

## IE PRACTICAL No. 1

Aim: Basics of R software.

- 1) R is a software for statistical analysis and data computing.
- 2) It is an effective data handling software and outcome storage is possible.
- 3) It is capable of graphical display.
- 4) It is a free software.

a) Solve the following

$$1) 4+6+8 \div 2 - 5$$

$$> 4+6+8/2 - 5$$

[1] 9



$$2) 2^2 + |-3| + \sqrt{45}$$

$$> 2^2 + \text{abs}(-3) + \text{sqrt}(45)$$

[1] 13.7082

$$3) 5^3 + 7 \times 5 \times 8 + 46/5$$

$$> 5^3 + 7 * 5 * 8 + 46/5$$

[1] 414.2

$$4) \sqrt{4^2 + 5 \times 3 + 7/6}$$

$$> \text{sqrt}(4^2 + 5 * 3 + 7/6)$$

[1] 5.671567

5) round off

$$96 \div 7 + 9 * 8$$

&gt; round(46/7 + 9\*8)

[2] 99

Q2) &gt; ((2,3,5,7)\*2

[1] 4 6 10 14

&gt; c(2,3,5,7)\*c(2,3)

[2] 4 9 10 21

&gt; ((2,3,5,7)\*x(2,3,6,2)

[2] 4 9 30 14

&gt; c(1,6,2,3)\*c(-2, -3, -4, -1)

[2] -2 -18 -8 -3

&gt; ((2,3,5,7)^2

[1] 4 9 25 49

&gt; c(4,8,8,9,4,5)^c(1,2,3)

[1] 4 36 512 916 2125

&gt; ((6,2,7,5)/c(4,5))

[1] 1.60 0.40 1.75 1.00

Q3) &gt; x = 20 &gt; y = 30 &gt; z = 2

&gt; x^2 + y^3 + z

[1] 27402

&gt; sqrt(x^2 + y)

[1] 26.73644

&gt; x^2 + y^2

[1] 1300

Q4) &gt; x &lt;- matrix(x = nrow=4, ncol=2, data = c(1, 2, 3, 4, 5, 6, 7, 8))

&gt; x [1] [2]

[1,] 1 5

[2,] 2 6

[3,] 3 7

[4,] 4 8

05) find  $8x+y$  and  $2x+3y$ , where  $X = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 1 \\ 5 & -5 & 3 \end{bmatrix}$

$$Y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$$

>  $X <- \text{matrix}(nrows=3, ncol=3, \text{data} = ((4, 7, 8, 12, 0, 1, 5, -5, 6, 10, 7, 15, -6, 5)))$

[1]  $\begin{bmatrix} [1,1] & [1,2] & [1,3] \end{bmatrix}$

$$\begin{bmatrix} [1,1] & 4 & -2 & 6 \end{bmatrix}$$

$$\begin{bmatrix} [2,1] & 7 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} [3,1] & 5 & -5 & 3 \end{bmatrix}$$

>  $Y <- \text{matrix}(nrows=3, ncol=3, \text{data} = (10, 12, 15, -5, -4, -6, 7, 9, 5))$

[2]  $\begin{bmatrix} [1,1] & [1,2] & [1,3] \end{bmatrix}$

$$\begin{bmatrix} [1,1] & 10 & -5 & 7 \end{bmatrix}$$

$$\begin{bmatrix} [2,1] & 12 & -4 & 9 \end{bmatrix}$$

$$\begin{bmatrix} [3,1] & 15 & -6 & 5 \end{bmatrix}$$

>  $X+Y$

[3]  $\begin{bmatrix} [1,1] & [1,2] & [1,3] \end{bmatrix}$

$$\begin{bmatrix} [1,1] & 14 & -2 & 13 \end{bmatrix}$$

$$\begin{bmatrix} [2,1] & 19 & -4 & 16 \end{bmatrix}$$

$$\begin{bmatrix} [3,1] & 24 & -11 & 8 \end{bmatrix}$$

>  $2*x + 3*y$

[4]  $\begin{bmatrix} [1,1] & [1,2] & [1,3] \end{bmatrix}$

$$\begin{bmatrix} [1,1] & 38 & -19 & 33 \end{bmatrix}$$

$$\begin{bmatrix} [2,1] & 50 & -12 & 41 \end{bmatrix}$$

$$\begin{bmatrix} [3,1] & 63 & -28 & 21 \end{bmatrix}$$

Q.6) Marks of Statistics of CS Batch B.

$x = c(60, 20, 35, 24, 46, 56, 55, 45, 27, 22, 47, 58, 54, 40, 50, 32, 36, 29, 35, 39)$

>  $y = c(data)$

>  $breaks = seq(20, 60, 5)$

>  $a = (x, breaks, right = FALSE)$

>  $b = table(a)$

>  $c = transform(b)$

>  $c$

	c	freq
1	[20, 25)	3
2	[25, 30)	2
3	[30, 35)	1
4	[35, 40)	4
5	[40, 45)	1
6	[45, 50)	3
7	[50, 55)	2
8	[55, 60)	4

Q8

## PRACTICAL No. 2

Topic : Probability distribution.

1) Check whether the followings are p.m.f or not

$x$	$P(x)$
0	0.1
1	0.2
2	-0.5
3	0.4
4	0.3
5	0.5

If the given data is p.m.f then  $\sum P(x) = 1$   
 $\therefore P(0) + P(1) + P(2) + P(3) + P(4) + P(5) \neq P(x)$   
 $= 0.1 + 0.2 - 0.5 + 0.4 + 0.3 + 0.5$   
 $= 1.0$

$\therefore P(2) = -0.5$ , it can't be a probability mass function  
 $\therefore P(x) \geq 0 \forall x$

$x$	$P(x)$
1	0.2
2	0.2
3	0.3
4	0.2
5	0.2

The condition for p.m.f is  $\sum P(x) = 1$

$$\begin{aligned} \sum P(x) &= P(1) + P(2) + P(3) + P(4) + P(5) \\ &= 0.2 + 0.2 + 0.3 + 0.2 + 0.2 \\ &= 1.1 \end{aligned}$$

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∴ The given data is not a pmf because the  $P(x) \neq 1$

x	P(x)
10	0.2
20	0.2
30	0.35
40	0.15
50	0.1

The condition for p.m.f is

i)  $P(x) \geq 0 \forall x$  satisfy

$$\begin{aligned} \sum P(x) &= P(10) + P(20) + P(30) + P(40) + P(50) \\ &= 0.2 + 0.2 + 0.35 + 0.15 + 0.1 \\ &= 1 \end{aligned}$$

∴ The given data is pmf.

Code:

> Prob = c(0.2, 0.2, 0.35, 0.15, 0.1)

> sum(Prob)

[1] 1

a.2) Find the c.d.f for the following p.m.f and

Sketch the graph

x	10	20	30	40	50
P(x)	0.2	0.2	0.35	0.15	0.1

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$$F(x) = 0$$

$$x < 10$$

$$0.2$$

$$10 \leq x < 20$$

$$0.4$$

$$20 \leq x < 30$$

$$0.75$$

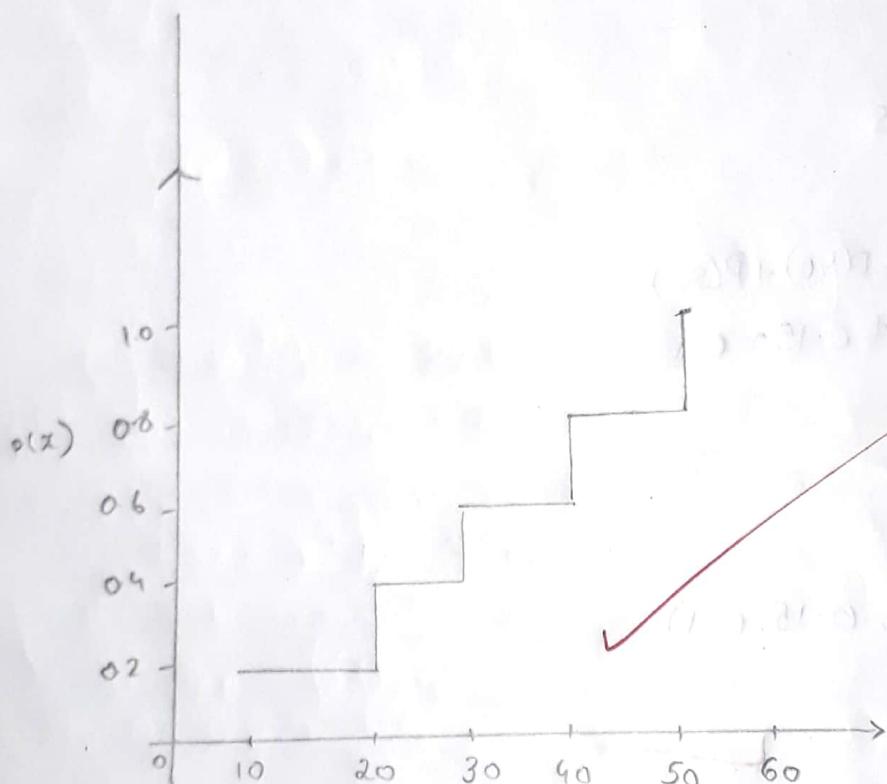
$$30 \leq x < 40$$

$$0.90$$

$$40 \leq x < 50$$

$$1.0$$

$$x \geq 50$$



$$> x = c(10, 20, 30, 40, 50)$$

$$> plot(x, cumsum(prob), "s")$$

(a) Find

x	1	2	3	4	5	6
P(x)	0.15	0.25	0.1	0.2	0.2	0.1

$$\begin{aligned}
 F(x) = 0 & \quad x < 1 \\
 0.15 & \quad 1 \leq x < 2 \\
 0.40 & \quad 2 \leq x < 3 \\
 0.50 & \quad 3 \leq x < 4 \\
 0.70 & \quad 4 \leq x < 5 \\
 0.90 & \quad 5 \leq x < 6 \\
 1.00 & \quad x \geq 6
 \end{aligned}$$

> Prob = (0.15, 0.25, 0.1, 0.2, 0.2, 0.1)

> sum(Prob)

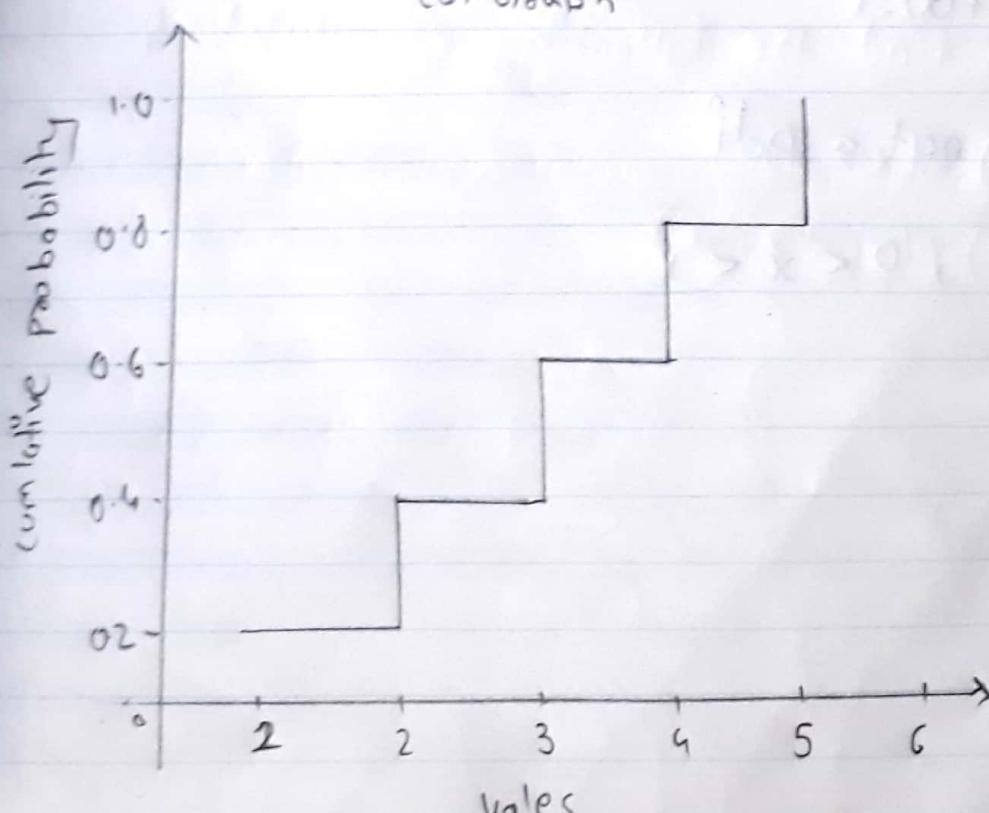
[1] 1

> cumsum(Prob)

[1] 0.15 0.40 0.50 0.70 0.90 1.00

> x = c(1, 2, 3, 4, 5, 6)

> Plot(x, ~~cumsum(Prob)~~, "s", xlab = "value",  
 ylab = "Cumulative probability", main = "CDF graph",  
 col = "brown")



Q.3) check that whether the following is p.d.f or not

(i)  $f(x) = 3-2x ; 0 \leq x \leq 1$

(ii)  $F(x) = 3x^2 ; 0 < x < 1$

(i)  $f(x) = 3-2x$

$$\rightarrow \int_0^1 f(x) dx$$

$$= \int_0^1 (3-2x) dx$$

$$= \int_0^1 3 dx - \int_0^1 2x dx$$

$$= [3x - x^2]_0^1 = 2$$

$$\therefore \text{The } \int_0^1 f(x) dx = 1$$

$\therefore$  It is not a pdf

(ii)  $f(x) = 3x^2 ; 0 < x < 1$

$$\int_0^1 f(x) dx$$

$$= \int_0^1 3x^2 dx$$

$$= 3 \int_0^1 x^2$$

$$= \left[ \frac{3x^3}{3} \right]_0^1$$

$$\therefore x^n = \frac{x^{n+1}}{n+1}$$

$$= x^3$$

$$= 1$$

The  $\{ f(x) = 1 \}$

$\therefore$  It is a pdf

Q

## Topic : Binomial distribution

#  $P(X=x) = \text{dbinom}(x, n, p)$

‡  $P(X < x) = \text{Pbinom}(x, n, p)$

#  $P(X > x) = 1 - \text{Pbinom}(x, n, p)$

‡ if  $x$  is known

$$P_1 = P(X \leq x) = \text{qbinom}(P_1, n, p)$$

1) find the probability of exactly 10 success in hundred trials with  $p=0.1$

2) Suppose there are 12 mcq, each question has 5 options, out of which 1 is correct. Find the probability of having exactly 4 correct answers.  
i) Atmost 4 correct answers  
ii) More than 5 correct answers.

3) Find the complete distribution when  $n=5$  &  $p=0.1$

4)  $n=12$ ,  $p=0.25$ , find the following probabilities

i)  $P(X=5)$       ii)  $P(X > 7)$

ii)  $P(X \leq 5)$       iv)  $P(5 < X < 7)$

1) > $x = \text{dbinom}(10, 100, 0.1)$

> $x$

[1] 0.1318653

2) > $\text{dbinom}(4, 12, 0.2)$

[1] 0.1328756

> $\text{pbinom}(4, 12, 0.2)$

[1] 0.927445

> $1 - \text{pbinom}(5, 15, 0.2)$

[1] 0.01940528

3)  $\text{dbinom}(0.5, 5, 0.1)$

0 - 0.59049

1 - 0.32805

2 - 0.07290

3 - 0.00810

4 - 0.00045

5 - 0.00001

4) 1)  $\text{dbinom}(5, 12, 0.25)$

[1] 0.1632414

2)  $\text{pbinom}(5, 12, 0.25)$

[1] 0.9455978

3)  $1 - \text{pbinom}(7, 12, 0.25)$

[1] 0.00278151

4)  $\text{dbinom}(6, 12, 0.25)$

[1] 0.64014945

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- 5) The probability of a Salesman making a sale to customer 0.15 . find the probability of  
1) No sales out of 10 customer.  
2) More than 3 sales out of 20 customer

6)

A Sales man has 20% probability of making a sales to customer out of 30 customers what minimum number of sales he can make with 88% of probability

→  $x$  follows binomial distribution with  $n=10$ ,  $p=0.3$  plot the graph of p.m.f and c.d.f

> dbinom(0, 10, 0.15)

[1] 0.1968744

> 1 - pbinom(3, 20, 0.15)

[1] 0.3522748

> qbinom(0.88, 30, 0.2)

[1] 9

>>n=10

>p=0.3

>x=0:n

> prob=dbinom(x,n,p)

>umpprob=pbinom(x,n,p)

>d=data.frame("Xvalues"=x, "probability"=prob)

>print d

	xvalues	probability
1	0	0.0282
2	1	0.1216
3	2	0.2334
4	3	0.2668
5	4	0.2061
6	5	0.1029
7	6	0.0368
8	7	0.0367
9	8	0.0890
10	9	0.0001
11	10	0.0000

6

## PRACTICAL - 5

Aim: Normal distribution.

#  $P(X=x) = dnorm(n, \mu, \sigma)$

#  $P(X \leq x) = pnorm(x, \mu, \sigma)$

#  $P(X > x) = 1 - pnorm(x, \mu, \sigma)$

# To generate random number from a normal distribution  
(in Random numbers)  
The R code is  $rnorm(n, \mu, \sigma)$

Q) A random variable  $X$  follows normal distribution with mean  $\mu = 12$  & S.d.  $\sigma = 3$ . Find

$$(i) P(X \leq 15)$$

$$(ii) P(10 \leq X \leq 13)$$

$$(iii) P(X > 14)$$

(iv) Generate 5 observations (RANDOM NUMBERS)

Ans

$$(i) P1 = pnorm(15, 12, 3)$$

> P1

$$[1] 0.8413447$$

> cat ("P(X \leq 15) = ", P1)

$$> P(X \leq 15) = 0.8413447$$

$$(2) P2 = pnorm(13, 12, 3) - pnorm(10, 12, 3)$$

> P2

$$[1] 0.3780661$$

>  $p(10 \leq x \leq 13) = 0.3780661$

iii)  $p_3 = 1 - \text{pnorm}(14, 12, 3)$

>  $p_3$

[1] 0.2524925

> cat("p(x > 14) = ", p3)

$p(x > 14) = 0.2524925$

>  $\text{rnorm}(5, 12, 3)$

[1] 14.98663 12.51616 13.47904 14.98075 19.73518

Q)  $x$  follows normal distribution with

$\mu = 10$ ,  $\sigma = 2$ . Find: ?

i)  $p(x \leq 7)$

ii)  $p(5 < x < 12)$

iii)  $p(x > 12)$

iv) Generate 10 random observation

v) Find  $k$  such that probability  $p(x < k) = 0.4$ .

Ans i)  $p1 = \text{pnorm}(7, 10, 2)$

p1

[1] 0.0668072

> cat("p(x \leq 7) = ", p1)

[1]  $p(x \leq 7) = 0.0668072$

ex

i)  $p_2 = \text{pnorm}(12, 10, 2) - \text{pnorm}(5, 10, 2)$

$p_2$

[1] 0.8351351

> cat (" $p(15 < x < 12) =$ ", p2)

-  $p(15 < x < 12) = 0.8351351$

ii)  $p_3 = 1 - \text{pnorm}(12, 10, 2)$

$p_3$

[1] 0.1586553

> cat (" $p(p(x > 12)) =$ ", p3)

-  $p(p(x > 12)) = 0.1586553$

> rnorm(10, 10, 2)

[1] 11.986324 12.155504 7.130492  
10.519359 5.637988 10.959963  
7.988735 9.336612 8.165376  
13.652133

> qnorm(0.4, 10, 2)

[1] 9.493306

- 3) Generate 5 random numbers from a normal distribution with mean = 15 & s.d = 4  
Find sample mean, median, s.d and print(cat)

4)  $\sim N(30, 100)$ , ( $\sigma^2 = 100$ ) find only  $P_1, P_2$   
(no cut command) 40

>  $P_1 = pnorm(40 | 30, 10)$

>  $P_1$

[1] 0.8413447

>  $P_2 = 1 - pnorm(35 | 30, 10)$

>  $P_2$

[1] 0.3085375

>  $P_3 = pnorm(35 | 30, 10) - pnorm(25 | 30, 10)$

>  $P_3$

[1] 0.3829249

> qnorm(0.6 | 30, 10)

[1] 32.53347

Ans >  $x = rnorm(5 | 15, 9)$

>  $x$

[1] 16.43602 12.58878 16.91096 17.37383 15.04296

>  $m = mean(x)$

>  $q_m$

[1] 15.67034

>  $med = median(x)$

>  $me$

[1] 16.43602

>  $varience = (n-1) * var(x) / n$

>  $varience$

[1] 2.5836

>sd = sqrt(variance)

>sd

[1] 1.72731

>(cat("sample mean is ", am))

→ Sample mean is 15.67034

>(cat("sample mean is ", mr))

→ Sample mean is 16.43602

>(cat("sample sd is ", sd))

→ Sample sd is 1.72731

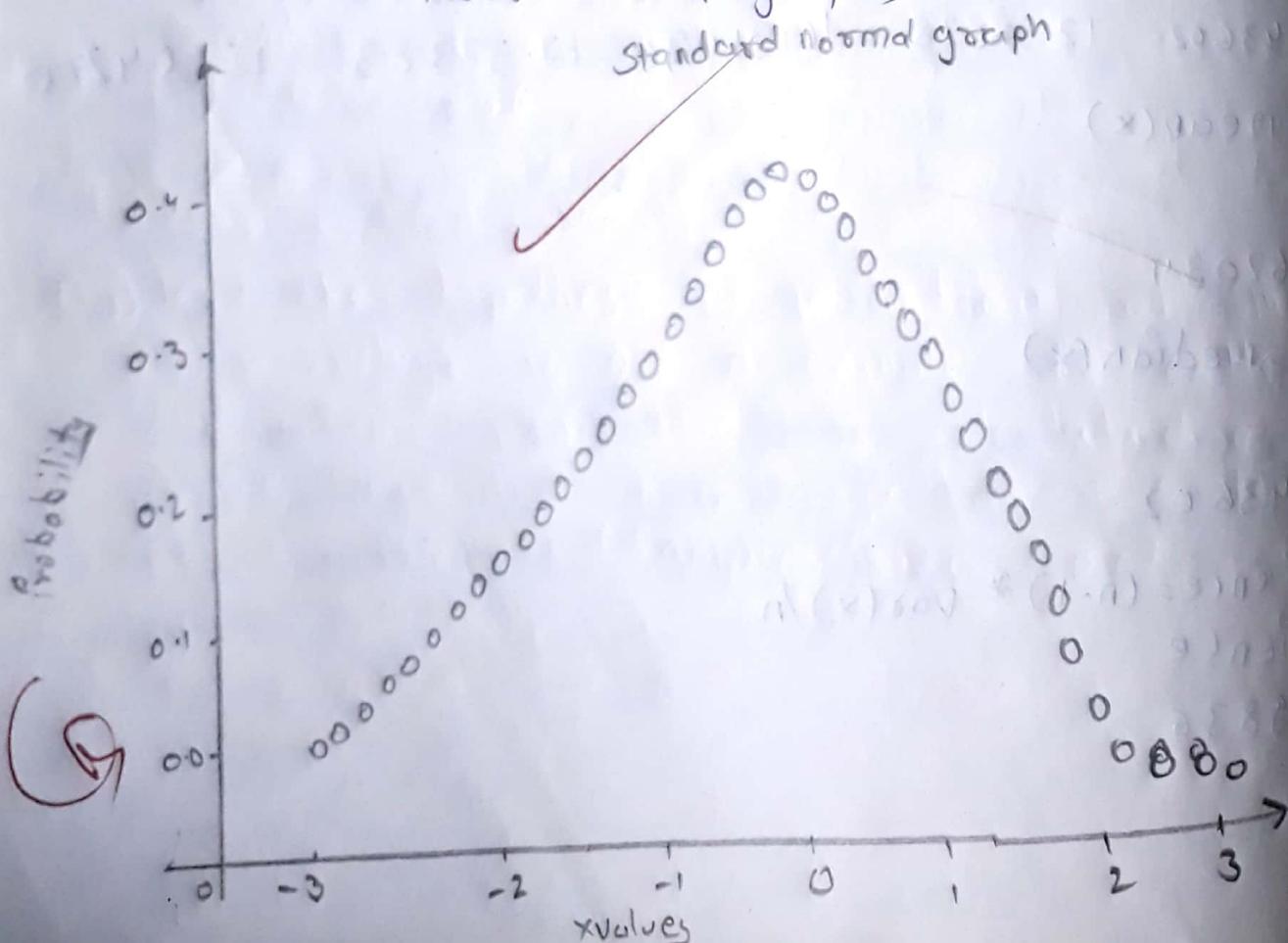
5) Plot the standard, normal graph

Ans

X = seq(-3, 3, by = 0.1)

Y = dnorm(X)

plot(X, Y, xlab = "xvalues", ylab = "probability",  
main = "standard normal graph")



## PRACTICAL - 5

### Normal & Z-test

Q.) Test of Hypothesis  $H_0: \mu = 15$ ,  $H_1: \mu \neq 15$ .

Random sample of size 400 is drawn and it is calculated the sample mean is 14. & the standard deviation is 3. Test the hypothesis at 5% level of significance.

$m \rightarrow$  mean       $\sigma \rightarrow$  populn

$\sigma \rightarrow$  sd       $n \rightarrow$  sample size

Sol<sup>n</sup>

$$> m_0 = 15$$

$$> m_x = 14$$

$$> s_d = 3$$

$$> n = 400$$

$$> z_{cal} = (m_x - m_0) / (s_d / (\sqrt{n}))$$

$$> z_{cal}$$

$$[1] -6.66667$$

> cat("calculate value at Z is = , zcal")

→ calculate value at Z is = -6.66667

> pvalue = 2 \* (1 - pnorm(abs(zcal)))

> pvalue

$$[1] 2.616796e-11$$

Since p value is less than 0.05 we reject  $H_0: \mu = 15$ .

Q.2) Test of hypothesis  $H_0: \mu = 10$ ,  $H_1: \mu \neq 10$ .

Random sample of size 400 is drawn with sample mean 10.2 & standard deviation 2.25. Test the hypothesis at 5% level of significance.

Sol<sup>n</sup>:

>  $m_0 = 10$

>  $m_x = 10.2$

>  $s_d = 2.25$

>  $n = 400$

>  $z_{cal} = (m_x - m_0) / (s_d / (\sqrt{n}))$

>  $z_{cal}$

[1] 1.77778

> cat("calculate value at z is = ",  $z_{cal}$ )

→ calculate value at z is = 1.77778

> pvalue = 2 \* (1 - pnorm(abs( $z_{cal}$ )))

> pvalue

[1] 0.07544036

Q.3) Test the hypothesis no proportion of smokers in a college is 0.2 a sample is collected and sample proportion is calculated as 0.125. Test the hypothesis at 5% level of significance (sample size = 400)

P - population

p - sample

$$> p = 0.125$$

$$> n = 400$$

$$> \alpha = 1 - P$$

$$> z_{\text{cal}} = (p - P) / \sqrt{P(1-P)/n}$$

$$> z_{\text{cal}}$$

$$[1] - 3.75$$

Q) last year farmer's lost 20% of their crops. A random sample of 60 fields are collected. It was found that 9 field crops are insect populated. Test the hypothesis at 1% level of significance.

$$> H_0: p = 0.2$$

$$> p = 9/60$$

$$> n = 60$$

$$> z_{\text{cal}} = (p - P) / \sqrt{P(1-P)/n}$$

$$> z_{\text{cal}}$$

~~$$[1] - 0.5682458$$~~

$$> p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> p_{\text{value}}$$

~~$$[1] 0.3329216$$~~

∴ The value is 0.1 so value is accepted.

<sup>Q1</sup>  
a) Test the hypothesis  $H_0: \mu = 12.5$  from the following sample at 5% level of significance

>  $x = ((12.25, 11.97, 12.15, 12.08, 12.31, 12.28, 11.94,$   
 $11.89, 12.16, 12.04))$

>  $n = \text{length}(x)$

>  $n$

[1] 10

>  $\bar{m}_x = \text{mean}(x)$

>  $\bar{m}_x$

[1] 12.107

> variance =  $(n-1) * \text{var}(x) / n$

> variance

[1] 0.019521

>  $s_d = \sqrt{\text{variance}}$

>  $s_d$

[1] 0.139776

>  $m_0 = 12.5$

>  $t = (\bar{m}_x - m_0) / (s_d / \sqrt{n})$

>  $t$

[1] -8.894909

> pvalue =  $2 * (1 - \text{pnorm}(\text{abs}(t)))$

> pvalue

[1] 0

$\therefore$  The value is less than 0.05 the value is accepted

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## PRACTICAL - 6

Ques: Large sample test.

- (a) Let the population mean the amount spent by customers in a restaurant is 250. A sample of 100 customers is selected. Sample mean is calculated as 275 and SD as 30. Test the hypothesis that population mean is 250 or not at 5% level of significance.
- (b) In a random sample of 100 students it is found that 75 use blue pen. Test the hypothesis that population proportion is 0.8 at 1% level of significance.

a)

$$\rightarrow H_0: \mu = 275 \text{ against } H_1: \mu \neq 275$$

$$\rightarrow \mu_0 = 250$$

$$\rightarrow \bar{x} = 275$$

$$\rightarrow n = 100$$

$$\rightarrow S_d = 30$$

$$\rightarrow z_{\text{cal}} = (\bar{x} - \mu_0) / (S_d / \sqrt{n})$$

$$\rightarrow z_{\text{cal}}$$

$$\rightarrow 2.333333$$

Q3

> pvalue =  $2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

> pvalue

[1] 0

> zcal["zcal:", "zcal"]

> zcal: 8.3333

> zcal["pvalue:", "pvalue"]

> pvalue: 0

$\therefore$  pvalue = 0 < 0.05 use reject  $H_0$  at 5% level of significance.

Q.2)  $H_0: p = 0.8$  against  $H_1: p \neq 0.8$

> P = 0.8

> Q = 1 - P

> P = 750 / 1000

> n = 1000

> zcal =  $(p - D) / (\sqrt{PQ/n})$

> zcal

[1] -3.952847

> pvalue =  $2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

> pvalue

[1] 7.72268e-05

$\therefore$  The value is less than 0.01, we reject !

A random sample of size 1000 & 2000 are drawn from two populations with same  $S.D = 2.5$ . The sample means are 67.5 & 68 resp. Test the hypothesis  
 $H_0: \mu_1 = \mu_2$  against  $H_1: \mu_1 \neq \mu_2$  at 5% level of significance.

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(a) The study of noise level in two hospital's is given below. Test the claim that the two hospital have same level of noise at one(1%) level of significance

	Hospital (A)	Hospital (B)
Size	84	39
Mean	61.2	59.4
SD	7.9	7.5

(b) In a sample of 600 student in a college 400 use blue ink in another college from the sample of 900 students 450 use blue ink. Test the hypothesis that the proportion of students using blue ink in two college are equal or not at 1% level of significance

Q.3)  $\rightarrow H_0: \mu_1 = \mu_2$  vs  $H_1: \mu_1 \neq \mu_2$

> n1 = 1000

> n2 = 2000

> mx1 = 67.5

> mx2 = 68

> sd1 = 2.5

> sd2 = 2.5

> zcal =  $(\bar{m}_1 - \bar{m}_2) / \sqrt{(\text{sd1}^2/n_1) + (\text{sd2}^2/n_2)}$

> zcal

[1] -5.163978

> zcal ("zcal:", zcal)

zcal: -5.163978

> pvalue = 2 \* (1 - pnorm(abs(zcal)))

> pvalue

[1] 2.417564e-07

> cat ("pvalue:", pvalue)

> pvalue: 2.417564e-07

∴ Rejected.

Q.4) > n1 = 84

> n2 = 34

> mx1 = 61.2

> mx2 = 59.4

> sd1 = 7.9

> sd2 = 7.5

> zcal =  $(\bar{m}_1 - \bar{m}_2) / \sqrt{(\text{sd1}^2/n_1) + (\text{sd2}^2/n_2)}$

> zcal

[1] 1.162528

> cat ("zcal:", zcal)

zcal: 1.162528

>pvalue =  $2^* (1 - pnorm(\text{abs}(zcal)))$

>pvalue

[1] 0.2950211

$\therefore$  The value is greater than 0.01, we accept the value.

Q5) >n1 = 600

>n2 = 300

>p1 = 400/600

>p2 = 450/300

>zcal =  $(p1 - p2) / \sqrt{p * q (1/n1 + 1/n2)}$

>zcal

[1] 6.381534

>pvalue =  $2^* (1 - pnorm(\text{abs}(zcal)))$

>pvalue

[1] 1.753222e-10

$\therefore$  The value is less than 0.01. The value is rejected.

Q6) First Sample size  $H_0: p_1 = p_2$  vs  $H_1: p_1 \neq p_2$ ,  $n_1 = 200$ ,  $n_2 = 200$

$p_1 = 44/200$ ,  $p_2 = 30/200$

>n1 = 200, >n2 = 200, >p1 = 44/200 >p2 = 30/200

>p =  $(n1 * p1 + n2 * p2) / (n1 + n2)$

>q = 1 - p

>zcal =  $(p1 - p2) / \sqrt{p * q (1/n1 + 1/n2)}$

>zcal

[1] 1.802741

>pvalue =  $2^* (1 - pnorm(\text{abs}(zcal)))$

>pvalue

[1] 0.07142888

$\therefore$  Accepted greater than 0.05

## PRACTICAL No. 7

Topic: Small Sample test

- The marks of 10 students are given by 66, 63, 66, 67, 68, 69, 70, 71, 72 test the hypothesis that the sample come from the population of 66.

$$H_0: \mu = 66$$

$$\rightarrow x = (66, 63, 66, 67, 68, 69, 70, 71, 72)$$

$t$ -test (1)

One Sample t-test

data: x

$$t = 68.319, df = 9, pvalue = 1.558 \times 10^{-13}$$

alternative hypothesis

True mean is not equal to 0

95 percent confidence interval

$$65.65171 \quad 70.14829$$

Sample estimates

means of x

$$67.9$$

∴ The pvalue is less than 0.05 we reject the hypothesis at 5% level of significance

Two groups of students scored the following marks. Test the hypothesis that there is no significant difference between 2 groups

GR1 - 18, 22, 21, 17, 20, 17, 23, 20, 22, 21

GR2 - 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

H<sub>0</sub>: There is no difference b/w 2 groups.

>x=c(18, 22, 21, 17, 20, 17, 23, 20, 22, 21)

>y=c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)

>t.test(x, y)

which two sample t-test

data: x and y

t = 2.2573, df = 16.376, pvalue = 0.03798

alternative hypothesis:

True difference in means is not equal to 0 to 95 percent confidence interval:

0.1628005 5.0371795

Sample estimate:

mean of x mean of y

20.1 17.5

>pvalue = 0.03798

>if(pvalue > 0.05) {cat("accept H<sub>0</sub>")}

else {cat("reject H<sub>0</sub>")}

reject H<sub>0</sub>.

## PAIRED T-TEST

3) The sales data of 6 shops before & after a special campaign are given below.

Before: 53, 28, 31, 48, 50, 42

After: 58, 29, 30, 55, 56, 45

Test the hypothesis that the campaign is effective or not.

H<sub>0</sub>: There is no significant difference of sales before & after campaign.

> X = c(Before)

> Y = c(After)

> t.test(x, y, paired = T, alternative = "greater")

Paired t-test

data: X & Y

t = -2.7815, df = 5, pvalue = 0.9806

alternative hypothesis:

True difference in means is greater than 0  
95 percent confidence interval:

-6.035547 inf

Sample estimates

mean of the difference

-3.5

∴ pvalue is greater than 0.05, we accept the hypothesis at 5% level of significance.

Following are the weight before & after the diet program. Is the diet program effective?

Before : 120, 125, 115, 130, 123, 119

after : 100, 114, 95, 90, 115, 99

H<sub>0</sub>: There is no significant difference.

> y = c(Before)

> z = c(after)

> t.test(x, y), paired = T, alternative = "less")  
paired t-test

data: x & y

t = -4.3458, df = 5, p-value = 0.0063

alternative hypothesis: true difference in means is less than 0.

95 percent confidence interval:

-inf 29.0295

sample estimates:

mean of the differences

19.83333

$\therefore$  p value is greater than 0.05 we accept the hypothesis at 5% level of significance.

5) 2 medicines are applied to two groups of patient resp.

$$GR1 = 10, 12, 13, 11, 14$$

$$GR2 = 8, 9, 12, 14, 15, 10, 5$$

Is there any significance difference b/w 2 medicines

H<sub>0</sub>: There is no significance difference

> x = c(grp1)

> y = c(grp2)

> t.test(x, y)

t = 0.80384, df = 9.7594, pvalue = 0.4406

alternative hypothesis: true difference in means is not equal to 0

95 percent confidence interval

- 0.9698553 4.2981886

Sample estimates:

mean of x mean of y

12.0000 10.3333

∴ pvalue is greater than 0.05 we accept the hypothesis at 5% level of significance

(g)

PRACTICAL-8

18

$$H_0: \mu = 55, H_1: \mu \neq 55$$

$$n = 100$$

$$\bar{m}_x = 52$$

$$m_0 = 55$$

$$s_d = 7$$

$$z_{\text{cal}} = (\bar{m}_x - m_0) / (s_d / \sqrt{n})$$

$$z_{\text{cal}}$$

$$[1] - 4.28714$$

$$p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

$$p\text{value}$$

$$[1] 1.82153 < 0.05$$

we reject

$$2) p = 350/700 \quad H_0: p = 1/2$$

$$n = 700$$

$$q = 1 - p$$

$$z = (p - P) / (s_q \sqrt{(p * q / n)})$$

$$z$$

$$[1] 6$$

$$p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

$$p\text{value}$$

$$[1] 1$$

Accept the pvalue at  $H_0: p = 1/2$

3)  $n_1 = 80$   
     $n_2 = 150$   
     $p_1 = 0.02$   
     $p_2 = 0.6$   
     $P = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$   
     $P$

[1] 0.014

$q = 1 - P$

$Z = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$

$Z$

[1] 0.003474737

$PV = 2 * (1 - \text{pnorm}(\text{abs}(Z)))$

$PV$

[1] 0.03708364

we reject

④  $H_0: \mu = 100$

$m_x = 99 \quad sd = 8$

$m_0 = 100 \quad n = 400$

$Z = (m_x - m_0) / (sd / \sqrt{n})$

$Z$

[1] -2.5

$PV = 2 * (1 - \text{pnorm}(\text{abs}(Z)))$

$PV$

[1] 0.0241933

we reject.

$\text{xx} = (63, 63, 68, 69, 71, 71, 72)$   
 $\text{t.test}(x)$

One Sample t-test

$t = 4.794$ , df = 6, p-value = 5.922e-09

alternative hypothesis:

$64 < \text{mean of } x$

mean of  $x$

68.14286

We reject  $H_0$

c)  $H_0: \mu = 100$

$\text{mu} = 1200$

$\text{Mx} = 1150$

$z = (\text{Mx} - \mu_0) / (\text{sd}(\text{sg}(\text{x})) / \sqrt{n})$

$z$

[1] -4 ✓

$p_value = 2 * (1 - pnorm(\text{abs}(z)))$

$p_value$

[1] 6.334248e-05

We reject

ep

7)  $H_0: \sigma_1 = \sigma_2$

>  $x = (166, 67, 75, 76, 82, 84, 88, 90, 92)$

>  $y = (164, 66, 74, 78, 82, 87, 92, 93, 95, 97)$ .

> var.test(x, y)

f test to compare two variances

t = 0.70686, numdf = 8, denomdf = 10, pvalue = 0.6305

45 percent confidence interval

0.1833662 3.086053

Sample estimates

ratio of variances

0.7068567

We accept  $H_0: \sigma_1 = \sigma_2$ .

8)

> n1 = 200

> n2 = 300

> p1 = 44/200

> p2 = 56/300

> p =  $(n1 * p1 + n2 * p2) / (n1 + n2)$

> q = 1 - p

> q

[1] 0.9128709

> PV =  $(2 * (1 - pnorm(abs(z))))$

> PV

[1] 0.3613104

P

0.2

we accept  $H_0$ .

(8)

## PRACTICAL - 9

50

### Chi-Square test & ANOVA

Q] Use the following data test whether the condition of home and condition of child are independent or not.

→ condition of home

	Clean	Dirty
Clean	70	50
Fairly clean	80	20
Dirty	35	45

→ H<sub>0</sub>: condition of home & child are independent

→  $x = ((70, 80, 35, 50, 20, 45))$

→  $m = 3$

→  $n = 2$

→  $y = \text{matrix}(x, nrow = m, ncol = n)$

→  $y$

[1] [1,2]

[1,1] 70 50

[2,1] 80 20

[3,1] 35 45

→  $pV = \text{chisq.test}(x)$

→  $pV$

Person's chi-squared test

data:  $x$

$\chi^2$ -squared = 25.646, df = 2, p-value = 2.698e-0.6

∴ H<sub>0</sub> is rejected, since pV is less than 0.05.

Q2

2) Test the hypothesis the vaccination & disease are independent or not.

Diseases	Affected	Not affected
Affected	70	46
Not affected	35	37

$H_0$ : Condition of disease & vaccination are independent

>  $X = ((70, 46, 35, 37))$

>  $m = 2$

>  $n = 2$

>  $Y = \text{matrix}(X, \text{ncol} = m, \text{nrow} = n)$ .

>  $Y$

[1,1]	[1,2]
70	46
[2,1]	35
37	

>  $Pv = \text{chisq.test}(Y)$

>  $Pv$

$\chi^2\text{-squared} = 2.8275, \text{df} = 1, P\text{-value} = 0.1545$

$H_0$  is accepted. Since  $Pv$  is more than 0.05

3) Perform a ANOVA for the following data

Type	Observation
A	50, 52
B	53, 55, 53
C	60, 58, 57, 56
D	52, 54, 54, 55

$H_0$ : The means are equal for A, B, C & D

>  $x_1 = c(50, 52)$

>  $x_2 = c(53, 55, 53)$

>  $x_3 = c(60, 58, 57, 56)$

>  $x_4 = c(52, 54, 54, 55)$

>  $d = \text{stack}(\text{list}(b1 = x1, b2 = x2, b3 = x3, b4 = x4))$

> names(d)

[1] "values" "ind"

> ~~one~~way.test(values ~ ind, data = d, var.equal = T)  
one-way analysis of means

data: values ~ ind

F = 11.735, num df = 3, denom df = 9, p-value =

> anova = aov(values ~ ind, data = d)

Summary(aov)

	df	Sum Sq	Mean Sq	fvalue	Pr(>f)
ind	3	71.06	23.688	11.73	0.00183**
Residuals	9	18.17	2.019		

Signif codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1

4) The following data gives the life of the tire of 4 brands.

TYPE	LIFE
A	20, 23, 18, 17, 18, 22, 24
B	19, 15, 17, 20, 16, 17
C	21, 19, 22, 17, 20
D	15, 14, 16, 18, 14, 16

-  $H_0$ : The average life of A, B, C, D are equal  
 >  $X1 = c(20, 23, 18, 17, 18, 22, 24)$   
 >  $X2 = c(19, 15, 17, 20, 16, 17)$   
 >  $X3 = c(21, 19, 22, 17, 20)$   
 >  $X4 = c(15, 14, 16, 18, 14, 16)$   
 >  $d = \text{stack}(\text{list}(b1=X1, b2=X2, b3=X3, b4=X4))$   
 >  $\text{names}(d)$   
 >  $\text{oneway.test}(\text{values} ~ \text{ind}, \text{data}=d, \text{var.eqv.al}=1)$   
 one way analysis of means

data :

$f = 6.8445$ , num df = 3, denom df = 20,  
 pvalue = 0.002349

>  $\text{anova} = \text{aov}(\text{values} ~ \text{ind}, \text{data} = d)$

Summary (anova)

	df	Sum Sq	Mean Sq	f value	P < (sf)
ind	3	91.44	30.479	6.545	0.002349
Residual	20	89.06	4.453		

How to import a CSV file in R software  
 > y = read.csv("C:/Users/admin/Desktop/stats.csv")  
 > print(x)

	stats	Maths
1	40	60
2	45	43
3	42	47
4	15	20
5	37	25
6	36	27
7	49	57
8	59	/
9	20	58
10	27	25

```

> am = mean(x$stats)
> am
[1] 37
> n = length(x$stats)
> sd = sqrt((n - 1) * var(x$stats)) / n
> sd
[1] 12.64911
> am = mean(x$maths)
> am
[1] 39.4
> sd = sqrt((n - 1) * var(x$maths)) / n
> sd
[1] 15.2
> cor(x$stats, x$maths)
[1] 0.830618

```

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