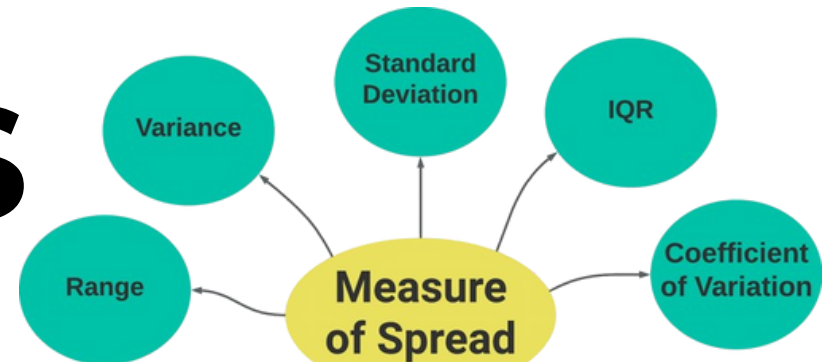


STATISTICS

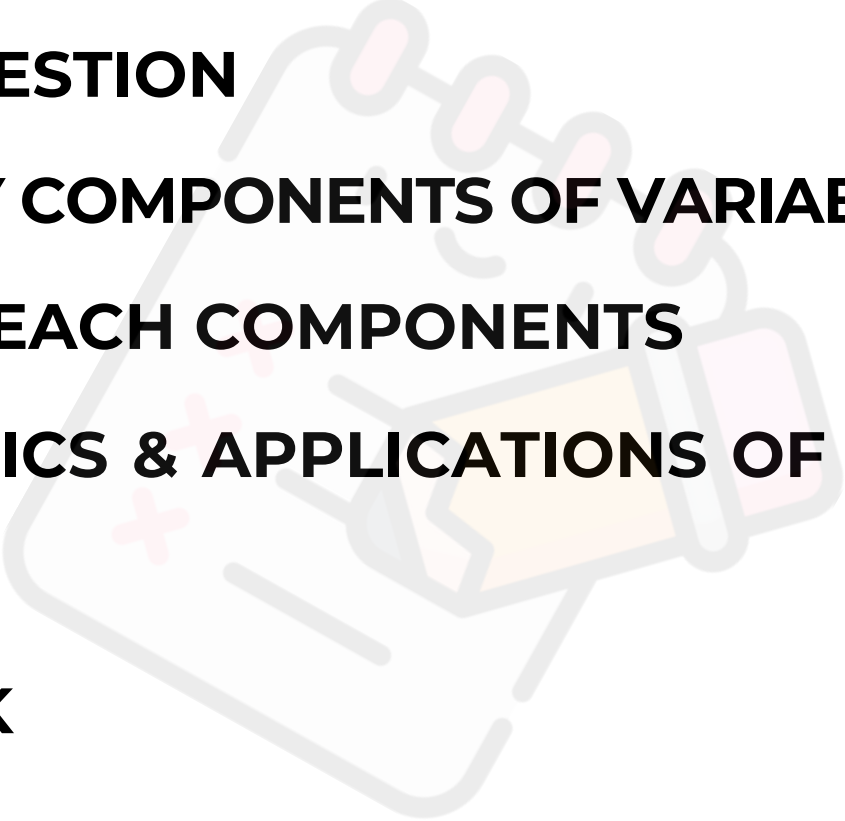

DESCRIPTIVE STATISTICS



Variability Part-2






Agenda

- **INTERVIEW QUESTION**
 - **REMAINING KEY COMPONENTS OF VARIABILITY**
 - **GET TO KNOW EACH COMPONENTS**
 - **CHARACTERISTICS & APPLICATIONS OF EACH COMPONENTS**
 - **PRACTICE TASK**
- 
- 

- 
- 
- **Interview Question** : Ok so **Standard Deviation** is simply the under root of **Variance**, then why do we square the deviations when calculating variance ?



- Remember this guy from my **previous post**, let's help him
 - Let's find out **why we do use square method** ,while calculating deviations or variability ???
- 

- Let's understand first why we are squaring to calculate deviation
- Example :

Data : 10,12,14,16,18

Step 1 - Mean Calculation Result = 14

Step 2 - Calculate Deviation from the mean for each datapoint

$10 - 14 = -4$, $12 - 14 = -2$, $14 - 14 = 0$, $16 - 14 = 2$, $18 - 14 = 4$

Step 3 - Sum the Deviation(**without squaring**) :

$-4 + (-2) + 0 + 2 + 4 = 0$



- **Observation** : The sum of the deviations is 0, even though the data points are clearly spread out.
- **Reason** : Negative and Positive values cancelled out each other.



Solution.....

Approach 1 : Mean Absolute Deviation (MAD)

Calculate the absolute value (modulus) of the deviations

Step 2 - Calculate **Absolute Deviation** from the mean for each datapoint

$$|10 - 14| = 4, \quad |12 - 14| = 2, \quad |14 - 14| = 0, \quad |16 - 14| = 2, \quad |18 - 14| = 4$$

Step 3 - Sum the **Absolute Deviations**

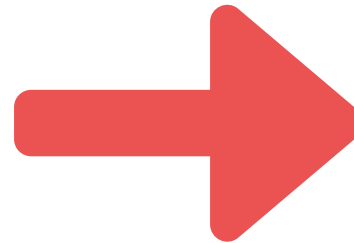
$$4 + 2 + 0 + 2 + 4 = 12$$

Step 4 - Mean Absolute Deviation

$$12/5 = 2.4 \quad \checkmark$$



So why
don't we
use this ???



WHY

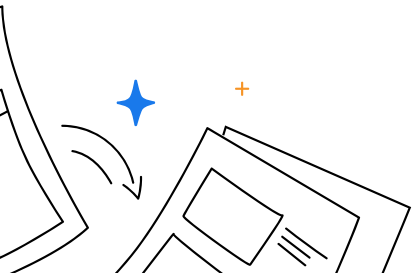
MAD is not used

- **Less Sensitivity to Outliers:** MAD is less sensitive to outliers, which can be a drawback if outliers are important to your analysis.
- **(V.IMP) Non-differentiability:** The absolute value function is not differentiable at zero, which can complicate mathematical operations, particularly in optimization problems or calculus-based methods. This makes MAD less convenient for more advanced statistical modeling and analysis compared to variance and standard deviation.
- **Lack of Relation to Normal Distribution:** Many statistical techniques, particularly those based on the normal distribution (like confidence intervals and hypothesis testing), rely on variance and standard deviation. MAD does not have the same direct relationship with these concepts, making it less suitable in these contexts.

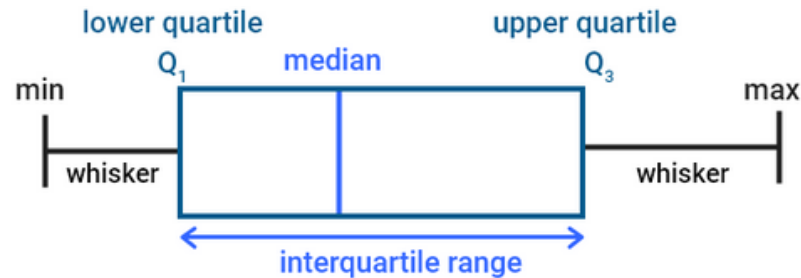


Let's Continue our Journey and explore remaining components of Variability :

- **Interquartile Range (IQR)**
- **Coefficient of Variation (CV)**



5 NUMBER SUMMARY



Minimum: The smallest data point in the dataset.

Q1 (First Quartile): The median of the lower half of the dataset (25th percentile).

Median (Q2 or Second Quartile): The middle value of the dataset (50th percentile).

Q3 (Third Quartile): The median of the upper half of the dataset (75th percentile).

Maximum: The largest data point in the dataset.

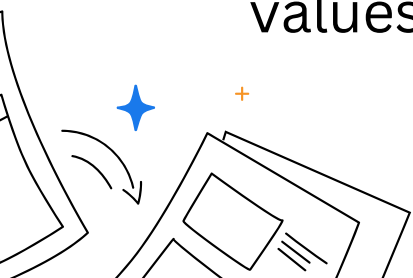


INTERQUARTILE RANGE (IQR)

- Interquartile Range (IQR) is **derived from the five-number summary**, which represents the range within which the central **50% of a dataset** lies.
- It is calculated as the difference between the third quartile (Q3) and the first quartile (Q1):

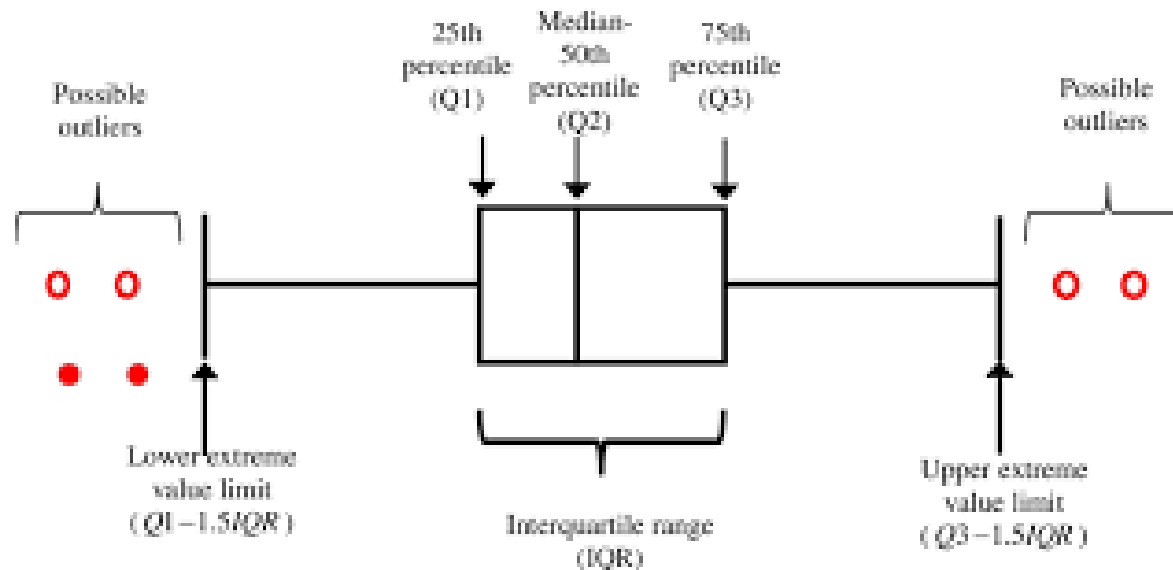
$$\text{IQR} = Q3 - Q1$$

- IQR is a **robust measure of variability** because it only considers the middle 50% of the data, ignoring extreme values (outliers).



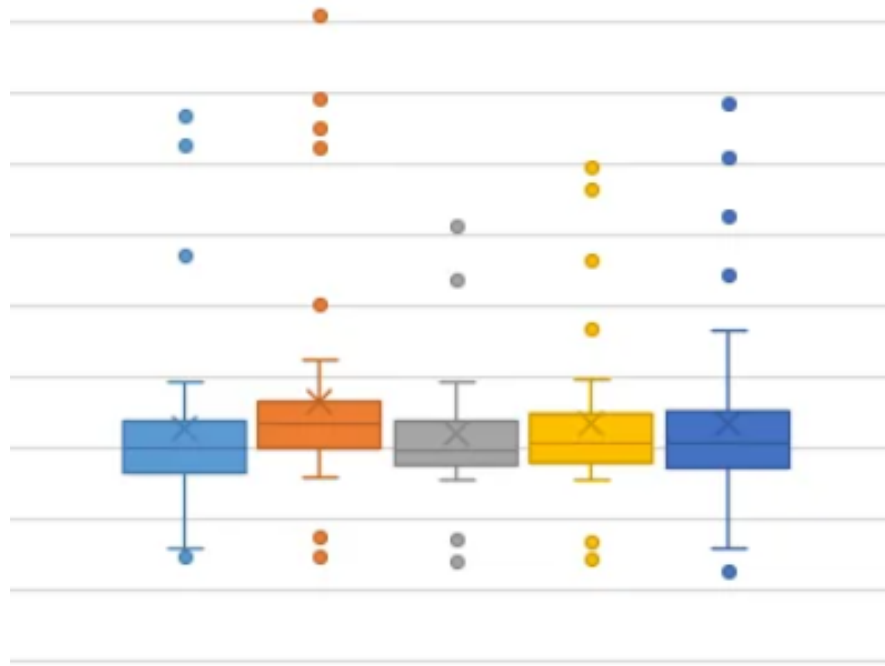
APPLICATION OF IQR

- **Identifying Outliers:** Data points that lie **below $Q1 - 1.5 \times IQR$** or **above $Q3 + 1.5 \times IQR$** are often considered outliers.



APPLICATION OF IQR

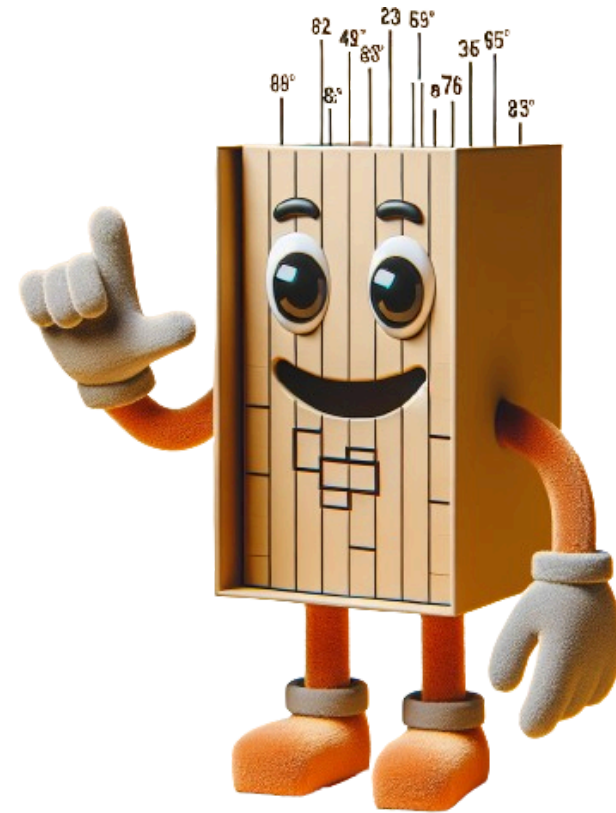
- **Comparison of Data** : Useful for comparing the spread of different datasets visually using **BOXPLOT**



**THANK YOU BRO FOR
SHOWING ME OUTLIERS
IN A GLANCE, SAVED
LOT OF MY TIME**






Data Analyst



BOX PLOT

COEFFICIENT OF VARIATION (CV)

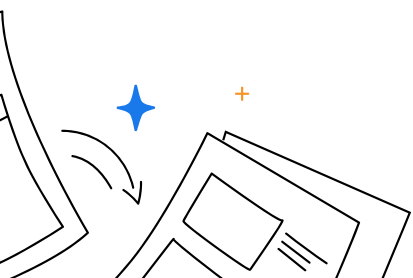

$$\text{Coefficient of Variation Formula} = \frac{\text{Standard Deviation}}{\text{Mean}}$$


- Coefficient of Variation (CV) is a statistical measure of the **relative variability** of data points in a dataset.
- The CV allows for the **comparison of the degree of variation** between different datasets, even if they have **different units or widely different means**.



APPLICATION OF CV

- **Comparing Risk:** In finance, the CV is often used to assess the risk-to-return ratio of an investment. A higher CV indicates more risk relative to the expected return.
- **Quality Control:** In manufacturing, the CV is used to assess the consistency of processes or product quality.
- **Unlike standard deviation,** which is an **absolute measure**, the CV provides a **relative measure** of variability in relation to the mean.



TASK FOR YOU

- Calculate 5 Number Summary for this data and also find out potential outliers :
2,3,5,7,8,10,11,13,14,15,18,19,21,22,25,28,30,100,105,110
- Utilize these 2 buddies :



THANK YOU

**Share your thoughts and
feedback !!**

