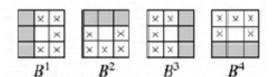
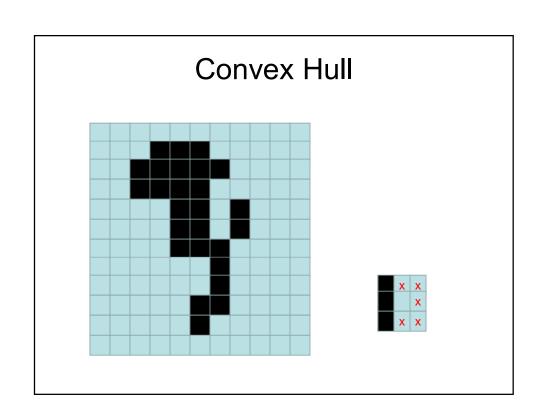
Convex Hull

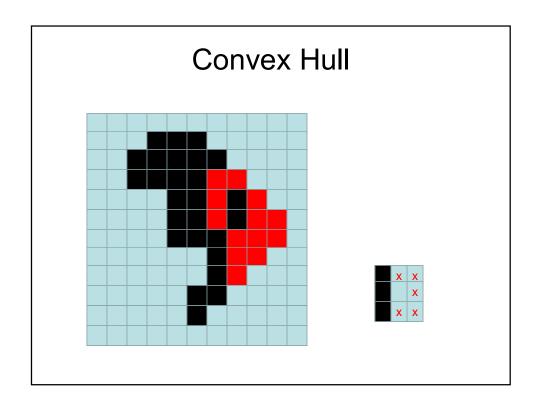
$$X_k^i = (X_{k-1} \otimes B^i) \cup A, \ i = 1, 2, 3, 4, \ k = 1, 2, \dots, \ X_0^i = A$$

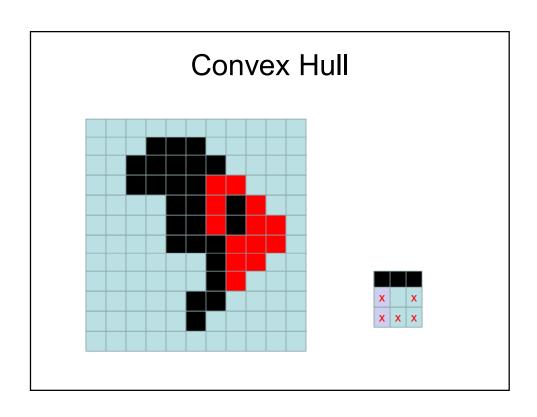
Now let $D^i=X^i_{\mathrm{conv}}$, where "conv" indicates convergence in the sense that $X^i_k=X^i_{k-1}$. Then the convex hull of A is

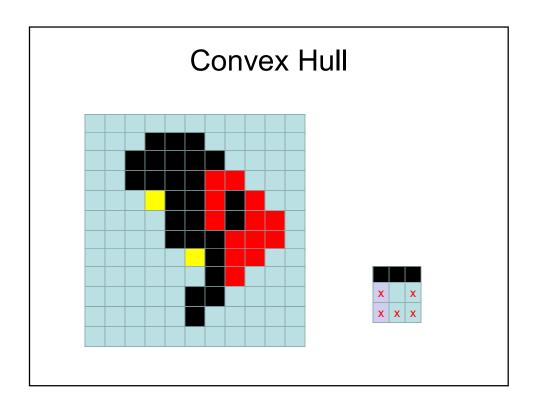
$$C(A) = \bigcup_{i=1}^4 D^i$$

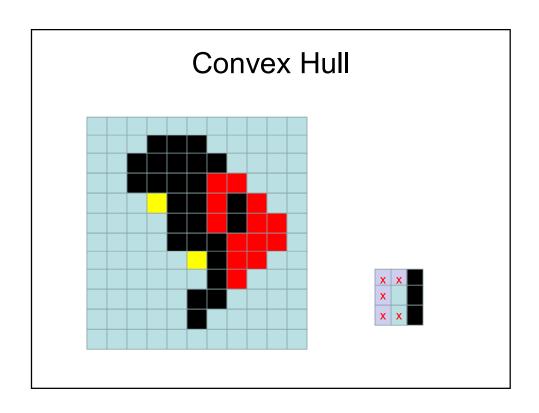


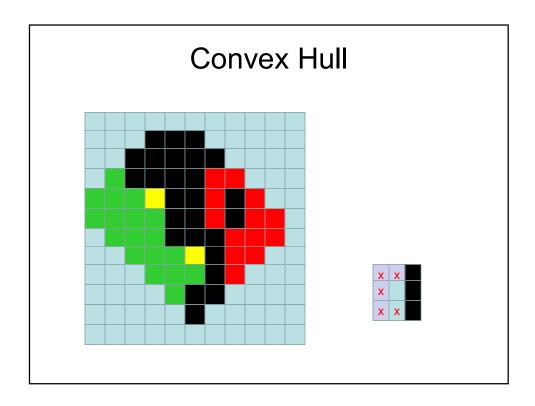


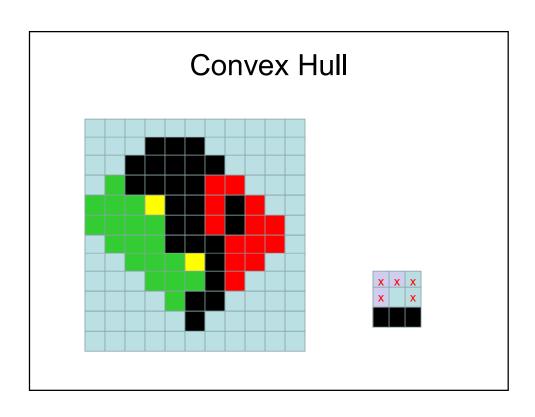


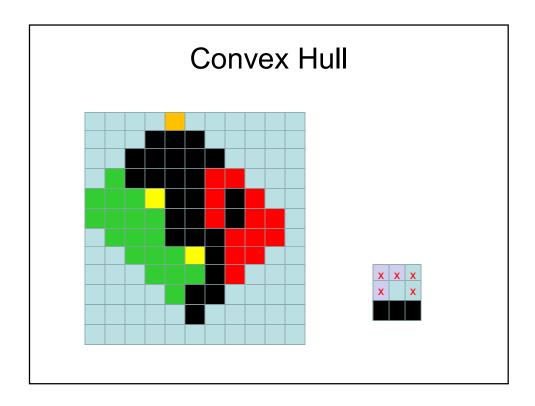


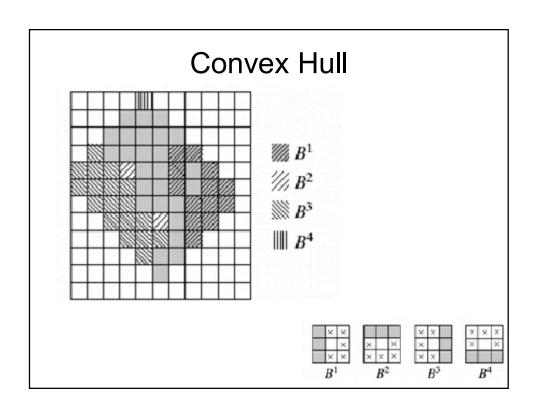








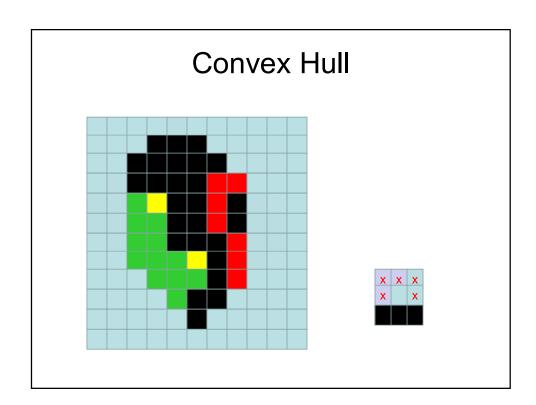




Convex Hull

Shortcoming of above algorithm: convex hull can grow beyond the minimum dimensions required to guarantee convexity

Possible solution: Limit growth so that it does not extend past the vertical and horizontal dimensions of the original set of points

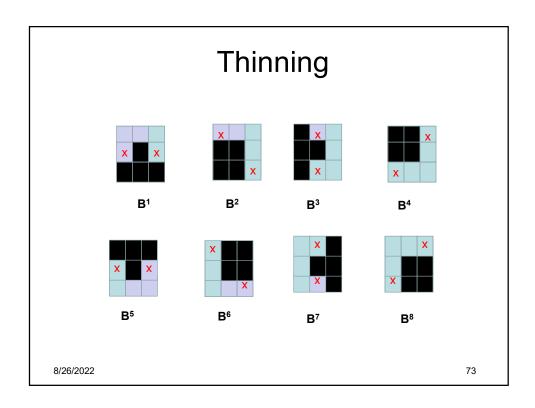


Thinning

 The thinning of a set A by a structuring element B, defined

$$A \otimes B = A - (A^{\circledast}B)$$
$$= A \cap (A^{\circledast}B)^{c}$$

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Thinning

$$A \otimes B = A - (A \otimes B)$$

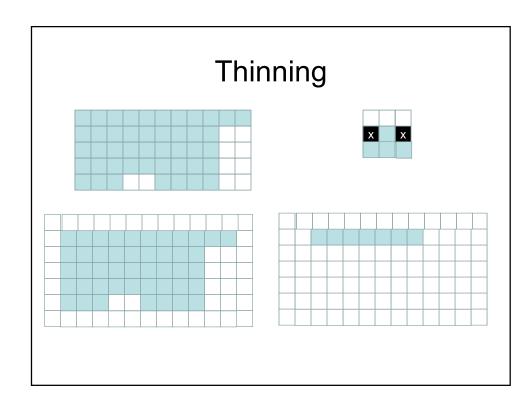
hit-or-miss transform/template matching

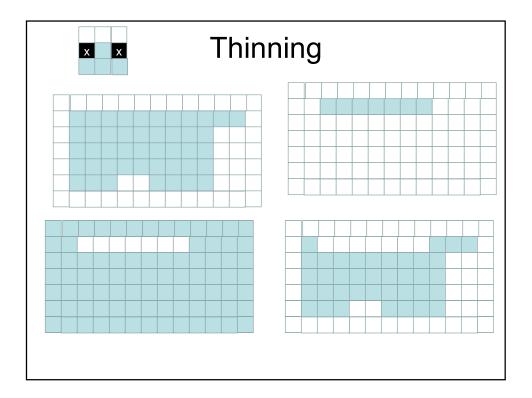
• Note that we are only interested in pattern matching of B in A, so no background operation is required of the hit-miss-transform.

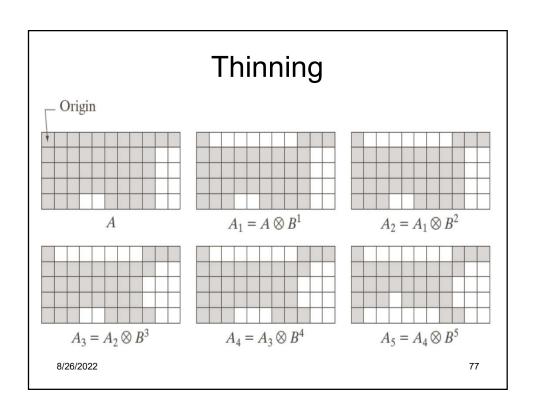
$${B} = {B^1, B^2, B^3, ..., B^n}$$

- •The structuring element B consists of a sequence of structuring elements, where B^i is the rotated version of B^{i-1} . Each structuring elements helps thinning in one direction. If there are 4 structuring elements thinning is performed from 4 directions separated by 90°. If 8 structuring elements are used the thinning is performed in 8 directions separated by 45°.
- •The process is to thin A by one pass with B^1 , then the result with one pass of B^2 , and continue until A is thinned with one pass of B^n .

$$A \otimes \{B\} = ((...((A \otimes B^1) \otimes B^2)...) \otimes B^n)$$







Thinning



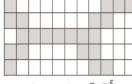






$$A_8 = A_6 \otimes B^{7,8}$$









 $A_{8,5} = A_{8,4} \otimes B^5$

 $A_{8,6} = A_{8,5} \otimes B^6$ No more changes after this.

 $A_{8,6}$ converted to m-connectivity.

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Thickening

The thickening is defined by the expression

$$A \square B = A \cup (A^{\circledast}B)$$

The thickening of A by a sequence of structuring element $\{B\}$

$$A \square \{B\} = ((...((A \square B^1) \square B^2)...) \square B^n)$$

In practice, the usual procedure is to thin the background of the set and then complement the result.

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