Categorization

Jaimie Murdock

IU Cognitive Science Program 810 Eigenmann Hall jammurdo@indiana.edu

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- Introduction
 - Definitions
 - Models
 - Utility
 - Representations
- 2 Algorithms
 - Introduction
 - k-means Nearest Neighbors
 - QT-clust
 - Information Theoretic Clustering

2 / 29

"Issues related to concepts and categorization are nearly ubiquitous in psychology because of people's natural tendancy to perceive a thing as something." - Goldstone & Kersten 2003

Different names for the same thing...

- Categorization
- Classification (machine learning)
- Clustering (data mining)
- Partitioning (mathematics)



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- Categorization
- Classification (machine learning)
- Clustering (data mining)
- Partitioning (mathematics)
- Chunking (memory)
- Object Recognition (vision)
- Semantics (linguistics)
- Named Entity Recognition (natural language processing)



What is categorization?

- The assignment of concepts to categories
- "Seeing something as X" Wittgenstein, Philosophical Investigations

What is categorization?

- The assignment of concepts to categories
- "Seeing something as X" Wittgenstein, Philosophical Investigations
- What is a concept?
 Whatever psychological state signifies thoughts of X
- What is a category?
 All entities that are appropriately categorized as X

Prototypes vs. Exemplars

Prototype Model

Do concepts determine categories? (Lakoff 1987)



Prototypes vs. Exemplars

Prototype Model

Do concepts determine categories? (Lakoff 1987)

Exemplar Model

Do categories determine concepts? (Nosofsky 1984)

Components of thought

- Components of thought
- Inductive Predictions

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- Components of thought
- Inductive Predictions
- Communication
- Cognitive Economy

Distinguishable stimuli can become treated as the same thing once they are placed in the same category (Sidman 1994)

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Things to remove from a burning house - photos, babies, cats

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Things to remove from a burning house - photos, babies, cats

Equivilence classes may not be uniquely human - sea lions (Schusterman, Reichmuth, Kastak 2000)

How are categories represented?

rules

How are categories represented?

- rules
- exemplars

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- rules
- exemplars
- prototypes

How are categories represented?

- rules
- exemplars
- prototypes
- boundaries

Algorithms

A process to assign concepts to categories

Algorithms

A process to assign concepts to categories

- k-means Nearest Neighbors (MacQueen 1967)
- QT-clust (Heyer et al. 1999)
- Information Theoretic Clustering (Gokcay & Principé 2002)

Components

Two key decisions in clustering: **distance function**

- Euclidean distance
- semantic similarity
- cross-entropy

cluster assignment

- nearest neighbor
- minimal diameter
- maximize cross-cluster distance

k-means Nearest Neighbors

Given n items, place into k groups

Initialize: Pick *k* centroids

Assign: Assign items to nearest centroid

Update: Recalculate centroids

Repeat until convergence of assignment

Data Structures

```
class Concept(object):
 # initialize the wrapper
 def __init__(self, value):
     self.value = value
     self. cluster = None
     self._previous_cluster = None
 # Properties to track cluster assignments
 @property
 def cluster(self):
     return self._cluster
 @cluster.setter
 def cluster(self, value):
     """ Track previous cluster assignment auto-magically.
                                                              11 11 11
     self._previous_cluster = self._cluster
     self. cluster = value
```

The Main Loop

```
def kmeans(k, population, min_delta=0):
 # initialize centroids with random members of the population
 centroids = [random.choice(population).value for i in range(k)]
 # delta is the number of elements that switch cluster
 # since all members will be changing on the first round,
 # we initialize delta to the length of the population
 delta = len(population)
 # test for convergence
 while delta > min delta:
     # assign population to clusters
     assign_clusters(population, centroids)
     # get number of elements which switched cluster
     delta = len([x for x in population
                      if x.cluster != x.previous_cluster])
     # update centroids
     centroids = update_centroids(population; centroids) > < E > E < < C
```

Assignment

Update

```
def get_centroids(population, k):
new centroids = []
 for cluster in range(k):
     # filter out the cluster population
     cluster_values = [x.value for x in population
                           if x.cluster == cluster]
     # generate the new centroid by taking the average of all exemplars
     # comprising the cluster. First, sum the dimensions:
     centroid = map(sum, zip(*cluster_values))
     # then take the average:
     centroid = [dimension / len(cluster values)
                     for dimension in centroid
     # add to our list of new centroids
     new_centroids.append(centroid)
```

The Main Loop

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QT-clust

Given n items, place into groups of ϵ diameter

Build: for each $i \in n$, build candidate cluster C_i

Select: pick largest C_i , remove elements from population

Repeat until all items are assigned.

Data Structures

The Main Loop

```
def qt_clust(thresh, population):
 while population:
     # build candidate clusters
     for x in population:
         x.build_cluster(population, thresh)
     # select the largest candidate cluster
     candidate = max(population, key=lambda x: len(x.cluster))
     # remove elements from the population
     for x in candidate cluster:
         population.remove(x)
     yield candidate
```

Build

```
class Concept(object):
 def build_cluster(self, population, thresh):
     # initialize the cluster
     self.cluster = [self]
     population.remove(self)
     while population:
         # find x, such that cluster diameter is minimized
         x = min(population, key=self._diameter_append)
         new_diameter = self._diameter_append(x)
         # if below quality threshold, append to cluster
         if new diameter < thresh:
             self.cluster.append(x)
             self.diameter = new_diameter
             population.remove(x)
         else:
             # otherwise terminate the loop
             break
```

The Main Loop

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     # remove elements from the population
     for x in candidate cluster:
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     yield candidate
```

Given n items, place into k groups, minimizing the value of the cross-entropy function (CEF)

Initialize: Assign all items to random clusters **Group:** for each $i \in n$, build group G_i of size M = n/k

Reassign: for each $i \in n$, see if switching G_i reduces CEF, permanently switch cluster assignment for $x \in G_i$ which minimizes CEF

Repeat until CEF reaches minima

Data Structures

The Main Loop

```
def info_theory(k, population):
 # assign random clusters
 for x in population:
     x.cluster = random.choice(range(k))
 # create initial group size
 group_size = len(population) / k
 # grow group size exponentially while hill-climbing
 while group_size < len(population):
     # assign groups
     for x in population:
         x.make_group(population, group_size)
     hillclimb(population, group_size, k)
     group_size *= 2
```

Hill Climbing

```
def hillclimb(population, group_size, k):
 orig_CEF = 1.0
                              # get baseline CEF
min_CEF = CEF(population, k) # initial min CEF
 while orig_CEF != min_CEF:
     for x in population:
         for member in x.group:
             # change cluster assignment
             member.cluster = x.cluster
         group_CEF = CEF(population, k)
         if group_CEF < min_CEF:
             # if CEF decreases, new min!
             min_CEF = group_CEF
         else:
             # restore previous cluster assignment
             for member in x.group:
                 member.cluster = x.previous_cluster
```

The Main Loop

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def info_theory(k, population):
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 # create initial group size
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 # grow group size exponentially while hill-climbing
 while group_size < len(population):
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