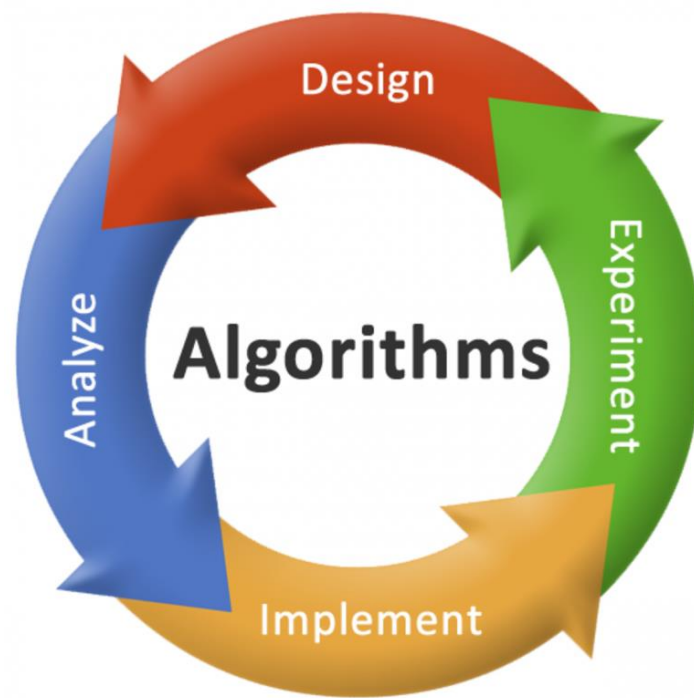


Design and Analysis of Algorithms Practical File



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TABLE OF CONTENTS

S.No	Practical	Page No.
1	Implement Insertion Sort (The program should report the number of comparisons)	3
2	Implement Merge Sort (The program should report the number of comparisons)	8
3	Implement Heap Sort(The program should report the number of comparisons)	12
4	Implement Randomized Quick sort (The program should report the number of comparisons)	19
5	Implement Radix Sort	23
6	Implement Bucket Sort	25
7	Implement Randomized Select	28
8	Implement Breadth-First Search in a graph	30
9	Implement Depth-First Search in a graph	34
10	Write a program to determine the minimum spanning tree of a graph using both Prims and Kruskals algorithm	36
11	Write a program to solve the weighted interval scheduling problem	44
12	Write a program to solve the 0-1 knapsack problem	48

PRACTICAL 1 : Implement Insertion Sort (The program should report the number of comparisons)

```
#include <bits/stdc++.h>

using namespace std;

//function to sort an array and return the number of comparisons
int insertion_sort(int arr[], int n)
{
    int comparison = 0;
    for (int i = 1; i < n; i++)
    {
        int current = arr[i];
        int j = i - 1;
        while (arr[j] > current && j >= 0)
        {
            arr[j + 1] = arr[j];
            j--;
            comparison++;
        }
        if (j >= 0)
        {
            comparison++;
        }
        arr[j + 1] = current;
    }
    return comparison;
}

//function to generate random array and create .csv file
```

```

void generate_random_array(int size, int check)
{
    fstream fout;

    int comp;

    int arr[size];

    for (int i = 0; i < size; i++)
    {
        arr[i] = (rand() % 100);
    }

    int n = sizeof(arr) / sizeof(arr[0]);

    if (check == 0) //average case
    {
        comp = insertion_sort(arr, size);

        fout.open("average_case.csv", ios::out | ios::app);

        fout << size << "," << comp << endl;
    }

    else if (check == 1) //best_case
    {
        sort(arr, arr + n);

        comp = insertion_sort(arr, size);

        fout.open("best_case.csv", ios::out | ios::app);

        fout << size << "," << comp << endl;
    }
}

```

```

else if (check == 2) //worst_case
{
    sort(arr, arr + n, greater<int>());
    comp = insertion_sort(arr, size);
    fout.open("worst_case.csv", ios::out | ios::app);
    fout << size << "," << comp << endl;
}
}

```

```

//average case
void average_case(int start, int end)
{
    int interval = (end - start) / 60;
    int count = 0;
    for (int i = start; i < end && count < 60; i += interval)
    {
        generate_random_array(i, 0);
        count++;
    }
}

```

```

//best_case
void best_case(int start, int end)
{
    int interval = (end - start) / 20;
    int count = 0;
    for (int i = start; i < end && count < 20; i += interval)

```

```
{  
    generate_random_array(i, 1);  
    count++;  
}  
}
```

//worst_case

```
void worst_case(int start, int end)  
{  
    int interval = (end - start) / 20;  
    int count = 0;  
    for (int i = start; i < end && count < 20; i += interval)  
    {  
        generate_random_array(i, 2);  
        count++;  
    }  
}
```

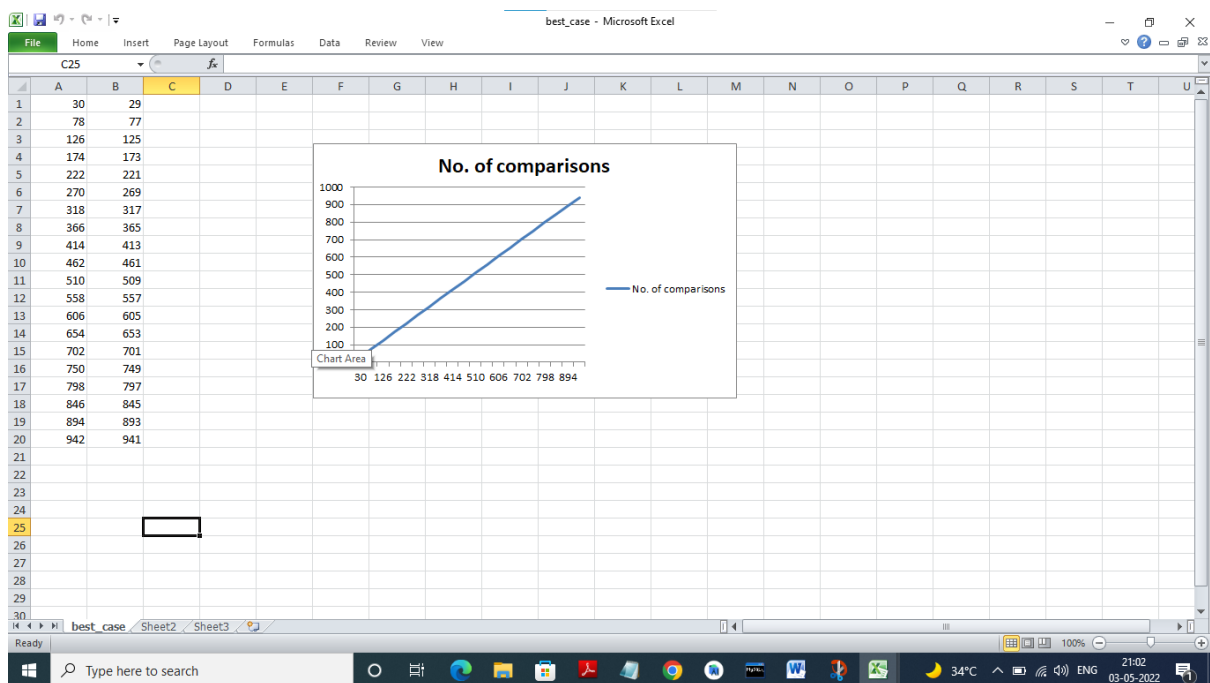
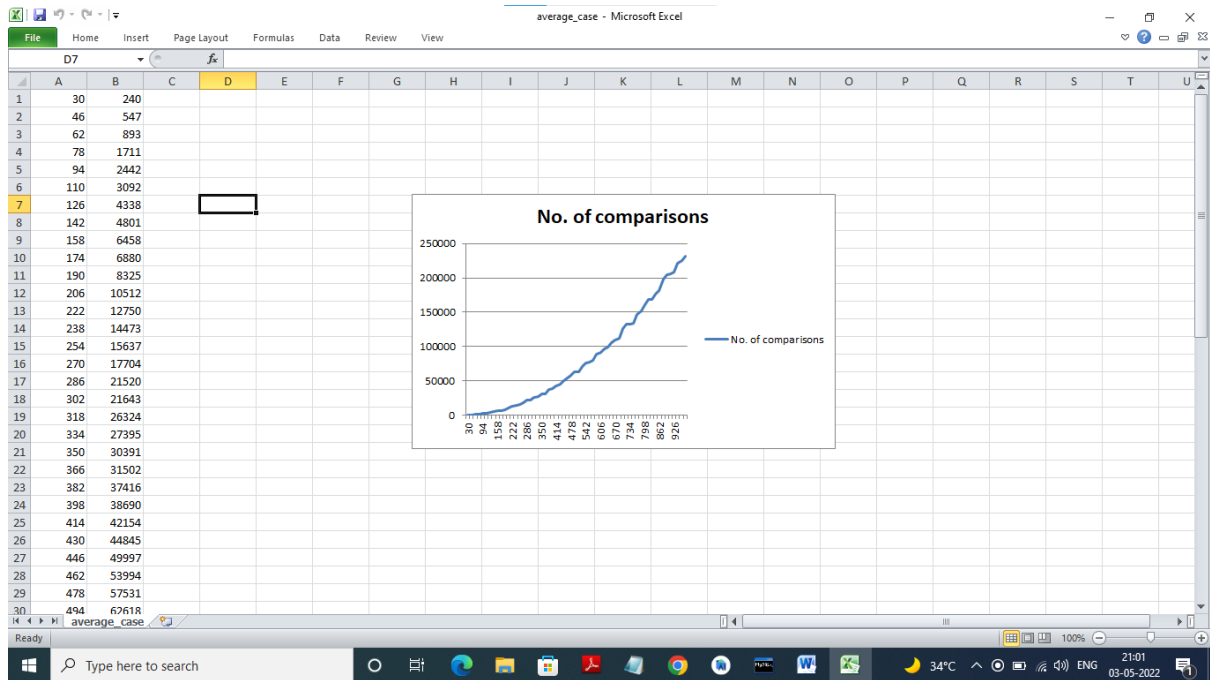
//main function

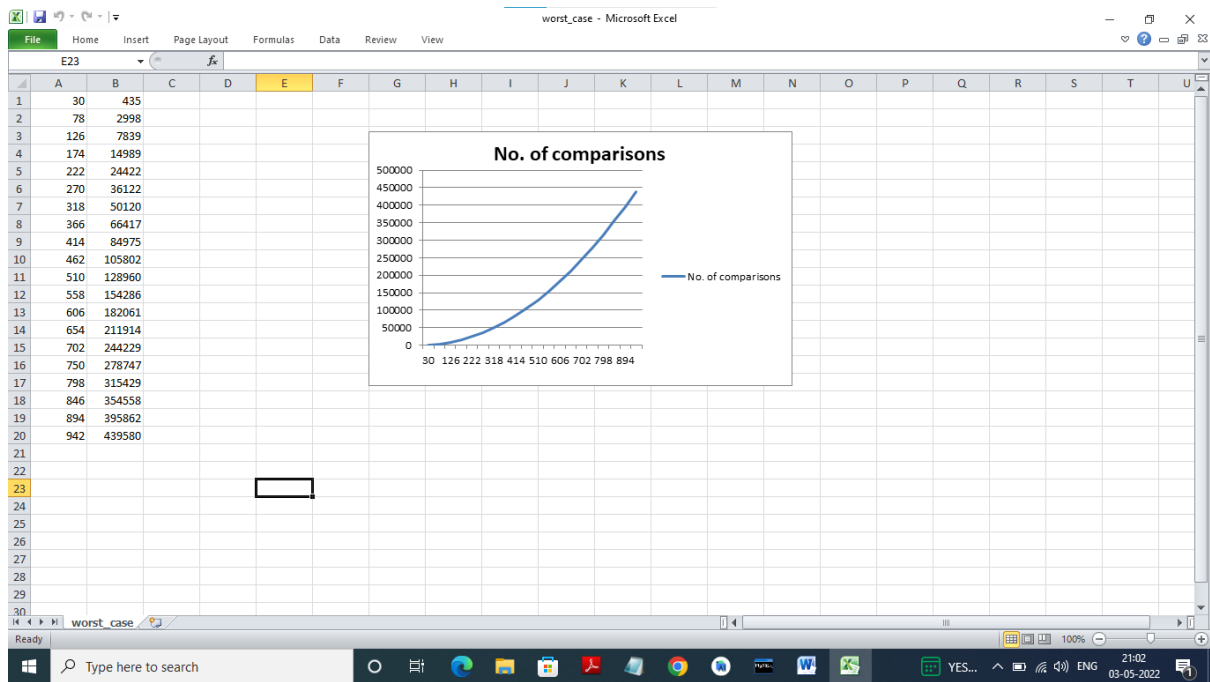
```
int main()  
{  
    int min_value = 30;  
    int max_value = 1000;  
  
    average_case(min_value, max_value);  
    best_case(min_value, max_value);  
    worst_case(min_value, max_value);  
}
```

```
return 0;
```

```
}
```

OUTPUT





PRACTICAL 2: Implement Merge Sort (The program should report the number of comparisons)

```
#include <bits/stdc++.h>
```

```
using namespace std;
```

```
int comp = 0;
```

```
int n = 0;
```

```
void printarray( int size,int comp){
```

```
    ofstream fout;
```

```
    fout.open("merge.csv", ios::out | ios::app);
```

```
    fout << size << ", " << comp << endl;
```

```
}
```

```
void merge(int arr[], int leftFirst, int leftLast, int rightFirst, int rightLast, int size){
```



```

int temparr[size];

int index = leftFirst;

int saveFirst = leftFirst;


while((leftFirst <= leftLast) && ( rightFirst <= rightLast)){//compare and select
smallest from two subarrays


    if(arr[leftFirst] < arr[rightFirst]){

        temparr[index] = arr[leftFirst];

        leftFirst++;

    }

    else

    {

        temparr[index] = arr[rightFirst];

        rightFirst++;

    }

    index++;

    comp++;

}


while(leftFirst <= leftLast){

    temparr[index] = arr[leftFirst];

    leftFirst++;

    index++;

```

```

    }

    while(rightFirst <= rightLast){

        temparr[index] = arr[rightFirst];

        rightFirst++;

        index++;

    }

    for(index = saveFirst; index <= rightLast; index++)

        arr[index] = temparr[index];

}

void mergesort(int a[], int start, int end, int size){

    if(start < end){

        int mid = (start+end)/2;

        int n=mid+1;

        mergesort(a,start, mid,size);

        mergesort(a,n,end,size);

        merge(a, start,mid, n, end, size);

    }

}

void randomNum(int size)

{

```

```

int arr[size];

for (int i = 0; i < size; i++)

{
    arr[i] = (rand() % 100);
}

int n = sizeof(arr) / sizeof(arr[0]);

int start = 0;

int end = n-1;

mergesort(arr, start, end, size);
}

int main(){


int min = 30;

int max = 1000;

int interval = (max - min) / 100;

int count = 0;

for (int i = min; i < max && count < 100; i += interval)

{
    randomNum(i );

    printarray(i,comp);


    count++;

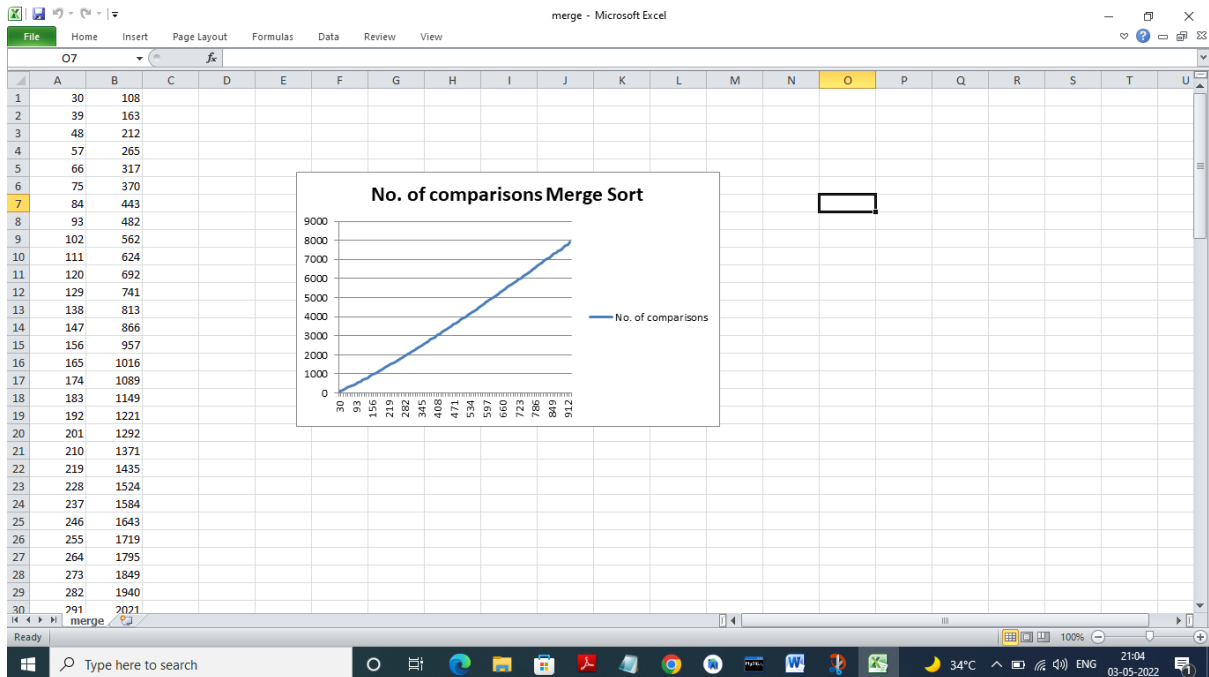
    comp=0;

}

```

}

OUTPUT



PRACTICAL 3 : Implement Heap Sort(The program should report the number of comparisons)

```
#include<iostream>
```

```
#include <algorithm>
```

```
#include<fstream>
```

```
using namespace std;
```

```
//Heapify function
```

```
void heapify(int arr[],int n,int i,int &count)
```

```
{
```

```
    int largest=i;
```

```
    int l=i*2+1;        //left child
```

```
int r=(i*2)+2;          //right child
```

```
if(l<n&&(count+=1)&&(arr[l]>arr[largest])) // If left child is larger than root
```

```
{
```

```
    largest=l;
```

```
}
```

```
if(r<n&&(count+=1)&&(arr[r]>arr[largest])) // If right child is larger than largest so far
```

```
{
```

```
    largest=r;
```

```
}
```

```
if(largest != i ) // If largest is not root
```

```
{
```

```
    swap(arr[i],arr[largest]);
```

```
    heapify(arr,n,largest,count); // Recursively heapify the affected sub-tree
```

```
}
```

```
}
```

```

//heap sort func

int Heap_Sort(int arr[],int n,int &comp)
{
    // For building heap
    for(int i=n/2-1;i>=0;i--)
    {
        heapify(arr,n,i,comp);

    }


    // for deletion from heap
    for(int i=n-1;i>=0;i--)
    {
        swap(arr[i],arr[0]);
        heapify(arr,i,0,comp);

    }


    return comp;
}


// For generating Random array

```

```
void generate_random_array(int arr[], int size)
```

```
{  
    for (int i = 0; i < size; i++)  
    {  
        arr[i] = (rand() % 100);  
    }  
}
```

```
// Average Case
```

```
void heap_avg(int num_cases = 100, int min_size = 30, int max_size = 1000)
```

```
{  
    int interval = (max_size - min_size) / num_cases;  
    int comp = 0;  
    for (int size = min_size, i = 0; i < num_cases; i++, size += interval)  
    {  
        int *Arr = new int[size];  
        generate_random_array(Arr, size);  
  
        fstream fout1;  
  
        Heap_Sort(Arr, size, comp);  
  
        fout1.open("HeapAverage.csv", ios::out | ios::app);
```

```

        fout1 << size << "," << comp << endl;

        comp = 0;
    }
}

//Best Case

void heap_best(int num_cases = 20, int min_size = 30, int max_size = 1000)
{
    int interval = (max_size - min_size) / num_cases;

    int comp = 0;

    for (int size = min_size, i = 0; i < num_cases; i++, size += interval)
    {
        int *Arr = new int[size];

        generate_random_array(Arr, size);

        sort(Arr, Arr + size, greater<int>());

        fstream fout1;

        Heap_Sort(Arr,size,comp);

        fout1.open("HeapBest.csv", ios::out | ios::app);

        fout1 << size << "," << comp << endl;

        comp = 0;
    }
}

```



```
}
```

```
//Worst Case
```

```
void heap_Worst(int num_cases = 20, int min_size = 30, int max_size = 1000)
```

```
{
```

```
    int interval = (max_size - min_size) / num_cases;
```

```
    int comp = 0;
```

```
    for (int size = min_size, i = 0; i < num_cases; i++, size += interval)
```

```
    {
```

```
        int *Arr = new int[size];
```

```
        generate_random_array(Arr, size);
```

```
        sort(Arr, Arr + size);
```

```
        fstream fout1;
```

```
        Heap_Sort(Arr,size,comp);
```

```
        fout1.open("HeapWorst.csv", ios::out | ios::app);
```

```
        fout1 << size << "," << comp << endl;
```

```
        comp = 0;
```

```
    }
```

```
}
```

```
int main()
```

```
{
```

```

heap_avg();

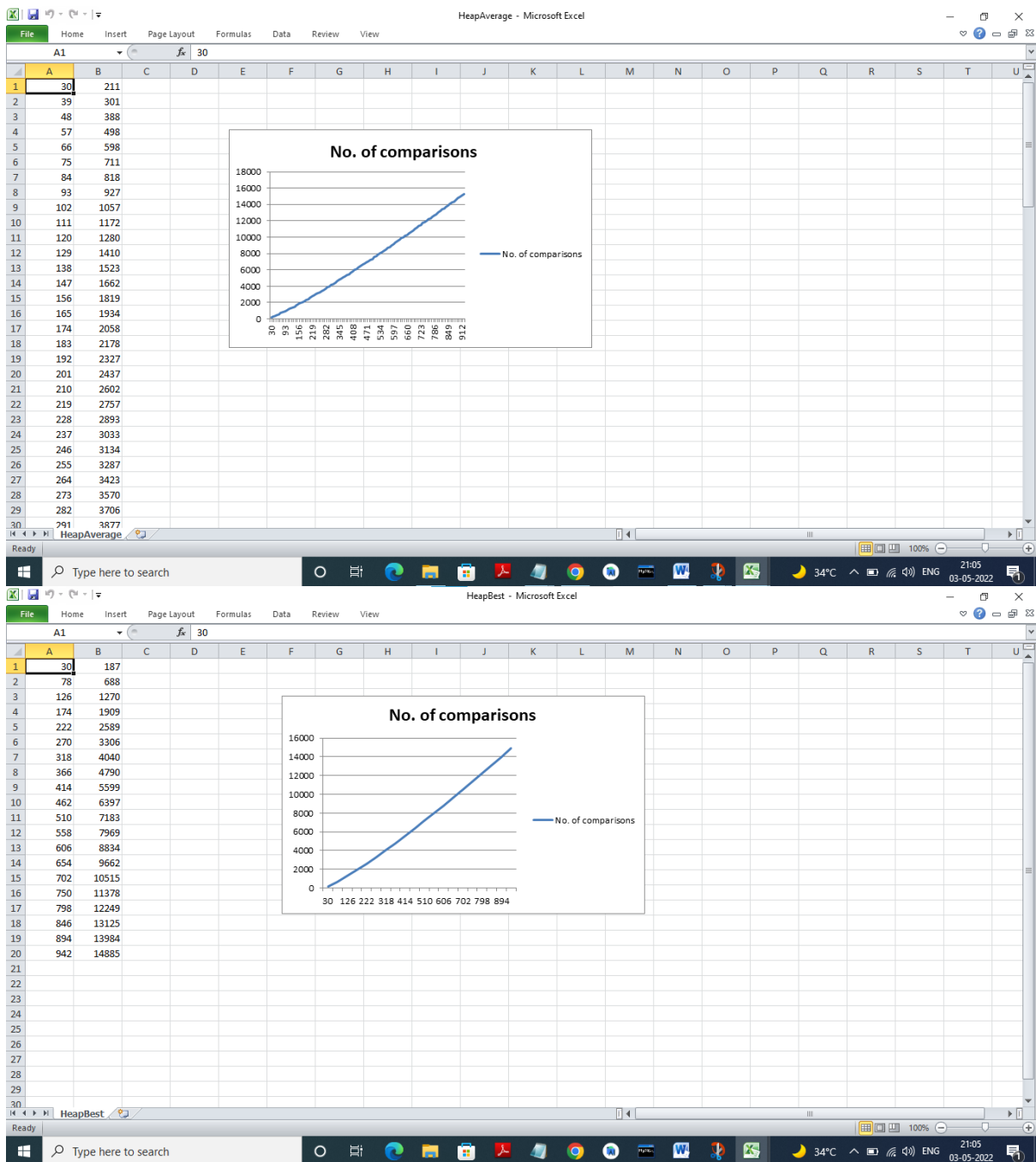
heap_best();

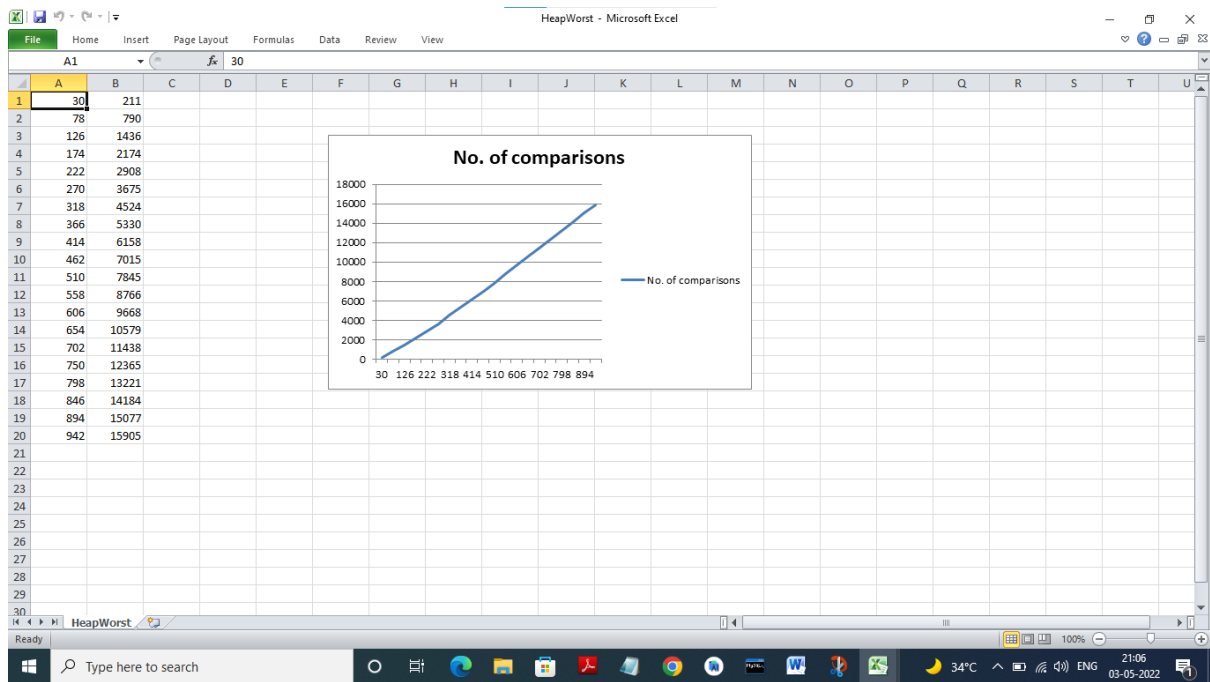
heap_Worst();

return 0;
}

```

OUTPUT





PRACTICAL 4 : Implement Randomized Quick sort (The program should report the number of comparisons)

```
#include <iostream>
```

```
#include <fstream>
```

```
using namespace std;
```

```
void swap(int *a, int *b)
```

```
{
```

```
    int t = *a;
```

```
    *a = *b;
```

```
    *b = t;
```

```
}
```

```
int partition(int arr[], int low, int high, int &numOfcomp)
```

```
{
```

```
    int pivot = arr[high];
```

```

int i = (low - 1);

for (int j = low; j <= high - 1; j++)
{
    if (numOfcomp++, arr[j] < pivot)
    {
        i++;

        swap(&arr[i], &arr[j]);
    }
}

swap(&arr[i + 1], &arr[high]);

return (i + 1);
}

int random_partition(int arr[], int low, int high, int &numOfcomp)
{
    int random_index = (rand() % (high + 1));

    if (arr[random_index] != arr[high])
        swap(&arr[random_index], &arr[high]);

    return partition(arr, low, high, numOfcomp);
}

void random_quickSort(int arr[], int low, int high, int &numOfcomp)

```

```

{
    if (low < high)
    {
        int pi = partition(arr, low, high, numOfcomp);
        random_quickSort(arr, low, pi - 1, numOfcomp);
        random_quickSort(arr, pi + 1, high, numOfcomp);
    }
}

```

```

void generate_random_array(int arr[], int size)

```

```

{
    for (int i = 0; i < size; i++)
    {
        arr[i] = (rand() % 1000);
    }
}

```

```

void average_case(int cases, int min, int max)

```

```

{
    ofstream average_case_file("average_quick_Random.csv");

    int interval = (((max - min) / cases) / 10.0) * 10;

    int count = 0;

    for (int i = min; count < cases; i += interval, count++)
    {

```

```

int *random_array = new int[i];

generate_random_array(random_array, i);

int numOfcomp = 0;

random_quickSort(random_array, 0, i - 1, numOfcomp);

average_case_file << i << "," << numOfcomp << "\n";

delete[] random_array;

}

average_case_file.close();

}

int main()

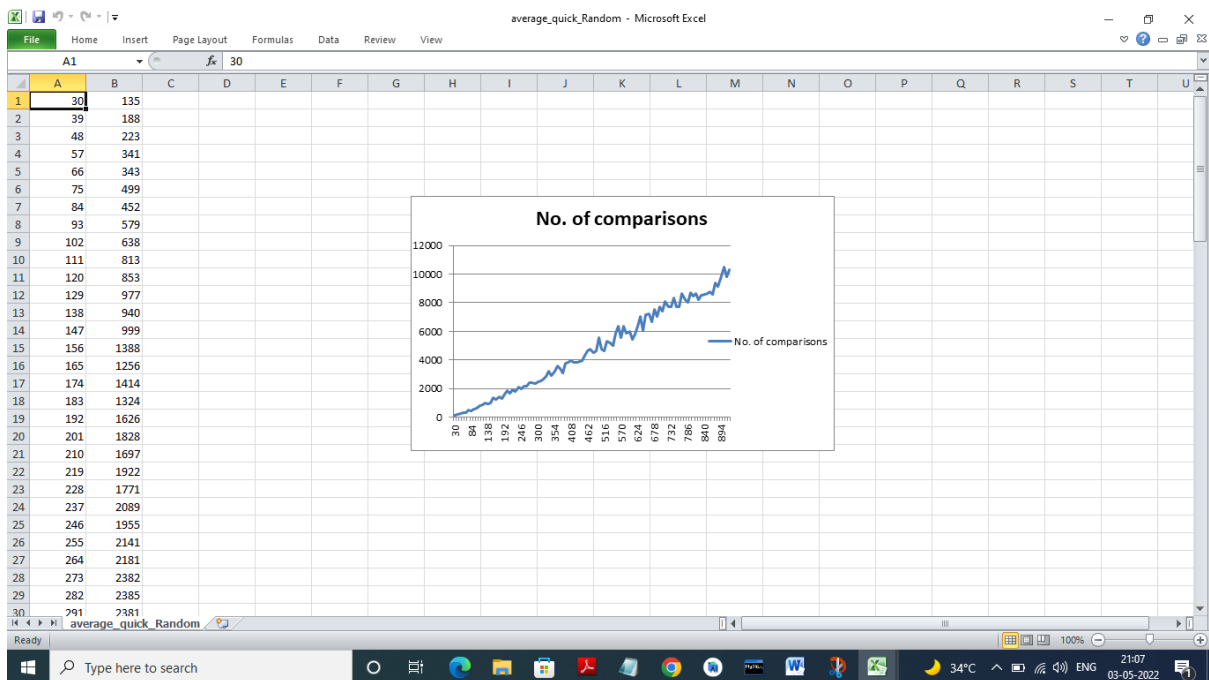
{

    average_case(100, 30, 1000);

}

```

OUTPUT



PRACTICAL 5 : Implement Radix Sort

```
#include <iostream>

using namespace std;

int getMax(int arr[], int n)
{
    int mx = arr[0];
    for (int i = 1; i < n; i++)
        if (arr[i] > mx)
            mx = arr[i];
    return mx;
}

// A function to do counting sort of arr[] according to
// the digit represented by exp.
void countSort(int arr[], int n, int exp)
{
    int output[n];
    int i, count[10] = { 0 };

    // Store count of occurrences in count[]
    for (i = 0; i < n; i++)
        count[(arr[i] / exp) % 10]++;

    // Change count[i] so that count[i] now contains actual
    // position of this digit in output[]
```

```
for (i = 1; i < 10; i++)  
    count[i] += count[i - 1];
```

```
// Build the output array
```

```
for (i = n - 1; i >= 0; i--) {  
    output[count[(arr[i] / exp) % 10] - 1] = arr[i];  
    count[(arr[i] / exp) % 10]--;  
}
```

```
for (i = 0; i < n; i++)  
    arr[i] = output[i];  
}
```

```
void radixsort(int arr[], int n)
```

```
{  
    int m = getMax(arr, n);  
  
    for (int exp = 1; m / exp > 0; exp *= 10)  
        countSort(arr, n, exp);  
}
```

```
void print(int arr[], int n)
```

```
{  
    for (int i = 0; i < n; i++)  
        cout << arr[i] << " ";  
}
```



```

}

int main()
{
    int arr[] = { 76, 34, 11, 88, 90, 3, 1 };
    int n = sizeof(arr) / sizeof(arr[0]);

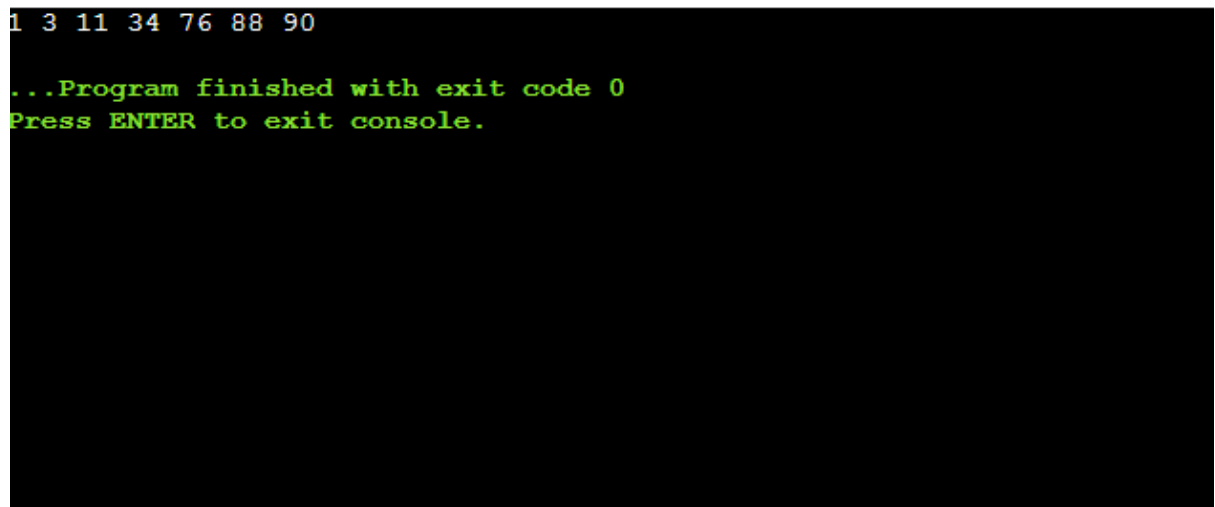
    radixsort(arr, n);

    print(arr, n);

    return 0;
}

```

OUTPUT



```

1 3 11 34 76 88 90
...Program finished with exit code 0
Press ENTER to exit console.

```

PRACTICAL 6 : Implement Bucket Sort

```

#include <iostream>

using namespace std;

int getMax(int a[], int n) // function to get maximum element from the given array
{
    int max = a[0];

```

```

for (int i = 1; i < n; i++)

    if (a[i] > max)

        max = a[i];

return max;
}

void bucket(int a[], int n) // function to implement bucket sort
{
    int max = getMax(a, n); //max is the maximum element of array

    int bucket[max], i;

    for (int i = 0; i <= max; i++)

    {

        bucket[i] = 0;

    }

    for (int i = 0; i < n; i++)

    {

        bucket[a[i]]++;

    }

    for (int i = 0, j = 0; i <= max; i++)

    {

        while (bucket[i] > 0)

        {

            a[j++] = i;

            bucket[i]--;

        }

    }
}

```

```

}

void printArr(int a[], int n) // function to print array elements
{
    for (int i = 0; i < n; ++i)
        cout<<a[i]<<" ";
}

int main()
{
    int a[] = {35, 56, 11, 9, 22, 1};

    int n = sizeof(a) / sizeof(a[0]); // n is the size of array

    cout<<"Before sorting array elements are - ";

    printArr(a, n);

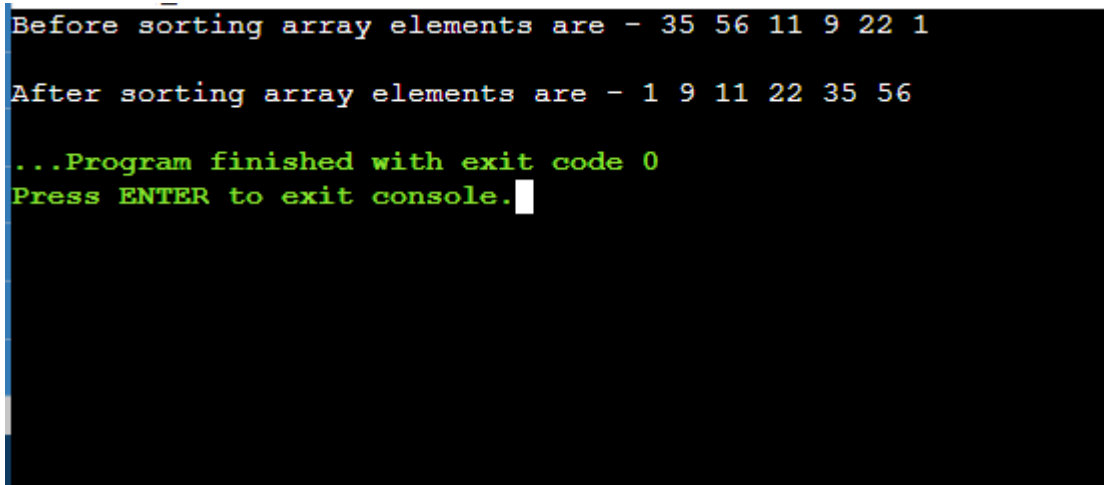
    bucket(a, n);

    cout<<"\n\nAfter sorting array elements are - ";

    printArr(a, n);
}

```

OUTPUT



```

Before sorting array elements are - 35 56 11 9 22 1

After sorting array elements are - 1 9 11 22 35 56

...Program finished with exit code 0
Press ENTER to exit console.

```

PRACTICAL 7 : Implement Randomized Select

```
#include <iostream>

using namespace std;

int random_partition(int *arr, int start, int end)
{
    int pivotIdx = start + rand() % (end - start + 1);

    int pivot = arr[pivotIdx];

    swap(arr[pivotIdx], arr[end]);

    pivotIdx = end;

    int i = start - 1;

    for (int j = start; j <= end - 1; j++)
    {
        if (arr[j] <= pivot)
        {
            i = i + 1;

            swap(arr[i], arr[j]);
        }
    }

    swap(arr[i + 1], arr[pivotIdx]);

    return i + 1;
}

int random_selection(int *arr, int start, int end, int k)
```

```

{
    int i = 0;

    if (start == end)
        return arr[start];

    if (k == 0)
        return -1;

    if (start < end)
    {
        int mid = random_partition(arr, start, end);
        i = mid - start + 1;

        if (i == k)
            return arr[mid];

        else if (k < i)
            return random_selection(arr, start, mid - 1, k);

        else
            return random_selection(arr, mid + 1, end, k - i);
    }
}

```

```

int main()
{
    int A[] = {9, 5, 7, 1, 10, 2, 3};

    int arr = random_selection(A, 0, 6, 5);
}

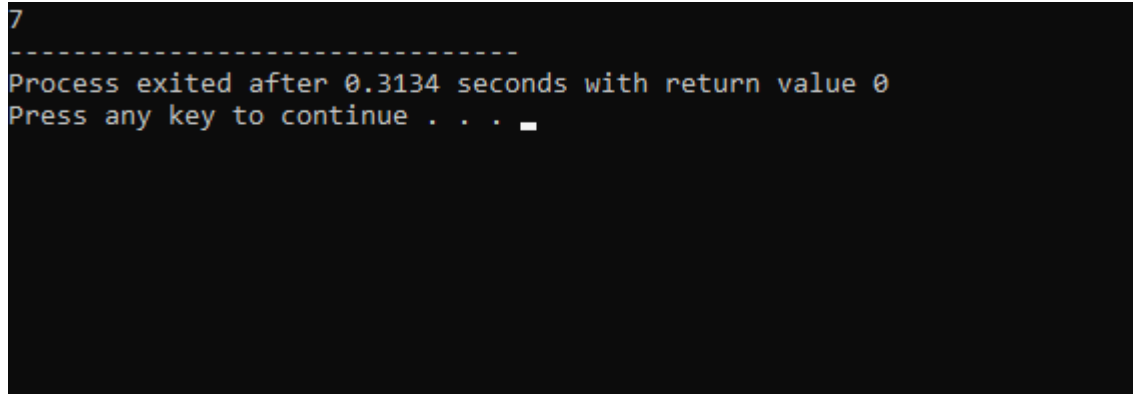
```

```
    cout << arr;

    return 0;

}
```

OUTPUT

A screenshot of a terminal window with a black background and white text. The text shows the number '7' on the first line, followed by a dashed line. The next line says 'Process exited after 0.3134 seconds with return value 0'. The final line says 'Press any key to continue . . . _' with a cursor at the end.

```
7
-----
Process exited after 0.3134 seconds with return value 0
Press any key to continue . . . _
```

PRACTICAL 8 : Implement Breadth-First Search in a graph

```
// Breadth First Search

#include<iostream>

#include <list>

using namespace std;

// This class represents a directed graph using
// adjacency list representation

class Graph

{

    int V;  // No. of vertices

    // Pointer to an array containing adjacency

    // lists

    list<int> *adj;
```

public:

Graph(int V); // Constructor

// function to add an edge to graph

void addEdge(int v, int w);

// prints BFS traversal from a given source s

void BFS(int s);

};

Graph::Graph(int V)

{

 this->V = V;

 adj = new list<int>[V];

}

void Graph::addEdge(int v, int w)

{

 adj[v].push_back(w); // Add w to v's list.

}

void Graph::BFS(int s)

{

 // Mark all the vertices as not visited

 bool *visited = new bool[V];

```

for(int i = 0; i < V; i++)

    visited[i] = false;


// Create a queue for BFS

list<int> queue;


// Mark the current node as visited and enqueue it
visited[s] = true;

queue.push_back(s);


// 'i' will be used to get all adjacent
// vertices of a vertex

list<int>::iterator i;


while(!queue.empty())

{

    // Dequeue a vertex from queue and print it

    s = queue.front();

    cout << s << " ";

    queue.pop_front();


    // Get all adjacent vertices of the dequeued
    // vertex s. If a adjacent has not been visited,
    // then mark it visited and enqueue it

    for (i = adj[s].begin(); i != adj[s].end(); ++i)

```



```

    {
        if (!visited[*i])
        {
            visited[*i] = true;
            queue.push_back(*i);
        }
    }
}
}
}

```

// Driver code

```

int main()
{
    // Create a graph given in the above diagram
    Graph g(4);

    g.addEdge(0, 1);
    g.addEdge(0, 2);
    g.addEdge(1, 2);
    g.addEdge(2, 0);
    g.addEdge(2, 3);
    g.addEdge(3, 3);

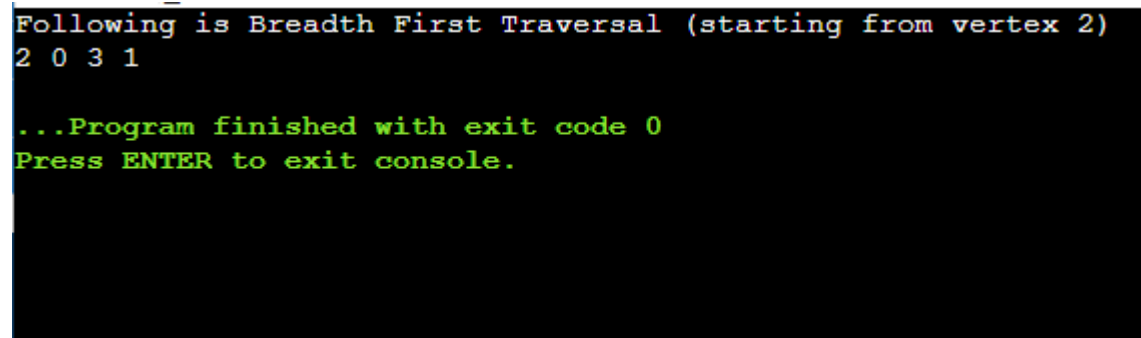
    cout << "Following is Breadth First Traversal "
         << "(starting from vertex 2) \n";

    g.BFS(2);
}

```

```
    return 0;
}
```

OUTPUT



```
Following is Breadth First Traversal (starting from vertex 2)
2 0 3 1

...Program finished with exit code 0
Press ENTER to exit console.
```

PRACTICAL 9 : Implement Depth-First Search in a graph

```
// Depth First Search
```

```
#include <bits/stdc++.h>
```

```
using namespace std;
```

```
// Graph class represents a directed graph
```

```
// using adjacency list representation
```

```
class Graph {
```

```
public:
```

```
    map<int, bool> visited;
```

```
    map<int, list<int> > adj;
```

```
// function to add an edge to graph
```

```
void addEdge(int v, int w);
```

```
// DFS traversal of the vertices
```

```

// reachable from v

void DFS(int v);

};

void Graph::addEdge(int v, int w)

{

    adj[v].push_back(w); // Add w to v's list.

}

void Graph::DFS(int v)

{

    // Mark the current node as visited and

    // print it

    visited[v] = true;

    cout << v << " ";

    // Recur for all the vertices adjacent

    // to this vertex

    list<int>::iterator i;

    for (i = adj[v].begin(); i != adj[v].end(); ++i)

        if (!visited[*i])

            DFS(*i);

}

// Driver code

```

```

int main()
{
    // Create a graph given in the above diagram

    Graph g;

    g.addEdge(0, 1);
    g.addEdge(0, 2);
    g.addEdge(1, 2);
    g.addEdge(2, 0);
    g.addEdge(2, 3);
    g.addEdge(3, 3);

    cout << "Following is Depth First Traversal"

        " (starting from vertex 2) \n";

    g.DFS(2);

    return 0;
}

```

OUTPUT

```

Following is Depth First Traversal (starting from vertex 2)
2 0 1 3

...Program finished with exit code 0
Press ENTER to exit console.

```

PRACTICAL 10 : Write a program to determine the minimum spanning tree of a graph using both Prim's and Kruskal's algorithm

PRIMS ALGORITHM

```
#include <bits/stdc++.h>

using namespace std;

// Number of vertices in the graph

#define V 5

// A utility function to find the vertex with minimum key value, from the set of vertices not
yet included in MST

int minKey(int key[], bool mstSet[])

{

    // Initialize min value

    int min = INT_MAX, min_index;

    for (int v = 0; v < V; v++)

        if (mstSet[v] == false && key[v] < min)

            min = key[v], min_index = v;

    return min_index;

}

// A utility function to print the constructed MST stored in parent[]

void printMST(int parent[], int graph[V][V])

{

    cout<<"Edge \tWeight\n";

    for (int i = 1; i < V; i++)

        cout<<parent[i]<<" - "<<i<<" \t"<<graph[i][parent[i]]<<" \n";

}
```

```
}
```

```
// Function to construct and print MST for a graph represented using adjacency matrix representation
```

```
void primMST(int graph[V][V])
```

```
{
```

```
    int parent[V]; // Array to store constructed MST
```

```
    int key[V]; // Key values used to pick minimum weight edge in cut
```

```
    bool mstSet[V]; // To represent set of vertices included in MST
```

```
    // Initialize all keys as INFINITE
```

```
    for (int i = 0; i < V; i++)
```

```
        key[i] = INT_MAX, mstSet[i] = false;
```

```
    // Always include 1st vertex in MST. Make key 0 so that this vertex is picked as first vertex.
```

```
    key[0] = 0;
```

```
    parent[0] = -1; // First node is always root of MST
```

```
    // The MST will have V vertices
```

```
    for (int count = 0; count < V - 1; count++)
```

```
{
```

```
    // Pick the minimum key vertex from the set of vertices not yet included in MST
```

```
    int u = minKey(key, mstSet);
```

```
    mstSet[u] = true; // Add the picked vertex to the MST Set
```

```

// Update key value and parent index of the adjacent vertices of the picked vertex.

// Consider only those vertices which are not yet included in MST

for (int v = 0; v < V; v++)

    // graph[u][v] is non zero only for adjacent vertices of m
    // mstSet[v] is false for vertices not yet included in MST

    // Update the key only if graph[u][v] is smaller than key[v]

    if (graph[u][v] && mstSet[v] == false && graph[u][v] < key[v])

        parent[v] = u, key[v] = graph[u][v];
}

// print the constructed MST
printMST(parent, graph);
}

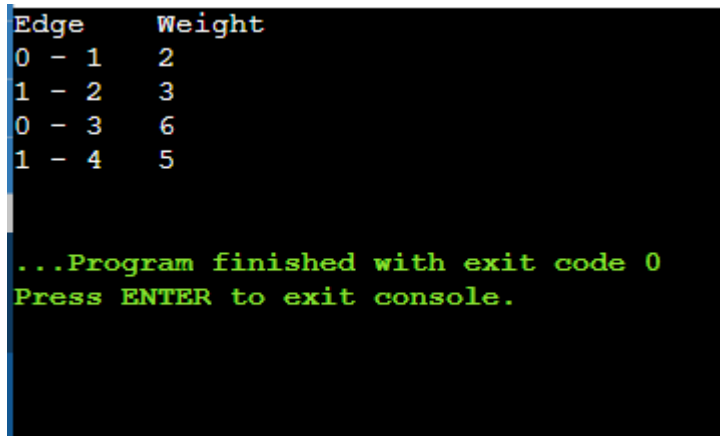
// Driver code
int main()
{
    int graph[V][V] = { { 0, 2, 0, 6, 0 },
                        { 2, 0, 3, 8, 5 },
                        { 0, 3, 0, 0, 7 },
                        { 6, 8, 0, 0, 9 },
                        { 0, 5, 7, 9, 0 } };

    // Print the solution
    primMST(graph);
}

```

```
    return 0;
}
```

OUTPUT



```
Edge    Weight
0 - 1    2
1 - 2    3
0 - 3    6
1 - 4    5

...Program finished with exit code 0
Press ENTER to exit console.
```

KRUSKALS ALGORITHM

```
#include <bits/stdc++.h>
```

```
using namespace std;
```

```
class DSU {
```

```
    int* parent;
```

```
    int* rank;
```

```
public:
```

```
    DSU(int n)
```

```
{
```

```
    parent = new int[n];
```

```
    rank = new int[n];
```



```

for (int i = 0; i < n; i++) {

    parent[i] = -1;

    rank[i] = 1;

}

}

// Find function

int find(int i)

{

    if (parent[i] == -1)

        return i;

    return parent[i] = find(parent[i]);

}

// union function

void unite(int x, int y)

{

    int s1 = find(x);

    int s2 = find(y);

    if (s1 != s2) {

        if (rank[s1] < rank[s2]) {

            parent[s1] = s2;

            rank[s2] += rank[s1];

        }

    }

}

```

```

        else {

            parent[s2] = s1;

            rank[s1] += rank[s2];

        }

    }

}

};

```

```

class Graph {

    vector<vector<int> > edgelist;

    int V;

public:

    Graph(int V) { this->V = V; }

    void addEdge(int x, int y, int w)

    {

        edgelist.push_back({ w, x, y });

    }

    void kruskals_mst()

    {

        // 1. Sort all edges

        sort(edgelist.begin(), edgelist.end());
    }
}

```

```

// Initialize the DSU

DSU s(V);

int ans = 0;

cout << "Following are the edges in the "

    "constructed MST"

    << endl;

for (auto edge : edgelist) {

    int w = edge[0];

    int x = edge[1];

    int y = edge[2];

    // take that edge in MST if it does form a cycle

    if (s.find(x) != s.find(y)) {

        s.unite(x, y);

        ans += w;

        cout << x << " -- " << y << " == " << w

            << endl;

    }

}

cout << "Minimum Cost Spanning Tree: " << ans;

}

};

int main()

{

    Graph g(4);

```

```

g.addEdge(0, 1, 10);

g.addEdge(1, 3, 15);

g.addEdge(2, 3, 4);

g.addEdge(2, 0, 6);

g.addEdge(0, 3, 5);

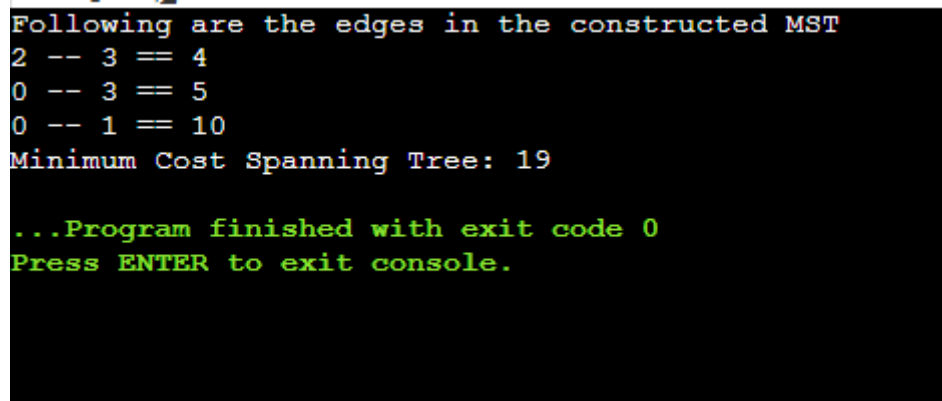

g.kruskals_mst();

return 0;

}

```

OUTPUT



```

Following are the edges in the constructed MST
2 -- 3 == 4
0 -- 3 == 5
0 -- 1 == 10
Minimum Cost Spanning Tree: 19

...Program finished with exit code 0
Press ENTER to exit console.

```

PRACTICAL 11 : Write a program to solve the weighted interval scheduling problem

```

#include <iostream>

#include <vector>

#include <algorithm>

using namespace std;


// Data structure to store a Job

struct Job

```

```

{
    int start, finish, weight;
};

void findMaxWeightJobs(vector<Job> jobs)
{
    // sort the jobs according to increasing order of their start time
    // sort(jobs.begin(), jobs.end(),
    //     [](Job &x, Job &y)
    //     {
    //         return x.start < y.start;
    //     });

    // output:The jobs involved in the maximum weight are (1, 4, 30) (4, 5, 60) (5, 9, 50)

    // sort the jobs according to increasing order of their finish time
    sort(jobs.begin(), jobs.end(),
        [](Job &x, Job &y)
        {
            return x.finish < y.finish;
        });

    // output:The jobs involved in the maximum weight are (1, 4, 30) (4, 5, 60) (5, 9, 50)

    // get the number of jobs
    int n = jobs.size();

```

```

// base case

if (n == 0)

{

    return;

}


// `tasks[i]` stores the index of non-conflicting jobs involved in the
// maximum weight, which ends with the i'th job

vector<int> tasks[n];


// `maxweight[i]` stores the total weight of jobs in `tasks[i]`

int maxWeight[n];


// consider every job

for (int i = 0; i < n; i++)

{

    // initialize current weight to 0

    maxWeight[i] = 0;


    // consider each `j` less than `i`

    for (int j = 0; j < i; j++)

    {

        // update i'th job if the j'th job is non-conflicting and leading to the
        // maximum weight

        if (jobs[j].finish <= jobs[i].start && maxWeight[i] < maxWeight[j])

```

```

    {
        tasks[i] = tasks[j];
        maxWeight[i] = maxWeight[j];
    }
}

// end current task with i'th job
tasks[i].push_back(i);
maxWeight[i] += jobs[i].weight;
}

// find an index with the maximum weight
int index = 0;
for (int i = 1; i < n; i++)
{
    if (maxWeight[i] > maxWeight[index])
    {
        index = i;
    }
}

cout << "The jobs involved in the maximum weight are ";
for (int i : tasks[index])
{
    cout << "(" << jobs[i].start << ", " << jobs[i].finish << ", "

```

```

        << jobs[i].weight << ") ";

    }

}

```

```
// Main Function(Driver Code)
```

```

int main()

{

    vector<Job> jobs{

        {0, 6, 60},

        {5, 9, 50},

        {1, 4, 30},

        {4, 5, 60},

        {5, 7, 30},

        {3, 5, 10},

        {7, 8, 10}};

```

```

    findMaxWeightJobs(jobs);

```

```

    return 0;

```

```

}

```

OUTPUT

```

The jobs involved in the maximum weight are (1, 4, 30) (4, 5, 60) (5, 9, 50)

...Program finished with exit code 0
Press ENTER to exit console.

```

PRACTICAL 12 : Write a program to solve the 0-1 knapsack problem

DYNAMIC PROGRAMMING

// Program to solve the 0-1 knapsack problem using dynamic programming.

```
#include <iostream>
```

```
using namespace std;
```

```
int max(int x, int y) {
```

```
    return (x > y) ? x : y;
```

```
}
```

```
int knapSack(int W, int w[], int v[], int n) {
```

```
    int i, wt;
```

```
    int K[n + 1][W + 1];
```

```
    for (i = 0; i <= n; i++) {
```

```
        for (wt = 0; wt <= W; wt++) {
```

```
            if (i == 0 || wt == 0)
```

```
                K[i][wt] = 0;
```

```
            else if (w[i - 1] <= wt)
```

```
                K[i][wt] = max(v[i - 1] + K[i - 1][wt - w[i - 1]], K[i - 1][wt]);
```

```
            else
```

```
                K[i][wt] = K[i - 1][wt];
```

```
        }
```

```
    }
```

```
    return K[n][W];
```

```
}
```

```

int main() {

    int n, W;

    cout << "Enter the number of items in a Knapsack : ";

    cin >> n;

    cout<<endl;

    int v[n], w[n];

    for (int i = 1; i <= n; i++) {

        cout << "Enter profit value and weight for item " << i << ": ";

        cin >> v[i];

        cin >> w[i];

    }

    cout << "\nEnter the capacity of knapsack : ";

    cin >> W;

    cout << "\nDynamic Problem choice solution : "<< knapSack(W, w, v, n);

    return 0;

}

```

OUTPUT

```

Enter the number of items in a Knapsack : 4

Enter profit value and weight for item 1: 3 2
Enter profit value and weight for item 2: 4 3
Enter profit value and weight for item 3: 5 4
Enter profit value and weight for item 4: 6 5

Enter the capacity of knapsack : 5

Dynamic Problem choice solution : 7

...Program finished with exit code 0
Press ENTER to exit console.

```

GREEDY

```
#include <iostream>

using namespace std;

void knapsack(int n, double weight[], double profit[], double capacity)
{
    double total_Profit = 0;
    int c = capacity;

    for (int i = 0; i < n; i++)
    {
        if (weight[i] > c)
            break;
        else
        {
            total_Profit += profit[i];
            c -= weight[i];
        }
    }

    cout << "\nMaximum profit : " << total_Profit;
}

// Main function(Driver Code)

int main()
```

```
{  
    double weight[20], profit[20], capacity;  
  
    cout << "\nEnter the no. of objects : ";  
  
    int num;  
  
    cin >> num;  
  
    cout << "\nEnter the weights and profits of each object (With space) : \n";  
  
    for (int i = 0; i < num; i++)  
    {  
        cin >> weight[i] >> profit[i];  
    }  
  
    cout << "\nEnter the capacity of knapsack : ";  
  
    cin >> capacity;  
  
    knapsack(num, weight, profit, capacity);  
  
    return 0;  
}
```

OUTPUT

```
Enter the no. of objects : 3  
  
Enter the weights and profits of each object (With space) :  
10 60  
20 100  
30 120  
  
Enter the capacity of knapsack : 50  
  
Maximum profit : 160  
  
...Program finished with exit code 0  
Press ENTER to exit console.
```