorted by key, return a list of tuples
x, y = zip(*lists) # unpack a list of pairs into two tuples
fig = plt.figure(figsize=(20,8))
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colorMap = new_cmap1(data_high_normalized)
sm = ScalarMappable(cmap=new_cmap1, norm=plt.Normalize(0,max(y)))
sm.set_array([])
char = plt.colorbar(sm)
char.set_label('Color', rotation=270, labelpad=25)
ax.bar(x, y, color=colorMap)
ax.set_xlabel('Datasets')
ax.set_ylabel('Number Of Samples')
plt.xticks(rotation=90)
plt.show()
```



Number of classes

```
classDict = {}
for key in dframesDict:
    d = dframesDict.get(key)
    classes = d['Y'].unique()
    classDict.update({key:len(classes)})
lists = sorted(classDict.items()) # sorted by key, return a list of tuples
x, y = zip(*lists) # unpack a list of pairs into two tuples
fig = plt.figure(figsize=(20,8))
ax = plt.axes()
# Reference for colormap: https://moonbooks.org/Articles/How-to-plot-a-bar-chart-with-a-colorbar-using-matplotlib
data_high_t_normalized = [x / max(y) for x in y]
my_cmap = plt.cm.get_cmap('GnBu')
new_cmap = truncate_colormap(my_cmap.copy(), 0.4, 0.7)
colorMap = new_cmap1(data_high_normalized)
sm = ScalarMappable(cmap=new_cmap1, norm=plt.Normalize(0,max(y)))
sm.set_array([])
char = plt.colorbar(sm)
char.set_label('Color', rotation=270, labelpad=25)
ax.bar(x, y, color=colorMap)
ax.set_xlabel('Datasets')
ax.set_ylabel('Number Of Classes')
plt.xticks(rotation=90)
plt.show()
```



Exercise 1: Dataset Imputation with KNN

1. List the datasets having missing values.

```
nanDataSets = getNaNDataSets(paddedDict)
nanDataSets
['AllGestureWiimoteX',
'DodgerLoopDay',
'DodgerLoopWeekend',
'GestureMidAirD1',
'GestureMidAirD3',
'GesturePebbleZ1',
'GesturePebbleZ2',
'MelbournePedestrian',
'PickupGestureWiimoteZ',
'ShakeGestureWiimoteZ',
'ShakeGestureWiimoteX',
'ShakeGestureWiimoteY']
```

2. For each dataset with missing values, and for each feature (timestamp) of it that has missing values impute the value by calculating the mean of its nearest K neighbors.

```
# Euclidian distance (X,Y)
def eculidianDistance(X,Y):
    s_sum = 0
    counter = np.count_nonzero(np.isnan(X))
    for x, y in zip(X, Y):
        if (np.isnan(x) or np.isnan(y)): # for missing values
            s_sum = (x - y) ** 2
        # https://jakob1-learn.org/stable/modules/generated/sklearn.metrics.pairwise.nan_euclidean_distances.html
    return np.sqrt(s_sum/(len(X)/counter))
```

kNearestNeighbours() takes a dataset with missing values and impute the missing values. First it calculates n twoDimension index of missing values in original matrix. Then it puts all missing values for a row in dict with key as row number. Now we iterate through this dict, calculate distance for each key in dictionary which is row and impute each col index which is stored in value of dict. For k nearest neighbours takes values for that column index average them and impute in the missing column for that row. Repeat the process for all rows.

```
def kNearestNeighbours(K,X,null):
    X=X.null
    r,X = X.shape
    # remove of all NaN in array
    indicesDict = dict()
    indexNaN = np.argwhere(np.isnan(X))
    for i in indexNaN:
        if i[0] not in indicesDict:
            indList = []
            indList.append(i[1])
            indicesDict.update({i[0]:indList})
        else:
            indList = indicesDict[i[0]]
            indList.append(i[1])
            indicesDict.update({i[0]:indList})
    # for each missing value in that row, finding average of nearest rows for that timestamp
    for i in col:
        for j in range(k):
            if ~np.isnan(X[ind(sortedDist[j][0])[0]]):
                sum = sum + X[ind(sortedDist[j][0])[0]][c]
            average = sum / k
            X[ind][c] = average
    return X
```

```
def transformNaN(dataDict, k): # calling kNearestNeighbours for every dataset with missing value
    dDict = dataDict
    listOfNaNDataSets = getNaNDataSets(dataDict)
    for d in listOfNaNDataSets:
        data = dataDict.get(d)
        listDict = {}
        array_sum = np.sum(data)
        array_has_nan = np.isnan(array_sum)
        if (array_has_nan):
            X = kNearestNeighbours(k, data.copy())
            dDict.update({d:X})
    return dDict
```

finalDict = transformNaN(paddedDict.copy(),5)

After imputation, we get no dataset with missing values.

```
nanDataSets = getNaNDataSets(finalDict)
nanDataSets
[]
```

3. Next, train a K-Nearest Neighbour classifier (pseudo-code given in slides) with majority voting and euclidean distance to maximize accuracy on the validation split by tuning K via grid search.

For this part, we need to split the dataset into train, validation and test according to given ratios of 0.7,0.15,0.15 respectively.

```
def splitDataFrames(npArray):
    train, valid, test = 0.7, 0.15, 0.15
    d = pd.DataFrame(npArray)
    d = d.rename(columns={'0': 'Y'})
    data_train = []
    data_valid = []
    data_test = []
    np.unique(d['Y'])
    classes = (d['Y']).unique()
    for c in classes:
        rowWithC = d[d['Y'] == c]
        if len(rowWithC)>0:
            data_train = np.concatenate((data_train, rowWithC[0:math.floor(len(rowWithC)*0.7)].to_numpy()), axis=0)
        else:
            data_train = np.concatenate((data_train, rowWithC[math.floor(len(rowWithC)*0.7):math.floor(len(rowWithC)*0.85)].to_numpy()), axis=0)
        if len(data_valid)>0:
            data_valid = np.concatenate((data_valid, rowWithC[math.floor(len(rowWithC)*0.7):math.floor(len(rowWithC)*0.85)].to_numpy()), axis=0)
        if len(data_test)>0:
            data_test = np.concatenate((data_test, rowWithC[math.floor(len(rowWithC)*0.85):].to_numpy()), axis=0)
    return np.array(data_train), np.array(data_valid), np.array(data_test)
```

```
splitDict = dict()
for key in finalDict:
    valueList = list()
    data_train, data_valid, data_test = splitDataFrames(finalDict.get(key).copy())
    valueList.append(data_train)
    valueList.append(data_valid)
    valueList.append(data_test)
    splitDict.update({key: valueList})
nanDataSets = getNaNDataSets(splitDict)
nanDataSets
[]
```

kNearestNeighboursClassifier() takes train data and validation data splits for each dataset. For each validation point calculates its distance for each training points and for k closest training points check with majority prediction for those points and assign it as predicted value and compute accuracy.

```
def kNearestNeighboursClassifier(k, trainData, validationData):
    r,c = validationData.shape
    count = 0
    for v in validationData:
        distInd = []
        for t in trainData:
            dist = eculidianDistance(v[1],t[1])
            distInd.append((int(dist),dist))
            ind = max(distInd, key=lambda x:x[1], argsort=1)
            sortedDist = distInd[ind[0]:ind[0]+k].argsort()
            predList = []
            for j in range(k):
                vPredict = max(distInd[ind[0]+j][0], key=lambda x:x[0])
                vPredict = max(predList, key=predict.count)
                if (vPredict == v[0]):
                    count+=1
            accuracy = (count/c)*100
    return (accuracy)
```

```
def kTuningClassifier(dataDic, kGrid):
    dDict = dataDic
    kList = list(range(1,6))
    for key in dataDic:
        data = dataDic.get(key)
        bestacc = 0
        bestk = kGrid[0]
        for k in kGrid:
            accuracy = kNearestNeighboursClassifier(k, data[0], data[1])
            if (accuracy>bestacc):
                bestacc = accuracy
                bestk = k
            kDict.update({key:np.array([bestk, bestacc])})
    return kDict
```

```
dList = dict(list(splitDict.items()))[5]
kNList = list(range(1,6))
kNDict = kTuningClassifier(dList, kNList)
kDict
{'ACSP1': array([1., 80.]),
'Adic': array([1., 62.06896552]),
'AllGestureWiimoteX': array([1., 64.66666667]),
'AllGestureWiimoteY': array([1., 75.33333333]),
'AllGestureWiimoteZ': array([1., 75.33333333]),
'ArrowWeald': array([100., 1.]),
'Beet': array([100., 1.]),
'BirdChiken': array([100., 1.]),
'Brussels': array([100., 1.]),
'Chebyshev': array([100., 1.]),
'Cityblock': array([100., 1.]),
'Cosine': array([100., 1.]),
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