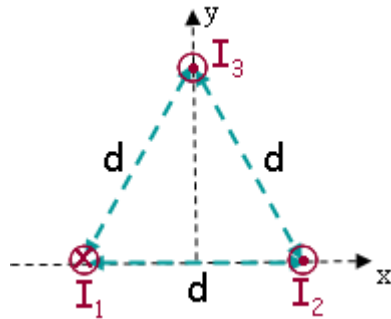


Three infinite straight wires are fixed in place and aligned parallel to the z-axis as shown. The wire at $(x,y) = (-21 \text{ cm}, 0)$ carries current $I_1 = 3.8 \text{ A}$ in the negative z-direction. The wire at $(x,y) = (21 \text{ cm}, 0)$ carries current $I_2 = 0.8 \text{ A}$ in the positive z-direction. The wire at $(x,y) = (0, 36.4 \text{ cm})$ carries current $I_3 = 5.5 \text{ A}$ in the positive z-direction.



- 1) What is $B_x(0,0)$, the x-component of the magnetic field produced by these three wires at the origin?

$$B_x(0,0) = \frac{\mu_0 I_3}{2\pi h}$$

The only x component contribution is from the I3 wire....

The constant $\mu_0 = 1.25663706 \times 10^{-6} \text{ m kg s}^{-2} \text{ A}^{-2}$

$$B_x(0,0) = \mu_0 (5.5 \text{ A}) / (2\pi \cdot 0.364 \text{ m}) = 3.02 \times 10^{-6} \text{ T}$$

- 2) What is $B_y(0,0)$, the y-component of the magnetic field produced by these three wires at the origin?

In this case, the only contributors to the y component are from I1 and I2.

$$B_y(0,0) = -\frac{\mu_0}{2\pi \frac{d}{2}} (I_1 + I_2) = -\frac{\mu_0}{\pi d} (I_1 + I_2)$$

$$B_y(0,0) = -\mu_0 (3.8 + 0.8) \text{ A} / (\pi \cdot 0.21 \cdot 2 \text{ m}) = -4.38 \times 10^{-6} \text{ T}$$

- 3) What is $F_x(1)$, the x-component of the force exerted on a one meter length of the wire carrying current I_1 ?

$$B_y(1) = -\frac{\mu_o I_3}{2\pi d} \sin(30^\circ) - \frac{\mu_o I_2}{2\pi d} \Rightarrow F_x(1) = -\frac{\mu_o I_1}{2\pi d} (I_3 \sin(30^\circ) + I_2)$$

$$F_x = -\mu \cdot 3.8 \text{ A} / (2\pi \cdot 21 \cdot 2) (5.5 \text{ A} \sin(30^\circ) + 0.8 \text{ A}) = -6.42 \times 10^{-6} \text{ N}$$

- 4) What is $F_y(1)$, the y-component of the force exerted on a one meter length of the wire carrying current I_1 ?

$$B_x(1) = \frac{\mu_o I_3}{2\pi d} \cos(30^\circ) \Rightarrow F_y(1) = -\frac{\mu_o I_1 I_3}{2\pi d} \cos(30^\circ)$$

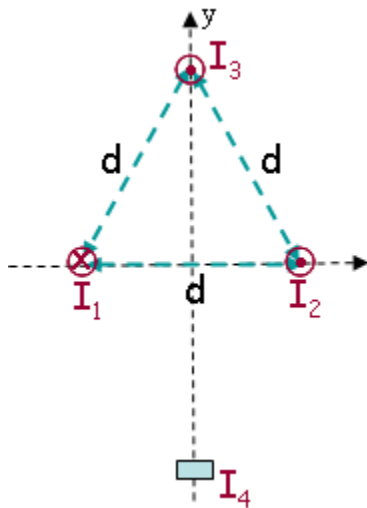
$$F_y = -\mu \cdot 3.8 \text{ A} \cdot 5.5 \text{ A} \cos(30^\circ) / (2 \cdot \pi \cdot 21 \text{ m}) = -8.61 \times 10^{-6} \text{ N}$$

- 5) What is $F_x(2)$, the x-component of the force exerted on a one meter length of the wire carrying current I_2 ?

$$B_y(2) = +\frac{\mu_o I_3}{2\pi d} \sin(30^\circ) - \frac{\mu_o I_1}{2\pi d} \Rightarrow F_x(2) = \frac{\mu_o I_2}{2\pi d} (I_1 - I_3 \sin(30^\circ))$$

$$F_x = -\mu \cdot 0.8 \text{ A} / (2\pi \cdot 21 \cdot 2) (3.8 \text{ A} \sin(30^\circ) - 5.5 \text{ A}) = 4 \times 10^{-7} \text{ N}$$

6)



Another wire is now added, also aligned with the z-axis at $(x, y) = (0, -36.4 \text{ cm})$ as shown. This wire carries current I_4 A. Which of the following statements is true?

- ☐ If I_4 is directed along the positive z-axis, then it is possible to make the y-component of the magnetic field equal to zero at the origin.
- ☐ If I_4 is directed along the negative z-axis, then it is possible to make the y-component of the magnetic field equal to zero at the origin.
- ☐ If I_4 is directed along the positive z-axis, then it is possible to make the x-component of the magnetic field equal to zero at the origin.
- ☐ If I_4 is directed along the negative z-axis, then it is possible to make the x-component of the magnetic field equal to zero at the origin.

Right Answer:

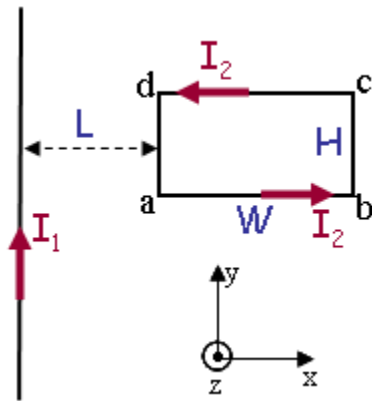
3

Feedback:

Your answer is correct! If the current I_4 flows in the same direction as the current I_3 , then the magnetic field it produces at the origin can cancel the field produced by the current I_3 . The field produced by both these currents is in the x-direction.

Recall question 1, the only contribution to the x component of the magnetic field at the origin is due to I_3 . That means if you place another current at I_4 think about how to make the magnetic field contributions be anti-parallel.

A rectangular loop of wire with sides $H = 23$ cm and $W = 54$ cm carries current $I_2 = 0.239$ A. An infinite straight wire, located a distance $L = 35$ cm from segment ad of the loop as shown, carries current $I_1 = 0.662$ A in the positive y-direction.



- 1) What is $F_{ad,x}$, the x-component of the force exerted by the infinite wire on segment ad of the loop?

Recall: $F = IL \times B$

$$F_{ad,x} = I_2 H \frac{\mu_0 I_1}{2\pi L}$$

$$F_{ad,x} = 0.239 \text{ A} \cdot 0.23 \text{ m} \cdot \mu_0 \cdot 0.662 \text{ A} / (2\pi \cdot 0.35 \text{ m}) = 2.07 \times 10^{-8} \text{ N}$$

- 2) What is $F_{bc,x}$, the x-component of the force exerted by the infinite wire on segment bc of the loop?

$$F_{bc,x} = -I_2 H \frac{\mu_0 I_1}{2\pi(L+W)}$$

Note the sign is opposite from before, you'd expect that because the current is going in the opposite direction here.

$$F_{bc,x} = -.239 \text{ A} \cdot .23 \text{ m} \cdot \mu \cdot .662 \text{ A} / (2\pi \cdot (.35 \text{ m} + .54 \text{ m})) = -.81 \times 10^{-9} \text{ N}$$

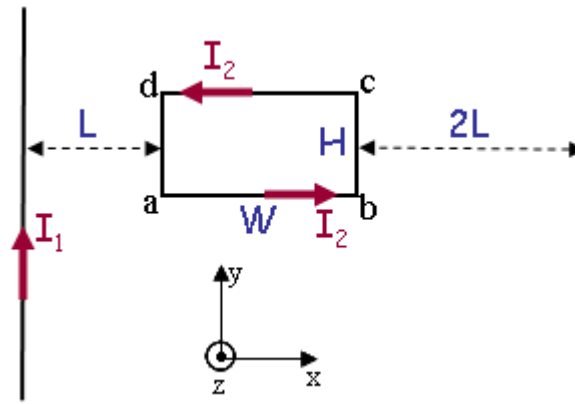
- 3) What is $F_{\text{net},y}$, the y-component of the net force exerted by the infinite wire on the loop?

Think about the possible contributions to F_y from the top and bottom wire and the directions of the currents...

$F_{\text{net},y} = 0$.

4)

Another infinite straight wire, aligned with the y-axis is now added at a distance $2L = 70 \text{ cm}$ from segment bc of the loop as shown. A current, I_3 , flows in this wire. The loop now experiences a net force of zero.



What is the direction of I_3 ?

- ☐ along the positive y-direction
- ☐ along the negative y-direction

Right Answer:

2

Feedback:

Your answer is correct! The current I_1 produces a net force on the loop in the positive x-direction. For the current I_3 to produce a net force on the loop that cancels the force from I_1 , it must be directed in the negative y-direction to create a magnetic field in the region of the loop that is directed in the negative z-direction.

Here I thought about how the B field lines from each wire would add up, and under what conditions they would cancel.

4) What is the magnitude of I_3 ?

$$I_1 \left(\frac{1}{L} - \frac{1}{L+W} \right) = I_3 \left(\frac{1}{2L} - \frac{1}{2L+W} \right) \Rightarrow I_3 = I_1 \left(\frac{2L(2L+W)}{L(L+W)} \right) = 2I_1 \frac{2L+W}{L+W}$$

The only forces to consider are the x components, (re problem 3). Set the forces due to each wire on the right and left vertical wire segments so that they are equal and opposite.

$I_3 = 2 \cdot .662 \text{ A} \cdot (2 \cdot .35 \text{ m} + .54 \text{ m}) / (.35 \text{ m} + .54 \text{ m}) = 1.844 \text{ A}$ (in the neg y direction, the problem asked for magnitude)