

DATA 621: Homework 1 (Group 2)

Moneyball Linear Regression

Contents

0.1	Introduction	1
0.2	Data Exploration	3
0.3	Data Preparation	8
0.4	Models	9
0.5	Model Selection	27
0.6	Conclusion	29
0.7	References	29

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0.1 Introduction

0.1.1 Assignment Objective

In this assignment, we analyze and model a baseball dataset containing multi-year game statistics for different teams. The objective is to build a multiple linear regression model on the training data to predict the number of wins for the team. We can only use the variables given to us (or variables that we derive from the variables provided).

0.1.1.1 Data There are 2 datasets provided - The Moneyball training dataset contains 17 columns and 2276 rows. Each record in the Money Ball training dataset represents a professional baseball team from the years 1871 to 2006 inclusive. Each record has the performance of the team for the given year, with all of the statistics adjusted to match the performance of a 162 game season. For this assignment, the target variable in the dataset is TARGET_WINS.

On the nex page is a short description of the variables of interest in the data set:

0.1.2 Purpose of Analysis

The purpose of the analysis is to find which of the predictors have significant ability to explain the variation in the response variable (number of wins by a team), and to make a prediction for all the records provided in the test data set.

0.1.3 Method

The method used is a multiple linear regression model on the training data to predict the number of wins for the team.

VARIABLE NAME	DEFINITION	THEORETICAL EFFECT
INDEX	Identification Variable (do not use)	None
TARGET_WINS	Number of wins	
TEAM_BATTING_H	Base Hits by batters (1B,2B,3B,HR)	Positive Impact on Wins
TEAM_BATTING_2B	Doubles by batters (2B)	Positive Impact on Wins
TEAM_BATTING_3B	Triples by batters (3B)	Positive Impact on Wins
TEAM_BATTING_HR	Homeruns by batters (4B)	Positive Impact on Wins
TEAM_BATTING_BB	Walks by batters	Positive Impact on Wins
TEAM_BATTING_HBP	Batters hit by pitch (get a free base)	Positive Impact on Wins
TEAM_BATTING_SO	Strikeouts by batters	Negative Impact on Wins
TEAM_BASERUN_SB	Stolen bases	Positive Impact on Wins
TEAM_BASERUN_CS	Caught stealing	Negative Impact on Wins
TEAM_FIELDING_E	Errors	Negative Impact on Wins
TEAM_FIELDING_DP	Double Plays	Positive Impact on Wins
TEAM_PITCHING_BB	Walks allowed	Negative Impact on Wins
TEAM_PITCHING_H	Hits allowed	Negative Impact on Wins
TEAM_PITCHING_HR	Homeruns allowed	Negative Impact on Wins
TEAM_PITCHING_SO	Strikeouts by pitchers	Positive Impact on Wins

Figure 1: Variables of Interest

0.2 Data Exploration

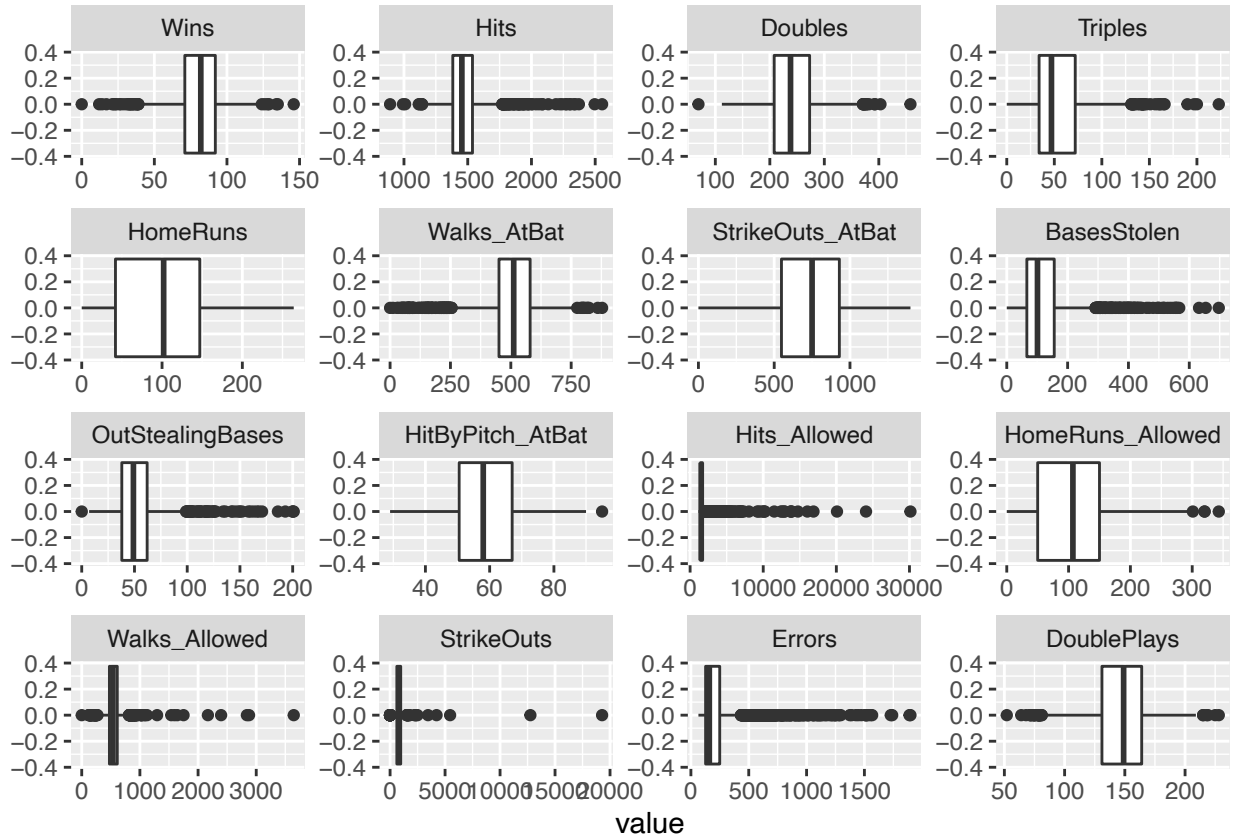
The first variable in the above table (INDEX) was dropped from the dataset due to the fact that it is merely a row identifier, and has no impact on the target variable (TARGET_WINS).

0.2.1 Summary Statistics

The first step in our data exploration was to compile summary statistics to give us some insight into the data prior to preparing the data for modeling. To make the variable names more readable, we removed the “TEAM_” prefix from each variable.

```
##           Wins           Hits           Doubles           Triples
## Min.      : 0.00    Min.      : 891    Min.      : 69.0    Min.      : 0.00
## 1st Qu.: 71.00    1st Qu.:1383    1st Qu.:208.0    1st Qu.: 34.00
## Median : 82.00    Median :1454    Median :238.0    Median : 47.00
## Mean     : 80.79    Mean     :1469    Mean     :241.2    Mean     : 55.25
## 3rd Qu.: 92.00    3rd Qu.:1537    3rd Qu.:273.0    3rd Qu.: 72.00
## Max.     :146.00    Max.     :2554    Max.     :458.0    Max.     :223.00
##
##           HomeRuns       Walks_AtBat       StrikeOuts_AtBat       BasesStolen
## Min.      : 0.00    Min.      : 0.0    Min.      : 0.0    Min.      : 0.0
## 1st Qu.: 42.00    1st Qu.:451.0    1st Qu.: 548.0    1st Qu.: 66.0
## Median :102.00    Median :512.0    Median : 750.0    Median :101.0
## Mean     : 99.61    Mean     :501.6    Mean     : 735.6    Mean     :124.8
## 3rd Qu.:147.00    3rd Qu.:580.0    3rd Qu.: 930.0    3rd Qu.:156.0
## Max.     :264.00    Max.     :878.0    Max.     :1399.0    Max.     :697.0
##
##                               NA's      :102    NA's      :131
## OutStealingBases HitByPitch_AtBat Hits_Allowed HomeRuns_Allowed
## Min.      : 0.0    Min.      :29.00    Min.      : 1137    Min.      : 0.0
## 1st Qu.: 38.0    1st Qu.:50.50    1st Qu.: 1419    1st Qu.: 50.0
## Median : 49.0    Median :58.00    Median : 1518    Median :107.0
## Mean     : 52.8    Mean     :59.36    Mean     : 1779    Mean     :105.7
## 3rd Qu.: 62.0    3rd Qu.:67.00    3rd Qu.: 1682    3rd Qu.:150.0
## Max.     :201.0    Max.     :95.00    Max.     :30132    Max.     :343.0
## NA's      :772    NA's      :2085
## Walks_Allowed       StrikeOuts           Errors           DoublePlays
## Min.      : 0.0    Min.      : 0.0    Min.      : 65.0    Min.      : 52.0
## 1st Qu.: 476.0    1st Qu.: 615.0    1st Qu.: 127.0    1st Qu.:131.0
## Median : 536.5    Median : 813.5    Median : 159.0    Median :149.0
## Mean     : 553.0    Mean     : 817.7    Mean     : 246.5    Mean     :146.4
## 3rd Qu.: 611.0    3rd Qu.: 968.0    3rd Qu.: 249.2    3rd Qu.:164.0
## Max.     :3645.0    Max.     :19278.0    Max.     :1898.0    Max.     :228.0
##
##                               NA's      :102    NA's      :286
```

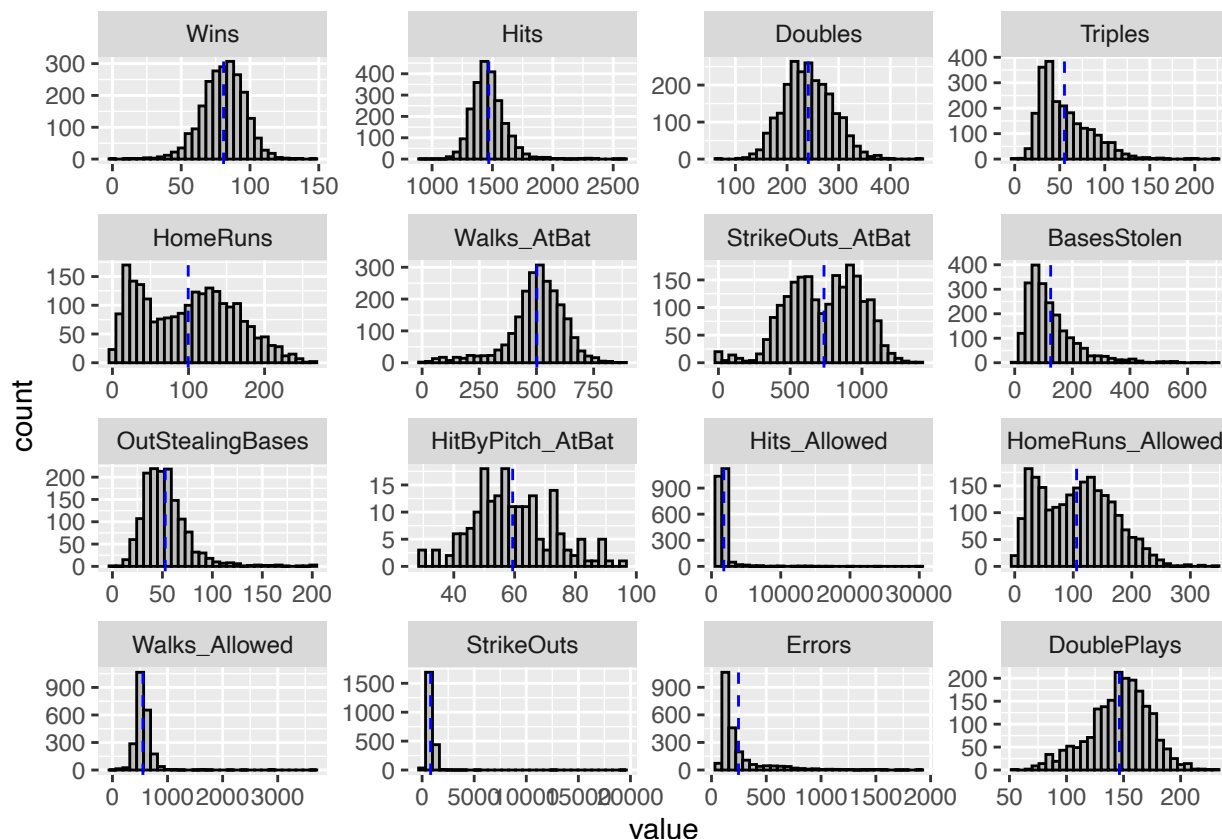
From the above, we see that there are 15 predictors and 1 response variable (Wins). Of the predictors, 6 have missing values. We then plotted boxplots for all the variables to get a sense of outliers.



From the box plots, we can see that quite a few predictors are very skewed in nature, such as Walks_Allowed and Hits_Allowed.

0.2.2 Variable Distributions

We created distribution plots for all the variables to check their shape visually and get a high-level, intuitive sense of normality.



The histograms provide additional confirmation that some of the variables are quite skewed. For example: Errors, Triples and Walks_AtBat. There are other variables with what look like bi-modal type of distributions. For example: StrikeOuts_AtBat. There are a couple of variables that look closer to the normal distribution. For example - the response variable Wins.

0.2.3 Feature Correlation

We now check which of the predictors are more correlated with the response variable as a mechanism to select which variables to include in the linear regression model. We also check the correlation between the predictors, since we'd like to avoid multi-collinearity.

Table 1: Correlation of Variables to Wins

	x
Hits	0.4699467
Doubles	0.3129840
Triples	-0.1243459
HomeRuns	0.4224168
Walks_AtBat	0.4686879
StrikeOuts_AtBat	-0.2288927
BasesStolen	0.0148364
OutStealingBases	-0.1787560
HitByPitch_AtBat	0.0735042
Hits_Allowed	0.4712343
HomeRuns_Allowed	0.4224668
Walks_Allowed	0.4683988
StrikeOuts	-0.2293648
Errors	-0.3866880
DoublePlays	-0.1958660

	Wins	Hits	Doubles	Triples	HomeRuns	Walks_AtBat	StrikeOuts_AtBat	BasesStolen
Wins	1.00	0.39	0.29	0.14	0.18	0.23	NA	NA
Hits	0.39	1.00	0.56	0.43	-0.01	-0.07	NA	NA
Doubles	0.29	0.56	1.00	-0.11	0.44	0.26	NA	NA
Triples	0.14	0.43	-0.11	1.00	-0.64	-0.29	NA	NA
HomeRuns	0.18	-0.01	0.44	-0.64	1.00	0.51	NA	NA
Walks_AtBat	0.23	-0.07	0.26	-0.29	0.51	1.00	NA	NA
StrikeOuts_AtBat	NA	NA	NA	NA	NA	NA	1	NA
BasesStolen	NA	NA	NA	NA	NA	NA	NA	1
OutStealingBases	NA	NA	NA	NA	NA	NA	NA	NA
HitByPitch_AtBat	NA	NA	NA	NA	NA	NA	NA	NA
Hits_Allowed	-0.11	0.30	0.02	0.19	-0.25	-0.45	NA	NA
HomeRuns_Allowed	0.19	0.07	0.45	-0.57	0.97	0.46	NA	NA
Walks_Allowed	0.12	0.09	0.18	0.00	0.14	0.49	NA	NA
StrikeOuts	NA	NA	NA	NA	NA	NA	NA	NA
Errors	-0.18	0.26	-0.24	0.51	-0.59	-0.66	NA	NA
DoublePlays	NA	NA	NA	NA	NA	NA	NA	NA


```
## Max. :120.00 Max. :1876 Max. :392.0 Max. :126.0
## HomeRuns Walks_AtBat StrikeOuts_AtBat BasesStolen
## Min. : 4.0 Min. :273.0 Min. : 268 Min. : 18.0
## 1st Qu.: 75.0 1st Qu.:472.0 1st Qu.: 598 1st Qu.: 62.0
## Median :118.0 Median :523.0 Median : 814 Median : 91.0
## Mean :115.6 Mean :527.9 Mean : 783 Mean :100.2
## 3rd Qu.:156.0 3rd Qu.:585.0 3rd Qu.: 955 3rd Qu.:131.0
## Max. :264.0 Max. :775.0 Max. :1399 Max. :289.0
## OutStealingBases Hits_Allowed HomeRuns_Allowed Walks_Allowed
## Min. : 11.00 Min. :1137 Min. : 4.0 Min. :320.0
## 1st Qu.: 41.00 1st Qu.:1407 1st Qu.: 79.0 1st Qu.:487.0
## Median : 49.00 Median :1490 Median :121.0 Median :537.0
## Mean : 52.06 Mean :1510 Mean :118.4 Mean :546.2
## 3rd Qu.: 58.00 3rd Qu.:1590 3rd Qu.:158.0 3rd Qu.:601.0
## Max. :201.00 Max. :2069 Max. :264.0 Max. :810.0
## StrikeOuts Errors DoublePlays
## Min. : 301.0 Min. : 65.0 Min. : 72.0
## 1st Qu.: 639.0 1st Qu.:122.0 1st Qu.:136.0
## Median : 824.0 Median :144.0 Median :151.0
## Mean : 805.5 Mean :161.9 Mean :150.4
## 3rd Qu.: 962.0 3rd Qu.:184.0 3rd Qu.:165.0
## Max. :1481.0 Max. :430.0 Max. :225.0
```

0.4 Models

0.4.1 Model 1

Model 1 includes the remaining variables in the dataset except for the one dropped earlier due to lots of missing values (HitByPitch_AtBat).

0.4.1.0.1 Model 1 Statistics Model 1 Summary Stats

```
##
## Call:
## lm(formula = Wins ~ Hits + Doubles + Triples + HomeRuns + Walks_AtBat +
## BasesStolen + Hits_Allowed + HomeRuns_Allowed + Errors +
## Walks_Allowed + StrikeOuts + StrikeOuts_AtBat + OutStealingBases +
## DoublePlays, data = mb_training_updated)
##
## Residuals:
## Min 1Q Median 3Q Max
## -32.236 -7.006 0.134 6.904 29.838
##
## Coefficients:
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 57.033963 6.166067 9.250 < 0.0000000000000002 ***
## Hits -0.035499 0.022113 -1.605 0.10860
## Doubles -0.054552 0.009026 -6.044 0.000000000183 ***
## Triples 0.186643 0.019712 9.468 < 0.0000000000000002 ***
## HomeRuns 0.241595 0.138884 1.740 0.08211 .
## Walks_AtBat 0.200978 0.064606 3.111 0.00190 **
## BasesStolen 0.076969 0.006573 11.709 < 0.0000000000000002 ***
```

```
## Hits_Allowed      0.065127    0.020521    3.174          0.00153 **
## HomeRuns_Allowed -0.145831    0.134764   -1.082          0.27935
## Errors            -0.124236    0.007365  -16.869 < 0.0000000000000002 ***
## Walks_Allowed    -0.159245    0.061932   -2.571          0.01021 *
## StrikeOuts        0.001674    0.032200    0.052          0.95854
## StrikeOuts_AtBat -0.023747    0.033436   -0.710          0.47765
## OutStealingBases -0.039104    0.014502   -2.696          0.00707 **
## DoublePlays       -0.109783    0.012606   -8.709 < 0.0000000000000002 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10.26 on 1774 degrees of freedom
## Multiple R-squared:  0.4045, Adjusted R-squared:  0.3998
## F-statistic: 86.07 on 14 and 1774 DF,  p-value: < 0.00000000000000022
```

We see that the adjusted R-squared for this model is 0.40 i.e. these predictors explain about 40% of the variability in the response variable.

Model 1 R Squared

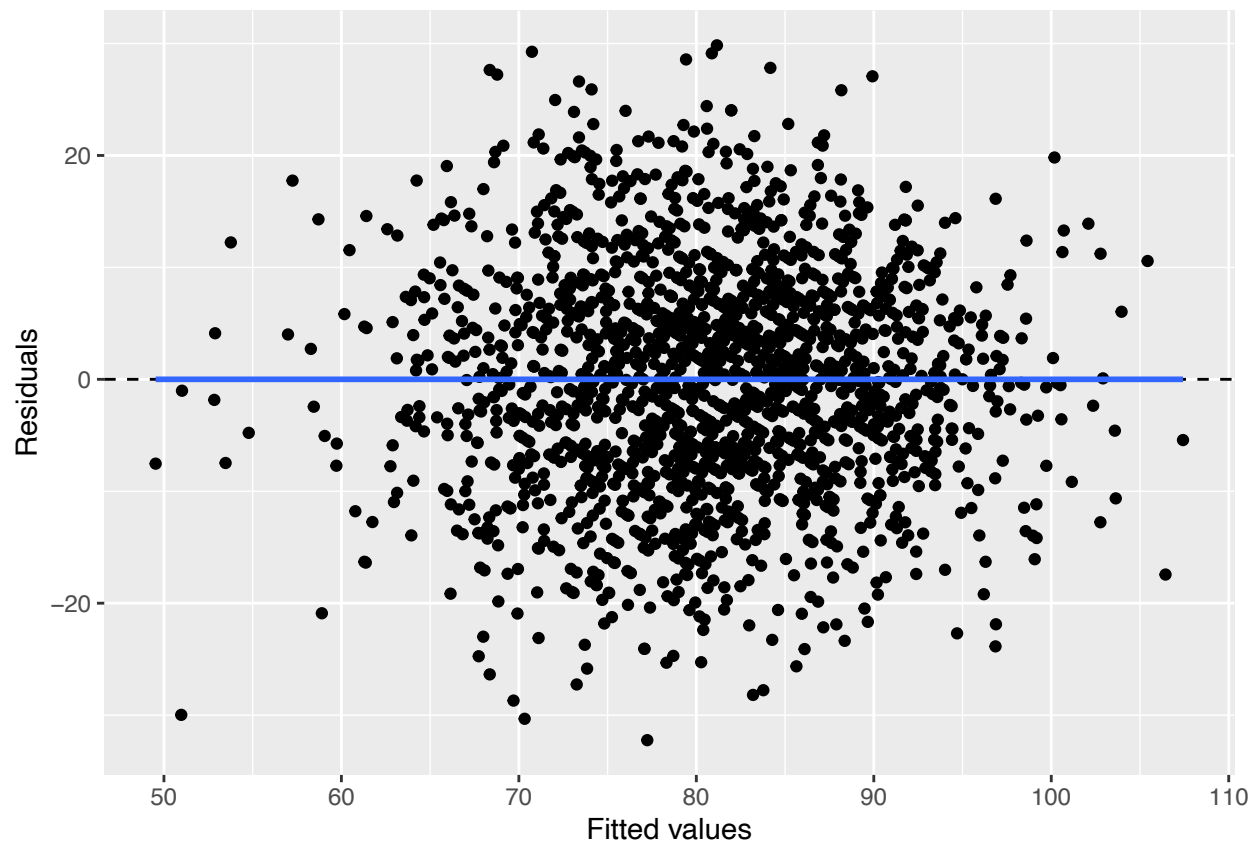
```
## [1] 0.4044997
```

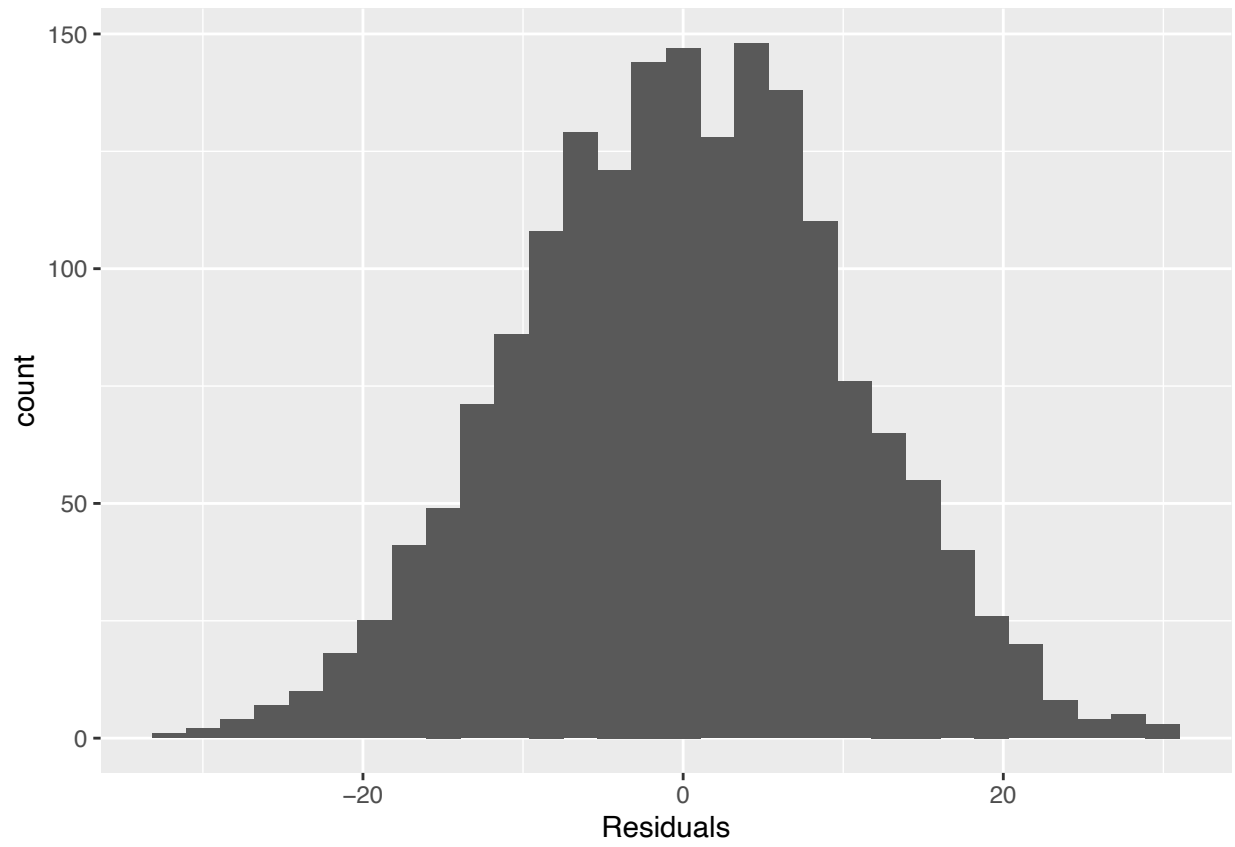
Model 1 Confidence Intervals

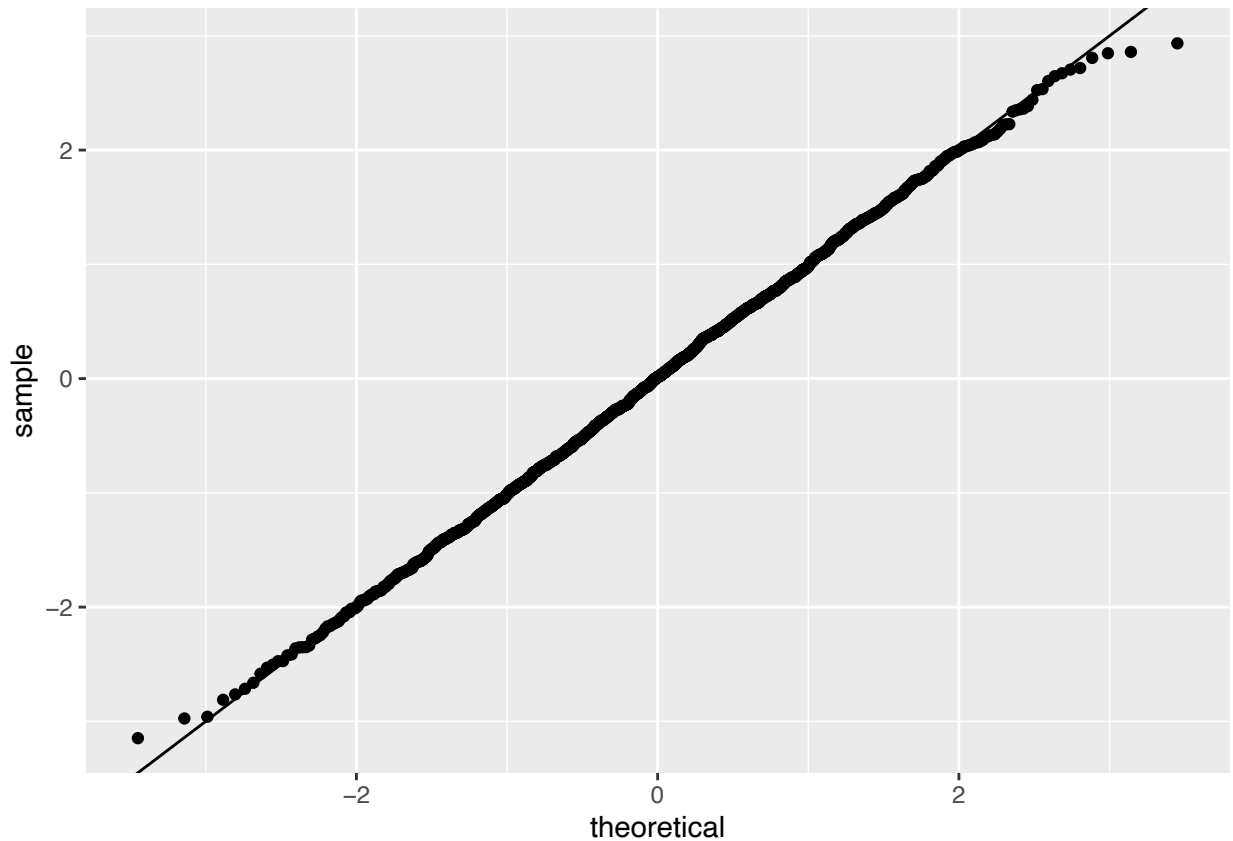
We calculate the 95% confidence intervals for each of the co-efficients and the intercept for this model.

```
##              2.5 %      97.5 %
## (Intercept)  44.94044362 69.127482832
## Hits         -0.07886950  0.007872103
## Doubles      -0.07225451 -0.036849474
## Triples       0.14798073  0.225304552
## HomeRuns     -0.03079800  0.513988472
## Walks_AtBat   0.07426677  0.327689717
## BasesStolen   0.06407675  0.089861282
## Hits_Allowed  0.02487963  0.105374808
## HomeRuns_Allowed -0.41014380 0.118482229
## Errors       -0.13868039 -0.109790758
## Walks_Allowed -0.28071180 -0.037777706
## StrikeOuts    -0.06148025  0.064828416
## StrikeOuts_AtBat -0.08932553 0.041830860
## OutStealingBases -0.06754688 -0.010661147
## DoublePlays   -0.13450771 -0.085058563
```

0.4.1.0.2 Model 1 Plots We plot the residuals versus the fitted values - it shows that the residuals are scattered fairly evenly and there doesn't seem to be a trend. The distribution of the residuals does not seem very skewed. The same can be seen through the qq-plot as well.







0.4.1.1 Model 2 Model 2 uses stepwise regression on the variables in Model 1 to create the best performing model.

Model 2 Summary Stats

```
##
## Call:
## lm(formula = Wins ~ Hits + Doubles + Triples + HomeRuns + Walks_AtBat +
##      BasesStolen + Hits_Allowed + HomeRuns_Allowed + Errors +
##      Walks_Allowed + StrikeOuts_AtBat + OutStealingBases + DoublePlays,
##      data = mb_training_updated)
##
## Residuals:
```

	Min	1Q	Median	3Q	Max
	-32.235	-7.017	0.138	6.908	29.818

```
##
## Coefficients:
```

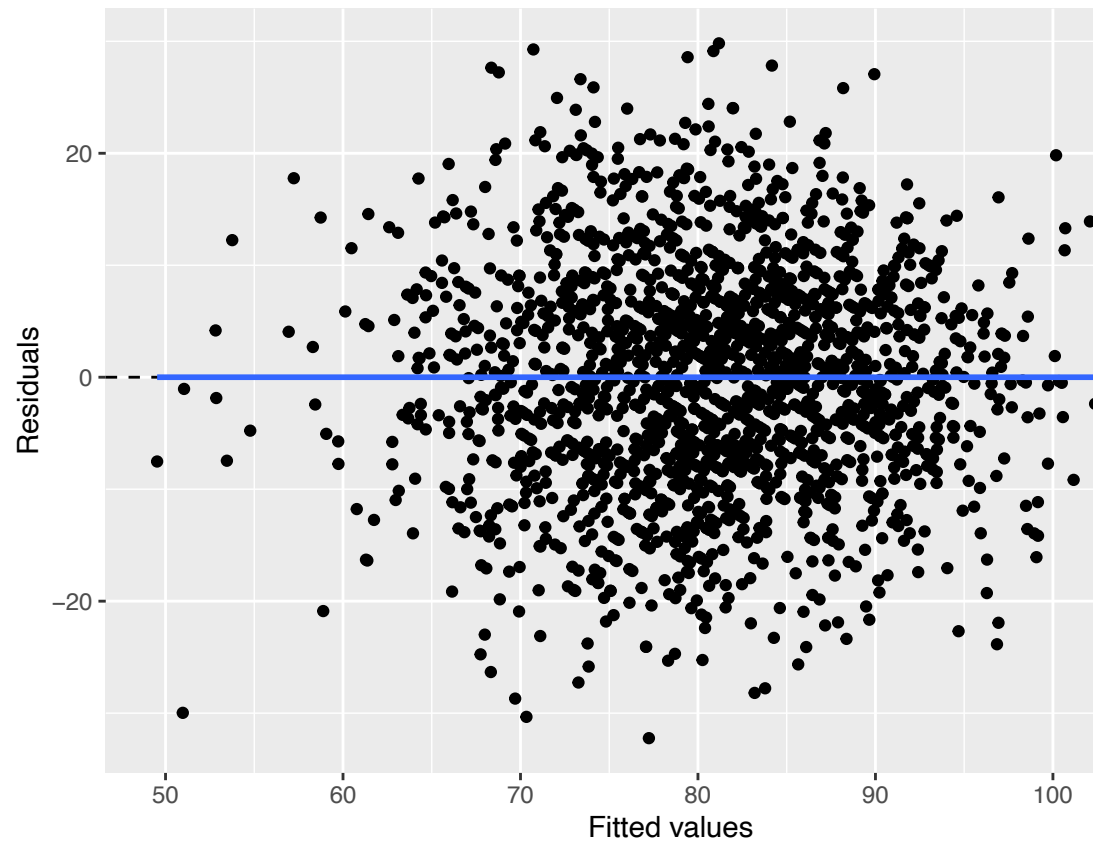
	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	57.054236	6.151995	9.274	< 0.0000000000000002 ***
Hits	-0.035845	0.021081	-1.700	0.089244 .
Doubles	-0.054553	0.009023	-6.046	0.00000000181 ***
Triples	0.186556	0.019637	9.500	< 0.0000000000000002 ***
HomeRuns	0.236397	0.096373	2.453	0.014264 *
Walks_AtBat	0.200201	0.062835	3.186	0.001467 **
BasesStolen	0.076979	0.006568	11.720	< 0.0000000000000002 ***
Hits_Allowed	0.065450	0.019551	3.348	0.000832 ***

```

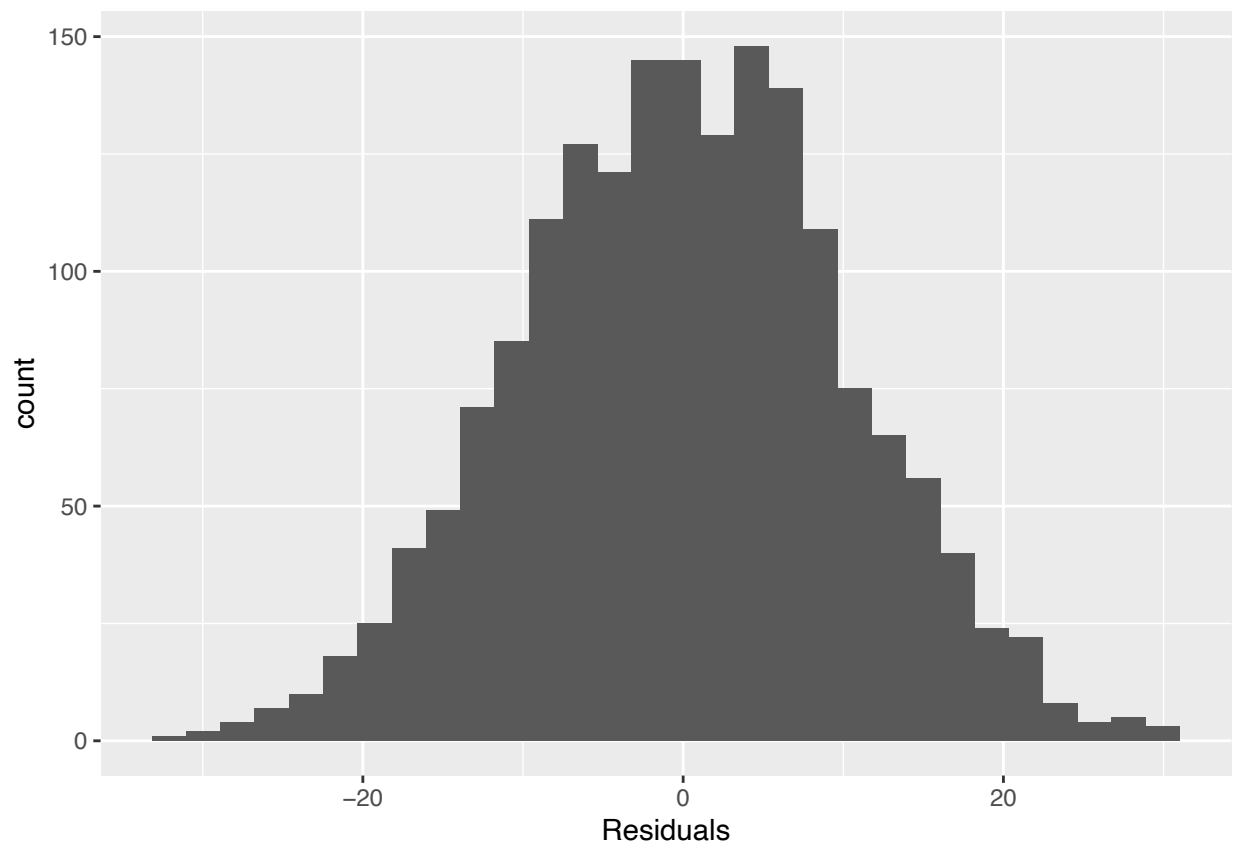
## HomeRuns_Allowed -0.140764  0.093058  -1.513          0.130547
## Errors           -0.124249  0.007359 -16.885 < 0.0000000000000002 ***
## Walks_Allowed    -0.158502  0.060243  -2.631          0.008586 **
## StrikeOuts_AtBat -0.022013  0.002395  -9.192 < 0.0000000000000002 ***
## OutStealingBases -0.039065  0.014479  -2.698          0.007039 **
## DoublePlays       -0.109815  0.012588  -8.724 < 0.0000000000000002 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10.26 on 1775 degrees of freedom
## Multiple R-squared:  0.4045, Adjusted R-squared:  0.4001
## F-statistic: 92.74 on 13 and 1775 DF, p-value: < 0.00000000000000022

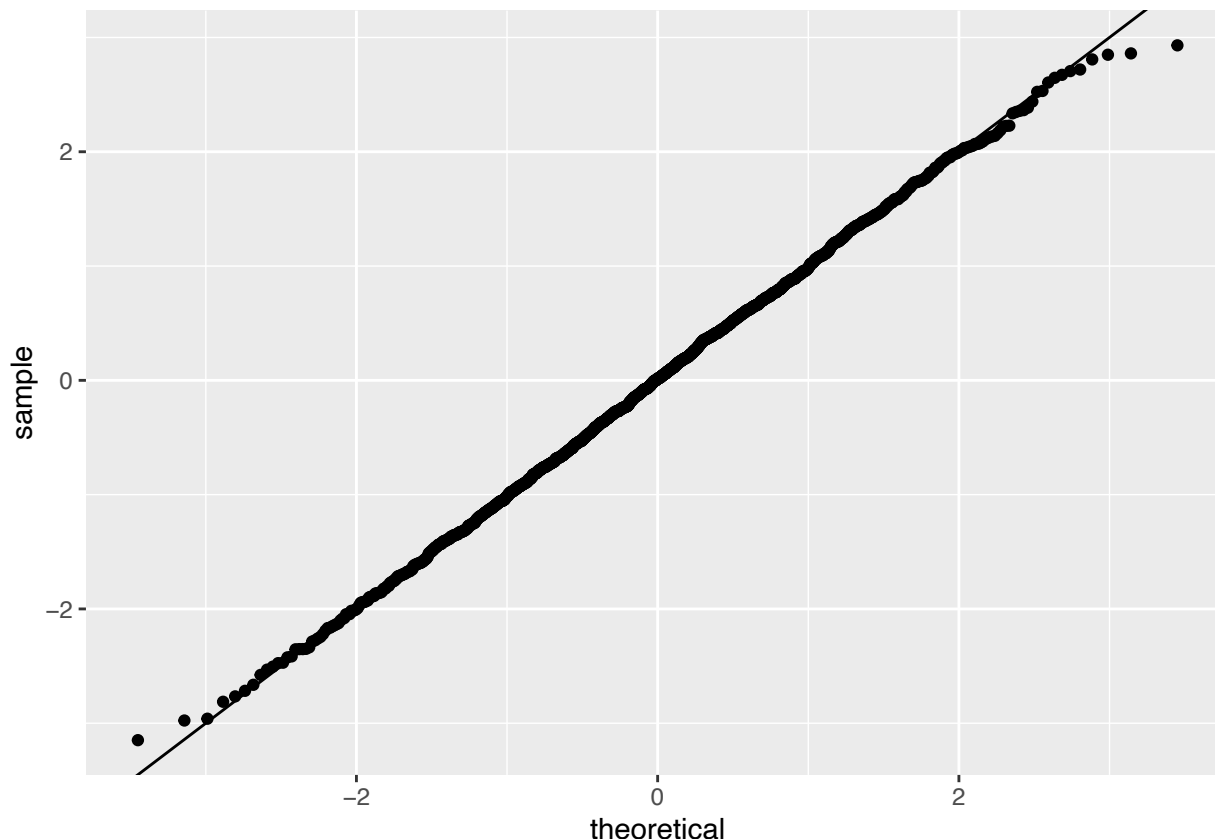
```

However we see minimal impact to the R-squared value, which remains around 0.40.



0.4.1.1.1 Model 2 Plots





Wins = Target_wins, Hits = Batting_h, Doubles = Batting_2b, Triples = Batting_3b, HomeRuns = Batting_hr, Walks_AtBat = Batting_bb, StrikeOuts_AtBat = Batting_so, BasesStolen = Baserun_sb, OutStealingBases = Baserun_cs, Hits_Allowed = Pitching_h, HitByPitch_AtBat = Batting_hbp, Errors = Fielding_e, HomeRuns_Allowed = Pitching_hr, Walks_Allowed = Pitching_bb, StrikeOuts = Pitching_so, DoublePlays = Fielding_dp

0.4.1.1.2 Model 3 For Model 3, we create a new dataframe and derive some new variables by transforming existing predictors to include in this dataframe: - Singles is derived as the difference between all Hits and Doubles, Triples and Home Runs - Homeruns difference is the difference between home runs scored and allowed.

We also include certain variables derived on the fly in the model - for example: the ratio between Home runs allowed and scores, the product of home runs allowed and scored, the reciprocal of Double plays and the cube of the stolen basis variable.

Model 3 Summary Stats

```
##
## Call:
## lm(formula = Wins ~ Hits + Doubles + Triples + Walks_AtBat +
##     BasesStolen + Hits_Allowed + Errors + Walks_Allowed + StrikeOuts +
##     Singles + Homeruns_diff + StrikeOuts_AtBat + I(HomeRuns_Allowed/HomeRuns) +
##     I(HomeRuns_Allowed * HomeRuns) + I(1/DoublePlays) + I(OutStealingBases^3),
##     data = mb_training_new)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
```



```
## -31.826  -7.049   0.066   6.960  31.025
##
## Coefficients:
##              Estimate      Std. Error t value
## (Intercept)  109.9453169993   40.2856609726   2.729
## Hits         0.0281580282    0.0440891477   0.639
## Doubles     -0.1735673380    0.0277600015  -6.252
## Triples      0.0602076781    0.0303537212   1.984
## Walks_AtBat  0.1904325935    0.0648354833   2.937
## BasesStolen  0.0687665386    0.0060907199  11.290
## Hits_Allowed 0.1198392065    0.0310629804   3.858
## Errors     -0.1235278847    0.0075827849 -16.291
## Walks_Allowed -0.1489662240    0.0621728192  -2.396
## StrikeOuts   0.0166499515    0.0340842858   0.488
## Singles     -0.1206931596    0.0272655274  -4.427
## Homeruns_diff -0.2229976419    0.1427124139  -1.563
## StrikeOuts_AtBat -0.0391231155    0.0354323522  -1.104
## I(HomeRuns_Allowed/HomeRuns) -85.2314174131   37.8641514196  -2.251
## I(HomeRuns_Allowed * HomeRuns) -0.0000688546    0.0000877940  -0.784
## I(1/DoublePlays) 2390.0964728930  257.2489261894   9.291
## I(OutStealingBases^3) 0.0000001113    0.0000004862   0.229
##              Pr(>|t|)
## (Intercept)      0.006413 **
## Hits             0.523126
## Doubles          0.000000000505 ***
## Triples          0.047462 *
## Walks_AtBat      0.003355 **
## BasesStolen      < 0.0000000000000002 ***
## Hits_Allowed     0.000118 ***
## Errors           < 0.0000000000000002 ***
## Walks_Allowed    0.016678 *
## StrikeOuts       0.625261
## Singles          0.000010157283 ***
## Homeruns_diff    0.118333
## StrikeOuts_AtBat 0.269672
## I(HomeRuns_Allowed/HomeRuns) 0.024509 *
## I(HomeRuns_Allowed * HomeRuns) 0.432984
## I(1/DoublePlays) < 0.0000000000000002 ***
## I(OutStealingBases^3) 0.819000
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10.25 on 1772 degrees of freedom
## Multiple R-squared:  0.4069, Adjusted R-squared:  0.4015
## F-statistic: 75.97 on 16 and 1772 DF, p-value: < 0.00000000000000022
```

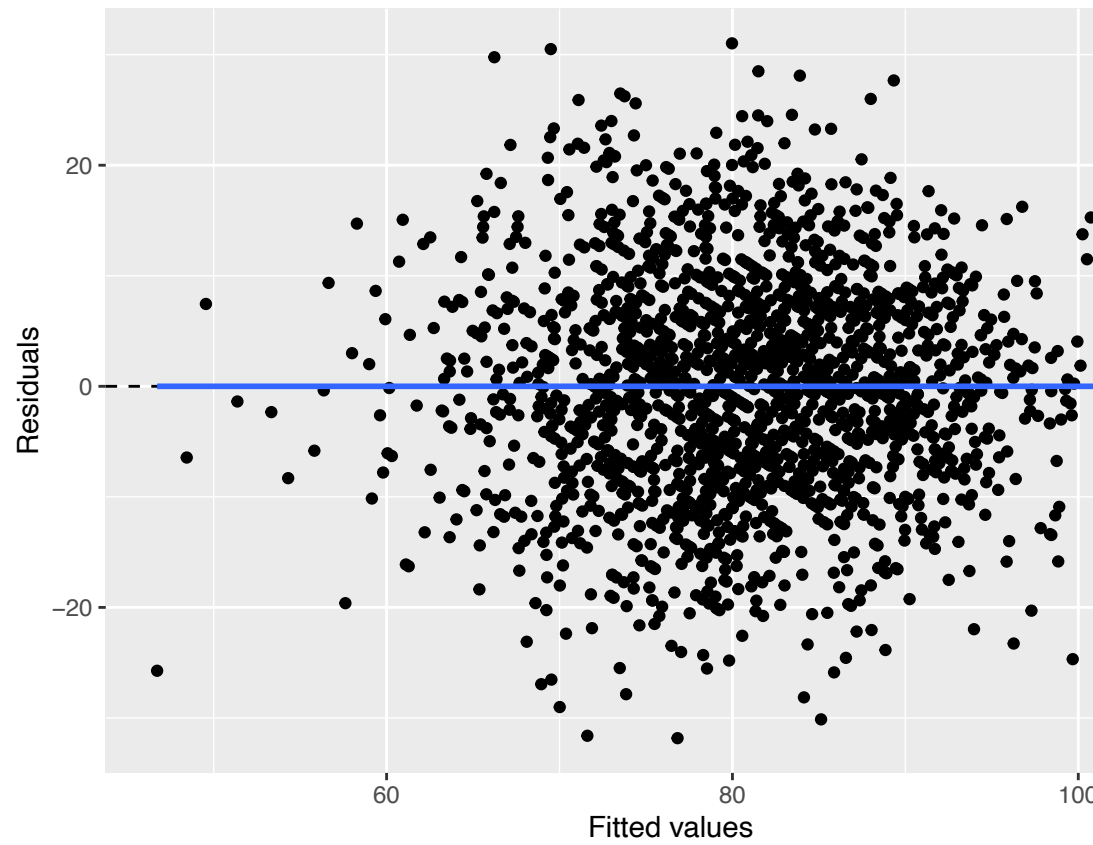
We don't see much change to the R-squared value.

Model 3 R-Squared

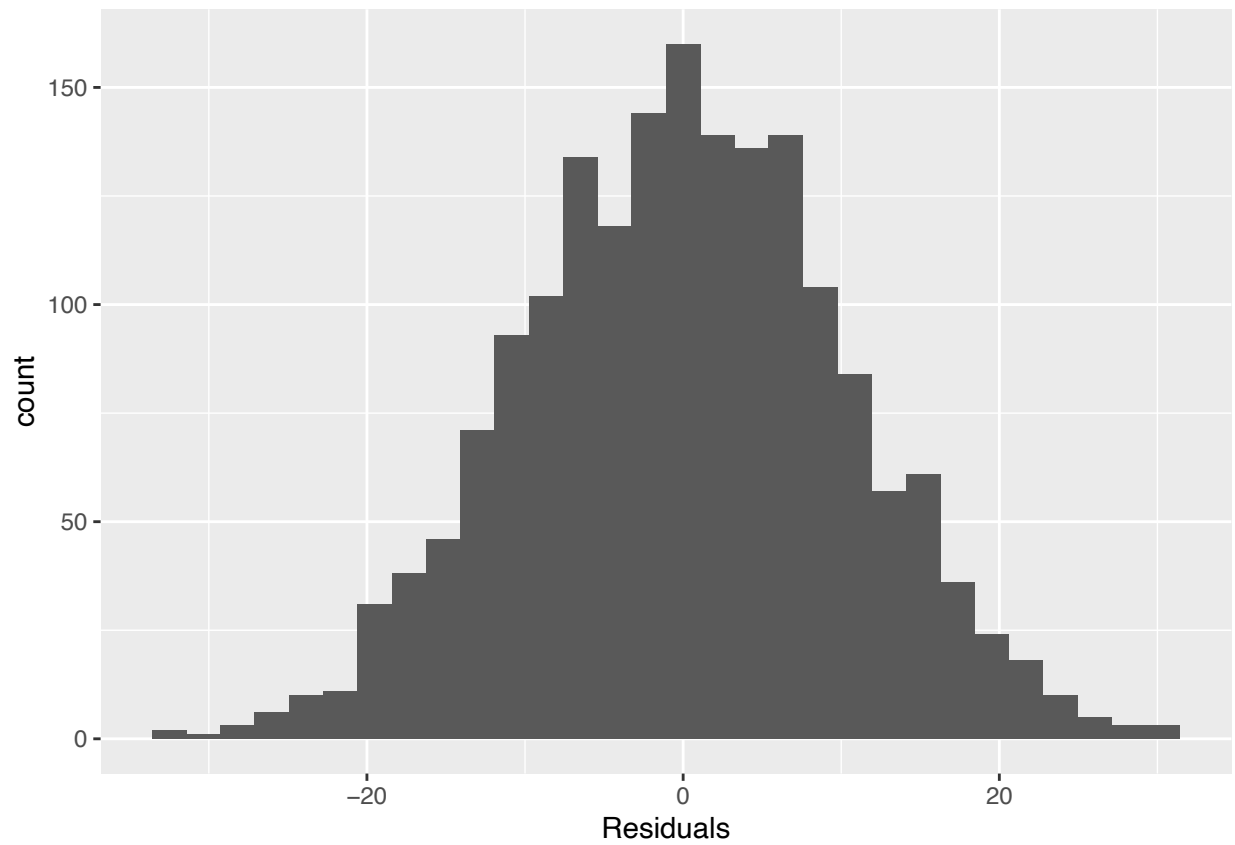
```
## [1] 0.4068615
```

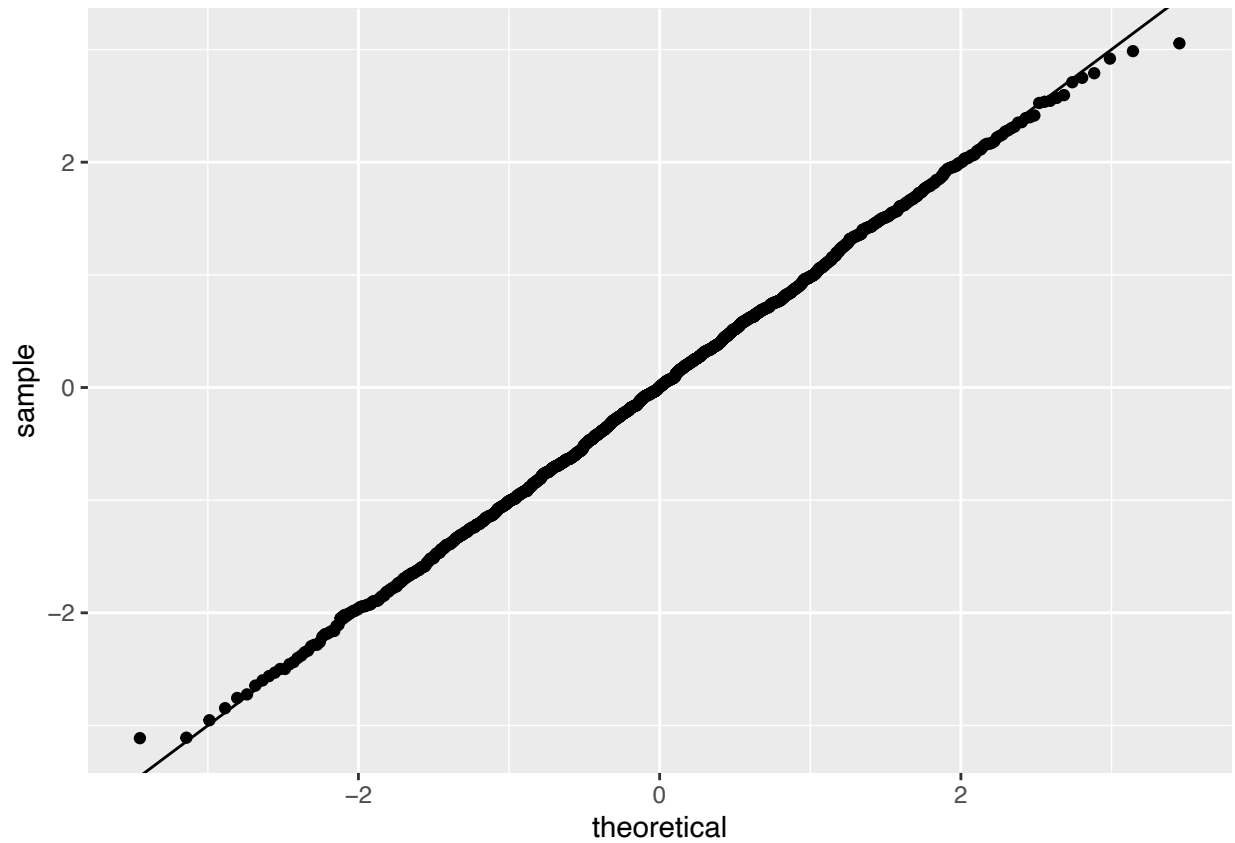
Model 3 Confidence Intervals

##	2.5 %	97.5 %
## (Intercept)	30.9329035984562	188.957730400225
## Hits	-0.0583141776004	0.114630233945
## Doubles	-0.2280131298677	-0.119121546135
## Triples	0.0006748143466	0.119740541945
## Walks_AtBat	0.0632705241893	0.317594662719
## BasesStolen	0.0568207875157	0.080712289602
## Hits_Allowed	0.0589152700712	0.180763142896
## Errors	-0.1384000282943	-0.108655741084
## Walks_Allowed	-0.2709060004136	-0.027026447629
## StrikeOuts	-0.0501996822336	0.083499585329
## Singles	-0.1741691375868	-0.067217181579
## Homeruns_diff	-0.5029000183358	0.056904734612
## StrikeOuts_AtBat	-0.1086167168480	0.030370485818
## I(HomeRuns_Allowed/HomeRuns)	-159.4945153196878	-10.968319506518
## I(HomeRuns_Allowed * HomeRuns)	-0.0002410453595	0.000103336128
## I(1/DoublePlays)	1885.5532182390721	2894.639727546878
## I(OutStealingBases^3)	-0.0000008422653	0.000001064801



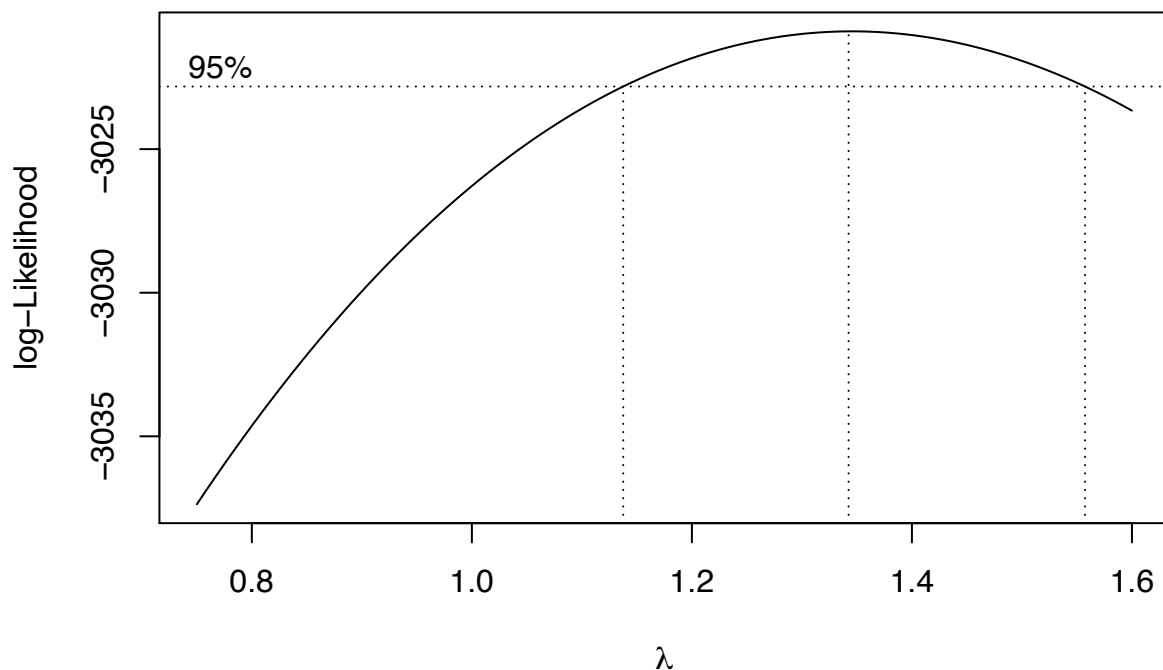
0.4.1.1.3 Model 3 Plots





There is not much change in the scatter plot of the residuals with the fitted values, and the distribution of errors does not seem to have changed much.

0.4.1.2 Model 4 - Box Cox transformation For our final model (Model 4), we do a Box Cox transformation on the response variable from Model 1 to see if it provides a better-fitting model. We plot the lambda and based on the plot, a lambda value of around 1.35 seems like the best value.



0.4.1.2.1 Model 4 Statistics Model 4 Summary Stats

```
##
## Call:
## lm(formula = (((Wins^1.35) - 1)/1.35) ~ Hits + Doubles + Triples +
##      HomeRuns + Walks_AtBat + BasesStolen + Hits_Allowed + HomeRuns_Allowed +
##      Errors + Walks_Allowed + StrikeOuts + StrikeOuts_AtBat +
##      OutStealingBases + DoublePlays, data = mb_training_updated)
##
## Residuals:
```

	Min	1Q	Median	3Q	Max
	-138.325	-33.262	-0.183	31.243	143.981

```
##
## Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	169.730793	28.446990	5.967	0.00000000292	***
Hits	-0.160624	0.102019	-1.574	0.11556	
Doubles	-0.251500	0.041641	-6.040	0.00000000188	***
Triples	0.859596	0.090943	9.452	< 0.0000000000000002	***
HomeRuns	1.088291	0.640737	1.698	0.08959	.
Walks_AtBat	0.922916	0.298057	3.096	0.00199	**
BasesStolen	0.351828	0.030326	11.602	< 0.0000000000000002	***
Hits_Allowed	0.296026	0.094672	3.127	0.00180	**
HomeRuns_Allowed	-0.640745	0.621730	-1.031	0.30288	
Errors	-0.560633	0.033978	-16.500	< 0.0000000000000002	***

```
## Walks_Allowed      -0.729399    0.285721   -2.553             0.01077 *
## StrikeOuts         0.007101    0.148555    0.048             0.96188
## StrikeOuts_AtBat   -0.110581    0.154256   -0.717             0.47355
## OutStealingBases   -0.183480    0.066905   -2.742             0.00616 **
## DoublePlays        -0.502375    0.058158   -8.638 < 0.0000000000000002 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 47.33 on 1774 degrees of freedom
## Multiple R-squared:  0.4028, Adjusted R-squared:  0.3981
## F-statistic: 85.46 on 14 and 1774 DF, p-value: < 0.00000000000000022
```

Model 4 R Squared

```
## [1] 0.4027743
```

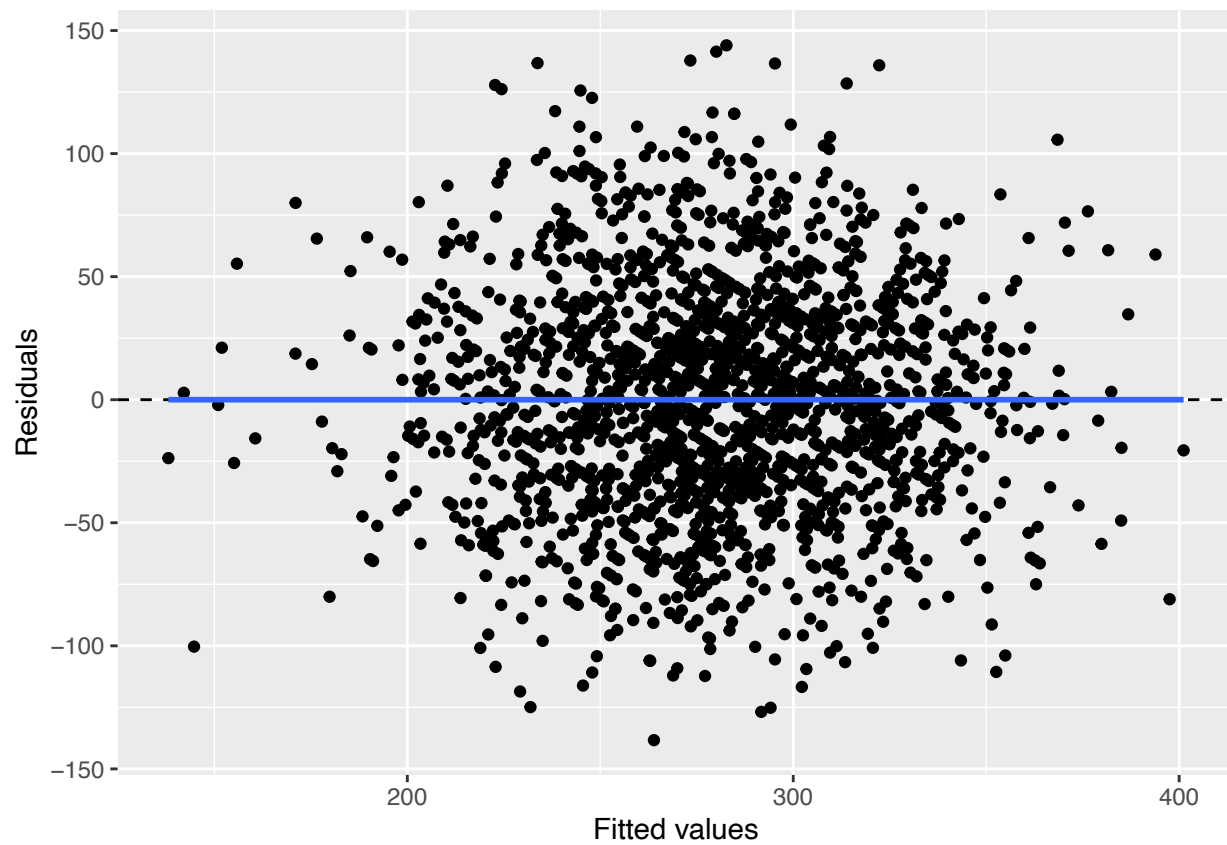
We don't see much impact on R-squared, possibly because the response variable was close to normal to begin with.

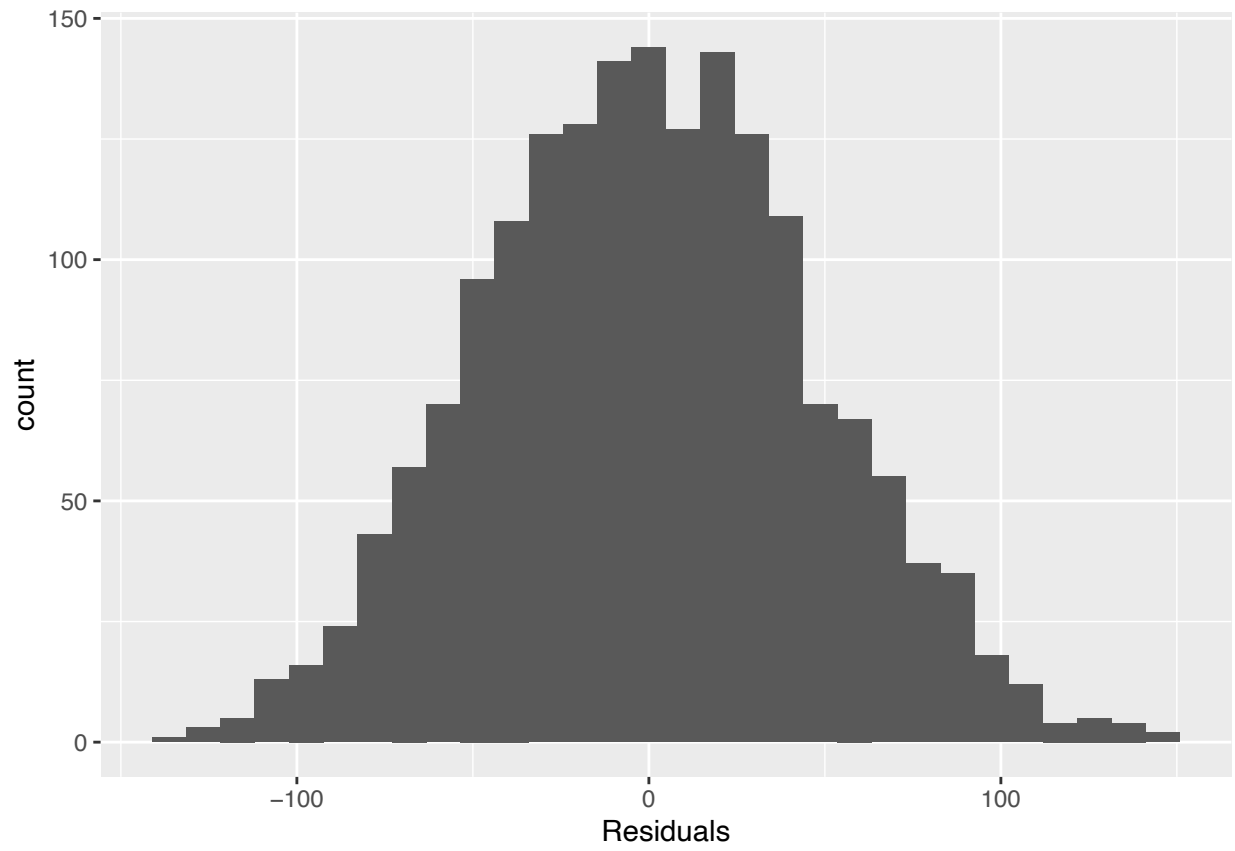
Model 4 Confidence Intervals

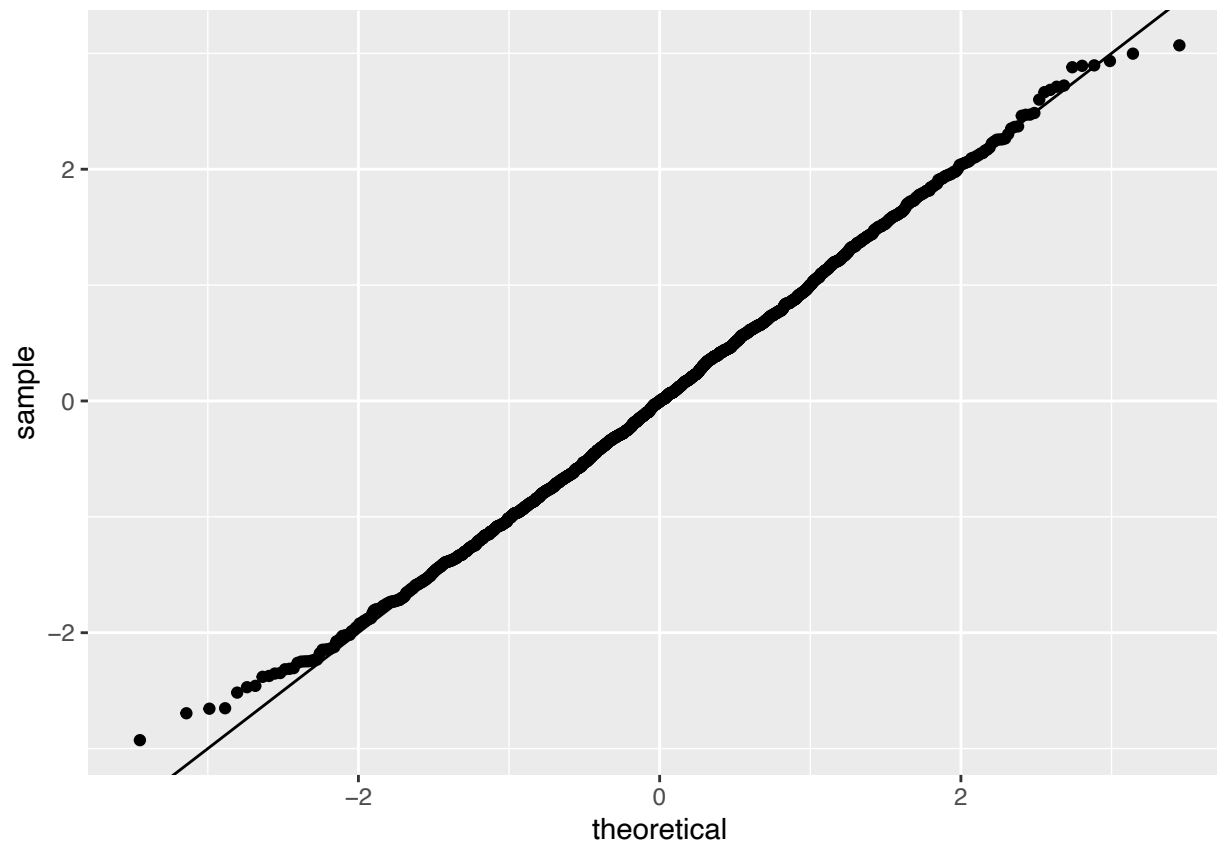
We calculate the 95% confidence intervals for each of the co-efficients and the intercept for this model.

```
##              2.5 %      97.5 %
## (Intercept)  113.9376512 225.52393496
## Hits        -0.3607137  0.03946645
## Doubles     -0.3331698 -0.16982958
## Triples      0.6812301  1.03796157
## HomeRuns    -0.1683880  2.34497038
## Walks_AtBat  0.3383354  1.50749568
## BasesStolen  0.2923498  0.41130605
## Hits_Allowed 0.1103447  0.48170712
## HomeRuns_Allowed -1.8601466 0.57865598
## Errors      -0.6272741 -0.49399258
## Walks_Allowed -1.2897845 -0.16901436
## StrikeOuts   -0.2842602  0.29846157
## StrikeOuts_AtBat -0.4131244 0.19196222
## OutStealingBases -0.3147009 -0.05225998
## DoublePlays  -0.6164411 -0.38830872
```

0.4.1.2.2 Model 4 Plots We plot the residuals versus the fitted values - it shows that the residuals are scattered fairly evenly and there doesn't seem to be a trend. The distribution of the residuals does not seem very skewed. The same can be seen through the qq-plot as well.







The residuals for this model behave similarly to the residuals from the previous model.

0.5 Model Selection

We decide to use model one for making predictions for the test dataset, since the other models do not provide a significant improvement over it.

0.5.0.1 Predicting the response variable for the test dataset We now predict the number of wins for the test data using model one.

```
## TEAM_BATTING_H TEAM_BATTING_2B TEAM_BATTING_3B TEAM_BATTING_HR
## Min. : 819 Min. : 44.0 Min. : 14.00 Min. : 0.00
## 1st Qu.:1387 1st Qu.:210.0 1st Qu.: 35.00 1st Qu.: 44.50
## Median :1455 Median :239.0 Median : 52.00 Median :101.00
## Mean :1469 Mean :241.3 Mean : 55.91 Mean : 95.63
## 3rd Qu.:1548 3rd Qu.:278.5 3rd Qu.: 72.00 3rd Qu.:135.50
## Max. :2170 Max. :376.0 Max. :155.00 Max. :242.00
##
## TEAM_BATTING_BB TEAM_BATTING_SO TEAM_BASERUN_SB TEAM_BASERUN_CS
## Min. : 15.0 Min. : 0.0 Min. : 0.0 Min. : 0.00
## 1st Qu.:436.5 1st Qu.: 545.0 1st Qu.: 59.0 1st Qu.: 38.00
## Median :509.0 Median : 686.0 Median : 92.0 Median : 49.50
## Mean :499.0 Mean : 709.3 Mean :123.7 Mean : 52.32
## 3rd Qu.:565.5 3rd Qu.: 912.0 3rd Qu.:151.8 3rd Qu.: 63.00
## Max. :792.0 Max. :1268.0 Max. :580.0 Max. :154.00
```

```

##          NA's :18          NA's :13          NA's :87
## TEAM_BATTING_HBP TEAM_PITCHING_H TEAM_PITCHING_HR TEAM_PITCHING_BB
## Min. :42.00    Min. : 1155    Min. : 0.0    Min. : 136.0
## 1st Qu.:53.50    1st Qu.: 1426    1st Qu.: 52.0    1st Qu.: 471.0
## Median :62.00    Median : 1515    Median :104.0    Median : 526.0
## Mean :62.37    Mean : 1813    Mean :102.1    Mean : 552.4
## 3rd Qu.:67.50    3rd Qu.: 1681    3rd Qu.:142.5    3rd Qu.: 606.5
## Max. :96.00    Max. :22768    Max. :336.0    Max. :2008.0
## NA's :240
## TEAM_PITCHING_SO TEAM_FIELDING_E TEAM_FIELDING_DP
## Min. : 0.0    Min. : 73.0    Min. : 69.0
## 1st Qu.: 613.0    1st Qu.: 131.0    1st Qu.:131.0
## Median : 745.0    Median : 163.0    Median :148.0
## Mean : 799.7    Mean : 249.7    Mean :146.1
## 3rd Qu.: 938.0    3rd Qu.: 252.0    3rd Qu.:164.0
## Max. :9963.0    Max. :1568.0    Max. :204.0
## NA's :18          NA's :31

```

0.5.1 Data Preparation, Test Data

The test data is prepared similarly to the training data, with columns renamed and missing values assigned an imputed value of the median.

```

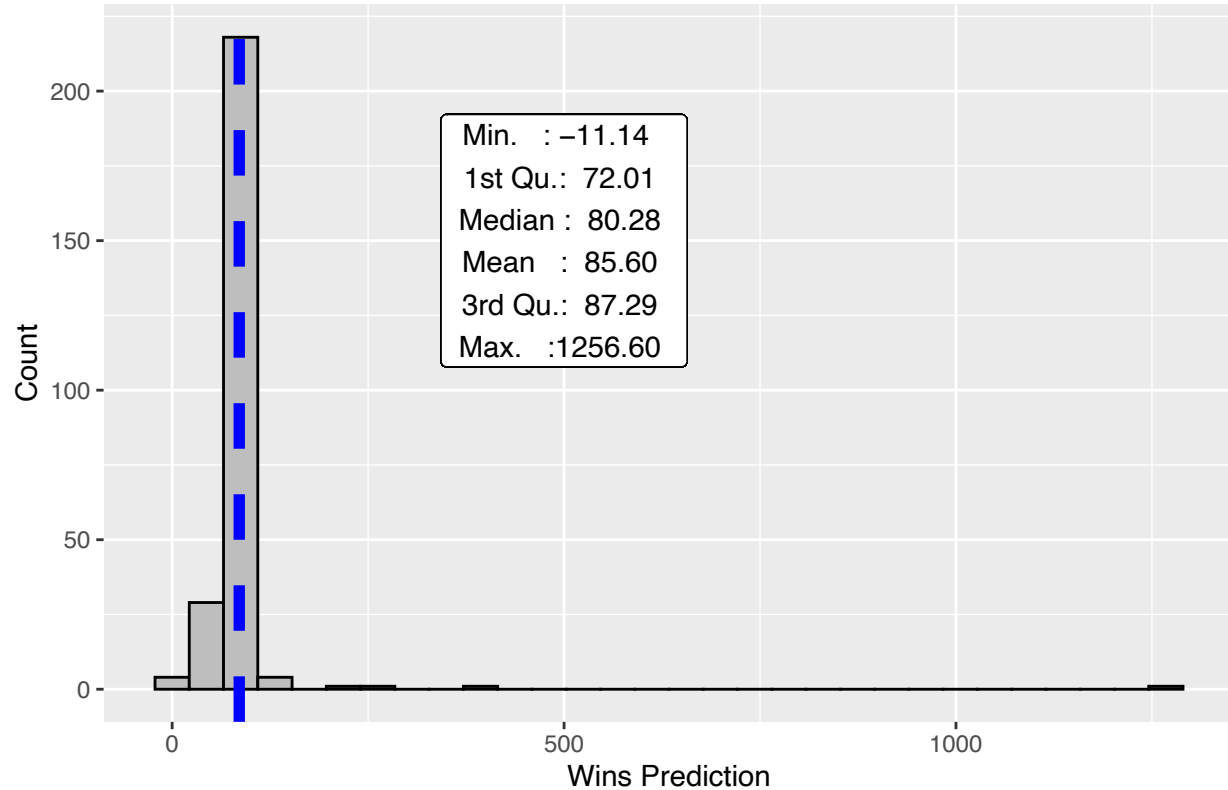
##      Hits      Doubles      Triples      HomeRuns
## Min. : 819    Min. : 44.0    Min. : 14.00    Min. : 0.00
## 1st Qu.:1387    1st Qu.:210.0    1st Qu.: 35.00    1st Qu.: 44.50
## Median :1455    Median :239.0    Median : 52.00    Median :101.00
## Mean :1469    Mean :241.3    Mean : 55.91    Mean : 95.63
## 3rd Qu.:1548    3rd Qu.:278.5    3rd Qu.: 72.00    3rd Qu.:135.50
## Max. :2170    Max. :376.0    Max. :155.00    Max. :242.00
## Walks_AtBat StrikeOuts_AtBat BasesStolen OutStealingBases
## Min. : 15.0    Min. : 0.0    Min. : 0.0    Min. : 0.00
## 1st Qu.:436.5    1st Qu.: 565.0    1st Qu.: 60.5    1st Qu.: 44.00
## Median :509.0    Median : 686.0    Median : 92.0    Median : 49.50
## Mean :499.0    Mean : 707.7    Mean :122.1    Mean : 51.37
## 3rd Qu.:565.5    3rd Qu.: 904.5    3rd Qu.:149.0    3rd Qu.: 56.00
## Max. :792.0    Max. :1268.0    Max. :580.0    Max. :154.00
## HitByPitch_AtBat Hits_Allowed HomeRuns_Allowed Walks_Allowed
## Min. :42.00    Min. : 1155    Min. : 0.0    Min. : 136.0
## 1st Qu.:62.00    1st Qu.: 1426    1st Qu.: 52.0    1st Qu.: 471.0
## Median :62.00    Median : 1515    Median :104.0    Median : 526.0
## Mean :62.03    Mean : 1813    Mean :102.1    Mean : 552.4
## 3rd Qu.:62.00    3rd Qu.: 1681    3rd Qu.:142.5    3rd Qu.: 606.5
## Max. :96.00    Max. :22768    Max. :336.0    Max. :2008.0
## StrikeOuts      Errors      DoublePlays
## Min. : 0.0    Min. : 73.0    Min. : 69.0
## 1st Qu.: 622.5    1st Qu.: 131.0    1st Qu.:134.5
## Median : 745.0    Median : 163.0    Median :148.0
## Mean : 795.9    Mean : 249.7    Mean :146.3
## 3rd Qu.: 927.5    3rd Qu.: 252.0    3rd Qu.:160.5
## Max. :9963.0    Max. :1568.0    Max. :204.0

```

0.5.2 Predicting Wins

We will look at the distribution of the predicted test data and create a table for the predicted wins.

Wins Prediction Histogram Plot



fit	lwr	upr
60.80215	40.58776	81.01653
67.69641	47.50656	87.88625
72.45775	52.28529	92.63021
83.37307	63.20421	103.54192
145.16145	68.69661	221.62629
75.81520	41.43534	110.19506

0.6 Conclusion

We conclude that model one which includes a majority of the predictors except one provides the best overall fit. While we did try additional models based on transformed variables, they did not provide a significant improvement, so we decided to go with model one. This model does not seem to violate the assumptions of linear regression.

0.7 References

Sellmair, Reinhard. "How to handle correlated Features?" June 25, 2018. <https://www.kaggle.com/reisel/how-to-handle-correlated-features>

Xie, Yihui, J. J. Allaire, and Garrett Golemund, *R Markdown: The Definitive Guide*, CRC Press December 14, 2020 <https://bookdown.org/yihui/rmarkdown/r-code.html>.

<https://rstatisticsblog.com/data-science-in-action/data-preprocessing/six-amazing-function-to-create-train-test-split-in-r/>

0.7.1 R Code

```
# =====
# Load Libraries and Disable Scientific Notation for Readability Purposes
# =====

knitr::opts_chunk$set(echo = TRUE)
# Disable scientific numbers for readability purposes.
options(scipen = 999)

library(MASS)
library(tidyverse)
library(dplyr)
library(reshape2)
library(kableExtra)
library(corrplot)
library(ggplot2)
library(Hmisc)
library(PerformanceAnalytics)
library(GGally)
library(ggpubr)
library(car)

# =====
# Load The Dataset and Summarize the Data
# =====

# Load in the training data.
url = "https://raw.githubusercontent.com/Jagdish16/CUNY_DATA_621/main/project_1/moneyball-training-data"
mb_training <- read.csv(url)

# Remove the INDEX variable as it is of no value in the data evaluation.
mb_training <- subset(mb_training, select = -c(INDEX))

# Summarize the test data.
summary(mb_training)

# =====
# Rename the Variables to be More Intuitive
# =====

# Rename the columns to be more intuitive.
mb_training <- mb_training %>%
  rename_with(~ gsub("TEAM_", "", .x)) %>%
  rename_with(stringr::str_to_title) %>%
  dplyr::rename(
    Wins = Target_wins,
    Hits = Batting_h,
```

```

Doubles = Batting_2b,
Triples = Batting_3b,
HomeRuns = Batting_hr,
Walks_AtBat = Batting_bb,
StrikeOuts_AtBat = Batting_so,
BasesStolen = Baserun_sb,
OutStealingBases = Baserun_cs,
Hits_Allowed = Pitching_h,
HitByPitch_AtBat = Batting_hbp,
Errors = Fielding_e,
HomeRuns_Allowed = Pitching_hr,
Walks_Allowed = Pitching_bb,
StrikeOuts = Pitching_so,
DoublePlays = Fielding_dp
)

# =====
# Box Plots
# =====

# Plot boxplots for all variables.
long <- mb_training %>% as.data.frame() %>% melt()

long %>%
  ggplot(aes(x=value)) + geom_boxplot() + facet_wrap(~variable, scales = 'free')

# =====
# Distribution Plots
# =====

# mean_data <- long %>% na.omit() %>% #omits na values only, not full cases
# group_by(variable) %>%
# summarise(mean = mean(value))

# long %>%
# ggplot(aes(x=value)) +
# geom_histogram(color = 'black', fill = 'gray', bins = 30) +
# geom_vline(data = mean_data, aes(xintercept = mean), linetype = 'dashed', color = 'blue') +
# facet_wrap(~variable, scales = 'free')

# =====
# Missing Data
# =====

# Create a table of variables sorted by percentage of missing data.
missing_data <- colSums(mb_training %>% sapply(is.na))
percentage_missing <- round(missing_data / nrow(mb_training) * 100, 2)
missing_values_table <- sort(percentage_missing, decreasing = TRUE)

missing_values_table %>%
  kable(caption = 'Breakdown of Variables by Percentage of Missing Data') %>%

```

```

kable_styling()

# Drop the HitByPitch_AtBat variable from the dataset.
mb_training <- mb_training %>% dplyr::select(-HitByPitch_AtBat)

# =====
# Handle Outliers
# =====

# Remove outlier rows for the 6 predictor variables.
mb_training_updated <- mb_training

# Remove outliers - Method 2.
for (n in c("Walks_Allowed", "BasesStolen", "StrikeOuts", "Hits_Allowed", "Errors", "Triples")) {
  Q <- quantile(mb_training[,n], probs = c(.25, .75), na.rm = TRUE)
  iqr <- IQR(mb_training[,n], na.rm = TRUE)
  # Upper Range.
  up <- Q[2] + 1.5 * iqr
  # Lower Range.
  low <- Q[1] - 1.5 * iqr
  mb_training_updated <- subset(mb_training_updated, mb_training_updated[,n] > (Q[1]-1.5 * iqr)&mb_traini
}

# Check the summary for the updated dataframe.
summary(mb_training_updated)

# Impute missing values with the median value for each remaining column.
mb_training_updated <- data.frame(sapply(mb_training_updated, function(x) ifelse(is.na(x), median(x), na

# Check the summary for the updated dataframe.
summary(mb_training_updated)

# =====
# Data Correlation
# =====

# Perform a correlation analysis on the data. In this analysis, we are only interested in the
# correlation of the predictor variables and the "TARGET_WINS" variable.
correlation_table <- cor(mb_training_updated, method = 'pearson', use = 'complete.obs')[,1]

# Remove the TARGET_WINS variable from the correlation table as it is redundant
# within the context of of our correlation analysis.
correlation_table <- correlation_table[-c(1)]

correlation_table %>%
  kable(caption = 'Correlation of Variables to Wins') %>% kable_styling()

# Calculate correlation between variables.
mb_training_updated_corr_matrix <- mb_training_updated %>% cor() %>% round(2) %>% as.matrix()
mb_training_updated_corr_matrix %>% kable() %>% kable_styling()

# flattenCorrMatrix
# cormat : matrix of the correlation coefficients.
# pmat : matrix of the correlation p-values.

```

```

flattenCorrMatrix <- function(cormat, pmat) {
  ut <- upper.tri(cormat)
  data.frame(
    row = rownames(cormat)[row(cormat)[ut]],
    column = rownames(cormat)[col(cormat)[ut]],
    cor = (cormat)[ut],
    p = pmat[ut]
  )
}

# Another method to check correlations and their significance.
corr.mat<-rcorr(as.matrix(mb_training_updated))

flattenCorrMatrix(corr.mat$r, corr.mat$p)%>% filter(row=='Wins') %>% arrange(-abs(cor))

# =====
# Check Normality of Predictors
# =====

# Run the Shapiro wilkes test for normality.
do.call(rbind, lapply(mb_training_updated, function(x) shapiro.test(x)[c("statistic", "p.value")]))

# =====
# Model 1
# =====

model_one <- lm(Wins ~ Hits + Doubles + Triples + HomeRuns +
  Walks_AtBat + BasesStolen + Hits_Allowed +
  HomeRuns_Allowed + Errors + Walks_Allowed + StrikeOuts +
  StrikeOuts_AtBat + OutStealingBases + DoublePlays,
  mb_training_updated)

# Model 1 summary stats.
summary(model_one)

# Model 1 R Squared.
summary(model_one)$r.squared

# Model 1 Confidence Intervals.
confint(model_one)

# Model 1 plots - residuals vs fitted values, residuals distribution.
ggplot(data = model_one, aes(x = .fitted, y = .resid)) +
  geom_point() + geom_hline(yintercept = 0, linetype = "dashed") +
  geom_smooth(se = FALSE) + xlab("Fitted values") + ylab("Residuals")

ggplot(data = model_one, aes(x = .resid)) + geom_histogram() + xlab("Residuals")

ggplot(data = model_one) + stat_qq(aes(sample = .stdresid)) + geom_abline()

# =====

```



```

# Model 2
# =====

# Model 2 uses stepwise regression on the variables in Model 1.
model_two <- stepAIC(model_one, direction = 'both', trace = FALSE)

# Model 2 summary stats.
summary(model_two)

# Model 2 plots - residuals vs fitted values, residuals distribution.
ggplot(data = model_two, aes(x = .fitted, y = .resid)) +
  geom_point() + geom_hline(yintercept = 0, linetype = "dashed") +
  geom_smooth(se = FALSE) + xlab("Fitted values") + ylab("Residuals")

ggplot(data = model_two, aes(x = .resid)) + geom_histogram() + xlab("Residuals")

ggplot(data = model_two) + stat_qq(aes(sample = .stdresid)) + geom_abline()

# =====
# Model 3
# =====

# Derive 2 new variables for Singles and Home run difference.
mb_training_new <- mb_training_updated %>% mutate(Singles = Hits - Doubles - Triples - HomeRuns)
mb_training_new <- mb_training_new %>% mutate(Homeruns_diff = HomeRuns_Allowed - HomeRuns)

model_three <- lm(Wins ~ Hits + Doubles + Triples + Walks_AtBat +
  BasesStolen + Hits_Allowed + Errors + Walks_Allowed +
  StrikeOuts + Singles + Homeruns_diff + StrikeOuts_AtBat +
  I(HomeRuns_Allowed/HomeRuns) + I(HomeRuns_Allowed*HomeRuns) +
  I(1/DoublePlays) + I(OutStealingBases^3),
  mb_training_new)

# Model 3 summary stats.
summary(model_three)

# Model 3 R-Squared.
summary(model_three)$r.squared

# Model 3 confidence intervals.
confint(model_three)

# Model 3 plots - residuals vs fitted values, residuals distribution.
ggplot(data = model_three, aes(x = .fitted, y = .resid)) +
  geom_point() + geom_hline(yintercept = 0, linetype = "dashed") +
  geom_smooth(se = FALSE) + xlab("Fitted values") + ylab("Residuals")

ggplot(data = model_three, aes(x = .resid)) + geom_histogram() + xlab("Residuals")

ggplot(data = model_three) + stat_qq(aes(sample = .stdresid)) + geom_abline()

```

```

# =====
# Model 4
# =====

# Model 4 - Box Cox method.
MASS::boxcox(model_one, lambda = seq(0.75, 1.6, by = 0.05), plotit = TRUE)

# Fit a model using a lambda value of 1.35 for the response variable.
model_cox = lm((((Wins ^ 1.35) - 1)/ 1.35) ~ Hits + Doubles + Triples + HomeRuns + Walks_AtBat +
  BasesStolen + Hits_Allowed + HomeRuns_Allowed + Errors +
  Walks_Allowed + StrikeOuts + StrikeOuts_AtBat + OutStealingBases +
  DoublePlays,
  mb_training_updated)

# Model 4 summary stats.
summary(model_cox)

# Model 4 R Squared.
summary(model_cox)$r.squared

# Model 4 confidence intervals.
confint(model_cox)

# Model 4 plots - residuals vs fitted values, residuals distribution.
ggplot(data = model_cox, aes(x = .fitted, y = .resid)) +
  geom_point() + geom_hline(yintercept = 0, linetype = "dashed") +
  geom_smooth(se = FALSE) + xlab("Fitted values") + ylab("Residuals")

ggplot(data = model_cox, aes(x = .resid)) + geom_histogram() + xlab("Residuals")

ggplot(data = model_cox) + stat_qq(aes(sample = .stdresid)) + geom_abline()

# =====
# Model Selection
# =====

# Predict the number of wins for the test data using model one.

# Load in the test data.
url2 <- 'https://raw.githubusercontent.com/Jagdishi6/CUNY_DATA_621/main/project_1/moneyball-evaluation-
mb_test <- read.csv(url2)

# Remove the INDEX variable as it is of no value in the data evaluation.
mb_test <- subset(mb_test, select = -c(INDEX))

# Summarize the test data.
summary(mb_test)

# Rename the test data variables to be more intuitive.
mb_test <- mb_test %>%
  rename_with(~ gsub("TEAM_", "", .x)) %>%
  rename_with(stringr::str_to_title) %>%

```

```

dplyr::rename(
  Hits = Batting_h,
  Doubles = Batting_2b,
  Triples = Batting_3b,
  HomeRuns = Batting_hr,
  Walks_AtBat = Batting_bb,
  StrikeOuts_AtBat = Batting_so,
  BasesStolen = Baserun_sb,
  OutStealingBases = Baserun_cs,
  Hits_Allowed = Pitching_h,
  HitByPitch_AtBat = Batting_hbp,
  Errors = Fielding_e,
  HomeRuns_Allowed = Pitching_hr,
  Walks_Allowed = Pitching_bb,
  StrikeOuts = Pitching_so,
  DoublePlays = Fielding_dp
)

# Impute missing values with the median value for each column.
mb_test_updated <- data.frame(sapply(mb_test, function(x) ifelse(is.na(x), median(x, na.rm = TRUE), x)))

# Summarize the test data.
summary(mb_test_updated)

# Predicting Wins in the test data and looking at the distribution.
mb_test_updated$predicted_wins <- predict(model_one, type = 'response', newdata = mb_test_updated)

ggplot(data = mb_test_updated, aes(x = predicted_wins)) +
  geom_histogram( color = 'black', fill = 'gray') +
  geom_vline(aes(xintercept = mean(predicted_wins)), linetype = 'dashed', size = 2, color = 'blue') +
  geom_label(aes(x = 500, y = 150, label= str_replace_all(toString(summary(mb_test_updated['predicted_wins']),
  labs(title = 'Wins Prediction Histogram Plot', y = 'Count', x = 'Wins Prediction'))

# Create a table of prediction and confidence intervals.
test_data <- predict(model_one, newdata = mb_test_updated, interval = 'prediction')
summary(test_data)

```