

①

$$\frac{1}{\sigma} + \frac{1}{i} = \frac{1}{f} \quad \text{where} \quad \sigma = |x_1|$$

$$i = |x_2|$$

$$f = \frac{\sigma \cdot i}{\sigma + i} = \underline{\underline{53.0 \text{ cm}}}$$

$$x_1 = -122 \text{ cm}$$

$$y_1 = 3.89 \text{ cm}$$

$$x_2 = -93.7 \text{ cm}$$

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$$\frac{y_2}{y_1} = -\frac{i}{\sigma} \Rightarrow y_2 = -\frac{i}{\sigma} \cdot y_1 = \underline{\underline{-2.99 \text{ cm}}}$$

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$$\frac{1}{\sigma} + \frac{1}{i} = \frac{1}{f} = \frac{1}{\sigma'} + \frac{1}{i'} = \frac{1}{\sigma'} + \frac{1}{2i}$$

$$\frac{1}{\sigma'} = \frac{1}{\sigma} + \frac{1}{i} - \frac{1}{2i} = \frac{1}{\sigma} + \frac{1}{2i}$$

$$\frac{y_2'}{y_1'} = \left(-\frac{i'}{\sigma'}\right) = (-2i) \cdot \left(\frac{1}{\sigma} + \frac{1}{2i}\right) = -\left(1 + 2\frac{i}{\sigma}\right)$$

$$y_2' = -\left(1 + 2\frac{i}{\sigma}\right) \cdot y_1' = -\left(1 + 2\frac{i}{\sigma}\right) \cdot y_1 = \underline{\underline{-9.87 \text{ cm}}}$$

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$$\frac{1}{\sigma''} + \frac{1}{i''} = \frac{1}{f} \Rightarrow 1 + \frac{\sigma''}{i''} = \frac{\sigma''}{f} \Rightarrow 1 - \frac{y_2''}{y_1''} = \frac{\sigma''}{f}$$

$$\therefore y_2'' = \frac{y_1'}{1 - \frac{\sigma''}{f}} = \underline{\underline{9.25 \text{ cm}}} \quad (y_1 = y_1'')$$

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(b) The ray is NOT related to a ~~para~~ position of focus \Rightarrow cannot go parallel with the ~~an~~ axis!

HW 27-2

①

$$\frac{1}{s} + \frac{1}{s'} = \frac{1}{f} \Rightarrow s = \frac{s' \cdot f}{s' - f} \quad (\text{Mirror equation})$$

$$\text{where } \left. \begin{array}{l} s' = 28.1 \text{ cm} \\ f = +52 \text{ cm} \end{array} \right\} \Rightarrow s = \underline{\underline{-61.13 \text{ cm}}}$$

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Magnification formula:

$$(y_2 = 4.3 \text{ cm})$$

$$\frac{y_2}{y_1} = -\frac{x_2}{x_1}$$

$$\text{Magnification } y_1 = \left(\frac{-x_1}{x_2} \right) \cdot y_2 \Rightarrow y_1 = \underline{\underline{+9.36 \text{ cm}}}$$

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Again:

$$s_{\text{new}} = \frac{s'_{\text{new}} \cdot f}{s'_{\text{new}} - f} = \underline{\underline{-19.25 \text{ cm}}}$$

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$$y_{2,\text{new}} = -\left(\frac{x_{2,\text{new}}}{x_{1,\text{new}}} \right) \cdot y_1 = \underline{\underline{6.82 \text{ cm}}}$$

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The image formed from any real object is always virtual and the magnitude of the image distance can be larger than the focal length of the mirror.