

# Sub: Compiler Construction

## Syntax Analysis PART 3

Compiled for: 7th Sem, CE, DDU

Compiled by: Niyati J. Buch

# Topics Covered

- Error Recovery in Predictive Parsing
- Bottom-up parsing
  - Shift Reduce Parsing
  - Conflict

# Error Recovery in Predictive Parsing

- Error recovery refers to the stack of a table-driven predictive parser, since it makes explicit the terminals and nonterminals that the parser hopes to match with the remainder of the input; the techniques can also be used with recursive-descent parsing.
- An error is detected during predictive parsing
  - when the terminal on top of the stack does not match the next input symbol
  - or when non terminal  $A$  is on top of the stack,  $a$  is the next input symbol, and  $M[A, a]$  is error (i.e., the parsing-table entry is empty).

# Panic Mode

- Panic-mode error recovery is based on the idea of skipping over symbols on the input until a token in a selected set of synchronizing tokens appears.
- Its effectiveness depends on the choice of synchronizing set.
- The sets should be chosen so that the parser recovers quickly from errors that are likely to occur in practice.
- The compiler designer must supply informative error messages that not only describe the error, they must draw attention to where the error was discovered.

# Few Heuristics

1. As a starting point, place all symbols in FOLLOW(A) into the synchronizing set for nonterminal A. If we skip tokens until an element of FOLLOW(A) is seen and pop A from the stack, it is likely that parsing can continue.
2. It is not enough to use FOLLOW(A) as the synchronizing set for A.
  - For example, if semicolons terminate statements, as in C, then keywords that begin statements may not appear in the FOLLOW set of the nonterminal representing expressions. A missing semicolon after an assignment may therefore result in the keyword beginning the next statement being skipped.

# Few Heuristics

3. If we add symbols in  $\text{FIRST}(A)$  to the synchronizing set for nonterminal  $A$ , then it may be possible to resume parsing according to  $A$  if a symbol in  $\text{FIRST}(A)$  appears in the input.
4. If a nonterminal can generate the empty string, then the production deriving  $\epsilon$  can be used as a default. Doing so may postpone some error detection, but cannot cause an error to be missed. This approach reduces the number of nonterminals that have to be considered during error recovery.

# Few Heuristics

5. If a terminal on top of the stack cannot be matched, a simple idea is to pop the terminal, issue a message saying that the terminal was inserted, and continue parsing. In effect, this approach takes the synchronizing set of a token to consist of all other tokens.

# EXAMPLE 2

$E \rightarrow TE'$

$\text{FIRST}(E) = \{ (, \text{id} \}$

$\text{FOLLOW}(E) = \{ ), \$ \}$

$E' \rightarrow +TE' \mid \epsilon$

$\text{FIRST}(E') = \{ +, \epsilon \}$

$\text{FOLLOW}(E') = \{ ), \$ \}$

$T \rightarrow FT'$

$\text{FIRST}(T) = \{ (, \text{id} \}$

$\text{FOLLOW}(T) = \{ +, ), \$ \}$

$T' \rightarrow *FT' \mid \epsilon$

$\text{FIRST}(T') = \{ *, \epsilon \}$

$\text{FOLLOW}(T') = \{ +, ), \$ \}$

$F \rightarrow (E) \mid \text{id}$

$\text{FIRST}(F) = \{ (, \text{id} \}$

$\text{FOLLOW}(F) = \{ *, +, ), \$ \}$

	Input Symbols					
Non-Terminals	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow \text{id}$			$F \rightarrow (E)$		

For each production  $A \rightarrow \alpha$  of the grammar, do the following:

1. For each terminal  $a$  in  $\text{FIRST}(\alpha)$ , add  $A \rightarrow \alpha$  to  $M[A, a]$ .
2. If  $\epsilon$  is in  $\text{FIRST}(\alpha)$ , then for each terminal  $b$  in  $\text{FOLLOW}(A)$ , add  $A \rightarrow \alpha$  to  $M[A, b]$ . If  $\epsilon$  is in  $\text{FIRST}(\alpha)$  and  $\$$  is in  $\text{FOLLOW}(A)$ , add  $A \rightarrow \alpha$  to  $M[A, \$]$  as well.



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$T \rightarrow FT'$

$FIRST(T) = \{ (, id \}$

$FOLLOW(T) = \{ +, ), \$ \}$

$T' \rightarrow *FT' \mid \epsilon$

$FIRST(T') = \{ *, \epsilon \}$

$FOLLOW(T') = \{ +, ), \$ \}$

$F \rightarrow (E) \mid id$

$FIRST(F) = \{ (, id \}$

$FOLLOW(F) = \{ *, +, ), \$ \}$

	Input Symbols					
Non-Terminals	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$	synch	synch
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$			$F \rightarrow (E)$		

The parsing table with "synch" indicating synchronizing tokens obtained from the FOLLOW set of the non terminal in question.

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$E \rightarrow TE'$

$FIRST(E) = \{ (, id \}$

$FOLLOW(E) = \{ ), \$ \}$

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$FIRST(E') = \{ +, \epsilon \}$

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$T \rightarrow FT'$

$FIRST(T) = \{ (, id \}$

$FOLLOW(T) = \{ +, ), \$ \}$

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$FIRST(T') = \{ *, \epsilon \}$

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$FIRST(F) = \{ (, id \}$

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	Input Symbols					
Non-Terminals	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$	synch	synch
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$			$F \rightarrow (E)$		

The parsing table with "synch" indicating synchronizing tokens obtained from the FOLLOW set of the non terminal in question.

# EXAMPLE 2

$E \rightarrow TE'$

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$T \rightarrow FT'$

$FIRST(T) = \{ (, id \}$

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$FIRST(F) = \{ (, id \}$

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	Input Symbols					
Non-Terminals	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$	synch	synch
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$	synch		$T \rightarrow FT'$	synch	synch
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$			$F \rightarrow (E)$		

The parsing table with "synch" indicating synchronizing tokens obtained from the FOLLOW set of the non terminal in question.

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$FIRST(T) = \{ (, id \}$

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$T' \rightarrow *FT' \mid \epsilon$

$FIRST(T') = \{ *, \epsilon \}$

$FOLLOW(T') = \{ +, ), \$ \}$

$F \rightarrow (E) \mid id$

$FIRST(F) = \{ (, id \}$

$FOLLOW(F) = \{ *, +, ), \$ \}$

	Input Symbols					
Non-Terminals	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$	synch	synch
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$	synch		$T \rightarrow FT'$	synch	synch
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$			$F \rightarrow (E)$		

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	Input Symbols					
Non-Terminals	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$	synch	synch
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$	synch		$T \rightarrow FT'$	synch	synch
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$	synch	synch	$F \rightarrow (E)$	synch	synch

The parsing table with "synch" indicating synchronizing tokens obtained from the FOLLOW set of the non terminal in question.

# Erroneous input ) id \* + id

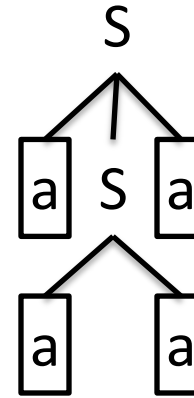
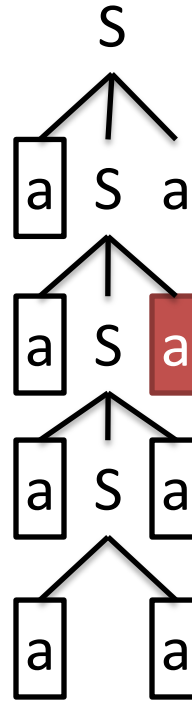
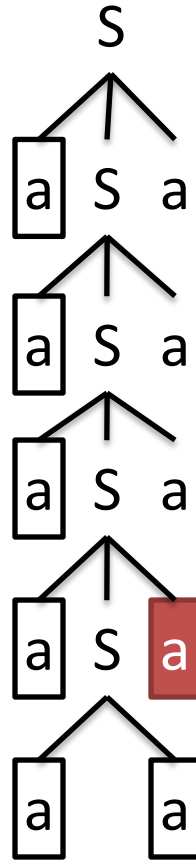
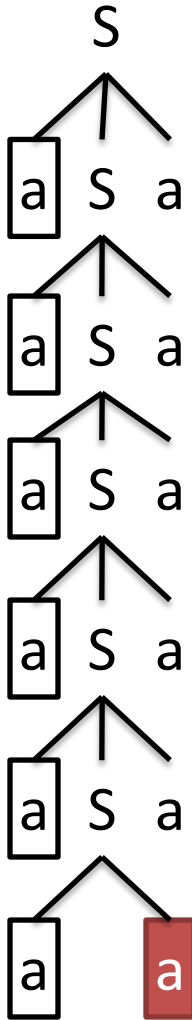
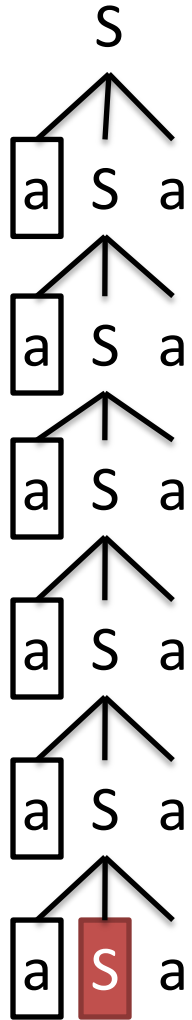
## The parser and error recovery mechanism

	Input Symbols					
Non-Terminals	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$	synch	synch
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$	synch		$T \rightarrow FT'$	synch	synch
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$	synch	synch	$F \rightarrow (E)$	synch	synch

Stack	Input	Remarks
\$ E	) id * + id \$	Error so skip the symbol
\$ E	id * + id \$	$E \rightarrow TE'$
\$ E' T	id * + id \$	$T \rightarrow FT'$
\$ E' T' F	id * + id \$	$F \rightarrow id$
\$ E' T' id	id * + id \$	MATCH so pop
\$ E' T'	* + id \$	$T' \rightarrow *FT'$
\$ E' T' F*	* + id \$	MATCH so pop
\$ E' T' F	+ id \$	Error so skip the symbol
\$ E' T' F	id \$	$F \rightarrow id$
\$ E' T' id	id \$	MATCH so pop
\$ E' T'	\$	$T' \rightarrow \epsilon$
\$ E'	\$	$E' \rightarrow \epsilon$
\$	\$	

G:  $S \rightarrow aSa \mid aa$   
input: aaaaaa

# Recursive Descent Parser



$G: S \rightarrow aSa \mid aa$

- $FIRST(S) = \{a\}$
- $FOLLOW(S) = \{\$, a\}$

	Input Symbols	
Non-Terminals	a	\$
S	$S \rightarrow aSa$ $S \rightarrow aa$	

For each production  $A \rightarrow \alpha$  of the grammar, do the following:

1. For each terminal  $a$  in  $FIRST(\alpha)$ , add  $A \rightarrow \alpha$  to  $M[A, a]$ .
2. If  $\epsilon$  is in  $FIRST(\alpha)$ , then for each terminal  $b$  in  $FOLLOW(A)$ , add  $A \rightarrow \alpha$  to  $M[A, b]$ . If  $\epsilon$  is in  $FIRST(\alpha)$  and  $\$$  is in  $FOLLOW(A)$ , add  $A \rightarrow \alpha$  to  $M[A, \$]$  as well.

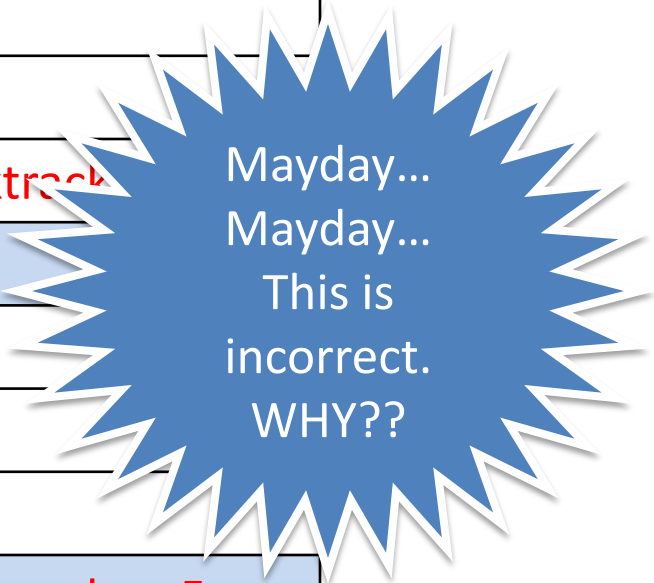


	STACK	INPUT	ACTION
1	\$ <b>S</b>	<b>a</b> aaaaa\$	$S \rightarrow aSa$
2	\$aS <b>a</b>	<b>a</b> aaaaa\$	MATCH, so pop
3	\$aS <b>S</b>	<b>a</b> aaaa\$	$S \rightarrow aSa$
4	\$aaS <b>a</b>	<b>a</b> aaaa\$	MATCH, so pop
5	\$aa <b>S</b>	<b>a</b> aaa\$	$S \rightarrow aSa$
6	\$aaaS <b>a</b>	<b>a</b> aaa\$	MATCH, so pop
7	\$aaa <b>S</b>	<b>a</b> aa\$	$S \rightarrow aSa$
8	\$aaaaS <b>a</b>	<b>a</b> aa\$	MATCH, so pop
9	\$aaaa <b>S</b>	<b>a</b> a\$	$S \rightarrow aSa$
10	\$aaaaaS <b>a</b>	<b>a</b> a\$	MATCH, so pop
11	\$aaaaa <b>S</b>	<b>a</b> \$	$S \rightarrow aSa$
12	\$aaaaaaS <b>a</b>	<b>a</b> \$	MATCH, so pop
13	\$aaaaaaS	\$	STACK not empty so <b>backtrack to 11</b>
14	\$aaaaa <b>S</b>	<b>a</b> \$	$S \rightarrow aa$
15	\$aaaaaa <b>a</b>	<b>a</b> \$	MATCH, so pop
16	\$aaaaaa	\$	STACK not empty so <b>backtrack to 9</b>

	STACK	INPUT	ACTION
16	\$aaaaaa	\$	STACK not empty so <b>backtrack to 9</b>
17	\$aaaa <b>S</b>	<b>aa</b> \$	$S \rightarrow aa$
18	\$aaaaa <b>a</b>	<b>a</b> \$	MATCH, so pop
19	\$aaaa <b>a</b>	<b>a</b> \$	MATCH, so pop
20	\$aaaa	\$	STACK not empty so <b>backtrack to 7</b>
21	\$aaa <b>S</b>	<b>aaa</b> \$	$S \rightarrow aa$
22	\$aaaaa <b>a</b>	<b>aaa</b> \$	MATCH, so pop
23	\$aaaa <b>a</b>	<b>a</b> \$	MATCH, so pop
24	\$aaa	a\$	MATCH, so pop
24	\$aa	\$	STACK not empty so <b>backtrack to 5</b>
25	\$aa <b>S</b>	<b>aaaa</b> \$	$S \rightarrow aa$
26	\$aaaa <b>a</b>	<b>aaaa</b> \$	MATCH, so pop
27	\$aaa <b>a</b>	<b>aaa</b> \$	MATCH, so pop
28	\$aa <b>a</b>	<b>aa</b> \$	MATCH, so pop
29	\$ <b>a</b>	<b>a</b> \$	MATCH, so pop
30	\$	\$	

There should be no back tracking in predictive parsing

	STACK	INPUT	ACTION
16	\$aaaaaa	\$	STACK not empty so <b>backtrack to 9</b>
17	\$aaaa <b>S</b>	<b>aa</b> \$	$S \rightarrow aa$
18	\$aaaaa <b>a</b>	<b>a</b> \$	MATCH, so pop
19	\$aaaa <b>a</b>	<b>a</b> \$	MATCH, so pop
20	\$aaaa	\$	STACK not empty so <b>backtrack</b>
21	\$aaa <b>S</b>	<b>aaa</b> \$	$S \rightarrow aa$
22	\$aaaa <b>a</b>	<b>aaa</b> \$	MATCH, so pop
23	\$aaaa <b>a</b>	<b>a</b> \$	MATCH, so pop
24	\$aaa	a\$	MATCH, so pop
24	\$aa	\$	STACK not empty so <b>backtrack to 5</b>
25	\$aa <b>S</b>	<b>aaaa</b> \$	$S \rightarrow aa$
26	\$aaaa <b>a</b>	<b>aaaa</b> \$	MATCH, so pop
27	\$aaa <b>a</b>	<b>aaa</b> \$	MATCH, so pop
28	\$aa <b>a</b>	<b>aa</b> \$	MATCH, so pop
29	\$ <b>a</b>	<b>a</b> \$	MATCH, so pop
30	\$	\$	



	STACK	INPUT	ACTION
16	\$aaaaaa	\$	STACK not empty so backtrack to 9
17	\$aaaaa <b>S</b>	<b>aa</b> \$	$S \rightarrow aa$
18	\$aaaaaa <b>a</b>	<b>aa</b> \$	MATCH, so pop
19	\$aaaaa <b>a</b>	<b>a</b> \$	MATCH, so pop
20	\$aaaa	\$	STACK not empty so
21	\$aaa <b>S</b>	<b>aaa</b> \$	$S \rightarrow aa$
22	\$aaaaa <b>a</b>	<b>aaa</b> \$	MATCH, so
23	\$aaaa <b>a</b>	<b>aa</b> \$	MATCH, so
24	\$aaa	<b>a</b> \$	MATCH, so
24	\$aa	\$	STACK not empty
25	\$aa <b>S</b>	<b>aaaa</b> \$	$S \rightarrow aa$
26	\$aaaa <b>a</b>	<b>aaaa</b> \$	MATCH, so pop
27	\$aaa <b>a</b>	<b>aaa</b> \$	MATCH, so pop
28	\$aa <b>a</b>	<b>aa</b> \$	MATCH, so pop
29	\$ <b>a</b>	<b>a</b> \$	MATCH, so pop
30	\$	\$	

WHY??

The grammar is not LL(1) so should not use predictive parsing.

Why is it not LL(1)??

Because it is not left factored grammar.

G:  $S \rightarrow aSa \mid aa$

## \*Predictive Parser

- Let's try to make this grammar LL(1)
- Common left factor **a** is observed.
- Making the grammar left-factored,  
 $S \rightarrow aS'$   
 $S' \rightarrow Sa \mid a$
- Again indirect left factoring is observed,  
 $S \rightarrow aS'$   
 $S' \rightarrow aA$   
 $A \rightarrow S'a \mid \epsilon$

G:  $S \rightarrow aSa \mid aa$

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 $S \rightarrow aS'$   
 $S' \rightarrow Sa \mid a$
- Again indirect left factoring is observed,  
 $S \rightarrow aS'$   
 $S' \rightarrow aA$   
 $A \rightarrow S'a \mid \epsilon$

	Input Symbols	
Non-Terminals	a	\$
S	$S \rightarrow aS'$	
S'	$S' \rightarrow aA$	
A	$A \rightarrow S'a$ $A \rightarrow \epsilon$	$A \rightarrow \epsilon$



G:  $S \rightarrow aSa \mid aa$

## \*Predictive Parser

- Let's try to make this grammar LL(1)
- Common left factor **a** is observed.
- Making the grammar left-factored,  
 $S \rightarrow aS'$   
 $S' \rightarrow Sa \mid a$
- Again indirect left factoring is observed,  
 $S \rightarrow AS'$   
 $S' \rightarrow aA$   
 $A \rightarrow S'a \mid \epsilon$

	Input Symbols	
Non-Terminals	a	\$
S	$S \rightarrow aS'$	
S'	$S' \rightarrow aA$	
A	$A \rightarrow S'a$ $A \rightarrow \epsilon$	$A \rightarrow \epsilon$

NOT LL(1)

As Look-ahead  
of one symbol is  
not sufficient.



# Bottom Up Parsing

# Bottom Up Parsing

- A **bottom-up parse** corresponds to the construction of a parse tree for an input string beginning at the leaves (the bottom) and working up towards the root (the top).
- It is convenient to describe parsing as the process of building parse trees, although a front end may in fact carry out a translation directly without building an explicit tree.

# Simple Example of $\text{id} * \text{id}$

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow ( E ) \mid \text{id}$

$\text{id} * \text{id}$

$\begin{array}{c} F \\ | \\ \text{id} \end{array} * \text{id}$

$\begin{array}{c} T \\ | \\ F \\ | \\ \text{id} \end{array} * \text{id}$

$\begin{array}{c} T \\ | \\ F \\ | \\ \text{id} \end{array} * \begin{array}{c} F \\ | \\ \text{id} \end{array}$

$\begin{array}{ccccc} & T & & & \\ & / \quad | \quad \backslash & & & \\ T & & * & & F \\ | & & & & | \\ F & & & & \text{id} \\ | & & & & \\ \text{id} & & & & \end{array}$

$\begin{array}{ccccc} & E & & & \\ & | & & & \\ & T & & & \\ & / \quad | \quad \backslash & & & \\ T & & * & & F \\ | & & & & | \\ F & & & & \text{id} \\ | & & & & \\ \text{id} & & & & \end{array}$

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$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow ( E ) \mid \text{id}$

$\boxed{\text{id}} * \text{id}$

$\begin{array}{c} F \\ | \\ \text{id} \end{array} * \text{id}$

$\begin{array}{c} T \\ | \\ F \\ | \\ \text{id} \end{array} * \text{id}$

$\begin{array}{c} T \\ | \\ F \\ | \\ \text{id} \end{array} * \begin{array}{c} F \\ | \\ \text{id} \end{array}$

$\begin{array}{ccccc} & T & & & \\ & / \quad | \quad \backslash & & & \\ T & & * & & F \\ | & & & & | \\ F & & & & \text{id} \\ | & & & & \\ \text{id} & & & & \end{array}$

$\begin{array}{ccccc} & E & & & \\ & | & & & \\ & T & & & \\ & / \quad | \quad \backslash & & & \\ T & & * & & F \\ | & & & & | \\ F & & & & \text{id} \\ | & & & & \\ \text{id} & & & & \end{array}$

# Simple Example of $\text{id} * \text{id}$

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow ( E ) \mid \text{id}$$

$$F \rightarrow \text{id}$$

$$\text{id} * \text{id} \quad \boxed{\begin{array}{c} F \\ | \\ \text{id} \end{array}} * \text{id}$$

$$\begin{array}{c} T \\ | \\ F \\ | \\ \text{id} \end{array} * \text{id}$$

$$\begin{array}{c} T \\ | \\ F \\ | \\ \text{id} \end{array} * \begin{array}{c} F \\ | \\ \text{id} \end{array}$$

$$\begin{array}{ccccc} & & T & & \\ & \swarrow & | & \searrow & \\ T & & * & & F \\ | & & & & | \\ F & & & & \text{id} \\ | & & & & \\ \text{id} & & & & \end{array}$$

$$\begin{array}{ccccc} & & E & & \\ & & | & & \\ & & T & & \\ & \swarrow & | & \searrow & \\ T & & * & & F \\ | & & & & | \\ F & & & & \text{id} \\ | & & & & \\ \text{id} & & & & \end{array}$$

# Simple Example of $\text{id} * \text{id}$

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow ( E ) \mid \text{id}$

$F \rightarrow \text{id}$

$T \rightarrow F$

$\text{id} * \text{id}$

$\begin{array}{c} F \\ | \\ \text{id} \end{array} * \text{id}$

$\boxed{\begin{array}{c} T \\ | \\ F \\ | \\ \text{id} \end{array}} * \text{id}$

$\begin{array}{c} T \\ | \\ F \\ | \\ \text{id} \end{array} * \begin{array}{c} F \\ | \\ \text{id} \end{array}$

$\begin{array}{ccccc} & & T & & \\ & \swarrow & | & \searrow & \\ T & & * & & F \\ | & & & & | \\ F & & & & \text{id} \\ | & & & & \\ \text{id} & & & & \end{array}$

$\begin{array}{ccccc} & & E & & \\ & & | & & \\ & & T & & \\ & \swarrow & | & \searrow & \\ T & & * & & F \\ | & & & & | \\ F & & & & \text{id} \\ | & & & & \\ \text{id} & & & & \end{array}$

# Simple Example of $\text{id} * \text{id}$

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow ( E ) \mid \text{id}$

$F \rightarrow \text{id}$

$T \rightarrow F$

$F \rightarrow \text{id}$

$\text{id} * \text{id}$

$\begin{array}{c} F \\ | \\ \text{id} \end{array} * \text{id}$

$\begin{array}{c} T \\ | \\ F \\ | \\ \text{id} \end{array} * \text{id}$

$\begin{array}{c} T \\ | \\ F \\ | \\ \text{id} \end{array} * \boxed{\begin{array}{c} F \\ | \\ \text{id} \end{array}}$

$\begin{array}{ccccc} & T & & & \\ & / \quad | \quad \backslash & & & \\ T & & * & & F \\ | & & & & | \\ F & & & & \text{id} \\ | & & & & \\ \text{id} & & & & \end{array}$

$\begin{array}{ccccc} & E & & & \\ & | & & & \\ & T & & & \\ & / \quad | \quad \backslash & & & \\ T & & * & & F \\ | & & & & | \\ F & & & & \text{id} \\ | & & & & \\ \text{id} & & & & \end{array}$

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$F \rightarrow ( E ) \mid \text{id}$

$F \rightarrow \text{id}$

$T \rightarrow F$

$F \rightarrow \text{id}$

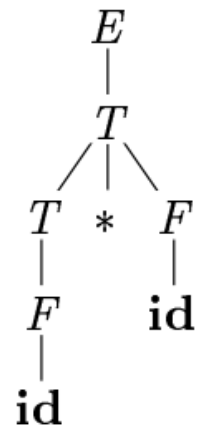
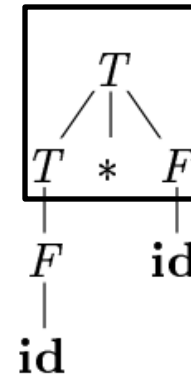
$T \rightarrow T * F$

$\text{id} * \text{id}$

$F * \text{id}$   
|  
 $\text{id}$

$T * \text{id}$   
|  
 $F$   
|  
 $\text{id}$

$T * F$   
|      |  
 $F$      $\text{id}$   
|  
 $\text{id}$





# Simple Example of $\text{id} * \text{id}$

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow ( E ) \mid \text{id}$

$F \rightarrow \text{id}$

$T \rightarrow F$

$F \rightarrow \text{id}$

$T \rightarrow T * F$

$E \rightarrow T$

$\text{id} * \text{id}$

$\begin{array}{c} F \\ | \\ \text{id} \end{array} * \text{id}$

$\begin{array}{c} T \\ | \\ F \\ | \\ \text{id} \end{array} * \text{id}$

$\begin{array}{c} T \\ | \\ F \\ | \\ \text{id} \end{array} * \begin{array}{c} F \\ | \\ \text{id} \end{array}$

$\begin{array}{ccccc} & T & & & \\ & / \quad | \quad \backslash & & & \\ T & & * & & F \\ | & & & & | \\ F & & & & \text{id} \\ | & & & & \\ \text{id} & & & & \end{array}$

$\begin{array}{ccccc} & E & & & \\ & | & & & \\ & T & & & \\ & / \quad | \quad \backslash & & & \\ T & & * & & F \\ | & & & & | \\ F & & & & \text{id} \\ | & & & & \\ \text{id} & & & & \end{array}$

# Simple Example of $\text{id} * \text{id}$

$$E \rightarrow E + T \mid T$$
$$T \rightarrow T * F \mid F$$
$$F \rightarrow ( E ) \mid \text{id}$$
$$F \rightarrow \text{id}$$
$$T \rightarrow F$$
$$F \rightarrow \text{id}$$
$$T \rightarrow T * F$$
$$E \rightarrow T$$
$$E \Rightarrow T \Rightarrow T * F \Rightarrow T * \text{id} \Rightarrow F * \text{id} \Rightarrow \text{id} * \text{id}$$

# Simple Example of id \* id

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow ( E ) \mid \text{id}$

$F \rightarrow \text{id}$

$T \rightarrow F$

$F \rightarrow \text{id}$

$T \rightarrow T * F$

$E \rightarrow T$

$E \Rightarrow T \Rightarrow T * F \Rightarrow T * \text{id} \Rightarrow F * \text{id} \Rightarrow \text{id} * \text{id}$



# Simple Example of $\text{id} * \text{id}$

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow ( E ) \mid \text{id}$

$F \rightarrow \text{id}$

$T \rightarrow F$

$F \rightarrow \text{id}$

$T \rightarrow T * F$

$E \rightarrow T$

$E \Rightarrow T \Rightarrow T * F \Rightarrow T * \text{id} \Rightarrow F * \text{id} \Rightarrow \text{id} * \text{id}$

Yay...

Rightmost Derivative  
in Reverse

# Bottom-up Parsing

- **Bottom-up parsing** during a left-to-right scan of the input constructs a rightmost derivation in reverse.
- Informally, a "**handle**" is a substring that matches **the body of a production**, and whose **reduction represents one step along the reverse of a rightmost derivation**.

# Handle during a parse of $\text{id} * \text{id}$

Right Sentential Form	Handle	Reducing Production
$\text{id} * \text{id}$	$\text{id}$	$F \rightarrow \text{id}$
$F * \text{id}$	$F$	$T \rightarrow F$
$T * \text{id}$	$\text{id}$	$F \rightarrow \text{id}$
$T * F$	$T * F$	$T \rightarrow T * F$
$T$	$T$	$E \rightarrow T$

a "**handle**" is a substring that matches **the body of a production**, and whose reduction represents one step **along the reverse of a rightmost derivation**.

# Example

$S \rightarrow aABe$

$A \rightarrow Abc \mid b$

$B \rightarrow d$

Input String : abbcde

# Example

$S \rightarrow aABe$

Input String : abbcd

$A \rightarrow Abc \mid b$

$B \rightarrow d$

$S \Rightarrow aA\textcolor{red}{B}e \Rightarrow a\textcolor{red}{A}de \Rightarrow a\textcolor{red}{A}bcde \Rightarrow abbcd$

Right Sentential Form	Handle	Reducing Production



# Example

$S \rightarrow aABe$

Input String : abbcd

$A \rightarrow Abc \mid b$

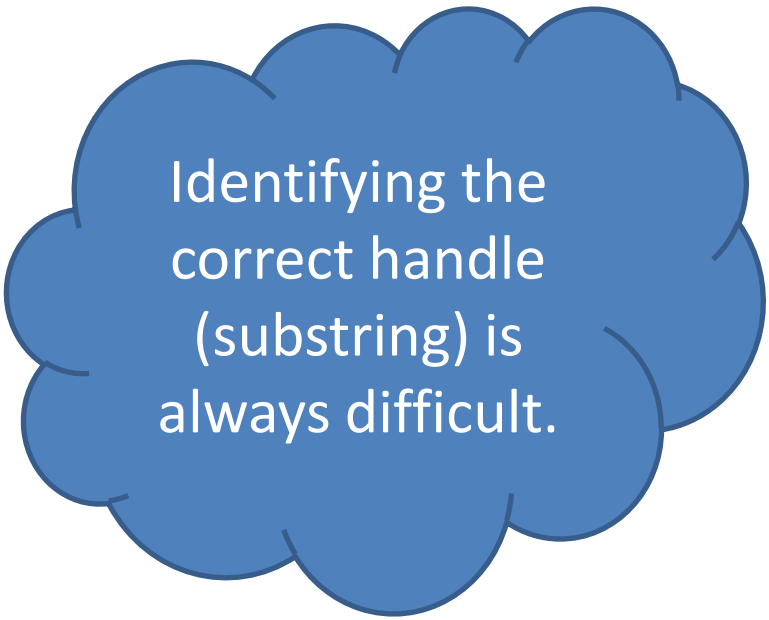
$B \rightarrow d$

$S \Rightarrow aA\textcolor{red}{B}e \Rightarrow a\textcolor{red}{A}de \Rightarrow a\textcolor{red}{A}bcde \Rightarrow abbcd$

Right Sentential Form	Handle	Reducing Production
a <b>b</b> cde	b	$A \rightarrow b$
a <b>A</b> bcde	Abc	$A \rightarrow Abc$
aA <b>d</b> e	d	$B \rightarrow d$
a <b>A</b> Be	aABe	$S \rightarrow aABE$

# Handle-pruning

- The process of discovering a handle & reducing it to the appropriate left-hand side is called **handle pruning**.
- Handle pruning forms the basis for a bottom-up parsing method.



Identifying the correct handle (substring) is always difficult.

# Shift-Reduce Parser

- **Shift-reduce parsing** is a form of bottom-up parsing in which a stack holds grammar symbols and an input buffer holds the rest of the string to be parsed.
- During a left-to-right scan of the input string, the parser shifts zero or more input symbols onto the stack, until it is ready to reduce a string of grammar symbols on top of the stack.
- It then reduces to the head of the appropriate production.
- The parser repeats this cycle until it has detected an error or until the stack contains the start symbol and the input is \$.

# Actions of shift-reduce parser

## 1. Shift

- Shift the next input symbol onto the top of the stack.

## 2. Reduce.

- The right end of the string to be reduced must be at the top of the stack.
- Locate the left end of the string within the stack and decide with what nonterminal to replace the string.

## 3. Accept.

- Announce successful completion of parsing.

## 4. Error.

- Discover a syntax error and call an error recovery routine.

# Shift Reduce Parsing with a Stack

- **Two problems:**
  - locate a handle and
  - decide which production to use (if there are more than two candidate productions).
- **General Construction: using a stack:**
  - “**shift**” input symbols into the stack until a handle is found on top of it.
  - “**reduce**” the handle to the corresponding non-terminal.
  - other operations:
    - “**accept**” when the input is consumed and only the start symbol is on the stack,
    - “**error**”

# Example 1

Input string: id1 \* id2

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow ( E ) \mid id$

STACK	INPUT	ACTION
\$	id1 * id2 \$	shift
\$ id1	* id2 \$	Reduce $F \rightarrow id$
\$ F	* id2 \$	Reduce $T \rightarrow F$
\$ T	* id2 \$	shift
\$ T *	id2 \$	shift
\$ T * id2	\$	Reduce $F \rightarrow id$
\$ T * F	\$	Reduce $T \rightarrow T * F$
\$ T	\$	Reduce $E \rightarrow T$
\$ E	\$	Accept

The use of a stack in shift-reduce parsing is justified by an important fact: the handle will always eventually appear on **top of the stack**, never inside.

$E \rightarrow E + T \mid T$
$T \rightarrow T * F \mid F$
$F \rightarrow ( E ) \mid id$

STACK	INPUT	ACTION
\$	id1 * id2 \$	shift
\$ id1	* id2 \$	Reduce $F \rightarrow id$
\$ F	* id2 \$	Reduce $T \rightarrow F$
\$ T	* id2 \$	shift
\$ T *	id2 \$	shift
\$ T * id2	\$	Reduce $F \rightarrow id$
\$ T * F	\$	Reduce $T \rightarrow T * F$
\$ T	\$	Reduce $E \rightarrow T$
\$ E	\$	Accept

Right Sentential Form	Handle	Reducing Production
id * id	id	$F \rightarrow id$
F * id	F	$T \rightarrow F$
T * id	id	$F \rightarrow id$
T * F	T * F	$T \rightarrow T * F$
T	T	$E \rightarrow T$

# Example 2

- For the grammar  $S \rightarrow 0S1 \mid 01$  indicate the handle in each of the following right-sentential forms:
  - a) 000111
  - b) 00S11

Right Sentential Form	Handle	Reducing Production
000111		
00S11		



# Example 2

- For the grammar  $S \rightarrow 0S1 \mid 01$  indicate the handle in each of the following right-sentential forms:
  - a) 000111
  - b) 00S11

Right Sentential Form	Handle	Reducing Production
000111	01	$S \rightarrow 01$
00S11		

To generate 000111,

$S \rightarrow 0\underline{S}1$

$\rightarrow 00\underline{S}11$

$\rightarrow 00\underline{01}11$

# Example 2

- For the grammar  $S \rightarrow 0S1 \mid 01$  indicate the handle in each of the following right-sentential forms:
  - a) 000111
  - b) 00S11

Right Sentential Form	Handle	Reducing Production
000111	01	$S \rightarrow 01$
00S11	0S1	$S \rightarrow 0S1$

To generate 00S11,

$S \rightarrow 0\underline{S}1$

$\rightarrow 00\underline{S}11$

# Example 3

- For the grammar  $S \rightarrow SS+ \mid SS* \mid a$  indicate the handle in each of the following right-sentential forms:
  - $SSS+a*+$
  - $SS+a*a+$
  - $aaa*a++$

Right Sentential Form	Handle	Reducing Production
$SSS+a*+$		
$SS+a*a+$		
$aaa*a++$		

# Example 3

- For the grammar  $S \rightarrow SS+ \mid SS* \mid a$  indicate the handle in each of the following right-sentential forms:

a)  $SSS+a*+$

b)  $SS+a*a+$

c)  $aaa*a++$

$S \rightarrow S\underline{S}+$   
 $\rightarrow SS\underline{S}^*+$   
 $\rightarrow S\underline{S}a^*+$   
 $\rightarrow S\underline{S}^+a^*+$

Right Sentential Form	Handle	Reducing Production
$SSS+a*+$	$SS^+$	$S \rightarrow SS^+$
$SS+a*a+$		
$aaa*a++$		

# Example 3

- For the grammar  $S \rightarrow S S + \mid S S * \mid a$  indicate the handle in each of the following right-sentential forms:

a)  $S S S + a * +$

b)  $S S + a * a +$

c)  $a a a * a + +$

$S \rightarrow S \underline{S} +$   
 $\rightarrow \underline{S} a +$   
 $\rightarrow S \underline{S} * a +$   
 $\rightarrow \underline{S} a * a +$   
 $\rightarrow S \underline{S} + a * a +$

Right Sentential Form	Handle	Reducing Production
$S S S + a * +$	$SS+$	$S \rightarrow SS+$
$S S + a * a +$	$SS+$	$S \rightarrow SS+$
$a a a * a + +$		

# Example 3

- For the grammar  $S \rightarrow SS+ \mid SS* \mid a$  indicate the handle in each of the following right-sentential forms:

a)  $SSS+a*+$

b)  $SS+a*a+$

c)  $aaa*a++$

$S \rightarrow S\underline{S}+$   
 $\rightarrow SSS\underline{++}$   
 $\rightarrow S\underline{S}a++$   
 $\rightarrow SSS\underline{*}a++$   
 $\rightarrow S\underline{S}a^*a++$   
 $\rightarrow \underline{S}aa^*a++$   
 $\rightarrow \underline{a}aa^*a++$

Right Sentential Form	Handle	Reducing Production
$SSS+a*+$	$SS+$	$S \rightarrow SS+$
$SS+a*a+$	$SS+$	$S \rightarrow SS+$
$aaa*a++$	$a$	$S \rightarrow a$

Give bottom-up parse for the input string 000111 according to the grammar  $S \rightarrow 0 S 1 \mid 0 1$

[illegible]

Give bottom-up parse for the input string 000111 according to the grammar  $S \rightarrow 0S1 \mid 01$

STACK	INPUT	ACTION
\$	0 0 0 1 1 1 \$	Shift
\$ 0	0 0 1 1 1 \$	Shift
\$ 0 0	0 1 1 1 \$	Shift
\$ 0 0 0	1 1 1 \$	Shift
\$ 0 0 <b>0 1</b>	1 1 \$	Reduce $S \rightarrow 0 1$
\$ 0 0 S	1 1 \$	Shift
\$ 0 <b>0 S 1</b>	1 \$	Reduce $S \rightarrow 0 S 1$
\$ 0 S	1 \$	Shift
\$ <b>0 S 1</b>	\$	Reduce $S \rightarrow 0 S 1$
\$ S	\$	Accept



Give bottom-up parse for the input string  $a a a * a + +$   
according to the grammar  $S \rightarrow S S + \mid S S * \mid a$

[illegible]

Give bottom-up parse for the input string  $a a a * a + +$   
 according to the grammar  $S \rightarrow S S + \mid S S * \mid a$

STACK	INPUT	ACTION
\$	a a a * a + + \$	Shift
\$ a	a a * a + + \$	Reduce $S \rightarrow a$
\$ S	a a * a + + \$	Shift
\$ S a	a * a + + \$	Reduce $S \rightarrow a$
\$ S S	a * a + + \$	Shift
\$ S S a	* a + + \$	Reduce $S \rightarrow a$
\$ S S S	* a + + \$	Shift
\$ S S S *	a + + \$	Reduce $S \rightarrow S S *$
\$ S S	a + + \$	Shift
\$ S S a	+ + \$	Reduce $S \rightarrow a$
\$ S S S	+ + \$	Shift
\$ S S S +	+ \$	Reduce $S \rightarrow S S +$
\$ S S	+ \$	Shift
\$ S S +	\$	Reduce $S \rightarrow S S +$
\$ S	\$	Accept

# Shift Reduce Conflict

- There are some context-free grammars for which shift-reduce parsing cannot be used.
- Every shift-reduce parser for such a grammar can reach a configuration in which the parser, knowing the entire stack and also the next  $k$  input symbols, cannot decide whether to shift or to reduce (**a shift/reduce conflict**), or cannot decide which of several reductions to make (**a reduce/reduce conflict**).

# Shift Reduce Conflict

- There are some syntactic constructs that give rise to such grammars.
- Technically, these grammars are not in the LR(k) class of grammars we refer to them as non-LR grammars.
  - The  $k$  in LR(k) refers to the number of symbols of lookahead on the input.
  - Grammars used in compiling usually fall in the LR(1) class, with one symbol of lookahead at most.
- An ambiguous grammar can never be LR.