DATA 621: Homework 1 (Group 2)

Moneyball Linear Regression

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Assignment Objective

In this assignment, we analyze and model a baseball dataset containing multi-year game statistics for different teams. The objective is to build a multiple linear regression model on the training data to predict the number of wins for the team. We can only use the variables given to us (or variables that we derive from the variables provided).

Data

There are 2 datasets provided - The Moneyball training dataset contains 17 columns and 2276 rows. Each record in the Money Ball training dataset represents a professional baseball team from the years 1871 to 2006 inclusive. Each record has the performance of the team for the given year, with all of the statistics adjusted to match the performance of a 162 game season. For this assignment, the target variable in the dataset is TARGET WINS.

Below is a short description of the variables of interest in the data set:

Purpose of Analysis

The purpose of the analysis is to find which of the predictors have significant ability to explain the variation in the response variable (number of wins by a team), and to make a prediction for all the records provided in the test data set.

Method

The method used is a multiple linear regression model on the training data to predict the number of wins for the team.

Data Exploration

The first variable in the above table (INDEX) was dropped from the dataset due to the fact that it is mearly a row identifier, and has no impact on the target variable (TARGET_WINS).

Summary Statistics

The first step in our data exploration was to compile summary statistics to give us some insight into the data prior to preparing the data for modeling. To make the variable names more readable, we removed the "TEAM_" prefix from each variable.

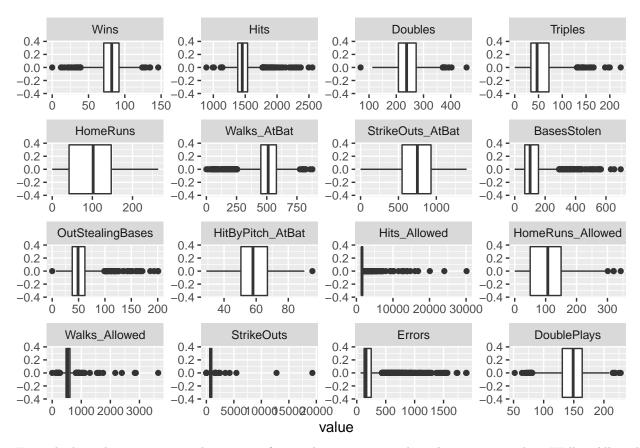
##	Wins	Hits	Doubles	Triples
##	Min. : 0.00	Min. : 891	Min. : 69.0	Min. : 0.00
##	1st Qu.: 71.00	1st Qu.:1383	1st Qu.:208.0	1st Qu.: 34.00
##	Median : 82.00	Median:1454	Median :238.0	Median : 47.00
##	Mean : 80.79	Mean :1469	Mean :241.2	Mean : 55.25

VARIABLE NAME	DEFINITION	THEORETICAL EFFECT
INDEX	Identification Variable (do not use)	None
TARGET_WINS	Number of wins	
TEAM_BATTING_H	Base Hits by batters (1B,2B,3B,HR)	Positive Impact on Wins
TEAM_BATTING_2B	Doubles by batters (2B)	Positive Impact on Wins
TEAM_BATTING_3B	Triples by batters (3B)	Positive Impact on Wins
TEAM_BATTING_HR	Homeruns by batters (4B)	Positive Impact on Wins
TEAM_BATTING_BB	Walks by batters	Positive Impact on Wins
TEAM_BATTING_HBP	Batters hit by pitch (get a free base)	Positive Impact on Wins
TEAM_BATTING_SO	Strikeouts by batters	Negative Impact on Wins
TEAM_BASERUN_SB	Stolen bases	Positive Impact on Wins
TEAM_BASERUN_CS	Caught stealing	Negative Impact on Wins
TEAM_FIELDING_E	Errors	Negative Impact on Wins
TEAM_FIELDING_DP	Double Plays	Positive Impact on Wins
TEAM_PITCHING_BB	Walks allowed	Negative Impact on Wins
TEAM_PITCHING_H	Hits allowed	Negative Impact on Wins
TEAM_PITCHING_HR	Homeruns allowed	Negative Impact on Wins
TEAM_PITCHING_SO	Strikeouts by pitchers	Positive Impact on Wins

Figure 1: Variables of Interest

```
3rd Qu.: 92.00
                     3rd Qu.:1537
                                     3rd Qu.:273.0
                                                      3rd Qu.: 72.00
                                                              :223.00
##
    Max.
           :146.00
                             :2554
                                             :458.0
                     Max.
                                     Max.
                                                      Max.
##
##
       HomeRuns
                      Walks_AtBat
                                      StrikeOuts_AtBat BasesStolen
##
    Min.
          : 0.00
                     Min.
                            : 0.0
                                      Min.
                                              :
                                                  0.0
                                                        Min.
##
    1st Qu.: 42.00
                      1st Qu.:451.0
                                      1st Qu.: 548.0
                                                        1st Qu.: 66.0
    Median :102.00
                     Median :512.0
                                      Median: 750.0
                                                        Median :101.0
##
          : 99.61
                             :501.6
                                              : 735.6
##
    Mean
                     Mean
                                      Mean
                                                        Mean
                                                                :124.8
                      3rd Qu.:580.0
##
    3rd Qu.:147.00
                                      3rd Qu.: 930.0
                                                        3rd Qu.:156.0
           :264.00
                            :878.0
##
    Max.
                     Max.
                                      Max.
                                              :1399.0
                                                        Max.
                                                                :697.0
                                              :102
##
                                      NA's
                                                        NA's
                                                                :131
##
    OutStealingBases HitByPitch_AtBat
                                       Hits_Allowed
                                                        HomeRuns_Allowed
##
    Min.
          : 0.0
                     Min.
                             :29.00
                                       Min.
                                               : 1137
                                                        Min.
                                                               : 0.0
##
    1st Qu.: 38.0
                      1st Qu.:50.50
                                       1st Qu.: 1419
                                                        1st Qu.: 50.0
##
    Median: 49.0
                     Median :58.00
                                       Median: 1518
                                                        Median :107.0
##
    Mean
          : 52.8
                     Mean
                            :59.36
                                       Mean
                                              : 1779
                                                        Mean
                                                                :105.7
##
    3rd Qu.: 62.0
                     3rd Qu.:67.00
                                       3rd Qu.: 1682
                                                        3rd Qu.:150.0
##
    Max.
           :201.0
                     Max.
                             :95.00
                                       Max.
                                               :30132
                                                        Max.
                                                                :343.0
    NA's
           :772
                     NA's
                             :2085
##
##
    Walks Allowed
                        StrikeOuts
                                             Errors
                                                           DoublePlays
##
    Min.
           :
               0.0
                     Min.
                             :
                                  0.0
                                        Min.
                                                : 65.0
                                                          Min.
                                                                  : 52.0
##
    1st Qu.: 476.0
                      1st Qu.:
                                615.0
                                        1st Qu.: 127.0
                                                          1st Qu.:131.0
    Median : 536.5
                     Median :
                                813.5
                                        Median : 159.0
                                                          Median :149.0
##
                                                : 246.5
          : 553.0
                                817.7
                                                          Mean
                                                                  :146.4
##
    Mean
                     Mean
                             :
                                        Mean
##
    3rd Qu.: 611.0
                      3rd Qu.:
                                968.0
                                        3rd Qu.: 249.2
                                                          3rd Qu.:164.0
##
    Max.
           :3645.0
                     Max.
                             :19278.0
                                        Max.
                                                :1898.0
                                                          Max.
                                                                  :228.0
##
                     NA's
                             :102
                                                          NA's
                                                                  :286
```

From the above, we see that there are 15 predictors and 1 response variable (Wins). Of the predictors, 6 have missing values. We then plotted boxplots for all the variables to get a sense of outliers.

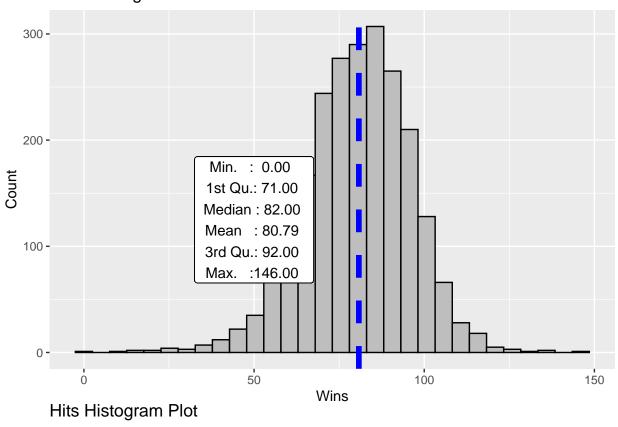


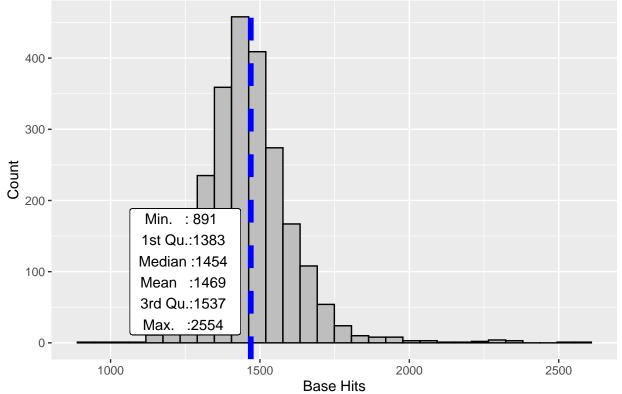
From the box plots, we can see that quite a few predictors are very skewed in nature, such as Walks_Allowed and Hits_Allowed.

Variable Distributions

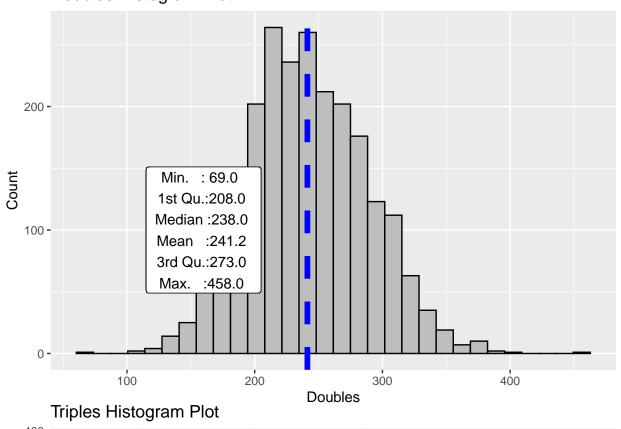
We created distribution plots for all the variables to check their shape visually and get a high-level, intuitive sense of normality.

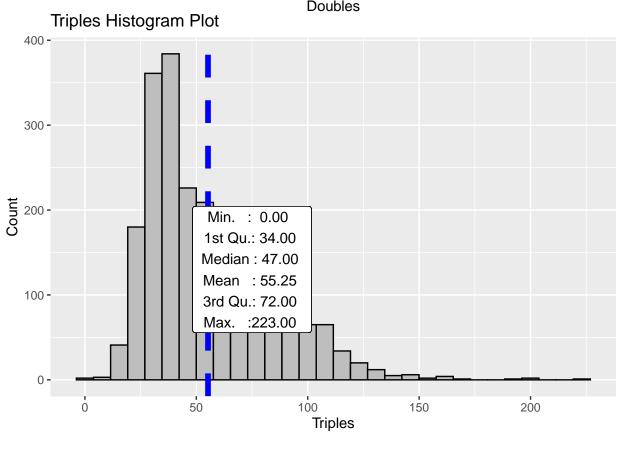




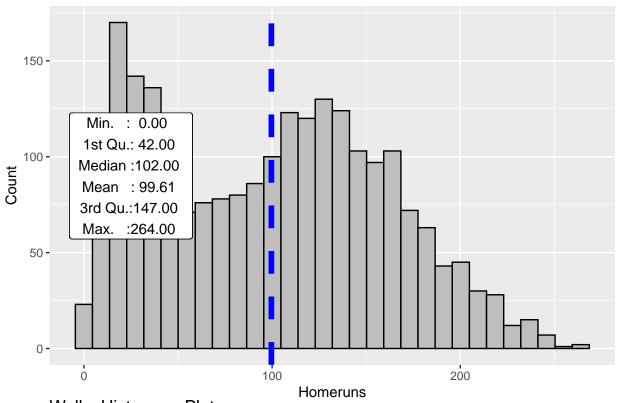


Doubles Histogram Plot

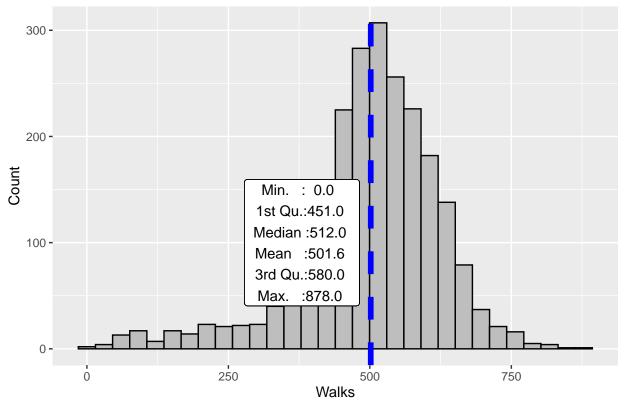




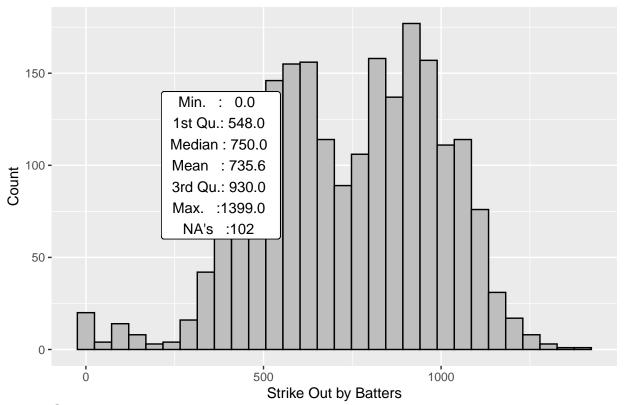
Homeruns Histogram Plot



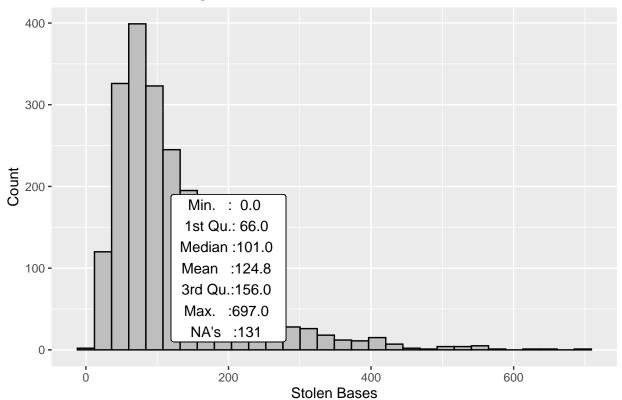
Walks Histogram Plot



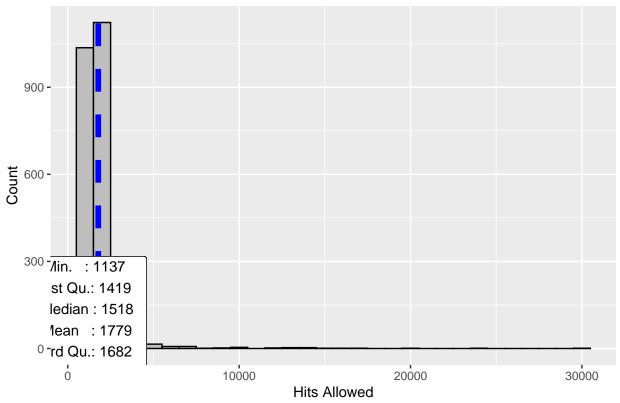
Strike Out by Batters Histogram Plot



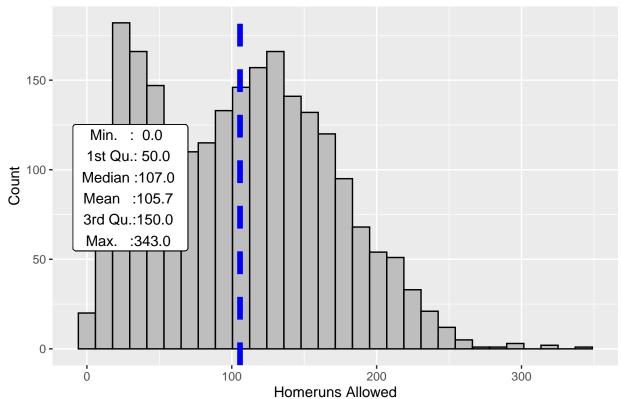
Stolen Bases Histogram Plot



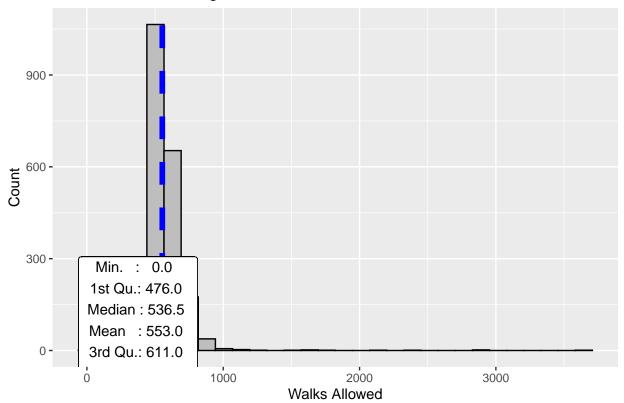
Hits Allowed Histogram Plot



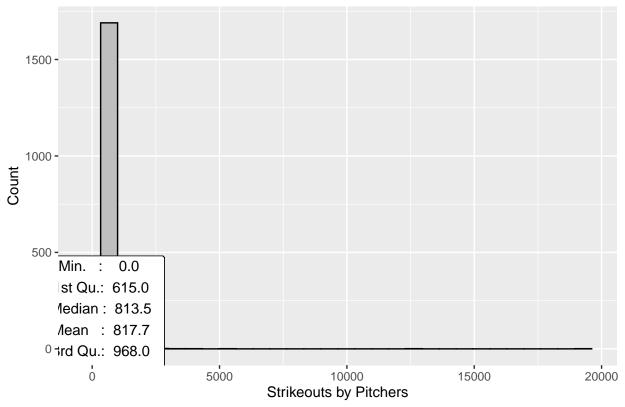
Homeruns Allowed Histogram Plot

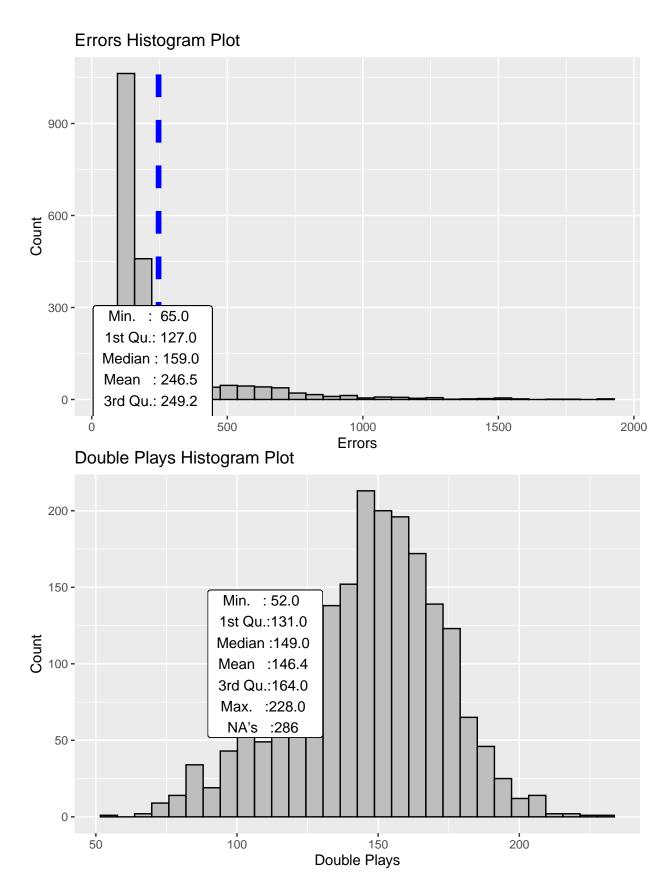


Walks Allowed Histogram Plot



Strikeouts by Pitchers Histogram Plot





The histograms provide additional confirmation that some of the variables are quite skewed. For example:

Table 1: Breakdown of Variables by Percentage of Missing Data

	X
HitByPitch_AtBat	91.61
OutStealingBases	33.92
DoublePlays	12.57
BasesStolen	5.76
StrikeOuts_AtBat	4.48
StrikeOuts	4.48
Wins	0.00
Hits	0.00
Doubles	0.00
Triples	0.00
HomeRuns	0.00
Walks_AtBat	0.00
Hits_Allowed	0.00
HomeRuns_Allowed	0.00
Walks_Allowed	0.00
Errors	0.00
	•

Errors, Triples and Walks_AtBat. There are other variables with what look like bi-modal type of distributions. For example: StrikeOuts_AtBat. There are a couple of variables that look closer to the normal distribution. For example - the response variable Wins.

Data Preparation

Missing Data - Handling NA values

We now dig deeper into the extent of missing data for the predictors.

91.61% percent of the rows are missing from the HitByPitch_AtBat variable, so we will remove this variable from the dataset completely. The percentage of missing data for the remaining variables with missing data is much less, and so excluding them from the final model could skew the results.

We now need to deal with 2 more data issues: 1) significant outliers 2) missing values

We could possibly drop rows with either of the 2 issues mentioned above, but then we may end up losing a fair amount of data. We therefore decided to remove the outliers for some of the more extreme cases, and then from the updated dataset, we imputed the missing values with the median of the respective predictor variable.

The following columns look like they have significant outliers: - Walks_Allowed - BasesStolen - StrikeOuts - Hits Allowed - Errors - Triples

Handling extreme values

##	Wins	Hits	Doubles	Triples
##	Min. : 21.00	Min. :1137	Min. :130.0	Min. : 11.0
##	1st Qu.: 72.00	1st Qu.:1385	1st Qu.:215.0	1st Qu.: 32.0
##	Median : 82.00	Median:1447	Median :244.0	Median: 42.0
##	Mean : 80.77	Mean :1457	Mean :246.9	Mean : 48.1
##	3rd Qu.: 90.00	3rd Qu.:1524	3rd Qu.:276.0	3rd Qu.: 60.0
##	Max. :120.00	Max. :1876	Max. :392.0	Max. :126.0
##				
##	HomeRuns	Walks_AtBat	StrikeOuts_AtBa	t BasesStolen

```
Min. : 4.0
                   Min.
                         :273.0
                                   Min. : 268
                                                   Min. : 18.0
   1st Qu.: 75.0
                   1st Qu.:472.0
                                   1st Qu.: 598
                                                   1st Qu.: 62.0
                                   Median: 814
   Median :118.0
                   Median :523.0
                                                   Median: 91.0
                                   Mean : 783
   Mean :115.6
                   Mean
                         :527.9
                                                   Mean :100.2
   3rd Qu.:156.0
                   3rd Qu.:585.0
                                   3rd Qu.: 955
                                                   3rd Qu.:131.0
##
   Max. :264.0
                   Max.
                          :775.0
                                   Max. :1399
                                                   Max. :289.0
##
##
                                   HomeRuns_Allowed Walks_Allowed
   OutStealingBases Hits_Allowed
                    Min. :1137
##
   Min. : 11.00
                                   Min. : 4.0
                                                   Min. :320.0
   1st Qu.: 38.00
                    1st Qu.:1407
                                   1st Qu.: 79.0
                                                   1st Qu.:487.0
   Median : 49.00
                    Median:1490
                                   Median :121.0
                                                   Median :537.0
   Mean : 52.82
                                   Mean :118.4
##
                    Mean :1510
                                                   Mean :546.2
   3rd Qu.: 62.00
                    3rd Qu.:1590
                                   3rd Qu.:158.0
                                                   3rd Qu.:601.0
##
   Max.
         :201.00
                    Max. :2069
                                   Max. :264.0
                                                   Max. :810.0
##
   NA's
          :356
##
     StrikeOuts
                        Errors
                                     DoublePlays
##
          : 301.0
                    Min. : 65.0
                                    Min. : 72.0
   Min.
   1st Qu.: 639.0
                    1st Qu.:122.0
                                    1st Qu.:136.0
   Median: 824.0
                    Median :144.0
                                    Median :151.0
##
   Mean : 805.5
                    Mean :161.9
                                    Mean :150.4
##
   3rd Qu.: 962.0
                    3rd Qu.:184.0
                                    3rd Qu.:165.0
   Max. :1481.0
                    Max. :430.0
                                    Max.
                                         :225.0
##
                                    NA's
                                          :21
##
        Wins
                         Hits
                                     Doubles
                                                     Triples
##
   Min. : 21.00
                    Min. :1137
                                   Min. :130.0
                                                  Min. : 11.0
   1st Qu.: 72.00
                    1st Qu.:1385
                                   1st Qu.:215.0
                                                  1st Qu.: 32.0
   Median: 82.00
                                                  Median: 42.0
##
                    Median:1447
                                   Median :244.0
                          :1457
##
   Mean : 80.77
                                   Mean :246.9
                                                  Mean : 48.1
                    Mean
   3rd Qu.: 90.00
                    3rd Qu.:1524
                                   3rd Qu.:276.0
                                                   3rd Qu.: 60.0
   Max. :120.00
                                   Max. :392.0
                                                  Max. :126.0
##
                    Max. :1876
##
      HomeRuns
                    Walks_AtBat
                                   StrikeOuts AtBat BasesStolen
##
         : 4.0
                   Min. :273.0
                                   Min. : 268
                                                   Min. : 18.0
   Min.
   1st Qu.: 75.0
                   1st Qu.:472.0
                                   1st Qu.: 598
                                                   1st Qu.: 62.0
##
   Median :118.0
                   Median :523.0
                                   Median: 814
                                                   Median: 91.0
   Mean :115.6
                   Mean :527.9
                                   Mean : 783
                                                   Mean :100.2
##
   3rd Qu.:156.0
                                   3rd Qu.: 955
                                                   3rd Qu.:131.0
                   3rd Qu.:585.0
                                   Max. :1399
   Max.
          :264.0
                   Max.
                         :775.0
                                                   Max. :289.0
##
   OutStealingBases Hits_Allowed
                                   HomeRuns_Allowed Walks_Allowed
                                   Min. : 4.0
   Min. : 11.00
                    Min. :1137
                                                   Min. :320.0
##
   1st Qu.: 41.00
                    1st Qu.:1407
                                   1st Qu.: 79.0
                                                   1st Qu.:487.0
   Median : 49.00
                    Median:1490
                                   Median :121.0
                                                   Median :537.0
   Mean : 52.06
                    Mean :1510
                                   Mean :118.4
##
                                                   Mean :546.2
##
   3rd Qu.: 58.00
                    3rd Qu.:1590
                                   3rd Qu.:158.0
                                                   3rd Qu.:601.0
   Max.
##
          :201.00
                    Max. :2069
                                   Max.
                                         :264.0
                                                   Max. :810.0
##
     StrikeOuts
                        Errors
                                     DoublePlays
                                    Min. : 72.0
##
   Min. : 301.0
                    Min. : 65.0
                    1st Qu.:122.0
##
   1st Qu.: 639.0
                                    1st Qu.:136.0
   Median: 824.0
                    Median :144.0
                                    Median :151.0
   Mean : 805.5
                    Mean :161.9
                                    Mean :150.4
   3rd Qu.: 962.0
                    3rd Qu.:184.0
                                    3rd Qu.:165.0
   Max.
         :1481.0
                    Max.
                         :430.0
                                    Max.
                                         :225.0
```

Table 2: Correlation of Variables to Wins

X
0.3505170
0.2177959
0.1065282
0.2269131
0.3031098
-0.0435931
0.1064962
-0.0072786
0.2476797
0.2286214
0.2883711
-0.0563730
-0.1921452
-0.0336770

Correlation between predictors, and between predictors and response variable

We now check which of the predictors are more correlated with the response variable as a mechanism to select which variables to include in the linear regression model. We also check the correlation between the predictors, since we'd like to avoid multi-collinearity.

	Wins	Hits	Doubles	Triples	HomeRuns	Walks_AtBat	StrikeOuts_AtBat	BasesStoler
Wins	1.00	0.35	0.22	0.11	0.23	0.30	-0.04	0.11
Hits	0.35	1.00	0.65	0.38	0.09	0.09	-0.37	-0.05
Doubles	0.22	0.65	1.00	-0.06	0.38	0.24	0.13	-0.13
Triples	0.11	0.38	-0.06	1.00	-0.65	-0.25	-0.72	0.26
HomeRuns	0.23	0.09	0.38	-0.65	1.00	0.40	0.71	-0.31
Walks_AtBat	0.30	0.09	0.24	-0.25	0.40	1.00	0.21	-0.15
StrikeOuts_AtBat	-0.04	-0.37	0.13	-0.72	0.71	0.21	1.00	-0.03
BasesStolen	0.11	-0.05	-0.13	0.26	-0.31	-0.15	-0.03	1.00
OutStealingBases	-0.01	0.00	-0.09	0.25	-0.34	-0.14	-0.18	0.48
Hits_Allowed	0.25	0.83	0.42	0.55	-0.18	-0.04	-0.56	0.05
HomeRuns_Allowed	0.23	0.11	0.38	-0.63	0.99	0.41	0.68	-0.32
Walks_Allowed	0.29	0.12	0.19	-0.11	0.26	0.95	0.05	-0.11
StrikeOuts	-0.06	-0.38	0.11	-0.69	0.68	0.20	0.98	-0.01
Errors	-0.19	0.11	-0.30	0.69	-0.71	-0.35	-0.65	0.36
DoublePlays	-0.03	0.17	0.18	-0.20	0.29	0.24	0.06	-0.39

##		row	column	cor	p
##	1	Wins	Hits	0.350517030	0.0000000000000000000000000000000000000
##	2	Wins	Walks_AtBat	0.303109751	0.0000000000000000000000000000000000000
##	3	Wins	Walks_Allowed	0.288371147	0.0000000000000000000000000000000000000
##	4	Wins	Hits_Allowed	0.247679739	0.0000000000000000000000000000000000000
##	5	Wins	${\tt HomeRuns_Allowed}$	0.228621353	0.0000000000000000000000000000000000000
##	6	Wins	HomeRuns	0.226913134	0.0000000000000000000000000000000000000
##	7	Wins	Doubles	0.217795857	0.0000000000000000000000000000000000000
##	8	Wins	Errors	-0.192145179	0.000000000000002220446
##	9	Wins	Triples	0.106528221	0.0000063172528612653878
##	10	Wins	BasesStolen	0.106496161	0.0000063581242804033877

Based on the p-values, we could exclude the following variables from the regression model: StrikeOuts_AtBat, DoublePlays and OutStealingBases

Check for normality of predictors

```
##
                statistic p.value
                0.9947889 0.000006590823
## Wins
## Hits
                0.9914032 0.000000009261481
## Doubles
                0.9941625 0.000001703453
## Triples
                0.9220854\ 0.0000000000000000000000000001836952
                0.985054 0.00000000001060377
## HomeRuns
## Walks_AtBat
                0.997932 0.02191374
## StrikeOuts_AtBat 0.9763299 0.000000000000001294876
## BasesStolen
                0.9449793 0.00000000000000000000000002635675
## Hits_Allowed
                0.9621216 \ 0.00000000000000000003232882
## HomeRuns_Allowed 0.9864998 0.000000000006503452
## Walks Allowed
                0.9909183 0.00000000410105
## StrikeOuts
                0.9879781 0.00000000004748167
## Errors
                0.9970724 0.001887928
## DoublePlays
```

From the above, it looks like most of the predictors are close to normality.

Model 1

Model 1 includes the remaining variables in the dataset except for the one dropped earlier due to lots of missing values.

Model 1 Statistics

Model 1 Summary Stats

```
##
## Call:
  lm(formula = Wins ~ Hits + Doubles + Triples + HomeRuns + Walks_AtBat +
##
##
       BasesStolen + Hits_Allowed + HomeRuns_Allowed + Errors +
##
       Walks Allowed + StrikeOuts + StrikeOuts AtBat + OutStealingBases +
       DoublePlays, data = mb_training_updated)
##
##
## Residuals:
       Min
                10 Median
                                3Q
                                       Max
  -32.236
           -7.006
                     0.134
                             6.904
                                    29.838
##
##
## Coefficients:
                     Estimate Std. Error t value
                                                             Pr(>|t|)
## (Intercept)
                    57.033963
                                6.166067
                                           9.250 < 0.0000000000000000 ***
## Hits
                    -0.035499
                                0.022113 -1.605
                                                               0.10860
## Doubles
                                0.009026 -6.044
                    -0.054552
                                                         0.0000000183 ***
## Triples
                     0.186643
                                0.019712
                                           9.468 < 0.0000000000000000 ***
## HomeRuns
                     0.241595
                                0.138884
                                           1.740
                                                               0.08211 .
```

```
## Walks_AtBat
                     0.200978
                                0.064606
                                           3.111
                                                               0.00190 **
## BasesStolen
                                          11.709 < 0.0000000000000000 ***
                     0.076969
                                0.006573
                     0.065127
## Hits Allowed
                                0.020521
                                           3.174
                                                               0.00153 **
## HomeRuns_Allowed -0.145831
                                          -1.082
                                                               0.27935
                                0.134764
## Errors
                    -0.124236
                                0.007365 -16.869 < 0.000000000000000 ***
## Walks Allowed
                    -0.159245
                                0.061932
                                         -2.571
                                                               0.01021 *
## StrikeOuts
                     0.001674
                                0.032200
                                           0.052
                                                               0.95854
## StrikeOuts AtBat -0.023747
                                0.033436
                                          -0.710
                                                               0.47765
## OutStealingBases -0.039104
                                0.014502
                                          -2.696
                                                               0.00707 **
## DoublePlays
                    -0.109783
                                0.012606
                                         -8.709 < 0.0000000000000000 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 10.26 on 1774 degrees of freedom
## Multiple R-squared: 0.4045, Adjusted R-squared: 0.3998
## F-statistic: 86.07 on 14 and 1774 DF, p-value: < 0.000000000000000022
```

We see that the adjusted R-squared for this model is 0.40 i.e. these predictors explain about 40% of the variability in the response variable.

Model 1 R Squared

[1] 0.4044997

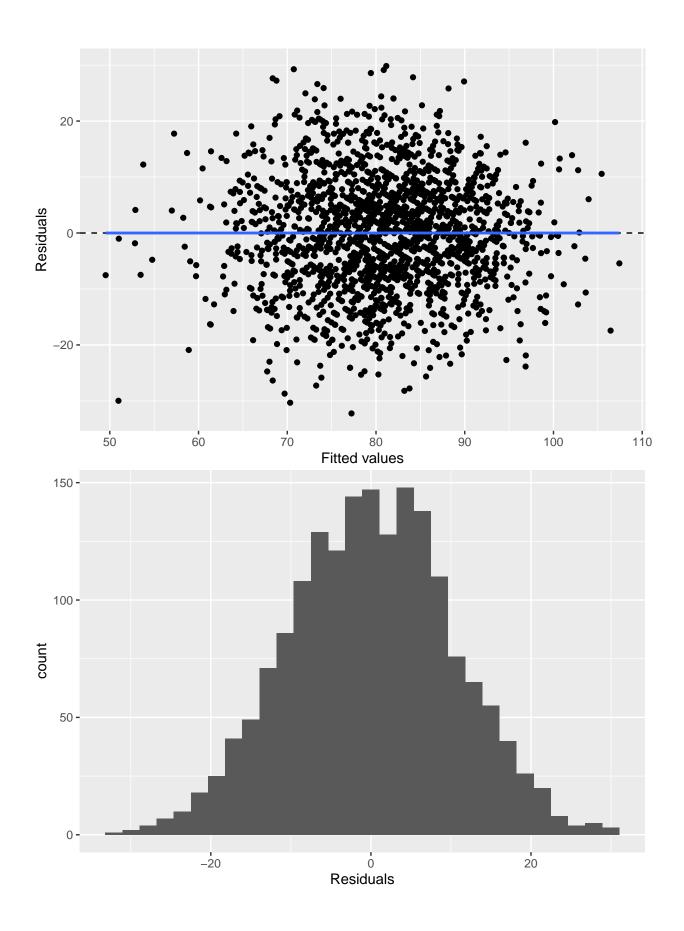
Model 1 Confidence Intervals

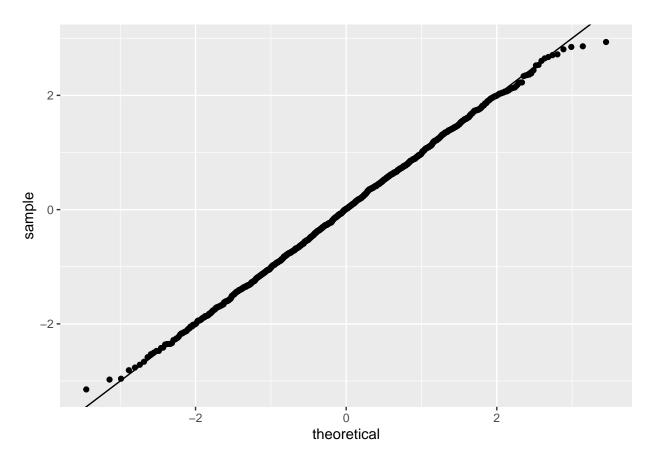
We calculate the 95% confidence intervals for each of the co-efficients and the intercept for this model.

```
2.5 %
                                      97.5 %
## (Intercept)
                    44.94044362 69.127482832
## Hits
                    -0.07886950 0.007872103
## Doubles
                    -0.07225451 -0.036849474
## Triples
                     0.14798073 0.225304552
## HomeRuns
                    -0.03079800
                                 0.513988472
## Walks_AtBat
                     0.07426677
                                 0.327689717
## BasesStolen
                     0.06407675
                                 0.089861282
## Hits_Allowed
                     0.02487963
                                 0.105374808
## HomeRuns Allowed -0.41014380
                                 0.118482229
## Errors
                    -0.13868039 -0.109790758
## Walks Allowed
                    -0.28071180 -0.037777706
## StrikeOuts
                    -0.06148025 0.064828416
## StrikeOuts AtBat -0.08932553 0.041830860
## OutStealingBases -0.06754688 -0.010661147
## DoublePlays
                    -0.13450771 -0.085058563
```

Model 1 Plots

We plot the residuals versus the fitted values - it shows that the residuals are scattered fairly evenly and there doesn't seem to be a trend. The distribution of the residuals does not seem very skewed. The same can be seen through the qq-plot as well.





Model 2

Model 2 uses stepwise regression on the variables in Model 1 to create the best performing model.

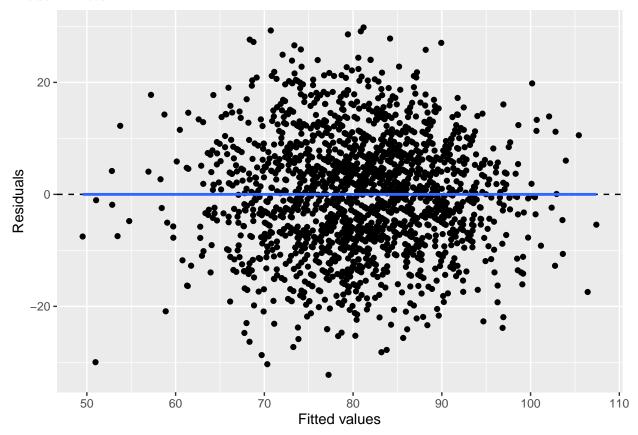
Model 2 Summary Stats

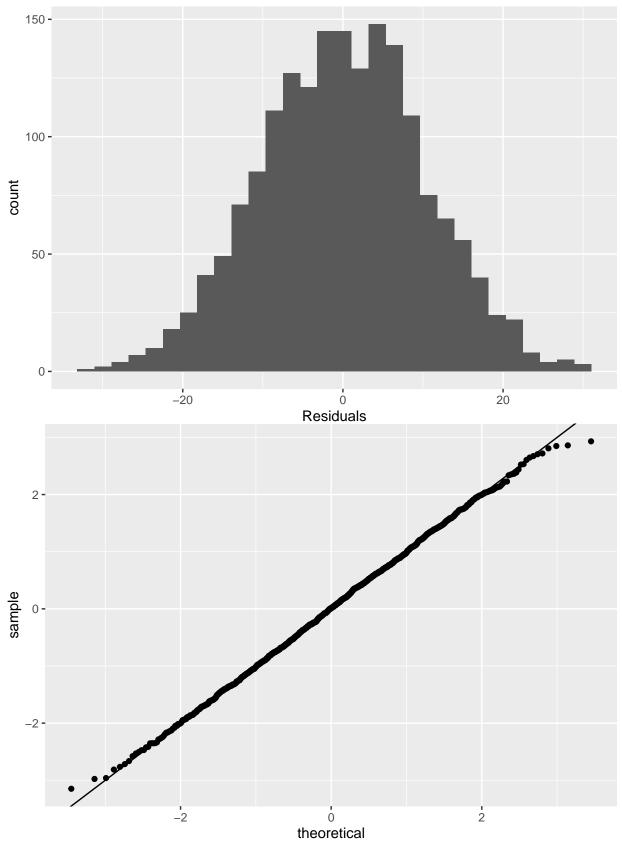
```
##
## Call:
## lm(formula = Wins ~ Hits + Doubles + Triples + HomeRuns + Walks_AtBat +
       BasesStolen + Hits_Allowed + HomeRuns_Allowed + Errors +
##
       Walks_Allowed + StrikeOuts_AtBat + OutStealingBases + DoublePlays,
##
##
       data = mb_training_updated)
##
## Residuals:
##
       Min
                1Q Median
                                 3Q
                                        Max
  -32.235 -7.017
                     0.138
                              6.908
                                     29.818
##
## Coefficients:
##
                     Estimate Std. Error t value
                                                              Pr(>|t|)
## (Intercept)
                    57.054236
                                6.151995
                                            9.274 < 0.000000000000000 ***
## Hits
                    -0.035845
                                0.021081
                                          -1.700
                                                               0.089244
## Doubles
                                          -6.046
                                                         0.0000000181 ***
                    -0.054553
                                0.009023
## Triples
                     0.186556
                                0.019637
                                            9.500 < 0.000000000000000 ***
## HomeRuns
                     0.236397
                                0.096373
                                            2.453
                                                              0.014264 *
## Walks_AtBat
                     0.200201
                                0.062835
                                            3.186
                                                              0.001467 **
                                          11.720 < 0.0000000000000000 ***
## BasesStolen
                                0.006568
                     0.076979
## Hits Allowed
                     0.065450
                                0.019551
                                            3.348
                                                              0.000832 ***
                                0.093058 -1.513
## HomeRuns_Allowed -0.140764
                                                              0.130547
```

```
## Errors
         -0.158502 0.060243 -2.631
## Walks_Allowed
                                 0.008586 **
## OutStealingBases -0.039065 0.014479 -2.698
                                 0.007039 **
          ## DoublePlays
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10.26 on 1775 degrees of freedom
## Multiple R-squared: 0.4045, Adjusted R-squared: 0.4001
```

However we see minimal impact to the R-squared value, which remains around 0.40.

Model 2 Plots





 $\label{eq:wins} \mbox{Wins} = \mbox{Target_wins}, \mbox{ Hits} = \mbox{Batting_h}, \mbox{ Doubles} = \mbox{Batting_2b}, \mbox{ Triples} = \mbox{Batting_3b}, \mbox{ HomeRuns} = \mbox{Batting_3b}, \mbox{ HomeRuns} = \mbox{Batting_3b}, \mbox{ HomeRuns} = \mbox{$

Batting_hr, Walks_AtBat = Batting_bb, StrikeOuts_AtBat = Batting_so, BasesStolen = Baserun_sb, OutStealingBases = Baserun_cs, Hits_Allowed = Pitching_h, HitByPitch_AtBat = Batting_hbp, Errors = Fielding_e, HomeRuns_Allowed = Pitching_hr, Walks_Allowed = Pitching_bb, StrikeOuts = Pitching_so, DoublePlays = Fielding_dp

Model 3

For Model 3, we create a new dataframe and derive some new variables by transforming existing predictors to include in this dataframe: - Singles is derived as the difference between all Hits and Doubles, Triples and Home Runs - Homeruns difference is the difference between home runs scored and allowed.

We also include certain variables derived on the fly in the model - for example: the ratio between Home runs allowed and scores, the product of home runs allowed and scored, the reciprocal of Double plays and the cube of the stolen basis variable.

Model 3 Summary Stats

```
##
## Call:
## lm(formula = Wins ~ Hits + Doubles + Triples + Walks_AtBat +
##
       BasesStolen + Hits_Allowed + Errors + Walks_Allowed + StrikeOuts +
       Singles + Homeruns_diff + StrikeOuts_AtBat + I(HomeRuns_Allowed/HomeRuns) +
##
       I(HomeRuns_Allowed * HomeRuns) + I(1/DoublePlays) + I(OutStealingBases^3),
##
       data = mb_training_new)
##
##
##
  Residuals:
##
                                 3Q
       Min
                1Q
                    Median
                                        Max
                                     31.025
##
   -31.826
            -7.049
                     0.066
                              6.960
##
## Coefficients:
##
                                          Estimate
                                                         Std. Error t value
## (Intercept)
                                    109.9453169993
                                                      40.2856609726
                                                                       2.729
## Hits
                                                                      0.639
                                      0.0281580282
                                                       0.0440891477
## Doubles
                                     -0.1735673380
                                                       0.0277600015
                                                                     -6.252
## Triples
                                      0.0602076781
                                                       0.0303537212
                                                                       1.984
## Walks AtBat
                                      0.1904325935
                                                       0.0648354833
                                                                       2.937
## BasesStolen
                                      0.0687665386
                                                       0.0060907199
                                                                     11.290
## Hits Allowed
                                      0.1198392065
                                                       0.0310629804
                                                                      3.858
## Errors
                                     -0.1235278847
                                                       0.0075827849 -16.291
## Walks_Allowed
                                     -0.1489662240
                                                       0.0621728192
                                                                     -2.396
## StrikeOuts
                                      0.0166499515
                                                       0.0340842858
                                                                       0.488
## Singles
                                     -0.1206931596
                                                       0.0272655274
                                                                     -4.427
## Homeruns_diff
                                     -0.2229976419
                                                       0.1427124139
                                                                      -1.563
## StrikeOuts_AtBat
                                     -0.0391231155
                                                       0.0354323522
                                                                     -1.104
## I(HomeRuns_Allowed/HomeRuns)
                                    -85.2314174131
                                                      37.8641514196
                                                                     -2.251
## I(HomeRuns_Allowed * HomeRuns)
                                     -0.0000688546
                                                       0.0000877940
                                                                     -0.784
## I(1/DoublePlays)
                                   2390.0964728930
                                                     257.2489261894
                                                                       9.291
## I(OutStealingBases^3)
                                      0.000001113
                                                       0.000004862
                                                                      0.229
##
                                                Pr(>|t|)
                                                0.006413 **
## (Intercept)
## Hits
                                                0.523126
## Doubles
                                         0.00000000505 ***
## Triples
                                                0.047462 *
## Walks AtBat
                                                0.003355 **
## BasesStolen
                                   < 0.000000000000000 ***
## Hits_Allowed
                                                0.000118 ***
```

```
< 0.00000000000000000000 ***
## Errors
## Walks_Allowed
                                              0.016678 *
## StrikeOuts
                                              0.625261
## Singles
                                        0.000010157283 ***
## Homeruns_diff
                                              0.118333
## StrikeOuts_AtBat
                                              0.269672
## I(HomeRuns_Allowed/HomeRuns)
                                              0.024509 *
## I(HomeRuns_Allowed * HomeRuns)
                                              0.432984
## I(1/DoublePlays)
                                  < 0.00000000000000000002 ***
## I(OutStealingBases^3)
                                              0.819000
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 10.25 on 1772 degrees of freedom
## Multiple R-squared: 0.4069, Adjusted R-squared: 0.4015
## F-statistic: 75.97 on 16 and 1772 DF, p-value: < 0.00000000000000022
```

We don't see much change to the R-squared value.

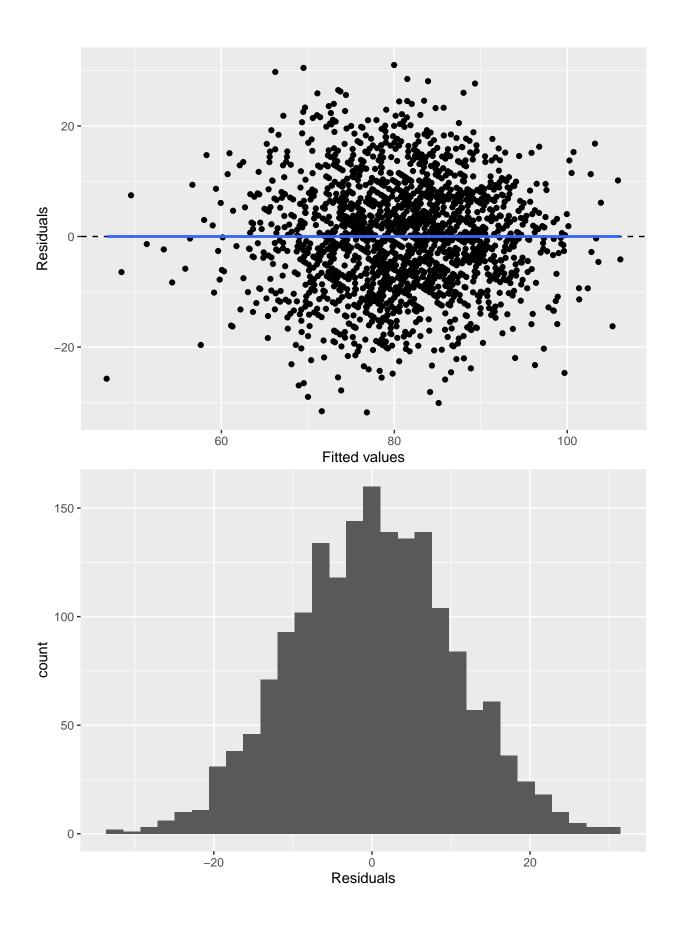
Model 3 R-Squared

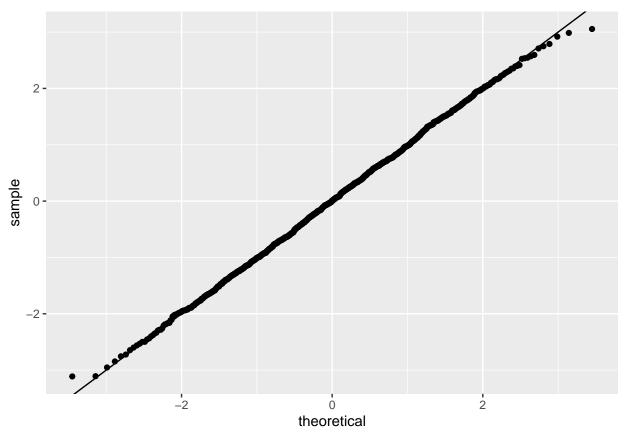
[1] 0.4068615

Model 3 Confidence Intervals

##		2.5 %	97.5 %
##	(Intercept)	30.9329035984562	188.957730400225
##	Hits	-0.0583141776004	0.114630233945
##	Doubles	-0.2280131298677	-0.119121546135
##	Triples	0.0006748143466	0.119740541945
##	Walks_AtBat	0.0632705241893	0.317594662719
##	BasesStolen	0.0568207875157	0.080712289602
##	Hits_Allowed	0.0589152700712	0.180763142896
##	Errors	-0.1384000282943	-0.108655741084
##	Walks_Allowed	-0.2709060004136	-0.027026447629
##	StrikeOuts	-0.0501996822336	0.083499585329
##	Singles	-0.1741691375868	-0.067217181579
##	Homeruns_diff	-0.5029000183358	0.056904734612
##	StrikeOuts_AtBat	-0.1086167168480	0.030370485818
##	I(HomeRuns_Allowed/HomeRuns)	-159.4945153196878	-10.968319506518
##	<pre>I(HomeRuns_Allowed * HomeRuns)</pre>	-0.0002410453595	0.000103336128
##	I(1/DoublePlays)	1885.5532182390721	2894.639727546878
##	<pre>I(OutStealingBases^3)</pre>	-0.0000008422653	0.000001064801

Model 3 Plots

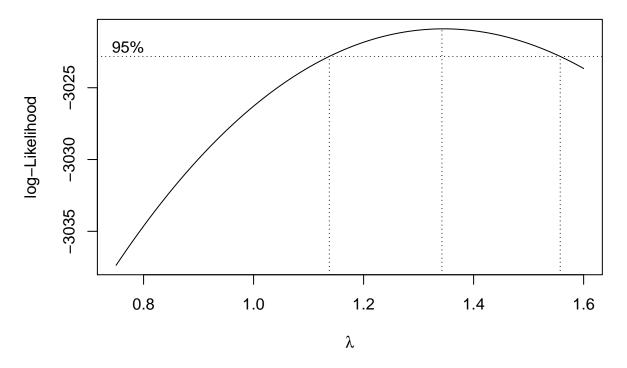




There is not much change in the scatter plot of the residuals with the fitted values, and the distribution of errors does not seem to have changed much.

Model 4 - Box Cox transformation

For our final model (Model 4), we do a Box Cox transformation on the response variable from Model 1 to see if it provides a better-fitting model. We plot the lambda and based on the plot, a lambda value of around 1.35 seems like the best value.



Model 4 Statistics

Model 4 Summary Stats

```
##
## Call:
## lm(formula = (((Wins^1.35) - 1)/1.35) ~ Hits + Doubles + Triples +
       HomeRuns + Walks AtBat + BasesStolen + Hits Allowed + HomeRuns Allowed +
##
       Errors + Walks_Allowed + StrikeOuts + StrikeOuts_AtBat +
##
       OutStealingBases + DoublePlays, data = mb_training_updated)
##
   Residuals:
##
##
        Min
                        Median
                                      3Q
                   1Q
                                              Max
             -33.262
                        -0.183
##
   -138.325
                                 31.243
                                         143.981
##
## Coefficients:
##
                       Estimate Std. Error t value
                                                                 Pr(>|t|)
## (Intercept)
                     169.730793
                                 28.446990
                                              5.967
                                                           0.00000000292 ***
                                             -1.574
## Hits
                      -0.160624
                                  0.102019
                                                                  0.11556
## Doubles
                      -0.251500
                                  0.041641
                                             -6.040
                                                           0.0000000188 ***
## Triples
                       0.859596
                                  0.090943
                                              9.452 < 0.0000000000000000 ***
## HomeRuns
                       1.088291
                                  0.640737
                                              1.698
                                                                  0.08959 .
## Walks AtBat
                       0.922916
                                  0.298057
                                              3.096
                                                                  0.00199 **
                                             11.602 < 0.0000000000000000 ***
## BasesStolen
                       0.351828
                                  0.030326
## Hits Allowed
                       0.296026
                                  0.094672
                                              3.127
                                                                  0.00180 **
## HomeRuns_Allowed
                                            -1.031
                      -0.640745
                                  0.621730
                                                                  0.30288
                                  0.033978 -16.500
## Errors
                      -0.560633
                                                    < 0.000000000000000 ***
## Walks_Allowed
                                             -2.553
                      -0.729399
                                  0.285721
                                                                  0.01077 *
## StrikeOuts
                                              0.048
                       0.007101
                                  0.148555
                                                                  0.96188
## StrikeOuts_AtBat
                      -0.110581
                                  0.154256
                                             -0.717
                                                                  0.47355
## OutStealingBases
                      -0.183480
                                  0.066905
                                             -2.742
                                                                  0.00616 **
## DoublePlays
                                             -8.638 < 0.000000000000000 ***
                      -0.502375
                                  0.058158
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 47.33 on 1774 degrees of freedom
## Multiple R-squared: 0.4028, Adjusted R-squared: 0.3981
## F-statistic: 85.46 on 14 and 1774 DF, p-value: < 0.000000000000000022</pre>
```

Model 4 R Squared

```
## [1] 0.4027743
```

We don't see much impact on R-squared, possibly because the response variable was close to normal to begin with

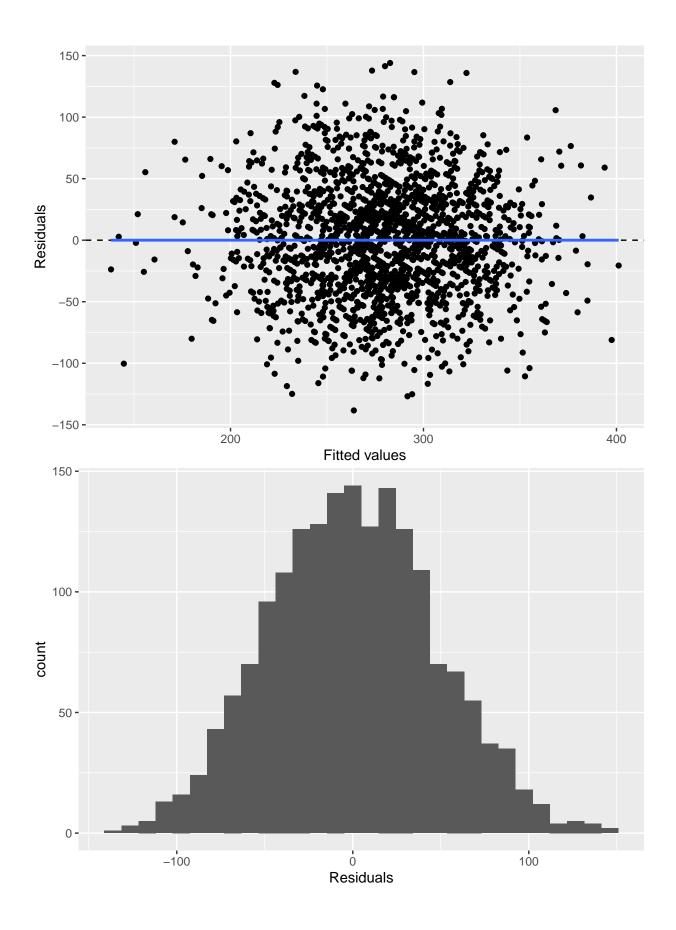
Model 4 Confidence Intervals

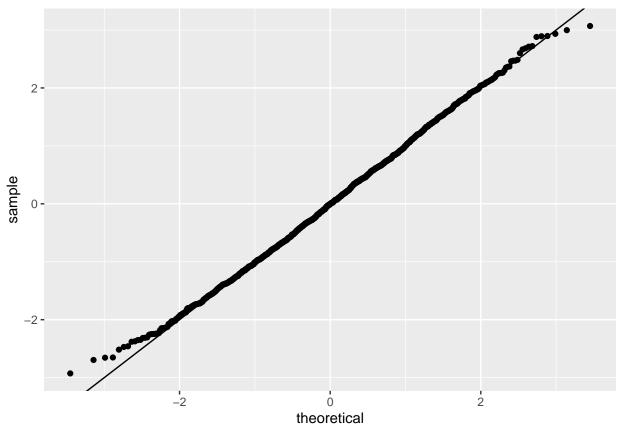
We calculate the 95% confidence intervals for each of the co-efficients and the intercept for this model.

##		2.5 %	97.5 %
##	(Intercept)	113.9376512	225.52393496
##	Hits	-0.3607137	0.03946645
##	Doubles	-0.3331698	-0.16982958
##	Triples	0.6812301	1.03796157
##	HomeRuns	-0.1683880	2.34497038
##	Walks_AtBat	0.3383354	1.50749568
##	BasesStolen	0.2923498	0.41130605
##	Hits_Allowed	0.1103447	0.48170712
##	${\tt HomeRuns_Allowed}$	-1.8601466	0.57865598
##	Errors	-0.6272741	-0.49399258
##	Walks_Allowed	-1.2897845	-0.16901436
##	StrikeOuts	-0.2842602	0.29846157
##	${\tt StrikeOuts_AtBat}$	-0.4131244	0.19196222
##	${\tt OutStealingBases}$	-0.3147009	-0.05225998
##	DoublePlays	-0.6164411	-0.38830872

Model 4 Plots

We plot the residuals versus the fitted values - it shows that the residuals are scattered fairly evenly and there doesn't seem to be a trend. The distribution of the residuals does not seem very skewed. The same can be seen through the qq-plot as well.





The residuals for this model behave similarly to the residuals from the previous model.

Model Selection

We decide to use model one for making predictions for the test dataset, since the other models do not provide a sgnificant improvement over it.

Predicting the response variable for the test dataset

We now predict the number of wins for the test data using model one.

```
##
    TEAM_BATTING_H TEAM_BATTING_2B TEAM_BATTING_3B
                                                      TEAM BATTING HR
##
           : 819
                   Min.
                           : 44.0
                                    Min.
                                            : 14.00
                                                       Min.
                                                              : 0.00
    1st Qu.:1387
                    1st Qu.:210.0
                                     1st Qu.: 35.00
##
                                                       1st Qu.: 44.50
##
    Median:1455
                    Median :239.0
                                    Median : 52.00
                                                       Median :101.00
           :1469
                                            : 55.91
##
    Mean
                    Mean
                           :241.3
                                    Mean
                                                              : 95.63
                                                       Mean
##
    3rd Qu.:1548
                    3rd Qu.:278.5
                                     3rd Qu.: 72.00
                                                       3rd Qu.:135.50
##
    Max.
           :2170
                           :376.0
                                            :155.00
                                                              :242.00
                    Max.
                                    Max.
                                                       Max.
##
##
    TEAM_BATTING_BB TEAM_BATTING_SO
                                      TEAM_BASERUN_SB TEAM_BASERUN_CS
##
           : 15.0
                     Min.
                            :
                                0.0
                                       Min.
                                              : 0.0
                                                        Min.
                                                               : 0.00
##
    1st Qu.:436.5
                     1st Qu.: 545.0
                                       1st Qu.: 59.0
                                                        1st Qu.: 38.00
##
    Median :509.0
                     Median: 686.0
                                       Median: 92.0
                                                        Median: 49.50
##
    Mean
           :499.0
                            : 709.3
                                              :123.7
                                                               : 52.32
                     Mean
                                       Mean
                                                        Mean
##
    3rd Qu.:565.5
                     3rd Qu.: 912.0
                                       3rd Qu.:151.8
                                                        3rd Qu.: 63.00
##
    Max.
           :792.0
                     Max.
                            :1268.0
                                       Max.
                                              :580.0
                                                        Max.
                                                               :154.00
##
                     NA's
                            :18
                                       NA's
                                              :13
                                                        NA's
                                                               :87
##
    TEAM_BATTING_HBP TEAM_PITCHING_H TEAM_PITCHING_HR TEAM_PITCHING_BB
##
    Min.
           :42.00
                             : 1155
                                       Min.
                                              : 0.0
                                                                : 136.0
                      Min.
                                                         Min.
```

```
1st Qu.:53.50
                     1st Qu.: 1426
                                      1st Qu.: 52.0
                                                        1st Qu.: 471.0
##
                     Median: 1515
    Median :62.00
                                      Median :104.0
                                                        Median : 526.0
                                                               : 552.4
##
    Mean
           :62.37
                     Mean
                            : 1813
                                      Mean
                                              :102.1
                                                        Mean
                      3rd Qu.: 1681
                                      3rd Qu.:142.5
                                                        3rd Qu.: 606.5
##
    3rd Qu.:67.50
##
    Max.
           :96.00
                      Max.
                             :22768
                                      Max.
                                              :336.0
                                                        Max.
                                                                :2008.0
##
   NA's
           :240
    TEAM_PITCHING_SO TEAM_FIELDING_E
                                       TEAM FIELDING DP
##
    Min.
           :
               0.0
                     Min.
                            : 73.0
                                       Min.
                                              : 69.0
##
    1st Qu.: 613.0
                      1st Qu.: 131.0
                                       1st Qu.:131.0
##
    Median: 745.0
                      Median : 163.0
                                       Median :148.0
    Mean
           : 799.7
                     Mean
                             : 249.7
                                       Mean
                                               :146.1
    3rd Qu.: 938.0
##
                      3rd Qu.: 252.0
                                       3rd Qu.:164.0
##
           :9963.0
                             :1568.0
                                               :204.0
    Max.
                     Max.
                                       Max.
##
    NA's
           :18
                                       NA's
                                               :31
```

Rename Columns

We now rename the columns for this test dataset to be more intuitive.

We impute the missing values with the median

We now check the summary to see if the missing values have been filled.

```
Hits
                       Doubles
                                       Triples
                                                         HomeRuns
##
    Min.
           : 819
                   Min.
                           : 44.0
                                    Min.
                                           : 14.00
                                                      Min.
                                                             : 0.00
    1st Qu.:1387
                   1st Qu.:210.0
                                    1st Qu.: 35.00
                                                      1st Qu.: 44.50
    Median:1455
                   Median :239.0
                                    Median : 52.00
                                                      Median :101.00
##
##
    Mean
           :1469
                   Mean
                           :241.3
                                    Mean
                                            : 55.91
                                                      Mean
                                                             : 95.63
                   3rd Qu.:278.5
##
    3rd Qu.:1548
                                    3rd Qu.: 72.00
                                                      3rd Qu.:135.50
##
    Max.
           :2170
                   Max.
                           :376.0
                                    Max.
                                            :155.00
                                                      Max.
                                                             :242.00
##
     Walks_AtBat
                    StrikeOuts_AtBat BasesStolen
                                                       OutStealingBases
##
    Min.
          : 15.0
                            :
                                0.0
                                      Min.
                                            : 0.0
                                                       Min.
                                                              : 0.00
                    Min.
##
                    1st Qu.: 565.0
                                      1st Qu.: 60.5
    1st Qu.:436.5
                                                       1st Qu.: 44.00
    Median :509.0
                    Median: 686.0
                                      Median: 92.0
                                                       Median: 49.50
##
    Mean
           :499.0
                    Mean
                           : 707.7
                                      Mean
                                              :122.1
                                                       Mean
                                                             : 51.37
##
    3rd Qu.:565.5
                    3rd Qu.: 904.5
                                      3rd Qu.:149.0
                                                       3rd Qu.: 56.00
##
    Max.
           :792.0
                    Max.
                            :1268.0
                                      Max.
                                              :580.0
                                                       Max.
                                                              :154.00
    HitByPitch_AtBat
##
                      Hits_Allowed
                                      HomeRuns_Allowed Walks_Allowed
##
    Min.
           :42.00
                     Min.
                            : 1155
                                            : 0.0
                                                        Min.
                                                              : 136.0
                                      Min.
##
    1st Qu.:62.00
                      1st Qu.: 1426
                                      1st Qu.: 52.0
                                                        1st Qu.: 471.0
##
    Median :62.00
                     Median: 1515
                                      Median :104.0
                                                        Median: 526.0
##
    Mean
           :62.03
                             : 1813
                                             :102.1
                                                               : 552.4
                     Mean
                                      Mean
                                                        Mean
##
    3rd Qu.:62.00
                      3rd Qu.: 1681
                                      3rd Qu.:142.5
                                                        3rd Qu.: 606.5
                             :22768
##
    Max.
           :96.00
                                              :336.0
                                                                :2008.0
                      Max.
                                      Max.
                                                        Max.
                                        DoublePlays
##
      StrikeOuts
                          Errors
##
           :
                             : 73.0
                                               : 69.0
    Min.
               0.0
                     Min.
                                       Min.
##
    1st Qu.: 622.5
                      1st Qu.: 131.0
                                       1st Qu.:134.5
##
    Median: 745.0
                      Median: 163.0
                                       Median :148.0
    Mean
          : 795.9
                             : 249.7
                                       Mean
                                               :146.3
                     Mean
##
    3rd Qu.: 927.5
                      3rd Qu.: 252.0
                                       3rd Qu.:160.5
    Max.
           :9963.0
                      Max.
                             :1568.0
                                       Max.
                                               :204.0
```

We create a table for the predicted wins.

```
## fit lwr upr
## Min. : -11.14 Min. :-298.56 Min. : 17.65
## 1st Qu.: 72.01 1st Qu.: 51.04 1st Qu.: 92.83
```

```
## Median: 80.28 Median: 59.67 Median: 100.67

## Mean: 85.60 Mean: 57.08 Mean: 114.11

## 3rd Qu.: 87.29 3rd Qu.: 66.81 3rd Qu.: 107.79

## Max. :1256.60 Max. : 440.64 Max. :2072.55
```

Conclusion

We conclude that model one which includes a majority of the predictors except one provides the best overall fit. While we did try additional models based on transformed variables, they did not provide a significant improvement, so we decided to go with model one. This model does not seem to violate the assumptions of linear regression.

References

Sellmair, Reinhard. "How to handle correlated Features?" June 25, 2018. https://www.kaggle.com/reisel/how-to-handle-correlated-features

Xie, Yihui, J. J. Allaire, and Garrett Grolemund, *R Markdown: The Definitive Guide*, CRC PressDecember 14, 2020 https://bookdown.org/yihui/rmarkdown/r-code.html.

https://rstatisticsblog.com/data-science-in-action/data-preprocessing/six-amazing-function-to-create-train-test-split-in-r/

R Code

```
# ------
# Load Libraries and Disable Scientific Notation for Readability Purposes
knitr::opts_chunk$set(echo = TRUE)
# Disable scientific numbers for readability purposes.
options(scipen = 999)
library(MASS)
library(tidyverse)
library(dplyr)
library(reshape2)
library(kableExtra)
library(corrplot)
library(ggplot2)
library(Hmisc)
library(PerformanceAnalytics)
library(GGally)
library(ggpubr)
library(car)
# Load The Dataset and Summarize the Data
# Load in the training data.
url = "https://raw.githubusercontent.com/Jagdish16/CUNY_DATA_621/main/project_1/moneyball-training-data
mb_training <- read.csv(url)</pre>
```

Remove the INDEX variable as it is of no value in the data evaluation.

```
mb_training <- subset(mb_training, select = -c(INDEX))</pre>
# Summarize the test data.
summary(mb_training)
# ------
# Rename the Variables to be More Intuitive
# ------
# Rename the columns to be more intuitive.
mb_training <- mb_training %>%
 rename_with(~ gsub("TEAM_", "", .x)) %>%
 rename_with(stringr::str_to_title) %>%
 dplyr::rename(
   Wins = Target_wins,
   Hits = Batting_h,
   Doubles = Batting 2b,
   Triples = Batting_3b,
   HomeRuns = Batting_hr,
   Walks_AtBat = Batting_bb,
   StrikeOuts_AtBat = Batting_so,
   BasesStolen = Baserun_sb,
   OutStealingBases = Baserun_cs,
   Hits_Allowed = Pitching_h,
   HitByPitch_AtBat = Batting_hbp,
   Errors = Fielding_e,
   HomeRuns_Allowed = Pitching_hr,
   Walks_Allowed = Pitching_bb,
   StrikeOuts = Pitching_so,
   DoublePlays = Fielding_dp
# Box Plots
# Plot boxplots for all variables.
long <- mb_training %>% as.data.frame() %>% melt()
long %>%
 ggplot(aes(x=value)) + geom_boxplot() + facet_wrap(~variable, scales = 'free')
# Distribution Plots
# ------
# Wins.
ggplot(mb_training, aes(x = Wins)) +
 geom_histogram(color = 'black', fill = 'gray', bins = 30) +
 geom_vline(aes(xintercept = mean(Wins)),
          linetype = 'dashed', size = 2, color = 'blue') +
```

```
geom_label(aes(x = 50, y = 125,
                 label = str_replace_all(toString(summary(mb_training['Wins'])), ',', '\n')
  labs(title = 'Wins Histogram Plot', y = 'Count', x = 'Wins')
# Hits.
ggplot(mb training, aes(x = Hits)) +
  geom histogram(color = 'black', fill = 'gray', bins = 30) +
  geom_vline(aes(xintercept = mean(Hits)),
             linetype = 'dashed', size = 2, color = 'blue') +
  geom_label(aes(x = 1250, y = 100,
                 label = str_replace_all(toString(summary(mb_training['Hits'])), ',', '\n')
  labs(title = 'Hits Histogram Plot', y = 'Count', x = 'Base Hits')
# Doubles.
ggplot(data = mb_training, aes(x = Doubles)) +
  geom histogram(color = 'black', fill = 'gray', bins = 30) +
  geom_vline(aes(xintercept = mean(Doubles)),
             linetype = 'dashed', size = 2, color = 'blue') +
  geom_label(aes(x = 160, y = 100,
                 label = str_replace_all(toString(summary(mb_training['Doubles'])), ',', '\n')
                 )) +
  labs(title = 'Doubles Histogram Plot', y = 'Count', x = 'Doubles')
# Triples.
ggplot(data = mb_training, aes(x = Triples)) +
  geom_histogram(color = 'black', fill = 'gray', bins = 30) +
  geom_vline(aes(xintercept = mean(Triples)),
             linetype = 'dashed', size = 2, color = 'blue') +
  geom_label(aes(x = 75, y = 130,
                 label = str_replace_all(toString(summary(mb_training['Triples'])), ',', '\n')
  labs(title = 'Triples Histogram Plot', y = 'Count', x = 'Triples')
# Homeruns.
ggplot(data = mb_training, aes(x = HomeRuns)) +
  geom_histogram(color = 'black', fill = 'gray', bins = 30) +
  geom vline(aes(xintercept = mean(HomeRuns)),
             linetype = 'dashed', size = 2, color = 'blue') +
  geom_label(aes(x = 25, y = 90,
                 label = str_replace_all(toString(summary(mb_training['HomeRuns'])), ',', '\n')
  labs(title = 'Homeruns Histogram Plot', y = 'Count', x = 'Homeruns')
# Walks.
ggplot(data = mb_training, aes(x = Walks_AtBat)) +
  geom_histogram(color = 'black', fill = 'gray', bins = 30) +
  geom_vline(aes(xintercept = mean(Walks_AtBat)),
             linetype = 'dashed', size = 2, color = 'blue') +
  geom_label(aes(x = 380, y = 100,
```

```
label = str_replace_all(toString(summary(mb_training['Walks_AtBat'])), ',', '\n')
                 )) +
  labs(title = 'Walks Histogram Plot', y = 'Count', x = 'Walks')
# Strike Out by Batters.
ggplot(data = mb_training, aes(x = StrikeOuts_AtBat)) +
  geom_histogram(color = 'black', fill = 'gray', bins = 30) +
  geom_vline(aes(xintercept = mean(StrikeOuts_AtBat)),
             linetype = 'dashed', size = 2, color = 'blue') +
  geom_label(aes(x = 380, y = 100,
                 label = str_replace_all(toString(summary(mb_training['StrikeOuts_AtBat'])), ',', '\n')
  labs(title = 'Strike Out by Batters Histogram Plot', y = 'Count', x = 'Strike Out by Batters')
# Stolen Bases.
ggplot(data = mb_training, aes(x = BasesStolen)) +
  geom_histogram(color = 'black', fill = 'gray', bins = 30) +
  geom_vline(aes(xintercept = mean(BasesStolen)),
             linetype = 'dashed', size = 2, color = 'blue') +
  geom_label(aes(x = 200, y = 100,
                 label = str_replace_all(toString(summary(mb_training['BasesStolen'])), ',', '\n')
  labs(title = 'Stolen Bases Histogram Plot', y = 'Count', x = 'Stolen Bases')
# Hits Allowed.
ggplot(data = mb_training, aes(x = Hits_Allowed)) +
  geom_histogram(color = 'black', fill = 'gray', bins = 30) +
  geom_vline(aes(xintercept = mean(Hits_Allowed)),
             linetype = 'dashed', size = 2, color = 'blue') +
  geom_label(aes(x = 1250, y = 100,
                 label = str_replace_all(toString(summary(mb_training['Hits_Allowed'])), ',', '\n')
                 )) +
  labs(title = 'Hits Allowed Histogram Plot', y = 'Count', x = 'Hits Allowed')
# Homeruns Allowed.
ggplot(data = mb_training, aes(x = HomeRuns_Allowed)) +
  geom_histogram(color = 'black', fill = 'gray', bins = 30) +
  geom_vline(aes(xintercept = mean(HomeRuns_Allowed)),
             linetype = 'dashed', size = 2, color = 'blue') +
  geom_label(aes(x = 30, y = 90,
                 label = str_replace_all(toString(summary(mb_training['HomeRuns_Allowed'])), ',', '\n')
  labs(title = 'Homeruns Allowed Histogram Plot', y = 'Count', x = 'Homeruns Allowed')
# Walks Allowed.
ggplot(data = mb_training, aes(x = Walks_Allowed)) +
  geom_histogram(color = 'black', fill = 'gray', bins = 30) +
  geom_vline(aes(xintercept = mean(Walks_Allowed)),
             linetype = 'dashed', size = 2, color = 'blue') +
```

```
geom_label(aes(x = 375, y = 100,
                label = str_replace_all(toString(summary(mb_training['Walks_Allowed'])), ',', '\n')
 labs(title = 'Walks Allowed Histogram Plot', y = 'Count', x = 'Walks Allowed')
# Strikeouts by Pitchers.
ggplot(data = mb_training, aes(x = StrikeOuts)) +
 geom_histogram(color = 'black', fill = 'gray', bins = 30) +
 geom_vline(aes(xintercept = mean(StrikeOuts)),
            linetype = 'dashed', size = 2, color = 'blue') +
 geom_label(aes(x = 425, y = 100,
               label = str_replace_all(toString(summary(mb_training['StrikeOuts'])), ',', '\n')
                )) +
 labs(title = 'Strikeouts by Pitchers Histogram Plot', y = 'Count', x = 'Strikeouts by Pitchers')
# Errors.
ggplot(data = mb_training, aes(x = Errors)) +
 geom_histogram(color = 'black', fill = 'gray', bins = 30) +
 geom_vline(aes(xintercept = mean(Errors)),
            linetype = 'dashed', size = 2, color = 'blue') +
 geom_label(aes(x = 225, y = 100,
               label = str replace all(toString(summary(mb training['Errors'])), ',', '\n')
                )) +
 labs(title = 'Errors Histogram Plot', y = 'Count', x = 'Errors')
# Double Plays.
ggplot(data = mb_training, aes(x = DoublePlays)) +
 geom_histogram(color = 'black', fill = 'gray', bins = 30) +
 geom_vline(aes(xintercept = mean(DoublePlays)),
            linetype = 'dashed', size = 2, color = 'blue') +
 geom_label(aes(x = 110, y = 100,
                label = str_replace_all(toString(summary(mb_training['DoublePlays'])), ',', '\n')
 labs(title = 'Double Plays Histogram Plot', y = 'Count', x = 'Double Plays')
# ------
# Missing Data
# ------
# Create a table of variables sorted by percentage of missing data.
missing_data <- colSums(mb_training %>% sapply(is.na))
percentage_missing <- round(missing_data / nrow(mb_training) * 100, 2)</pre>
missing_values_table <- sort(percentage_missing, decreasing = TRUE)</pre>
missing_values_table %>%
 kable(caption = 'Breakdown of Variables by Percentage of Missing Data') %%
 kable_styling()
# Drop the HitByPitch_AtBat variable from the dataset.
mb_training <- mb_training %>% dplyr::select(-HitByPitch_AtBat)
```

```
# Handle Outliers
# Remove outlier rows for the 6 predictor variables.
mb_training_updated <- mb_training</pre>
# Remove outliers - Method 2.
for (n in c("Walks_Allowed", "BasesStolen", "StrikeOuts", "Hits_Allowed", "Errors", "Triples")) {
   Q <- quantile(mb_training[,n], probs = c(.25, .75), na.rm = TRUE)
   iqr <- IQR(mb_training[,n], na.rm = TRUE)</pre>
   # Upper Range.
   up <- Q[2] + 1.5 * iqr
   # Lower Range.
   low \leftarrow Q[1] - 1.5 * iqr
   mb_training_updated <- subset(mb_training_updated, mb_training_updated[,n] > (Q[1]-1.5 * iqr)&mb_training_updated[,n] > (Q[1]-1.5 * iqr)&mb_training_updat
# Check the summary for the updated dataframe.
summary(mb_training_updated)
# Impute missing values with the median value for each remaining column.
mb_training_updated <- data.frame(sapply(mb_training_updated, function(x) ifelse(is.na(x), median(x, na
# Check the summary for the updated dataframe.
summary(mb_training_updated)
# Data Correlation
# Perform a correlation analysis on the data. In this analysis, we are only interested in the
# correlation of the predicter variables and the "TARGET_WINS" variable.
correlation_table <- cor(mb_training_updated, method = 'pearson', use = 'complete.obs')[,1]</pre>
# Remove the TARGET_WINS variable from the correlation table as it is redundant
# within the context of of our correlation analysis.
correlation_table <- correlation_table[-c(1)]</pre>
correlation_table %>%
   kable(caption = 'Correlation of Variables to Wins') %>% kable styling()
# Calculate correlation between variables.
mb_training_updated_corr_matrix <- mb_training_updated %>% cor() %>% round(2) %>% as.matrix()
mb_training_updated_corr_matrix %>% kable() %>% kable_styling()
# flattenCorrMatrix
# cormat : matrix of the correlation coefficients.
# pmat : matrix of the correlation p-values.
flattenCorrMatrix <- function(cormat, pmat) {</pre>
   ut <- upper.tri(cormat)</pre>
   data.frame(
       row = rownames(cormat)[row(cormat)[ut]],
       column = rownames(cormat)[col(cormat)[ut]],
```

```
cor =(cormat)[ut],
   p = pmat[ut]
}
# Another method to check correlations and their significance.
corr.mat<-rcorr(as.matrix(mb_training_updated))</pre>
flattenCorrMatrix(corr.mat$r, corr.mat$P)%>% filter(row=='Wins') %>% arrange(-abs(cor))
# Check Normality of Predictors
# -----
# Run the Shapiro wilkes test for normality.
do.call(rbind, lapply(mb_training_updated, function(x) shapiro.test(x)[c("statistic", "p.value")]))
# Model 1
# ------
model_one <- lm(Wins ~ Hits + Doubles + Triples + HomeRuns +</pre>
             Walks_AtBat + BasesStolen + Hits_Allowed +
             HomeRuns_Allowed + Errors + Walks_Allowed + StrikeOuts +
             StrikeOuts_AtBat + OutStealingBases + DoublePlays,
             mb_training_updated)
# Model 1 summary stats.
summary(model_one)
# Model 1 R Squared.
summary(model_one)$r.squared
# Model 1 Confidence Intervals.
confint(model one)
# Model 1 plots - residuals vs fitted values, residuals distribution.
ggplot(data = model_one, aes(x = .fitted, y = .resid)) +
 geom_point() + geom_hline(yintercept = 0, linetype = "dashed") +
 geom_smooth(se = FALSE) + xlab("Fitted values") + ylab("Residuals")
ggplot(data = model_one, aes(x = .resid)) + geom_histogram() + xlab("Residuals")
ggplot(data = model_one) + stat_qq(aes(sample = .stdresid)) + geom_abline()
# Model 2
# Model 2 uses stepwise regression on the variables in Model 1.
model_two <- stepAIC(model_one, direction = 'both', trace = FALSE)</pre>
```

```
# Model 2 summary stats.
summary(model_two)
# Model 2 plots - residuals vs fitted values, residuals distribution.
ggplot(data = model_two, aes(x = .fitted, y = .resid)) +
 geom_point() + geom_hline(yintercept = 0, linetype = "dashed") +
 geom_smooth(se = FALSE) + xlab("Fitted values") + ylab("Residuals")
ggplot(data = model_two, aes(x = .resid)) + geom_histogram() + xlab("Residuals")
ggplot(data = model_two) + stat_qq(aes(sample = .stdresid)) + geom_abline()
# Model 3
# Derive 2 new variables for Singles and Home run difference.
mb_training_new <- mb_training_updated %>% mutate(Singles = Hits - Doubles - Triples - HomeRuns)
mb_training_new <- mb_training_new %>% mutate(Homeruns_diff = HomeRuns_Allowed - HomeRuns)
model_three <- lm(Wins ~ Hits + Doubles + Triples + Walks_AtBat +</pre>
                BasesStolen + Hits Allowed + Errors + Walks Allowed +
                StrikeOuts + Singles + Homeruns_diff + StrikeOuts_AtBat +
                I(HomeRuns_Allowed/HomeRuns) + I(HomeRuns_Allowed*HomeRuns) +
                I(1/DoublePlays) + I(OutStealingBases^3),
                mb_training_new)
# Model 3 summary stats.
summary(model_three)
# Model 3 R-Squared.
summary(model_three)$r.squared
# Model 3 confidence intervals.
confint(model three)
# Model 3 plots - residuals vs fitted values, residuals distribution.
ggplot(data = model_three, aes(x = .fitted, y = .resid)) +
 geom_point() + geom_hline(yintercept = 0, linetype = "dashed") +
 geom_smooth(se = FALSE) + xlab("Fitted values") + ylab("Residuals")
ggplot(data = model_three, aes(x = .resid)) + geom_histogram() + xlab("Residuals")
ggplot(data = model_three) + stat_qq(aes(sample = .stdresid)) + geom_abline()
# Model 4
# Model 4 - Box Cox method.
```

```
MASS::boxcox(model_one, lambda = seq(0.75, 1.6, by = 0.05), plotit = TRUE)
# Fit a model using a lambda value of 1.35 for the response variable.
model_cox = lm((((Wins ^ 1.35) - 1)/ 1.35) ~ Hits + Doubles + Triples + HomeRuns + Walks_AtBat +
   BasesStolen + Hits_Allowed + HomeRuns_Allowed + Errors +
   Walks_Allowed + StrikeOuts + StrikeOuts_AtBat + OutStealingBases +
   DoublePlays,
   mb_training_updated)
# Model 4 summary stats.
summary(model_cox)
# Model 4 R Squared.
summary(model_cox)$r.squared
# Model 4 confidence intervals.
confint(model_cox)
# Model 4 plots - residuals vs fitted values, residuals distribution.
ggplot(data = model_cox, aes(x = .fitted, y = .resid)) +
 geom_point() + geom_hline(yintercept = 0, linetype = "dashed") +
 geom_smooth(se = FALSE) + xlab("Fitted values") + ylab("Residuals")
ggplot(data = model_cox, aes(x = .resid)) + geom_histogram() + xlab("Residuals")
ggplot(data = model_cox) + stat_qq(aes(sample = .stdresid)) + geom_abline()
# Model Selection
# -----
# Predict the number of wins for the test data using model one.
# Load in the test data.
url2 <- 'https://raw.githubusercontent.com/Jagdish16/CUNY_DATA_621/main/project_1/moneyball-evaluation-
mb_test <- read.csv(url2)</pre>
# Remove the INDEX variable as it is of no value in the data evaluation.
mb test <- subset(mb test, select = -c(INDEX))</pre>
# Summarize the test data.
summary(mb_test)
# Rename the test data variables to be more intuitive.
mb_test <- mb_test %>%
 rename_with(~ gsub("TEAM_", "", .x)) %>%
 rename_with(stringr::str_to_title) %>%
 dplyr::rename(
   Hits = Batting_h,
   Doubles = Batting_2b,
   Triples = Batting_3b,
   HomeRuns = Batting_hr,
```

```
Walks_AtBat = Batting_bb,
   StrikeOuts_AtBat = Batting_so,
   BasesStolen = Baserun_sb,
   OutStealingBases = Baserun_cs,
   Hits_Allowed = Pitching_h,
   HitByPitch_AtBat = Batting_hbp,
   Errors = Fielding_e,
   HomeRuns_Allowed = Pitching_hr,
   Walks_Allowed = Pitching_bb,
   StrikeOuts = Pitching_so,
   DoublePlays = Fielding_dp
# Impute missing values with the median value for each column.
mb_test_updated <- data.frame(sapply(mb_test, function(x) ifelse(is.na(x), median(x, na.rm = TRUE), x))
# Summarize the test data.
summary(mb_test_updated)
# Predicting Wins in the test data and looking at the distribution.
mb_test_updated$predicted_wins <- predict(model_one, type = 'response', newdata = mb_test_updated)</pre>
ggplot(data = mb_test_updated, aes(x = predicted_wins)) +
  geom_histogram( color = 'black', fill = 'gray') +
  geom_vline(aes(xintercept = mean(predicted_wins)), linetype = 'dashed', size = 2, color = 'blue') +
  geom_label(aes(x = 500, y = 150, label= str_replace_all(toString(summary(mb_test_updated['predicted_windstring)
  labs(title = 'Wins Prediction Histogram Plot', y = 'Count', x = 'Wins Prediction')
# Create a table of prediction and confidence intervals.
test_data <- predict(model_one, newdata = mb_test_updated, interval = 'prediction')</pre>
summary(test_data)
```