

## Day 1 - Code Java Smart

# Check for Prime Number

We know that any **integer number** can be written in the form of  **$6k+i$** , where '**k**' is a **non-negative integer** (like 0, 1, 2, 3, ...) and '**i**' is a number between **0 and 5** (so i can be 0, 1, 2, 3, 4, or 5). If we look closely, we'll notice that when i is 0, 2, 3, or 4, the numbers  **$6k$ ,  $6k+2$ ,  $6k+3$ , and  $6k+4$**  are all divisible by either 2 or 3. But prime numbers greater than 3 can't be divisible by 2 or 3. Therefore, the only forms left that a prime number can have are  **$6k+1$  or  $6k+5$**  (since these forms are not divisible by 2 or 3).

Instead of checking every number up to the  $\sqrt{n}$  to see if it divides n, we only check numbers of the form  $6k+1$  and  $6k+5$ . This optimized approach for calculating  $\sqrt{n}$  reduces the number of operations and achieves a threefold performance improvement compared to a standard method.

## Program

```
static boolean isPrime (int n) {  
  
    // Check if n is 1 or 0  
    if (n <= 1)  
        return false;  
  
    // Check if n is 2 or 3  
    if (n == 2 || n == 3)  
        return true;
```

```
// Check whether n is divisible by 2 or 3
if (n % 2 == 0 || n % 3 == 0)
    return false;

// Check from 5 to square root of n
// Iterate i by (i+6)
for (int i = 5; i <= Math.sqrt(n); i = i + 6)
    if (n % i == 0 || n % (i + 2) == 0)
        return false;

return true;
}
```