

CTA PRACTICAL 10 20MCED08

Practical 6

Implement 0-1 knapsack problem using dynamic programming.

Introduction

Given weights and values of n items, put these items in a knapsack of capacity W to get the maximum total value in the knapsack.

In other words, given two integer arrays val[0..n-1] and wt[0..n-1] which represent values and weights associated with n items respectively.

Also given an integer W which represents knapsack capacity, find out the maximum value subset of val[] such that sum of the weights of this subset is smaller than or equal to W.

Knapsack 0-1 Algorithm Finding the Items

| <u>Items:</u> | Knapsack: |
|---------------|-----------|
| 1: (2,3) | Item 2 |
| 2: (3,4) | |
| 3: (4.5) | <u> </u> |
| 4: (5,6) | |

| i / w | 0 | 1 | 2 | 3 | 4 | 5 |
|-------|-----|---|------------|---|---|---|
| 0 | 0 🔻 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 6 | $\sqrt{3}$ | 3 | 3 | 3 |
| 2 | 0 | 0 | 3 | 4 | 4 | 7 |
| 3 | 0 | 0 | 3 | 4 | 5 | 7 |
| 4 | 0 | 0 | 3 | 4 | 5 | 7 |

$$1 = 1$$

$$k = 2$$

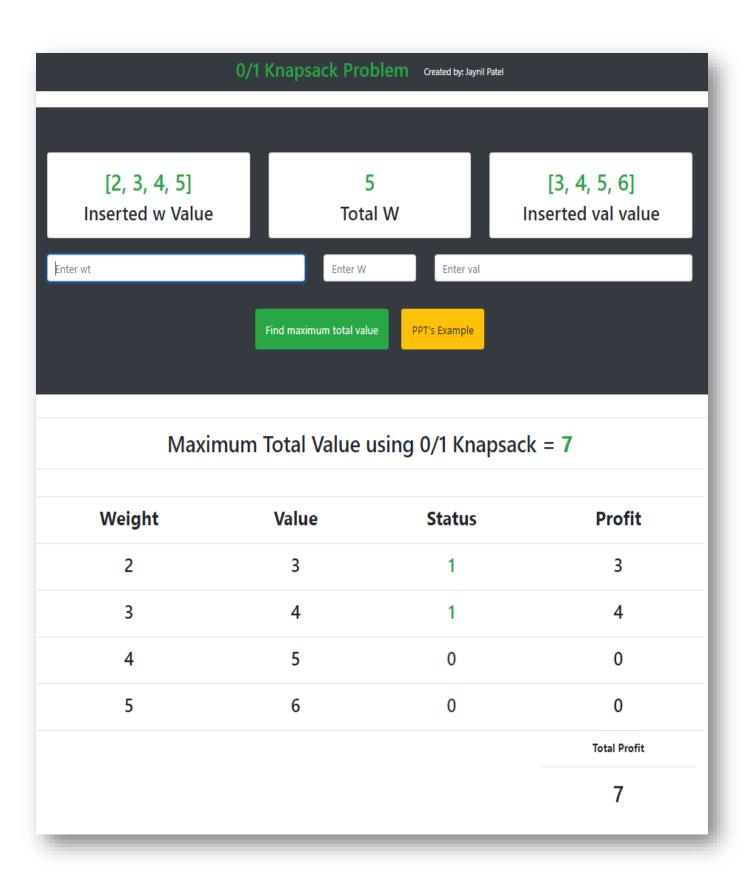
$$v_i = 3$$

$$w_i = 2$$

$$B[i,k] = 3$$

$$B[i-1,k] = 0$$

O/1 Knapsack(Simulation) using Python + Flask



0/1 Knapsack using Python

```
def ks01(W, wt, val, n):
    matrix = [[0 \text{ for } x \text{ in } range(W + 1)] \text{ for } x \text{ in } range(n + 1)]
    for i in range(n + 1):
        for w in range(W + 1):
            if i == 0 or w == 0:
                 matrix[i][w] = 0
            elif wt[i-1] <= w:
                 matrix[i][w] = max(val[i-1] + matrix[i-1][w-wt[i-1]], matrix[i-1][w])
                 matrix[i][w] = matrix[i-1][w]
    res = matrix[n][W]
    profit = matrix[n][W]
    finalList = []
    W = W
    for i in range(n, 0, -1):
        if res <= 0:
            break
        if res == matrix[i - 1][w]:
            finalList.append([wt[i-1],val[i-1],0])
            finalList.append([wt[i-1],val[i-1],1])
            res = res - val[i - 1]
            w = w - wt[i - 1]
    finalList.reverse()
    print("Max Profit = ",profit)
    print("\nWeight \t Value \t Status\n")
    for v in finalList:
        print(v[0],"\t",v[1],"\t",v[2])
    return profit
# W = 8
wt = [2,3,4,5]
val = [3,4,5,6]
W = 5
ans = ks01(W, wt, val, len(val))
```

Output:

Max Profit = 7

| Weight | Value | Status |
|--------|-------|--------|
| 2 | 3 | 1 |
| 3 | 4 | 1 |
| 4 | 5 | 0 |
| 5 | 6 | 0 |

Observation:

Here we have used the dynamic approach to solve the knapsack Problem and we create a matrix (2d) for W columns and N = len(weight) rows so we are traversing all the W for all the Weights so the time complexity is O(N * W).