

$$P(X=Y) = .08 + .15 + .10 + .07 = .40$$

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National University of Computer & Emerging Sciences
Artificial Intelligence (CS401)

Quiz#6

Dated: April 24, 2014

Marks: 20

Time: 20 min.

Std-ID: _____

Question No. 1

Mr. Ali is shifted to a new house. He came to know that his neighbor has 2 children. Once he saw Omar his neighbor's son. What is the probability that Omar's sibling is a sister?

Consider the experiment of selecting a random family having two children. The sample space is $S = \{BB, BG, GB, GG\}$, where, e.g., outcome "BG" means that the first-born child is a boy and the second-born is a girl. Assuming boys and girls are equally likely to be born, the 4 elements of S are equally likely. The event, E , that the neighbor has a son is the set $E = \{BB, BG, GB\}$. The event, F , that the neighbor has one boy and one girl (i.e., Omar has a sister) is the set $F = \{BG, GB\}$. We want to compute

$$P(F|E) = P(F \cap E) / P(E) = P(\{GB, BG\}) / P(\{BB, BG, GB\}) = (2/4) / (3/4) = 2 / 3$$

Question No. 2

There are two lotteries selling counters, let X be the number of customers present at first counter at any time of the day, and Y be the number of customers present at the second counter at the same time. As X and Y both can be random processes their joint probability can be represented as below:

X / Y	0	1	2	3
0	0.08	0.07	0.04	0.00
1	0.06	0.15	0.05	0.04
2	0.05	0.04	0.10	0.06
3	0.00	0.03	0.04	0.07
4	0.00	0.01	0.05	0.06

- a. What is the probability that there is no customer at both the counters?

$$P(X=0 \text{ and } Y=0) = 0.08$$

- b. What is the probability that the numbers of customer at both counters are identical in number?

$$P(X==Y) = 0.40$$