

Support Vector Machine

Extra Class



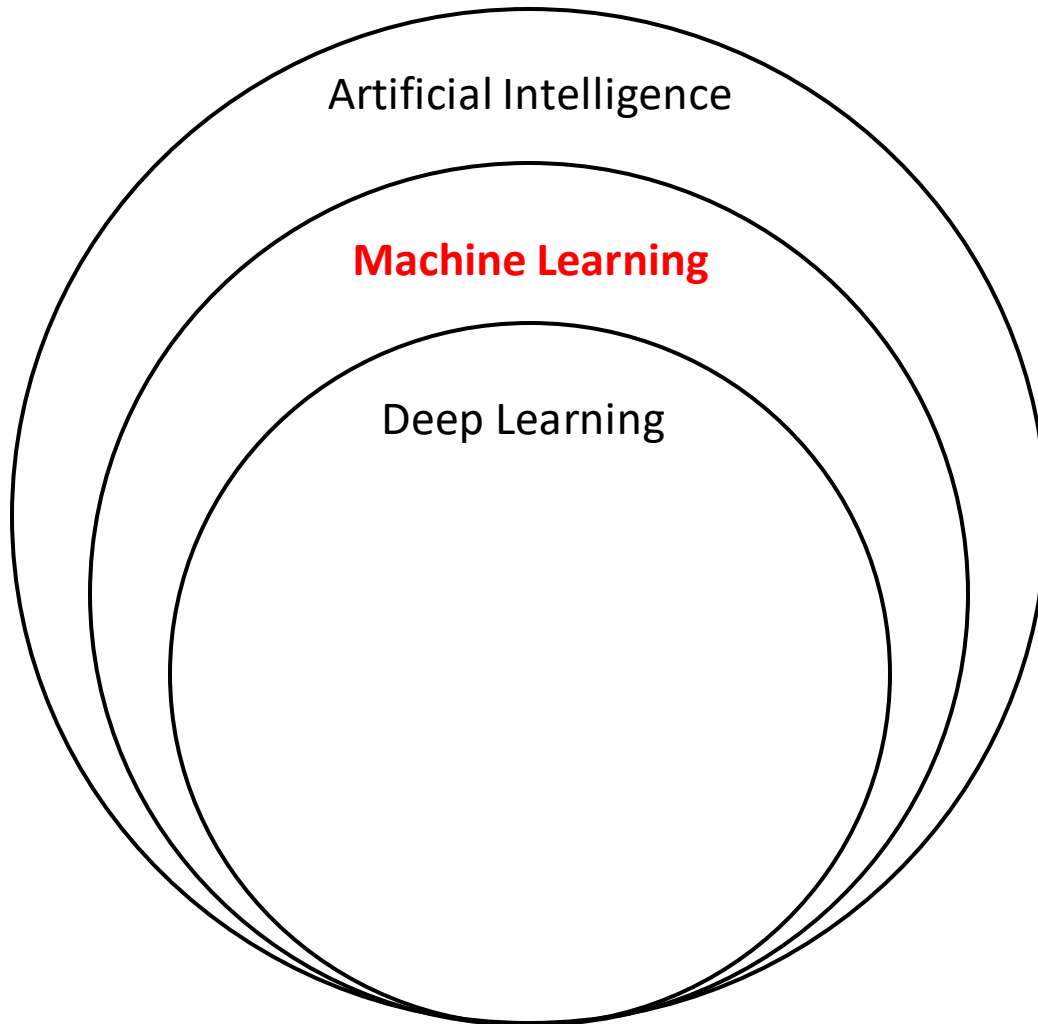
Dinh-Thang Duong – TA

Outline

- **Introduction**
- **Support Vector Machine**
- **Code Examples**
- **Question**

Introduction

❖ Getting Started



Machine Learning (ML): A branch of AI and Computer Science which focuses on the use of data and algorithms to imitate the way that humans learn, gradually improving its accuracy.

Introduction

❖ Getting Started

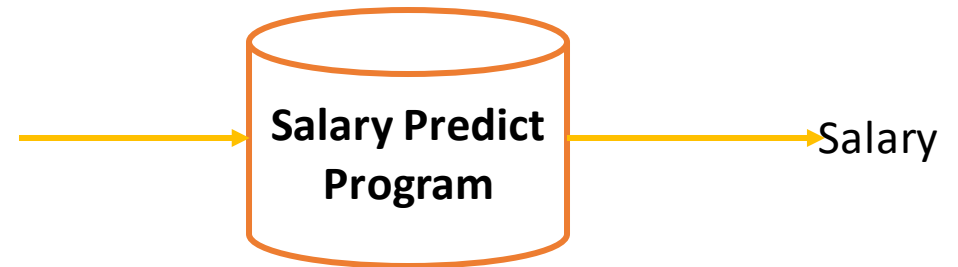
Suppose you got some dataset:

	Name	Team	Number	Position	Age	Height	Weight	College	Salary
0	Avery Bradley	Boston Celtics	0.0	PG	25.0	6-2	180.0	Texas	7730337.0
1	Jae Crowder	Boston Celtics	99.0	SF	25.0	6-6	235.0	Marquette	6796117.0
2	John Holland	Boston Celtics	30.0	SG	27.0	6-5	205.0	Boston University	NaN
3	R.J. Hunter	Boston Celtics	28.0	SG	22.0	6-5	185.0	Georgia State	1148640.0
4	Jonas Jerebko	Boston Celtics	8.0	PF	29.0	6-10	231.0	NaN	5000000.0
5	Amir Johnson	Boston Celtics	90.0	PF	29.0	6-9	240.0	NaN	12000000.0
6	Jordan Mickey	Boston Celtics	55.0	PF	21.0	6-8	235.0	LSU	1170960.0
7	Kelly Olynyk	Boston Celtics	41.0	C	25.0	7-0	238.0	Gonzaga	2165160.0
8	Terry Rozier	Boston Celtics	12.0	PG	22.0	6-2	190.0	Louisville	1824360.0
9	Marcus Smart	Boston Celtics	36.0	PG	22.0	6-4	220.0	Oklahoma State	3431040.0
10	Jared Sullinger	Boston Celtics	7.0	C	24.0	6-9	260.0	Ohio State	2569260.0
11	Isaiah Thomas	Boston Celtics	4.0	PG	27.0	5-9	185.0	Washington	6912869.0
12	Evan Turner	Boston Celtics	11.0	SG	27.0	6-7	220.0	Ohio State	3425510.0
13	James Young	Boston Celtics	13.0	SG	20.0	6-6	215.0	Kentucky	1749840.0

And you want to make a program to automatically predict value of 1 column based on others.

Input

Name,
Team,
Number,
Position,
Age,
Height,
Weight,
College



Output

Salary

$X(\text{Name, Team, Number, Position, Age, Height, Weight, College}) \rightarrow Y(\text{Salary})$

Introduction

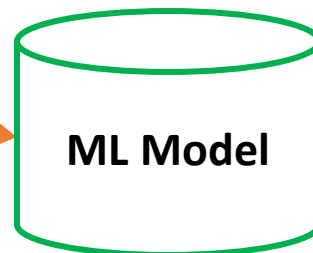
❖ Getting Started

Input X

Output Y

	Name	Team	Number	Position	Age	Height	Weight	College	Salary
0	Avery Bradley	Boston Celtics	0.0	PG	25.0	6-2	180.0	Texas	7730337.0
1	Jae Crowder	Boston Celtics	99.0	SF	25.0	6-6	235.0	Marquette	6796117.0
2	John Holland	Boston Celtics	30.0	SG	27.0	6-5	205.0	Boston University	NaN
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4	Jonas Jerebko	Boston Celtics	8.0	PF	29.0	6-10	231.0	NaN	5000000.0
5	Amir Johnson	Boston Celtics	90.0	PF	29.0	6-9	240.0	NaN	2000000.0
6	Jordan Mickey	Boston Celtics	55.0	PF	21.0	6-8	235.0	LSU	1170960.0
7	Kelly Olynyk	Boston Celtics	41.0	C	25.0	7-0	238.0	Gonzaga	2165160.0
8	Terry Rozier	Boston Celtics	12.0	PG	22.0	6-2	190.0	Louisville	1824360.0
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13	James Young	Boston Celtics	13.0	SG	20.0	6-6	215.0	Kentucky	1749840.0

Using this data to
“train” an ML Model



Input

Name,
Team,
Number,
Position,
Age,
Height,
Weight,
College



Output

Salary

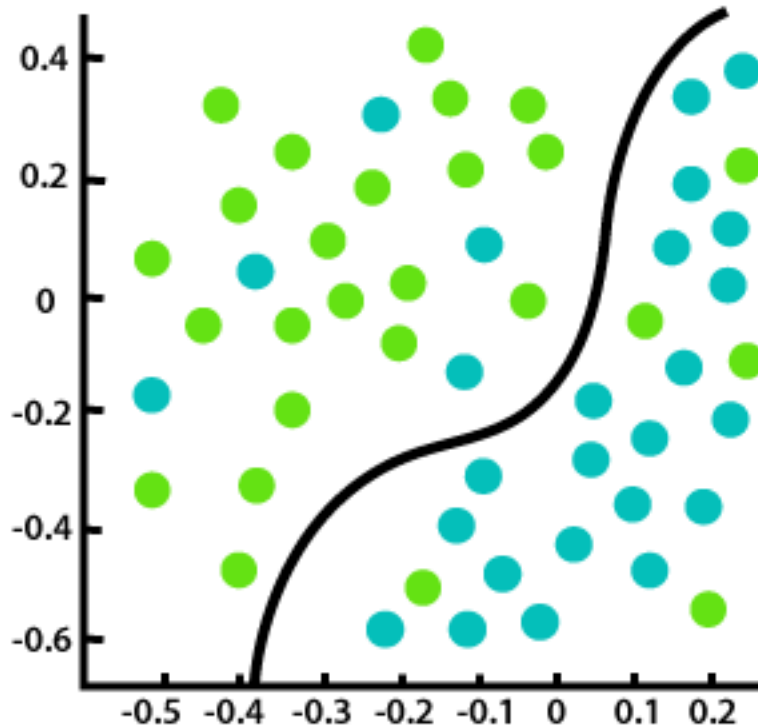
Use the trained model to predict
Salary based on any given input

Since we **use a labeled dataset to train** ML Model.

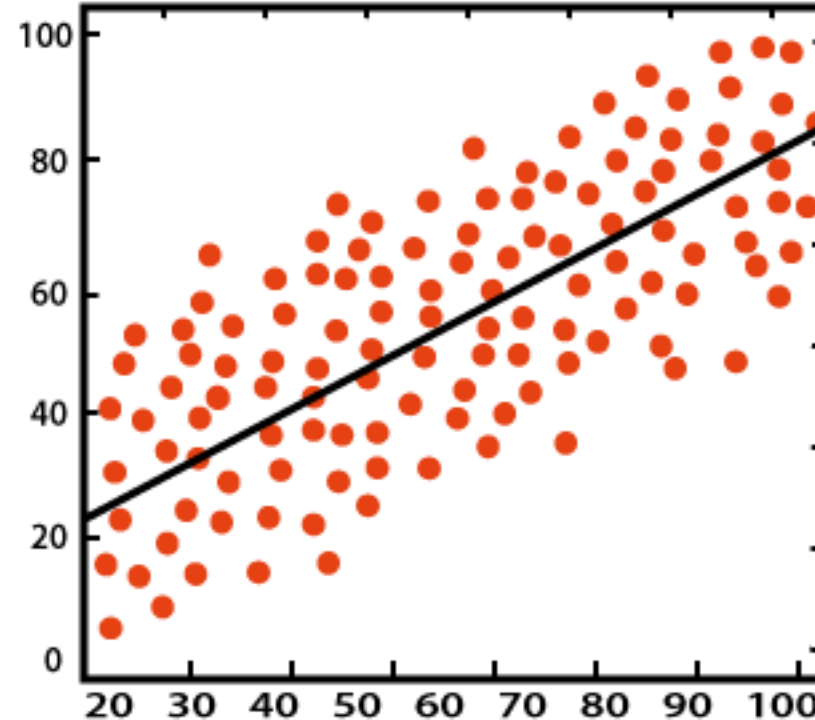
=> This is called **Supervised-learning**.

Introduction

❖ Supervised Learning



Classification



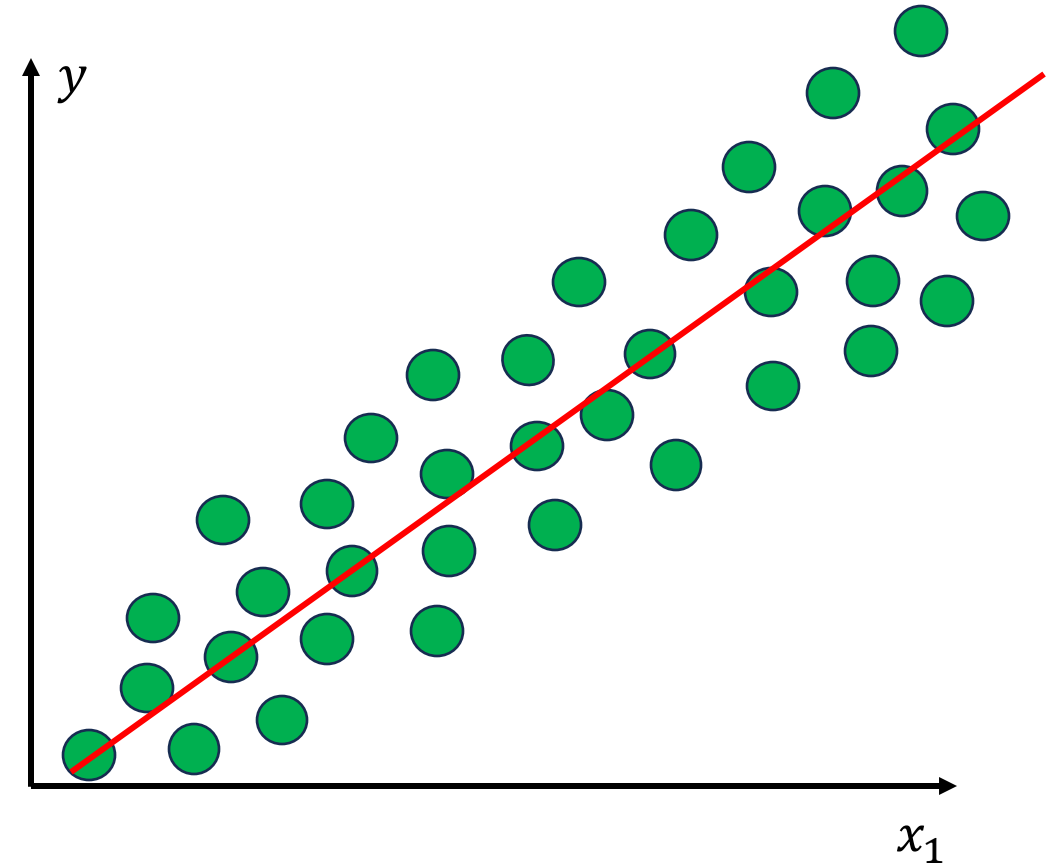
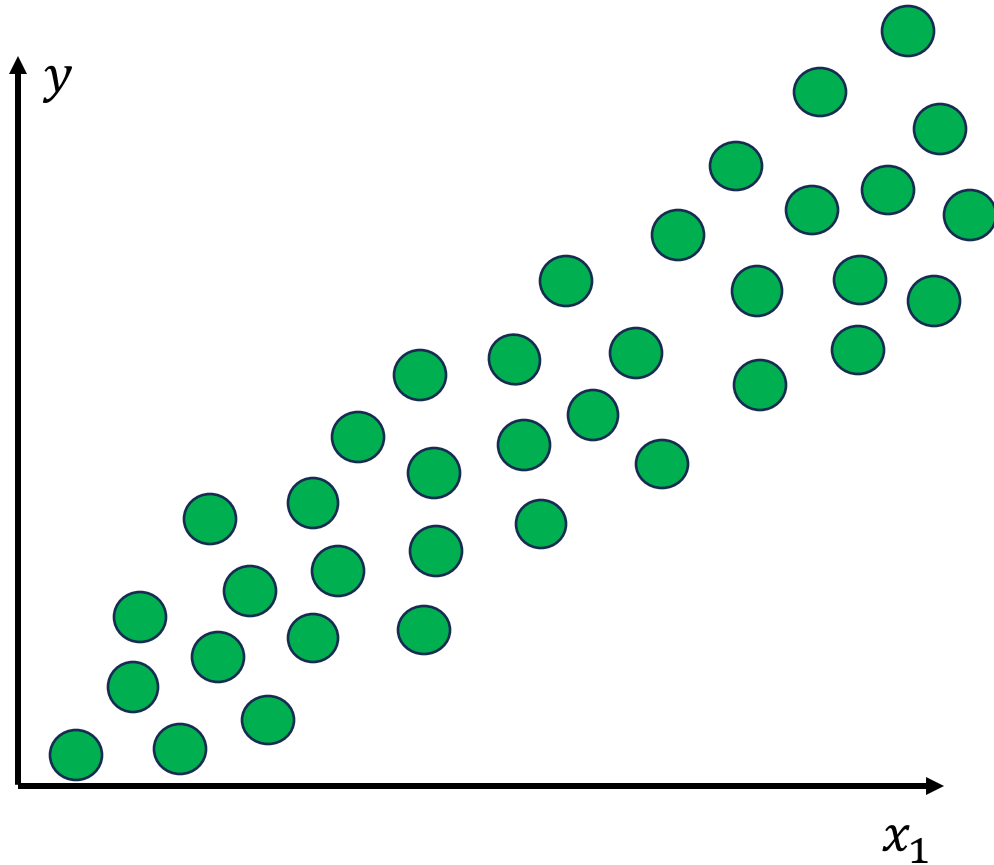
Regression

In ML Supervised-learning algorithms, we often deal with Regression and Classification

Introduction

❖ Supervised Learning: Regression

Regression: A task involving predicting a **continuous value** based on given inputs.

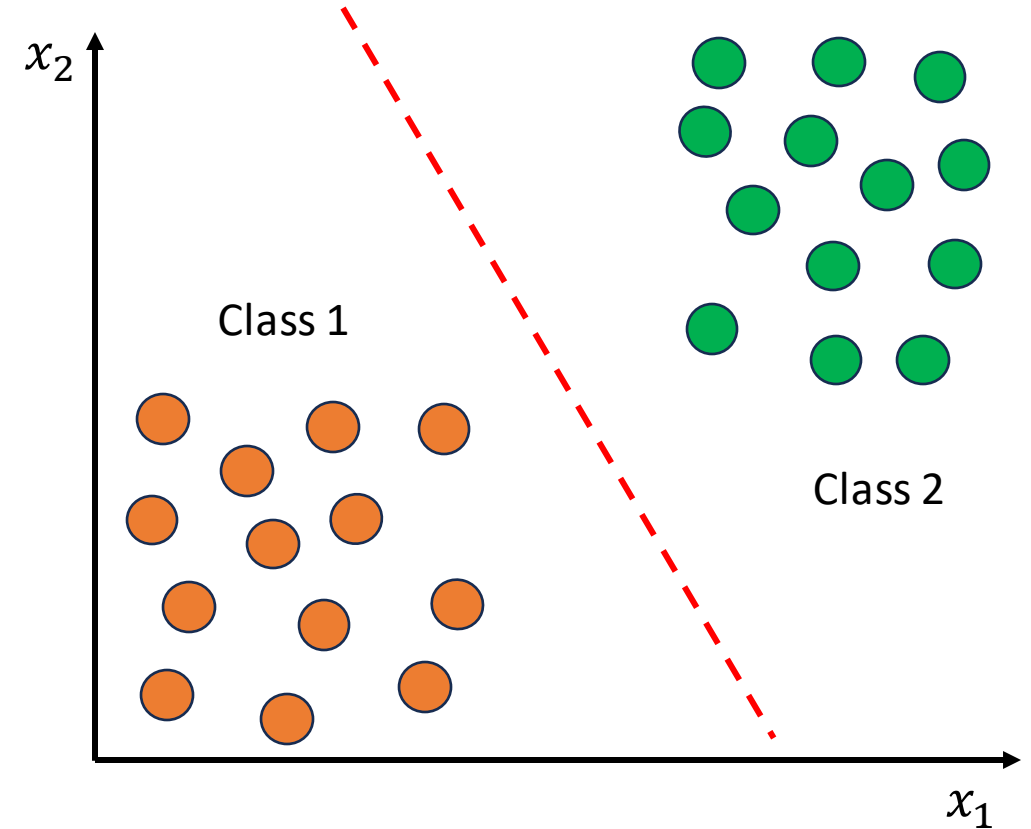
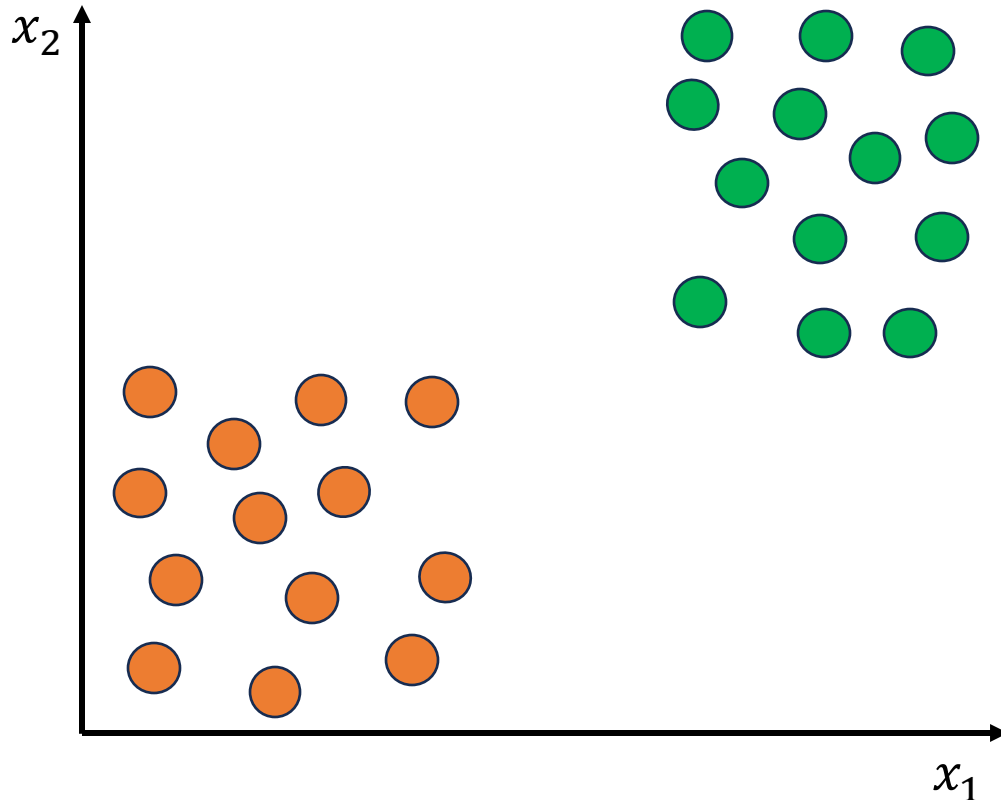


In general, we want to find the line that best fit the data distribution.

Introduction

❖ Supervised Learning: Classification

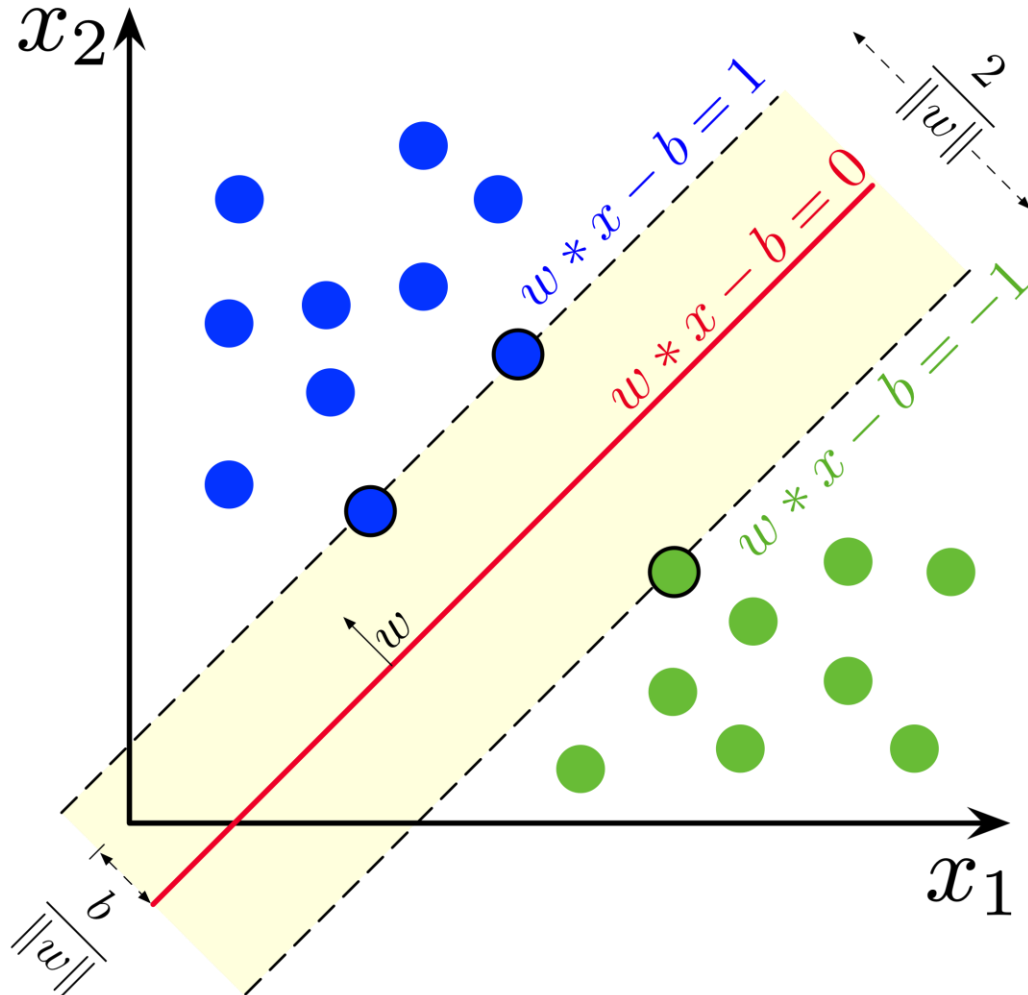
Classification: A task involving predicting a **discrete (categorical) value** based on given inputs.



In general, we want to find the line that best separates the dataset into classes.

Support Vector Machine

❖ Introduction

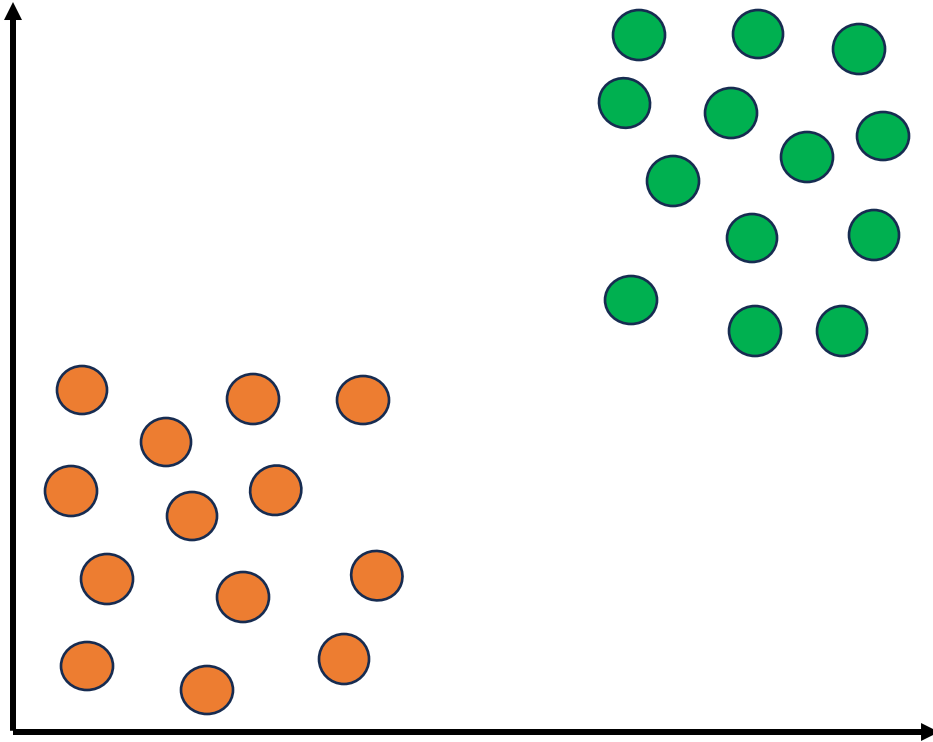


Support Vector Machine (SVM): A supervised-learning ML algorithm that works by identifying the optimal hyperplane that best separates data into different classes.

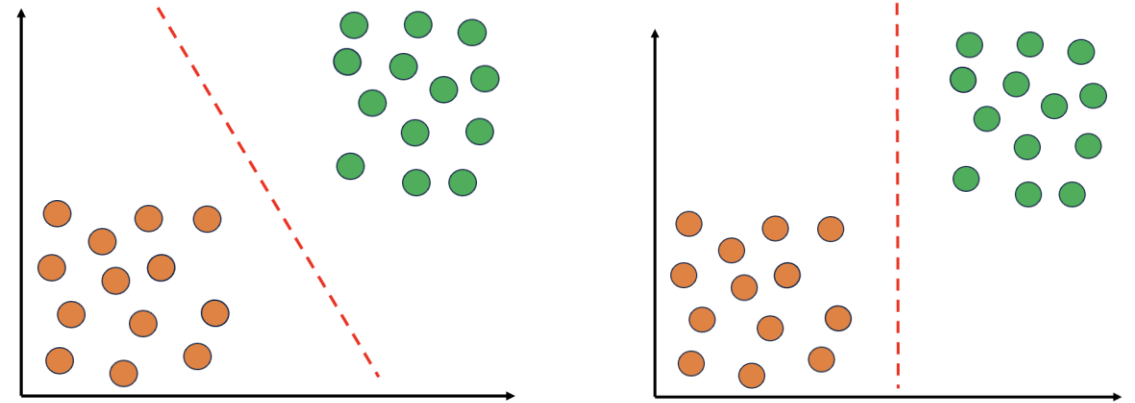
SVM was originally built for classification task (SVC) but was later modified to fit for regression task (SVR) too.

Support Vector Machine

❖ Getting Started



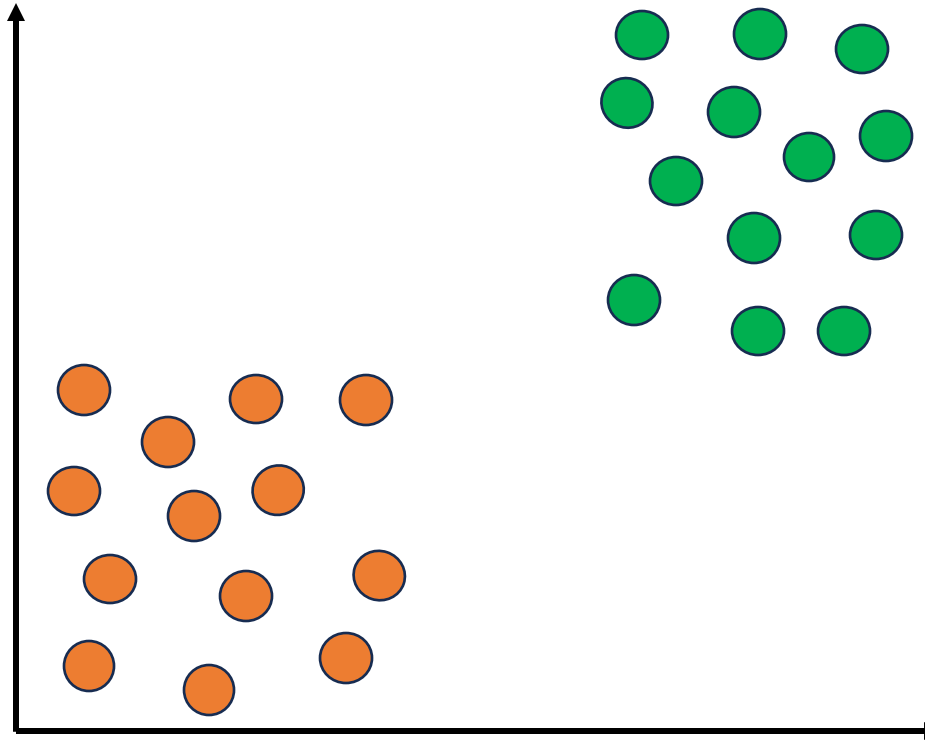
Assume we have a linearly separable dataset



Linearly separable data: A dataset that can be fully separated into classes using a single line.

Support Vector Machine

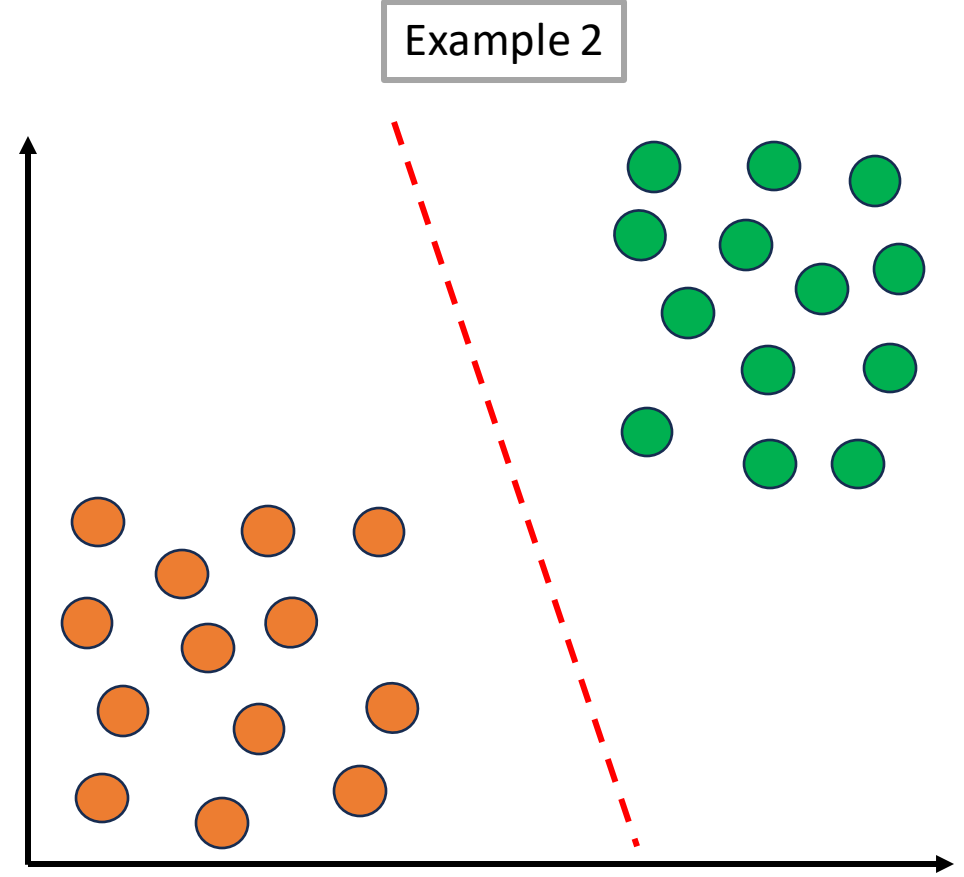
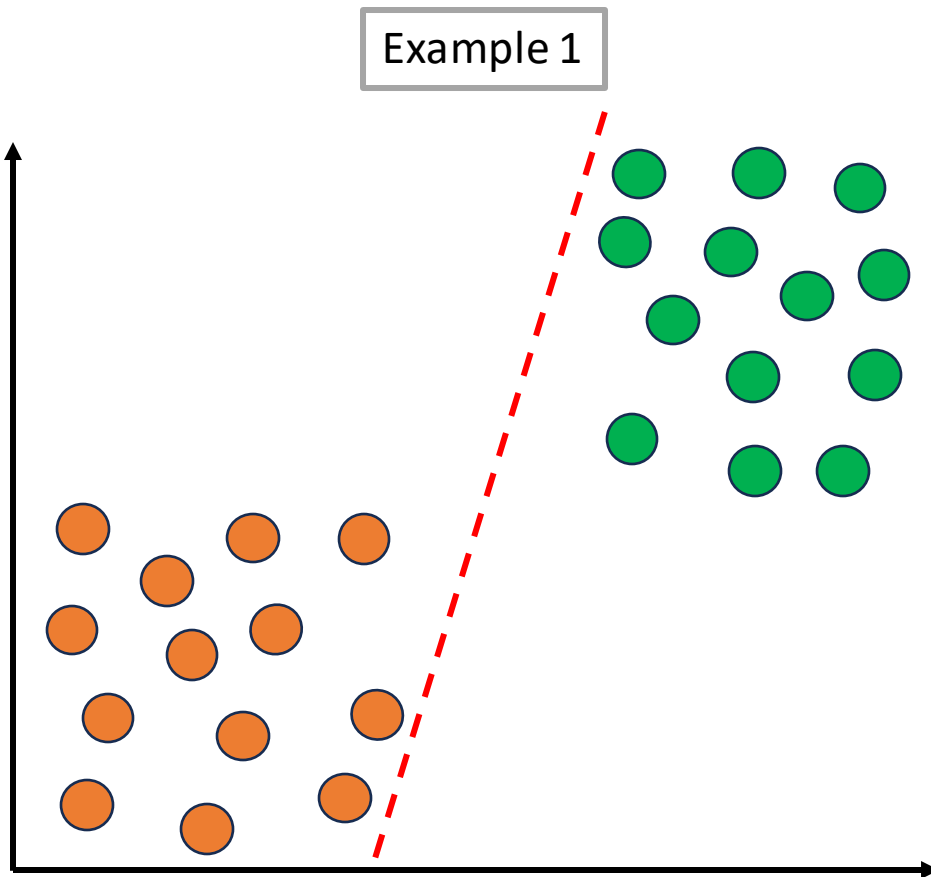
❖ Getting Started



How should we draw a line so that we can perfectly separate this dataset into 2 classes?

Support Vector Machine

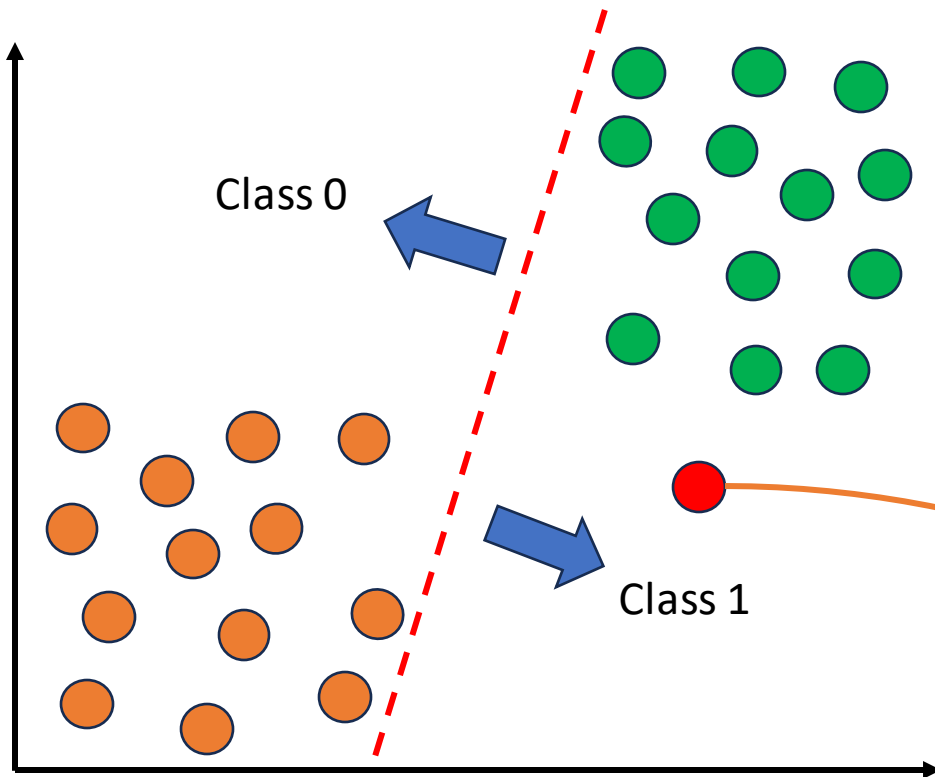
❖ Getting Started



There are many ways to draw the line

Support Vector Machine

❖ Getting Started

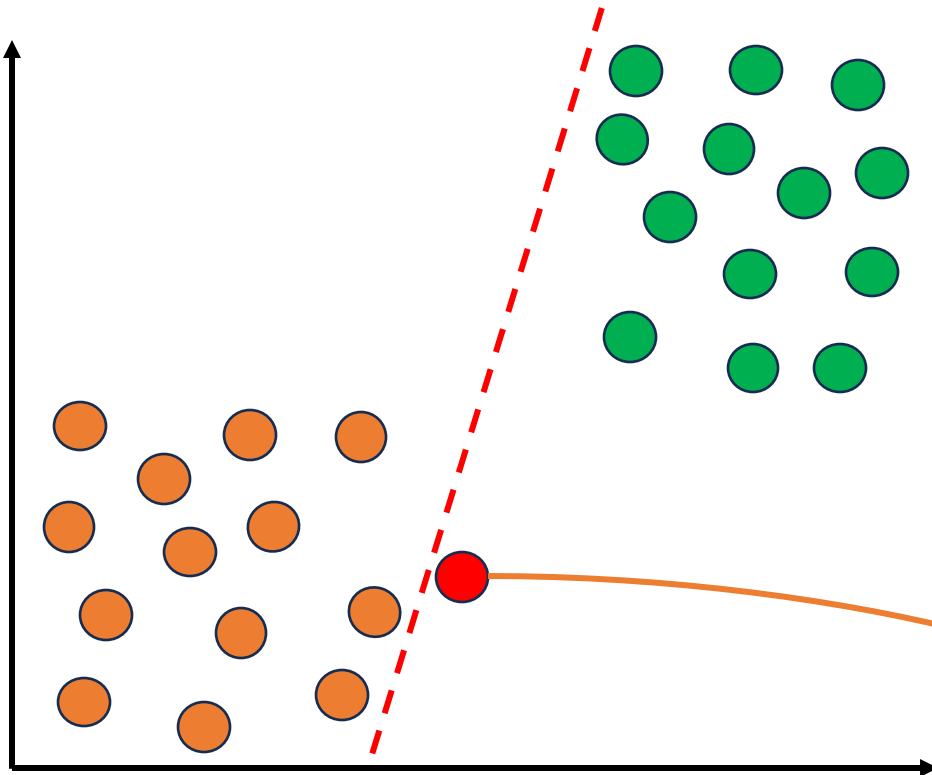


With this line, we can now determine whether a new data point belongs to Class 0 or Class 1 based on which side of the line it falls on.

This point is classified as **Class 1** since it lies on right hand side of the line.

Support Vector Machine

❖ Getting Started



However, in this situation, the result seems wrong since the point is more closer to Class 0.

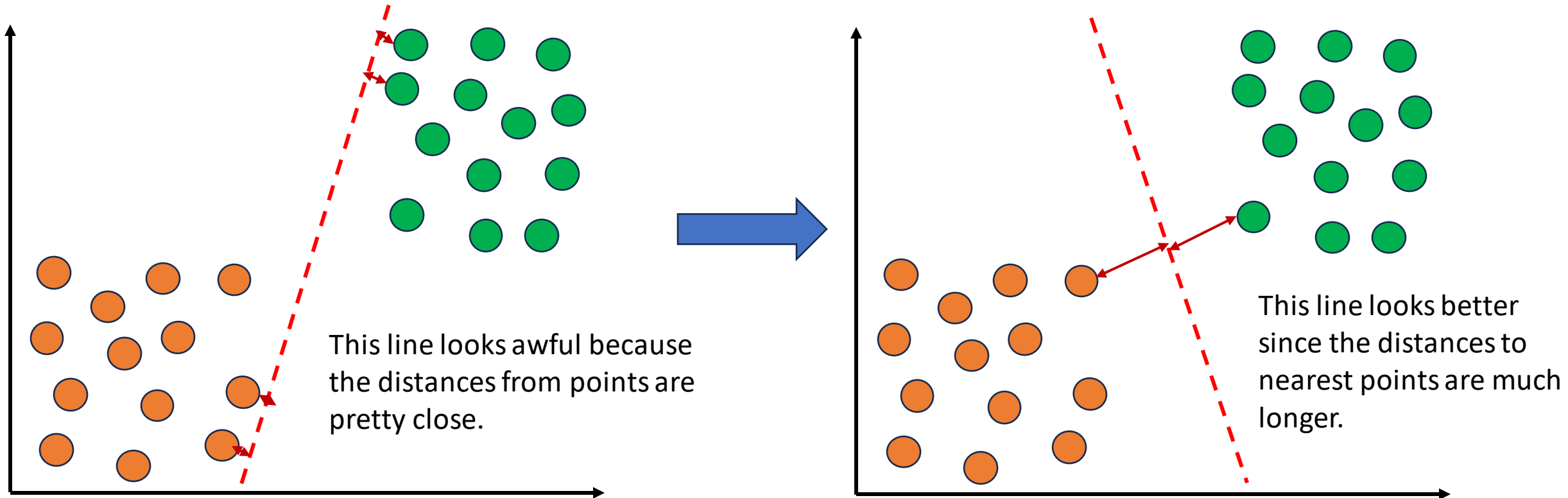
=> This line is not really optimal

What would be the best line?

This point is classified as **Class 1** since it lies on right hand side of the line.

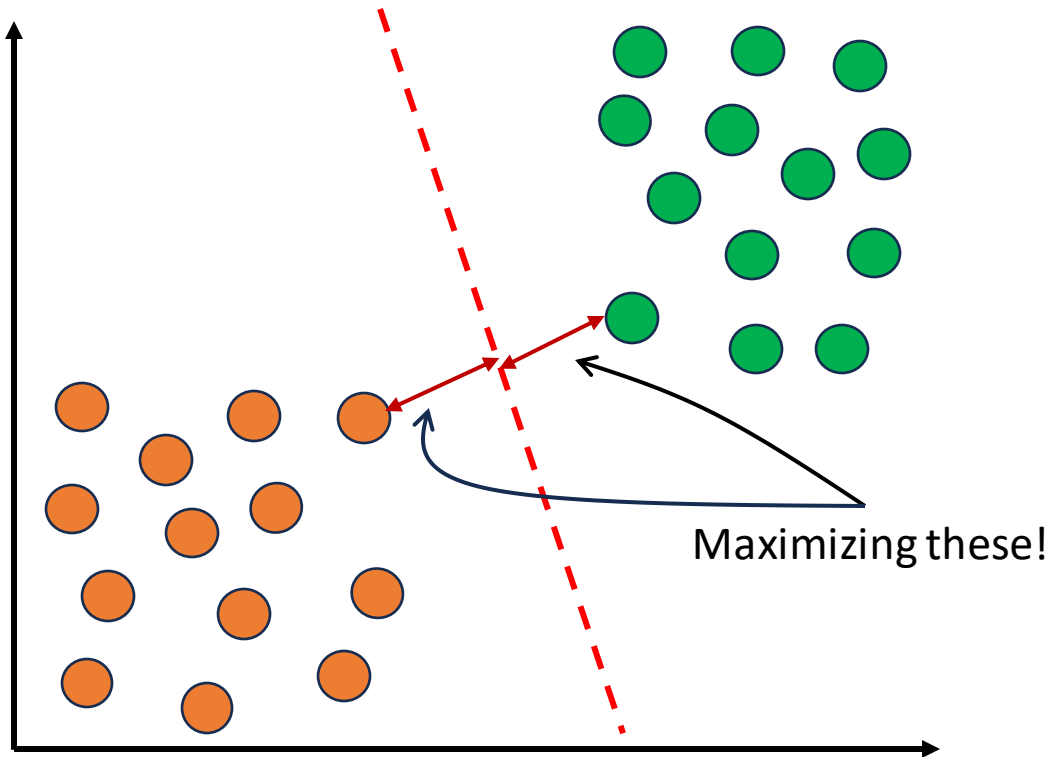
Support Vector Machine

❖ Getting Started



Support Vector Machine

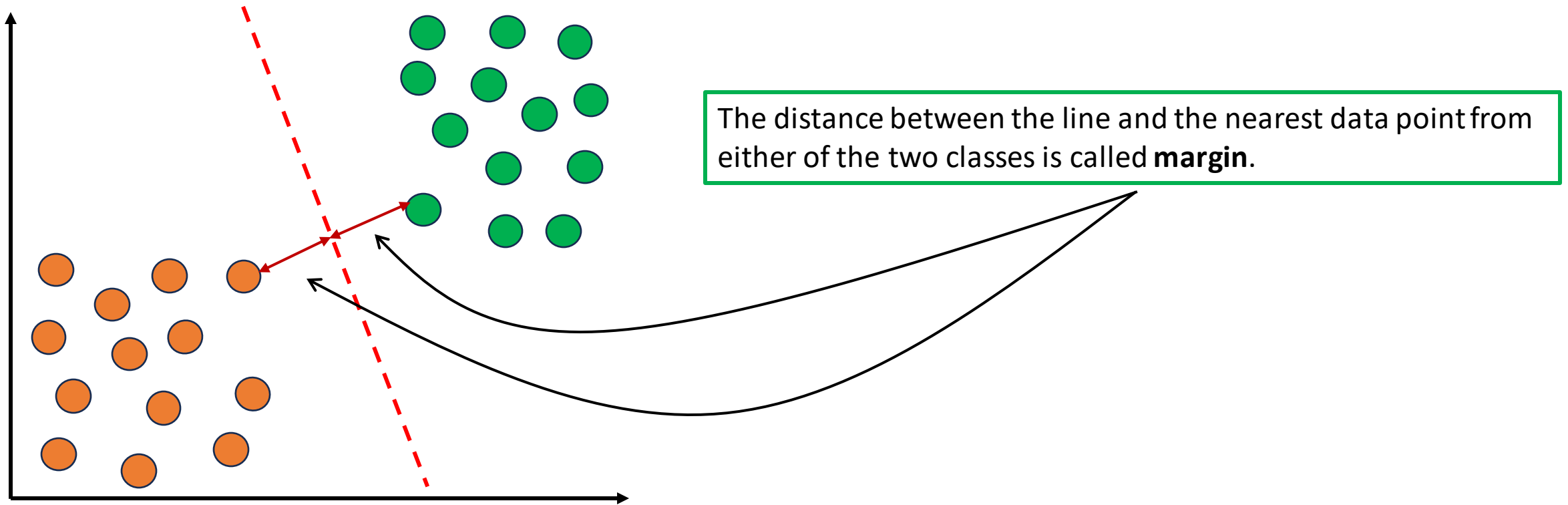
❖ Idea



Idea: Find the line that best separates the data into classes while maximizing the distances between nearest points.

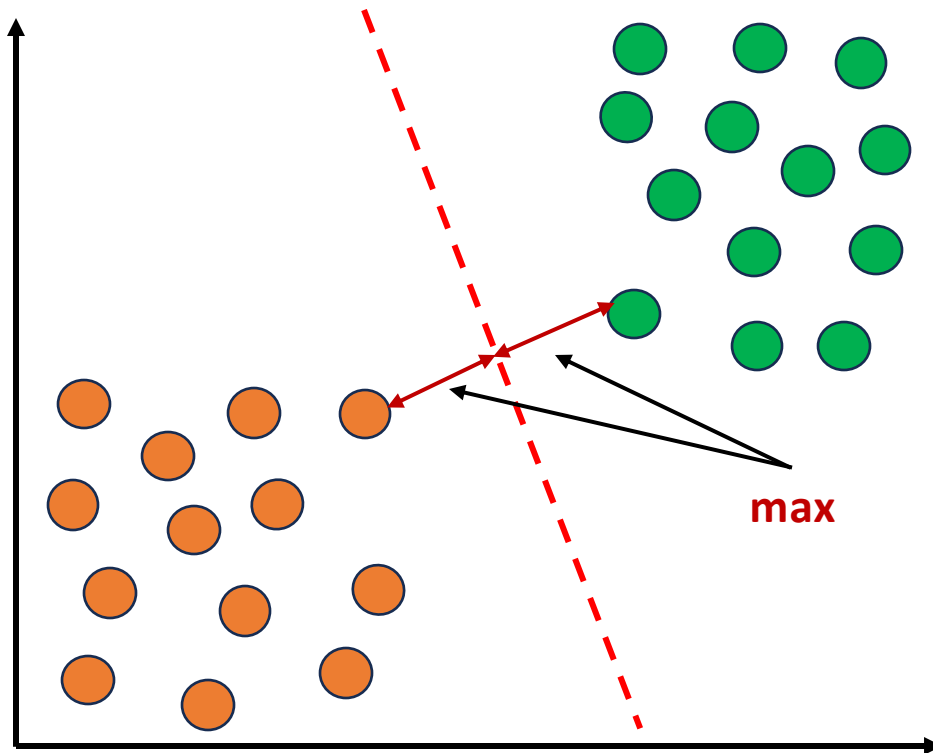
Support Vector Machine

❖ Margin



Support Vector Machine

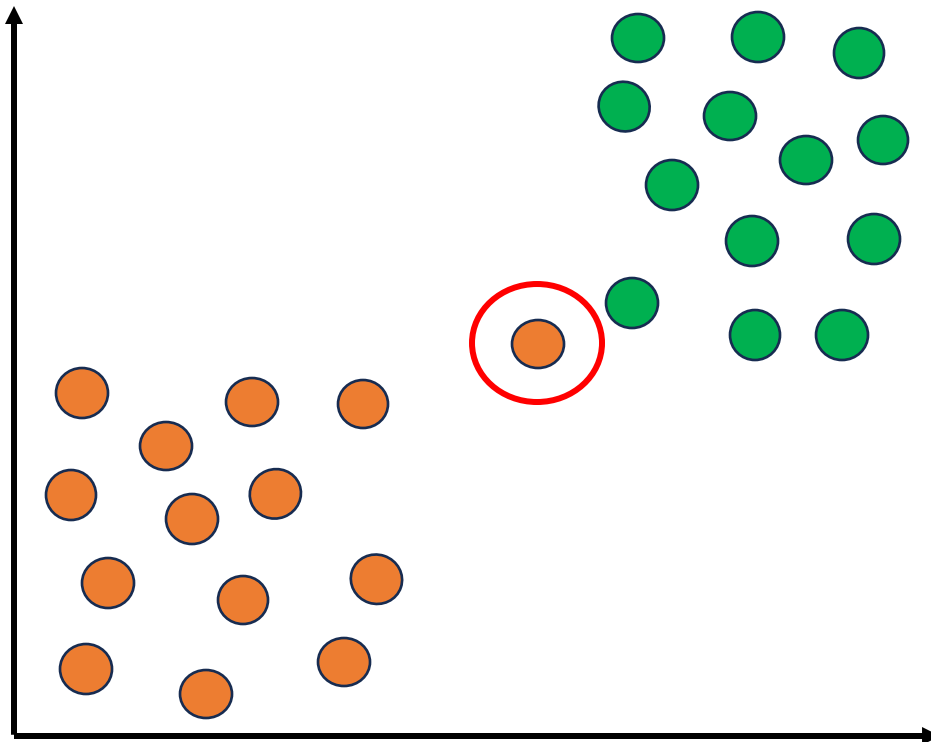
❖ Hard Margin Classifier Idea



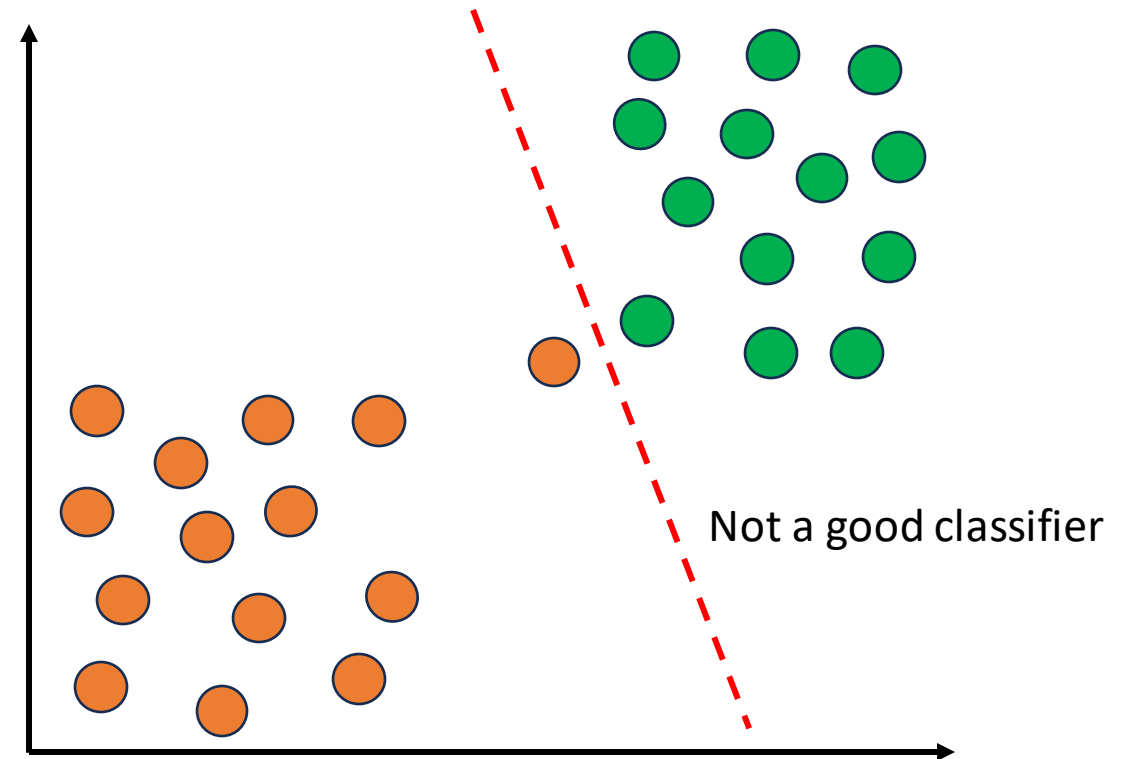
Idea: Find the line that best separates the data into classes while **maximizing the margin**. This is called **Hard Margin Classifier**.

Support Vector Machine

❖ Hard Margin Classifier Problem



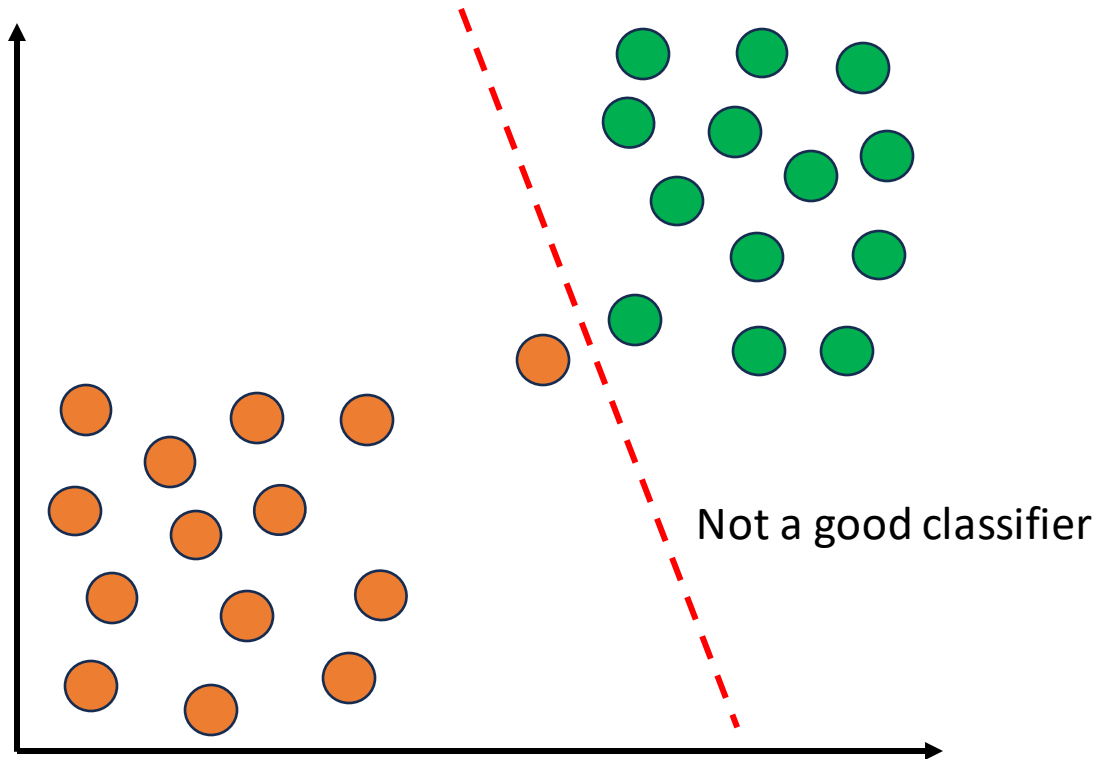
However, assume we have **an outlier**



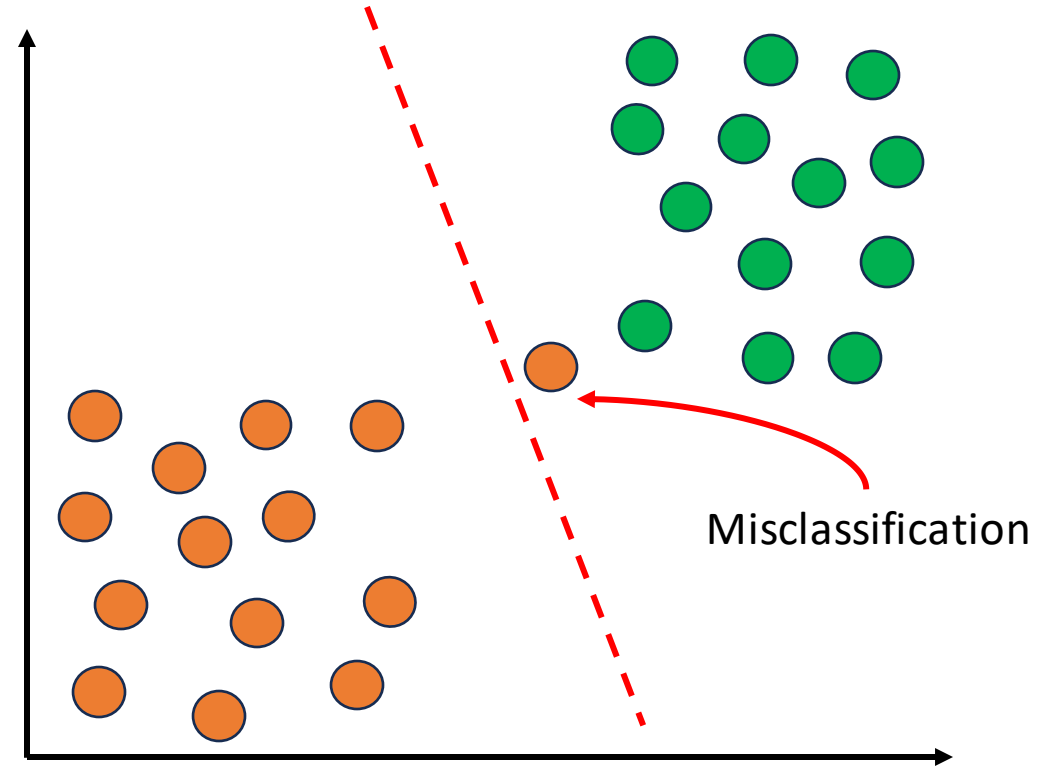
Using Hard Margin Classifier, we might have a line like this.

Support Vector Machine

❖ Soft Margin Classifier



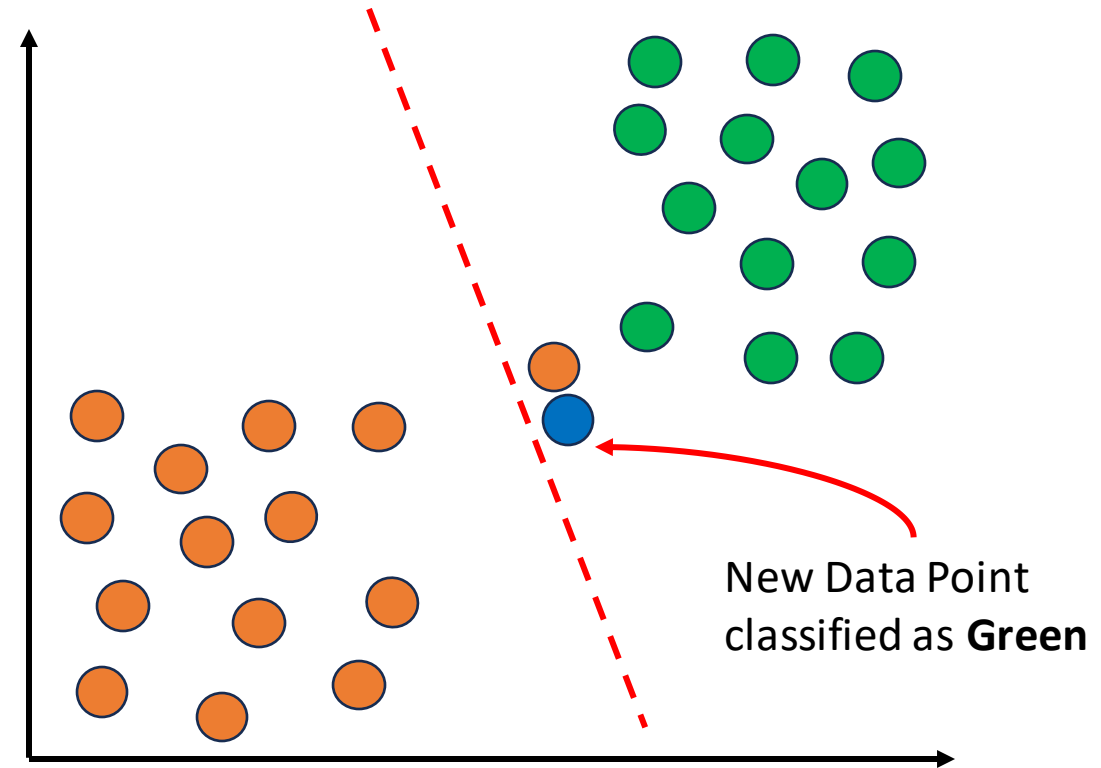
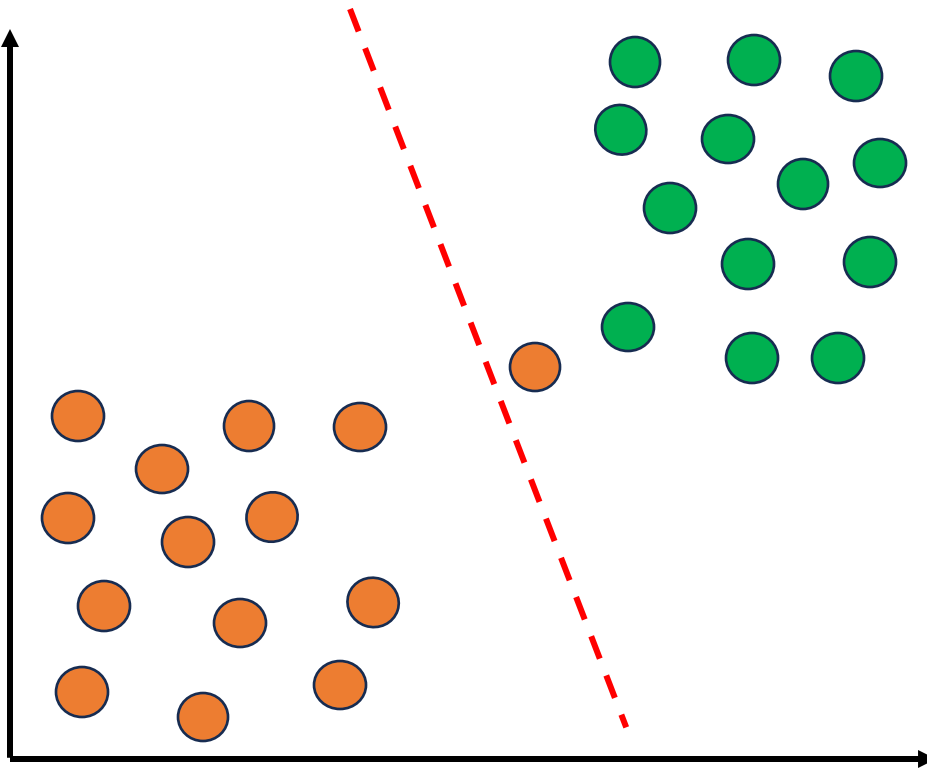
How to avoid this case?



To avoid this, we should **allow misclassification**

Support Vector Machine

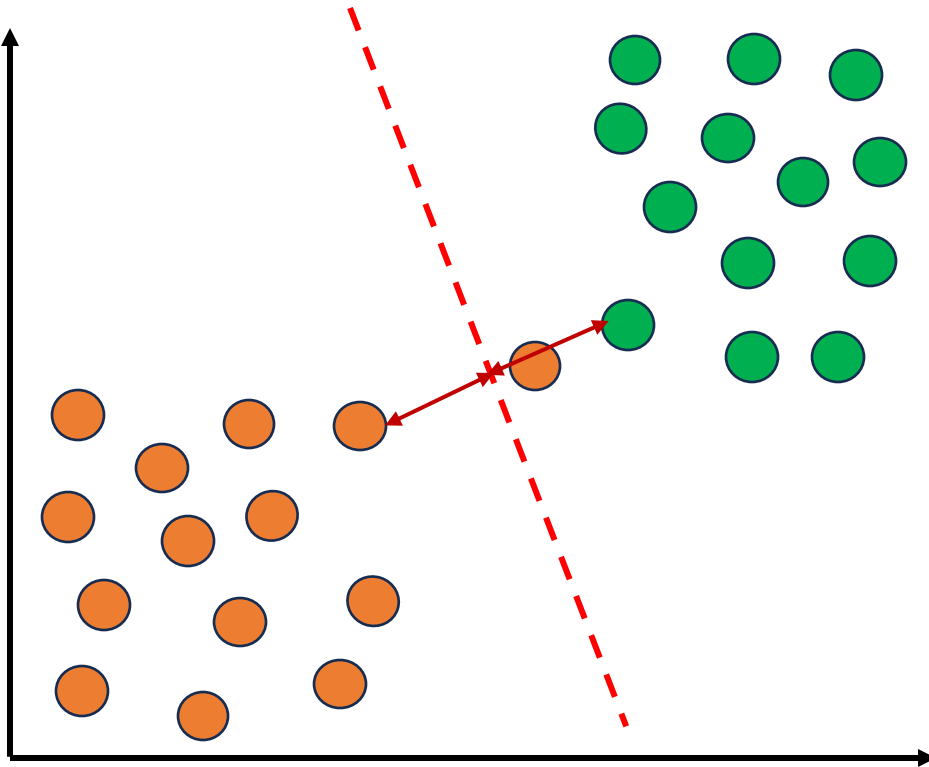
❖ Soft Margin Classifier



However, when we have a new data point, we might get it right.

Support Vector Machine

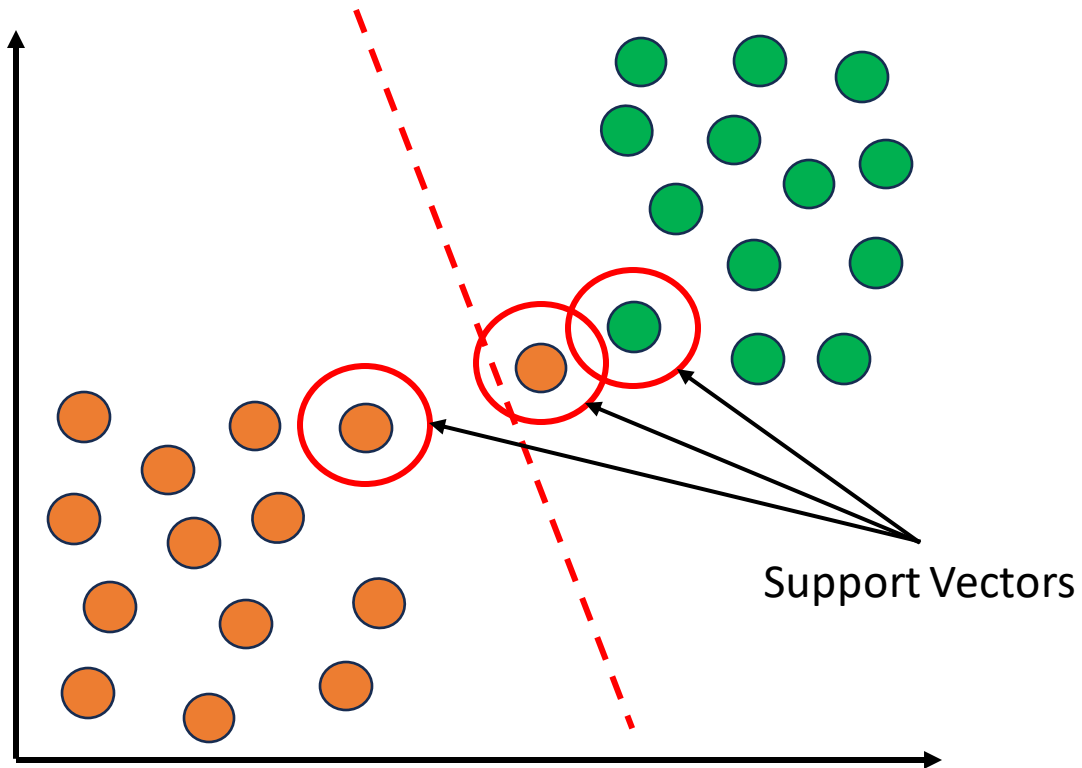
❖ Soft Margin Classifier



When we **allow misclassifications**, the distance between the observations and the decision boundary is called **Soft Margin** => **Soft Margin Classifier (Support Vector Classifier)**.

Support Vector Machine

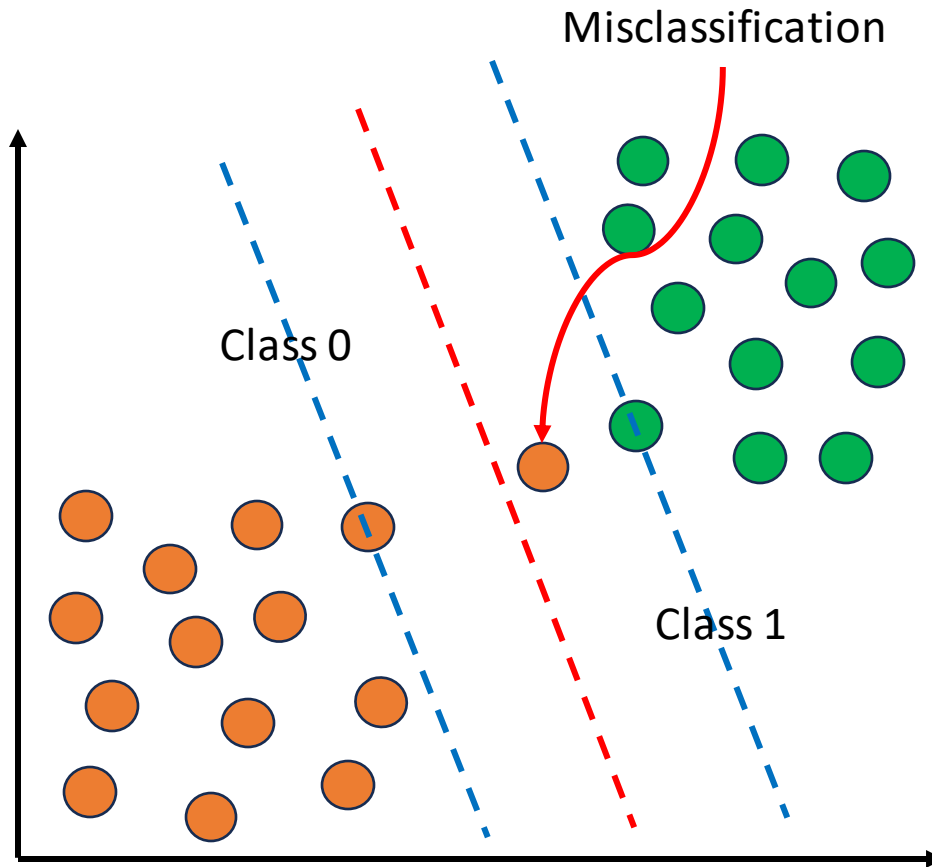
❖ Why “Support” Vector Classifier



We called “Support” Vector Classifier because the **data points on the edge and within the Soft Margin** are called Support Vectors.

Support Vector Machine

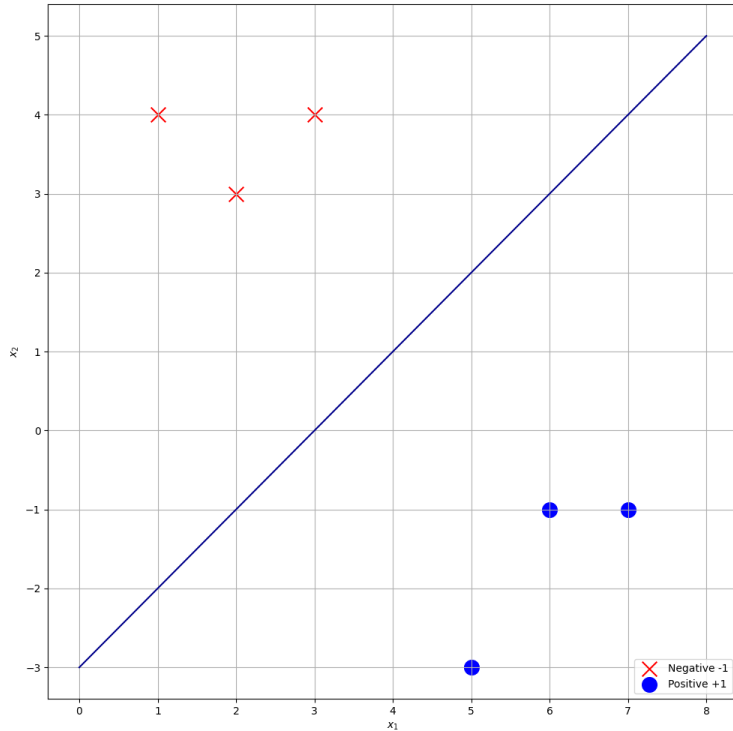
❖ Why “Support” Vector Classifier



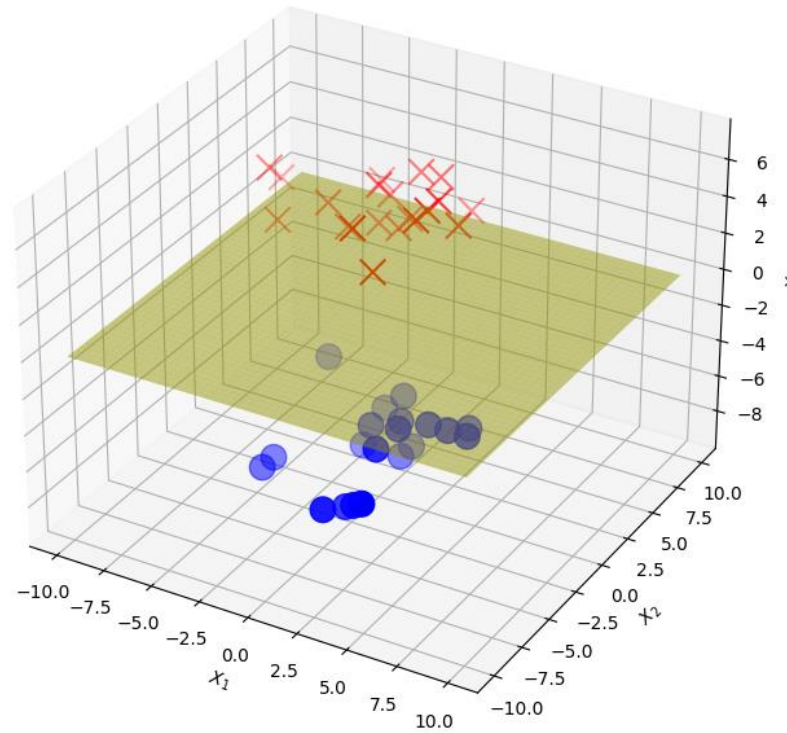
To better have a sense of relation between data points and Soft Margin, we draw two parallel lines to the Decision Boundary on Support Vectors.

Support Vector Machine

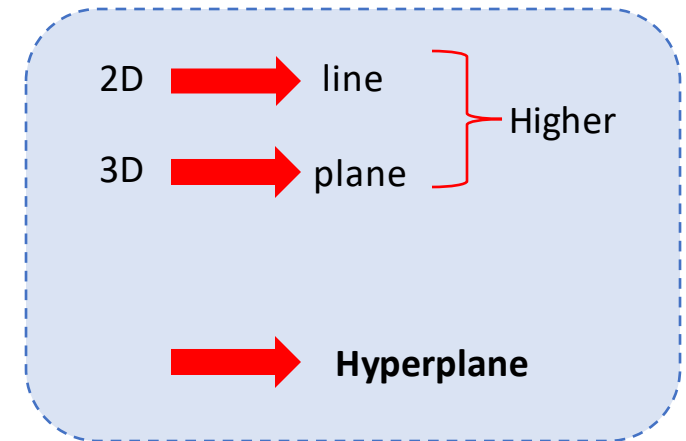
❖ SVC: Hyperplane



In 2D space, decision boundary is a line

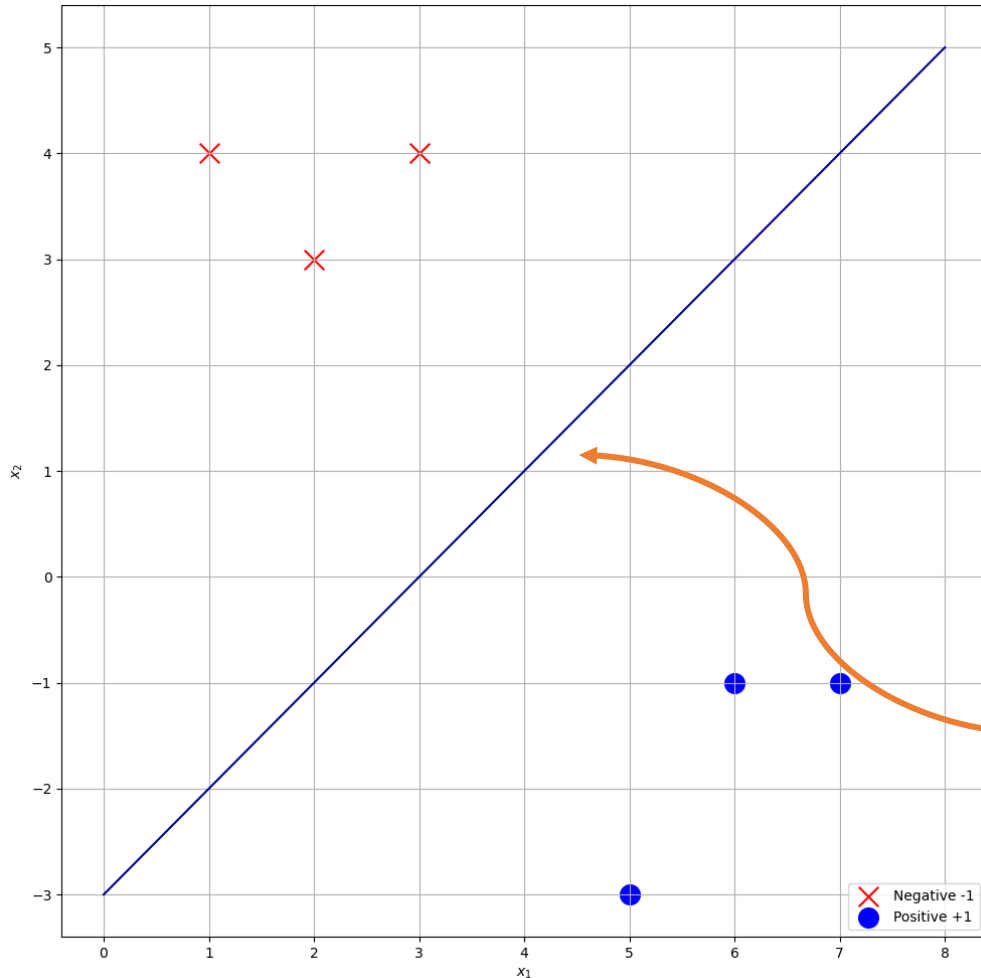


But in 3D, decision boundary is instead a plane



Support Vector Machine

❖ SVC: Hyperplane



Equation of Hyperplane

$$w \cdot x + b = 0$$

Hypothesis Function $h(x)$

- $h(x_i) = \begin{cases} +1 & \text{if } w \cdot x + b \geq 0 \\ -1 & \text{if } w \cdot x + b < 0 \end{cases}$
- $h(x_i) = \text{sign}(w \cdot x + b)$

With $w = (1, -1)$ and $b = -3$ we get this hyperplane.

We use the hypothesis function to predict the class of a data point.

Support Vector Machine

❖ SVC: Prediction

X1	X2	Y
3	4	-1
1	4	-1
2	3	-1
6	-1	1
7	-1	1
5	-3	1

With $w = (1, -1)$ and $b = -3$, the equation of hyperplane becomes:

$$w \cdot x + b = x_1 - x_2 - 3 = 0$$

$$(1*3) + (-1*4) + (-3) = -7 < 0 \rightarrow y_{predict} = -1$$

Classifying a data point using the hyperplane.

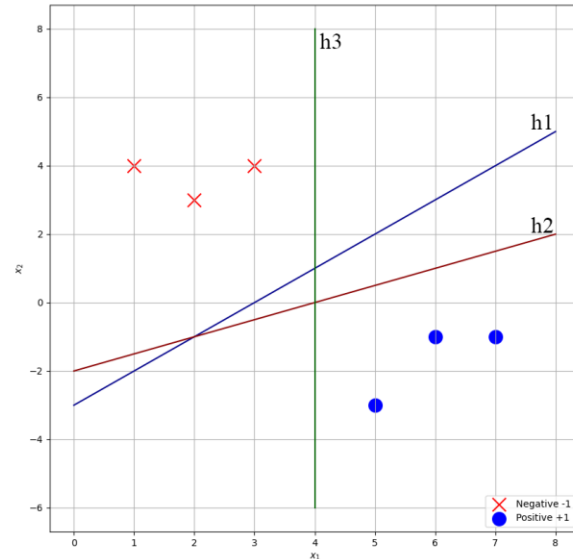
$$(1*7) + (-1*-1) + (-3) = 5 > 0 \rightarrow y_{predict} = +1$$

In this example, we use X1 and X2 to predict Y.

Support Vector Machine

❖ SVC: Hyperplane

Changing the value
of \mathbf{W} gives us
different
hyperplanes



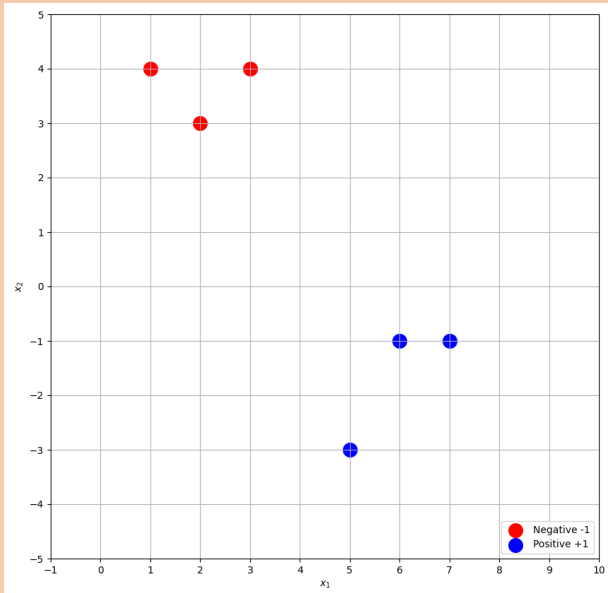
Where is
the optimal
hyperplane?



How do we
find it?

Training phase

x1	x2	y
3	4	-1
1	4	-1
2	3	-1
6	-1	1
7	-1	1
5	-3	1



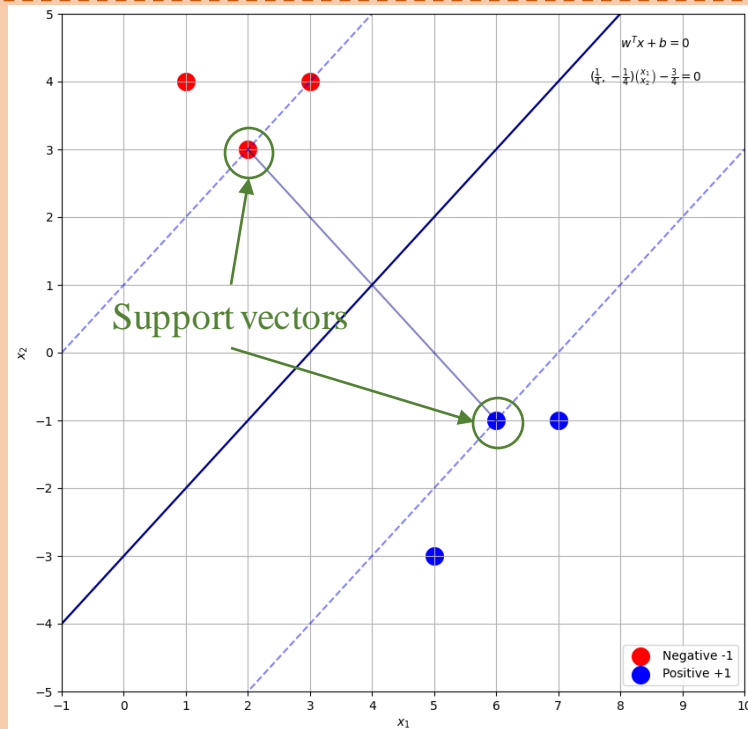
Linearly separable dataset

```

1 import numpy as np
2 from sklearn.svm import SVC
3
4 X = np.array([[3,4],[1,4],[2,3],
5               [6,-1],[7,-1],[5,-3]])
6
7 y = np.array([-1,-1,-1,1,1,1])
8
9 clf = SVC(kernel = 'linear')
10 clf.fit(X, y)
11
12 w = clf.coef_
13 b = clf.intercept_
14 print(w)
15 # >>> [[ 0.25 -0.25]]
16 print(b)
17 # >>> [-0.75]

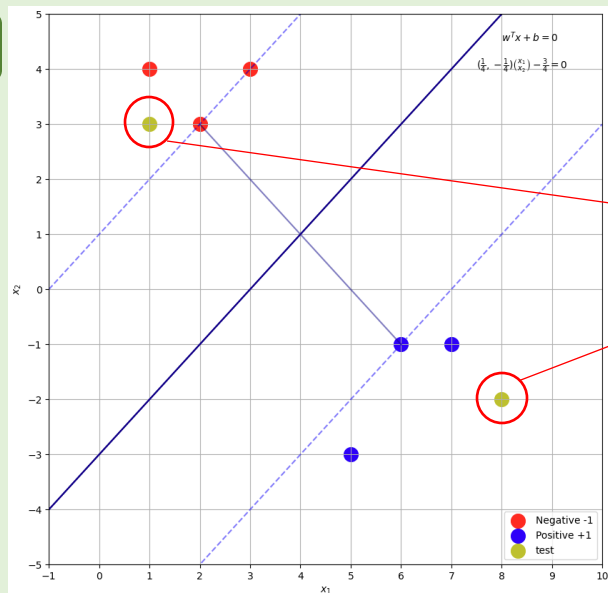
```

Compute w and b using sklearn



Test phase

x1	x2
8	-2
1	3



$$w^T \cdot x_i + b \leq -1 \text{ for } x_i \text{ having class } -1$$

$$w^T \cdot x_i + b \geq 1 \text{ for } x_i \text{ having class } +1$$

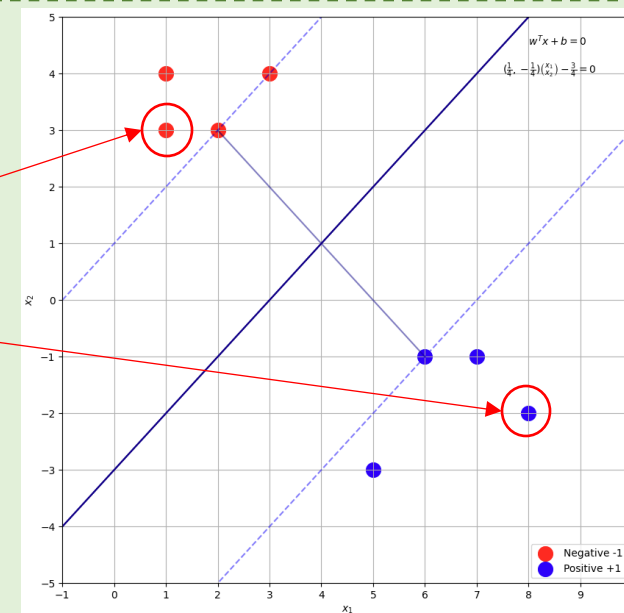
$$0.25 \cdot 1 + (-0.25) \cdot 3 + (-0.75) = -1.25 < -1$$

$$0.25 \cdot 8 + (-0.25) \cdot (-2) + (-0.75) = 1.75 > 1$$

```

1 X_test = np.array([[8,-2],
2                    [1,3]])
3 y_pred = clf.predict(X_test)
4 print(y_pred)
5 # >>> [1 -1]

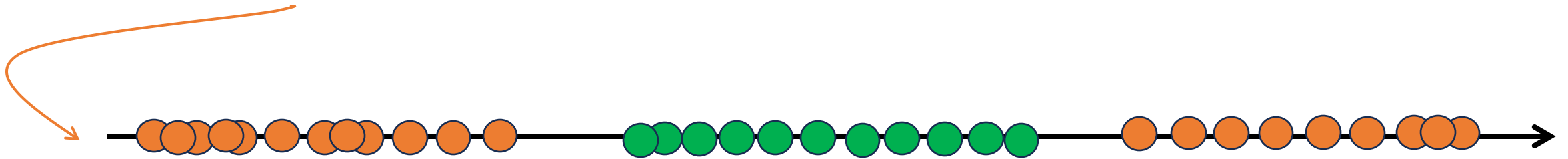
```



Support Vector Machine

❖ SVC Problem

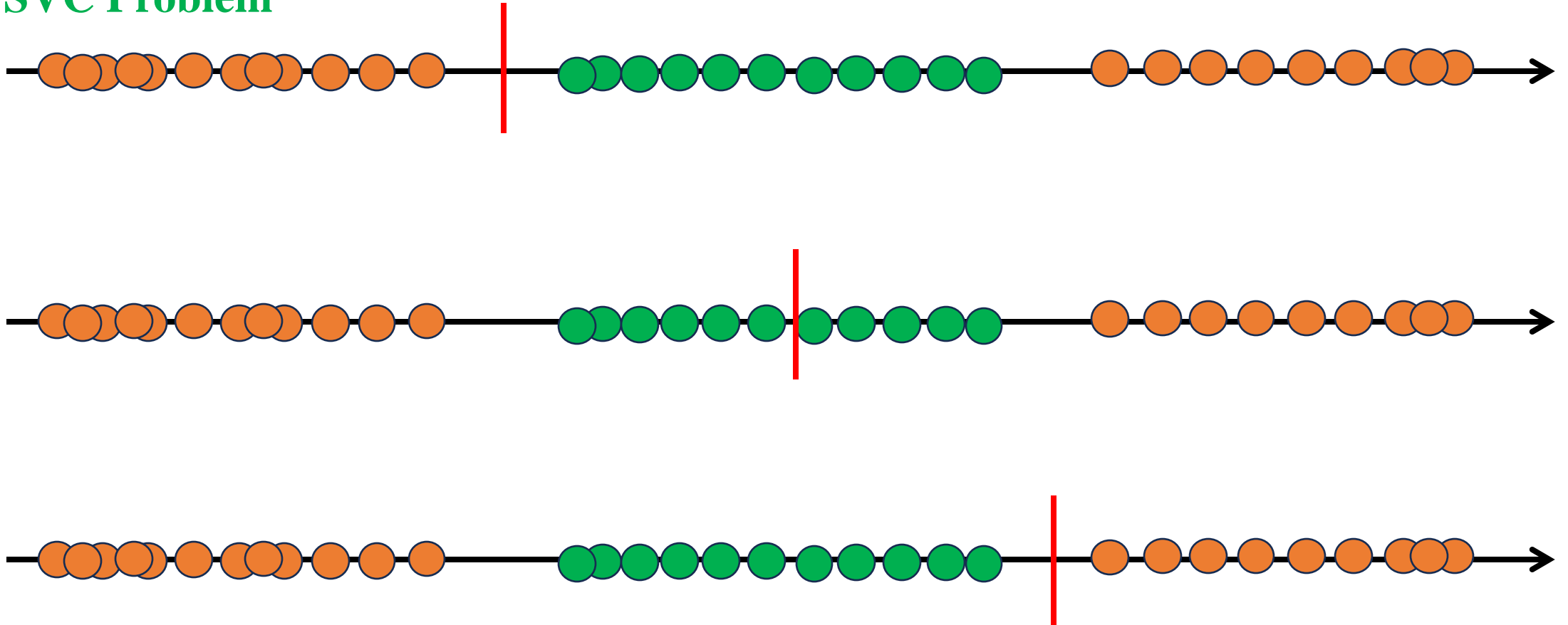
1-Dimensional Space



Can SVC handle this kind of data?

Support Vector Machine

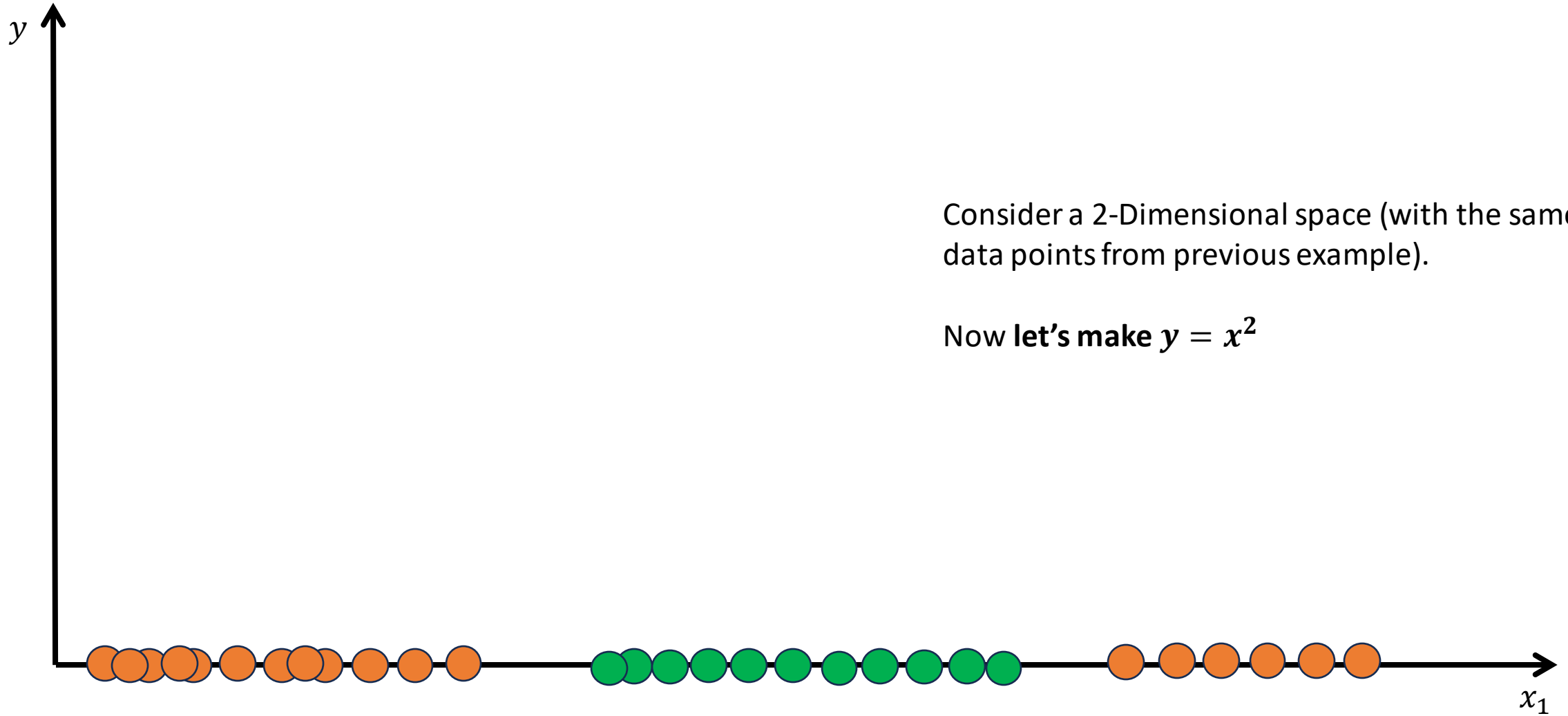
❖ SVC Problem



In general, it is hard for Hard/Soft Margin Classifier to handle this kind of data

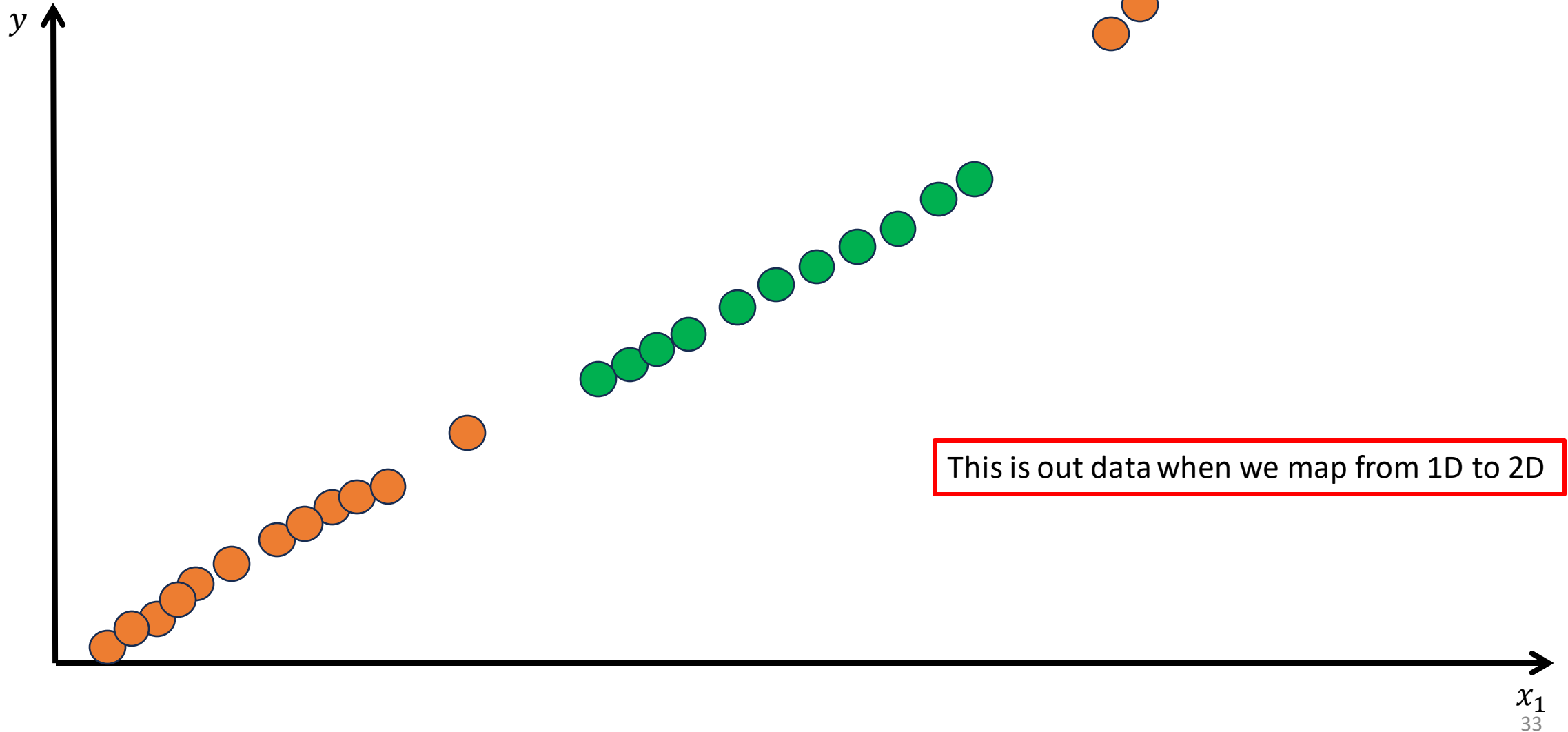
Support Vector Machine

❖ SVM Idea



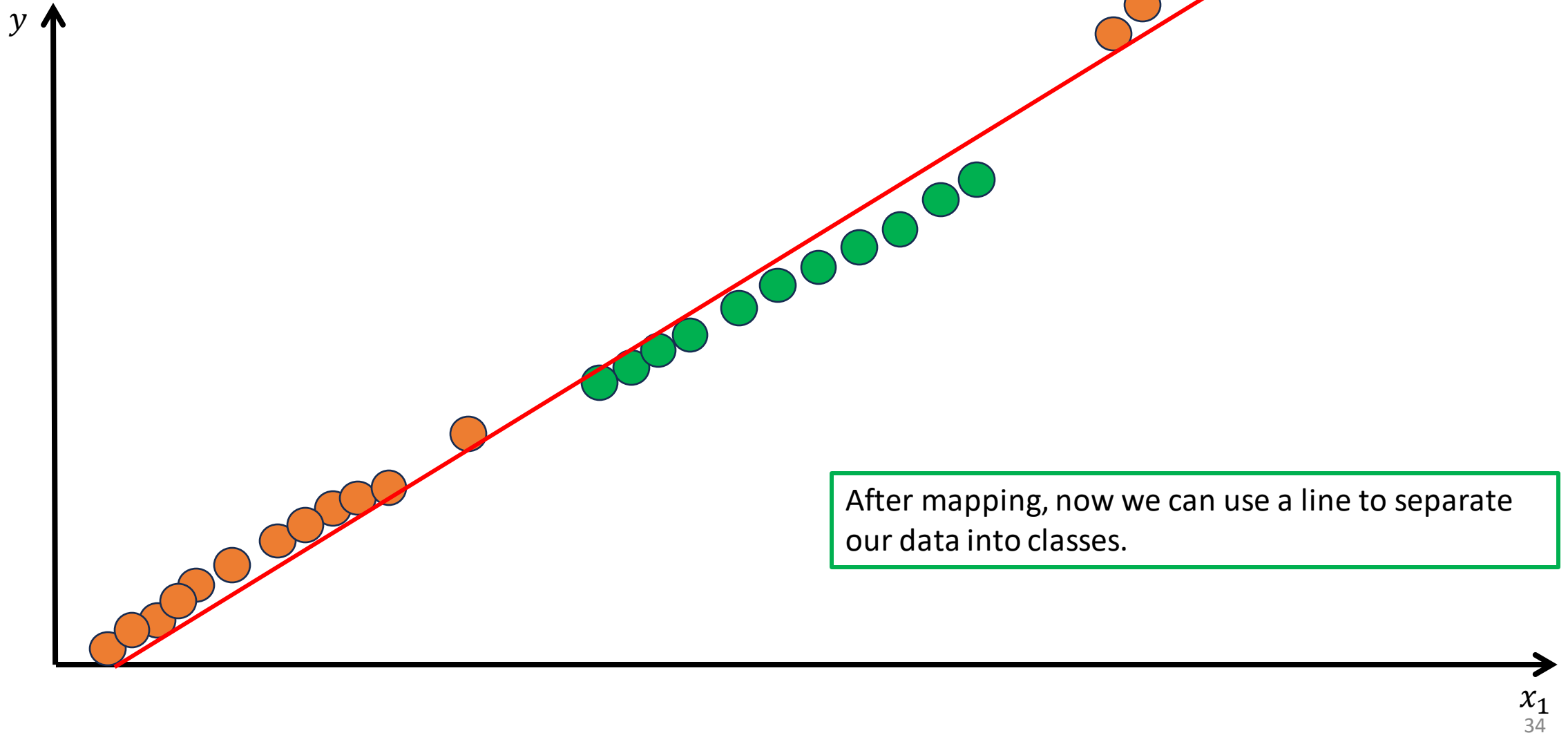
Support Vector Machine

❖ SVM Idea



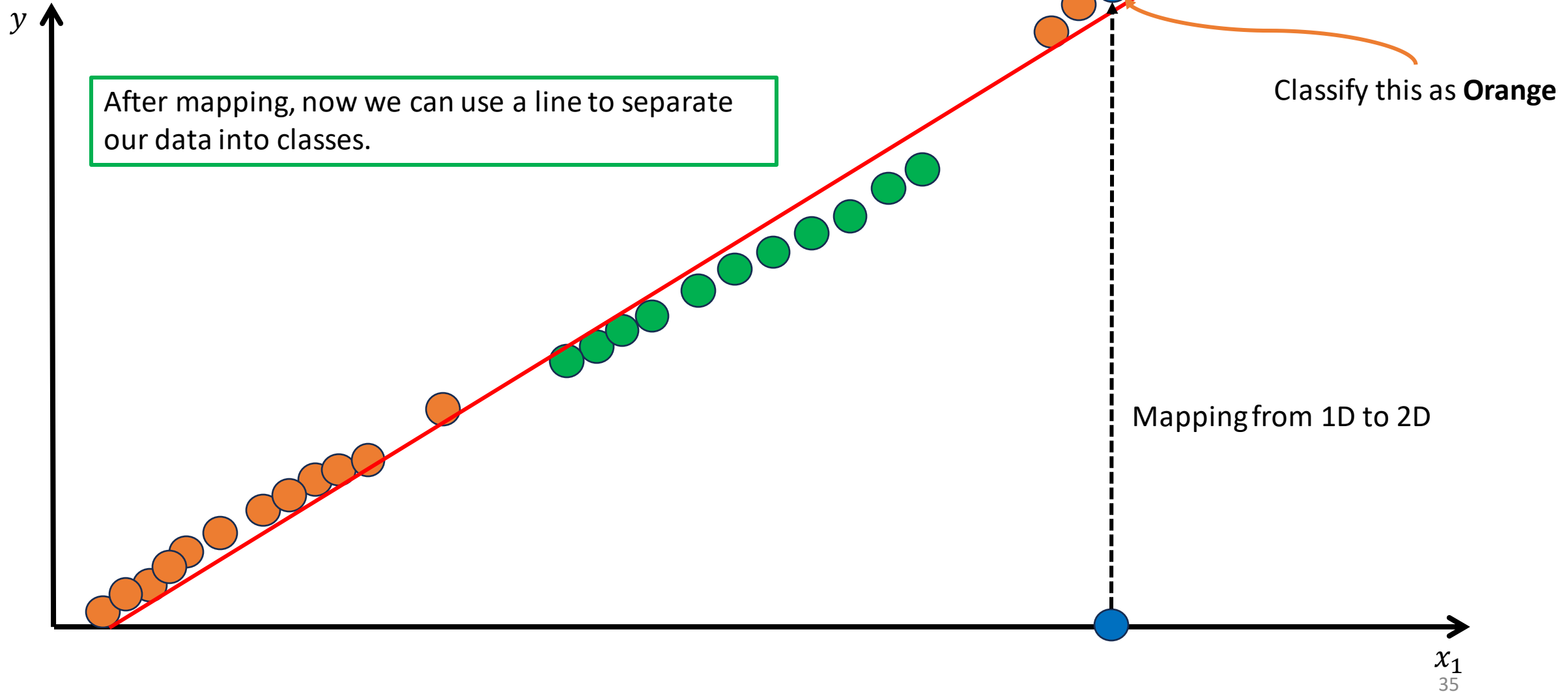
Support Vector Machine

❖ SVM Idea



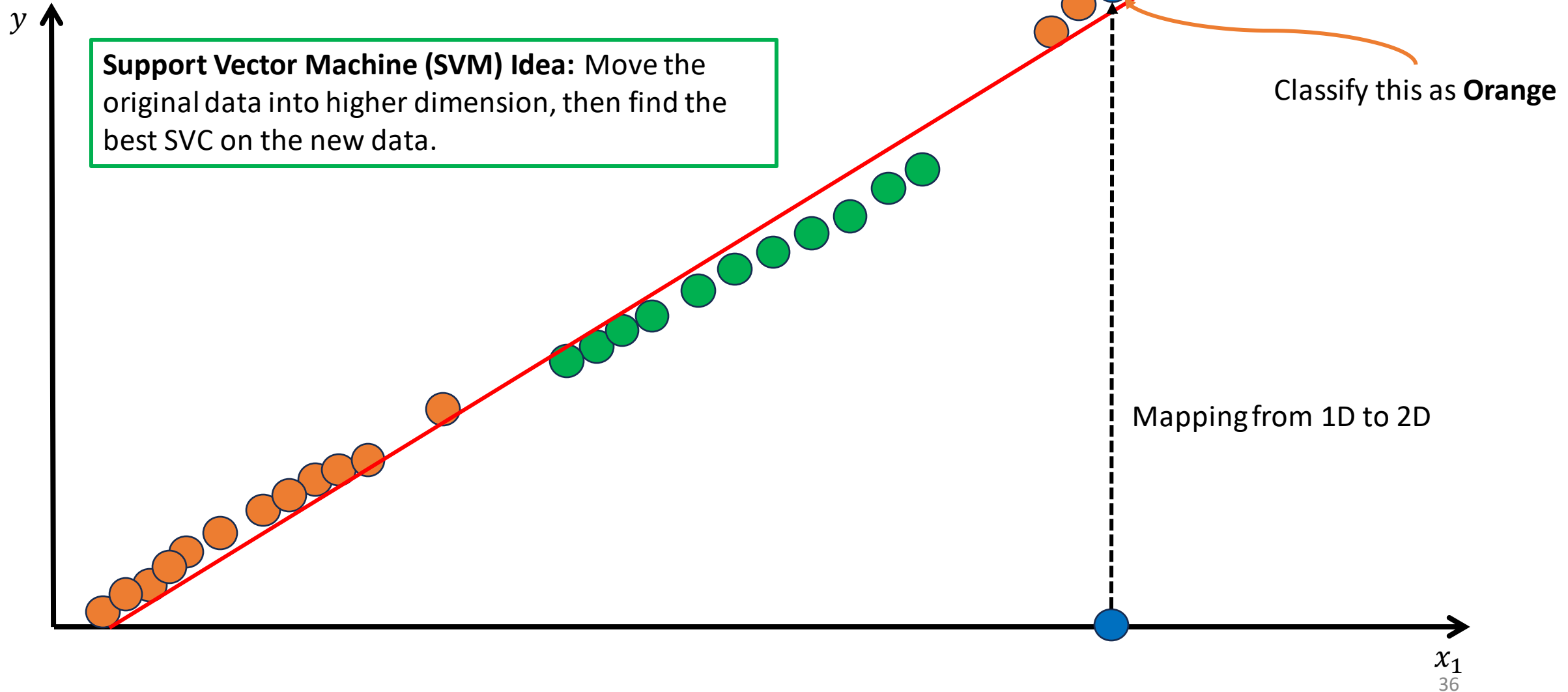
Support Vector Machine

❖ SVM Idea



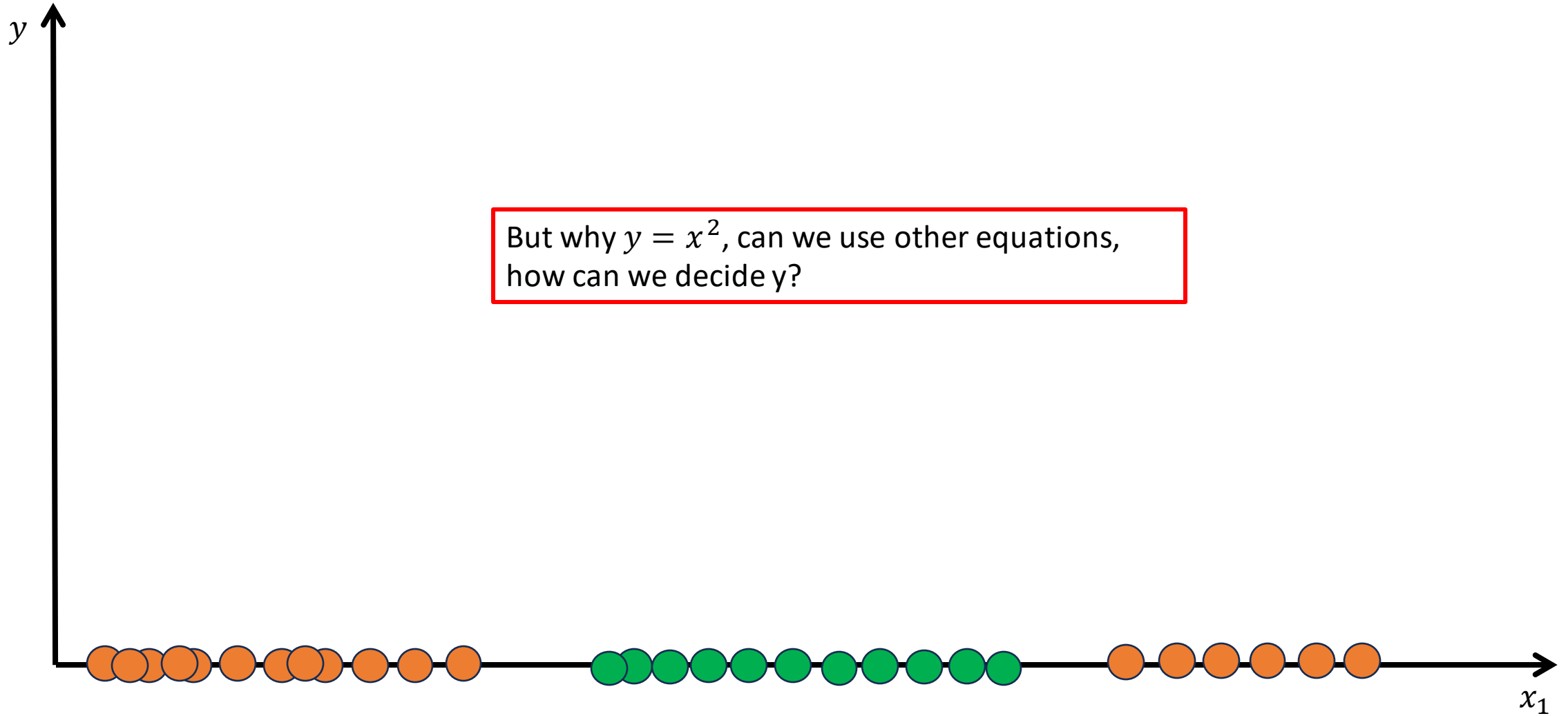
Support Vector Machine

❖ SVM Idea



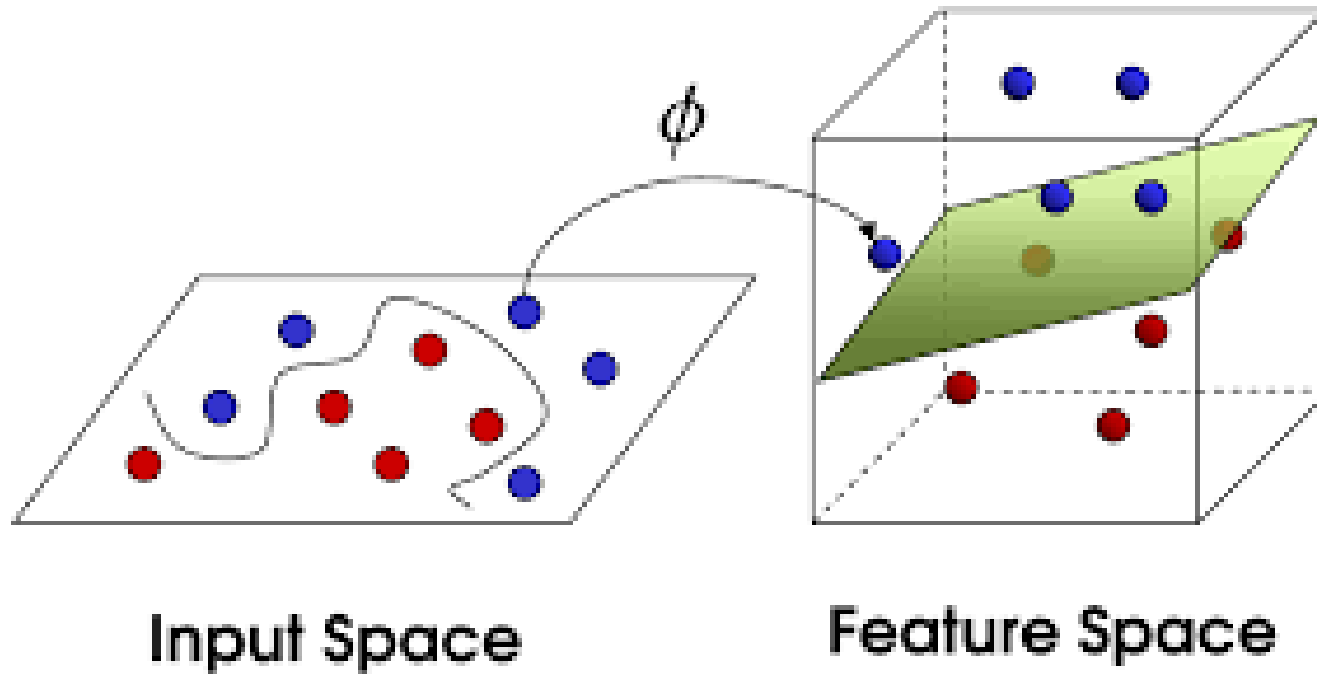
Support Vector Machine

❖ SVM Idea



Support Vector Machine

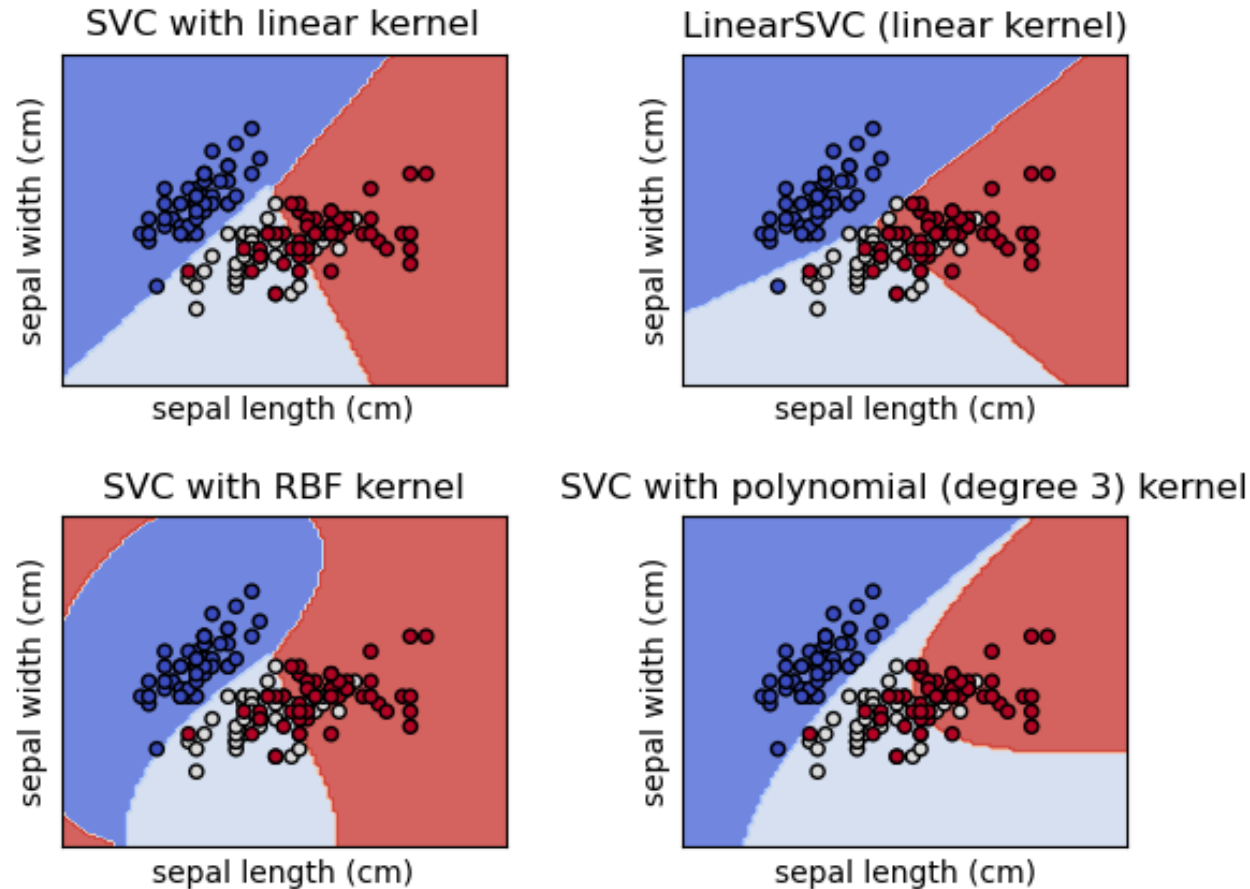
❖ Kernel



To decide the y , or to decide SVC in higher dimensions, we use **Kernel Functions**.

Support Vector Machine

❖ Type of kernels



In general, we have some kernel types:

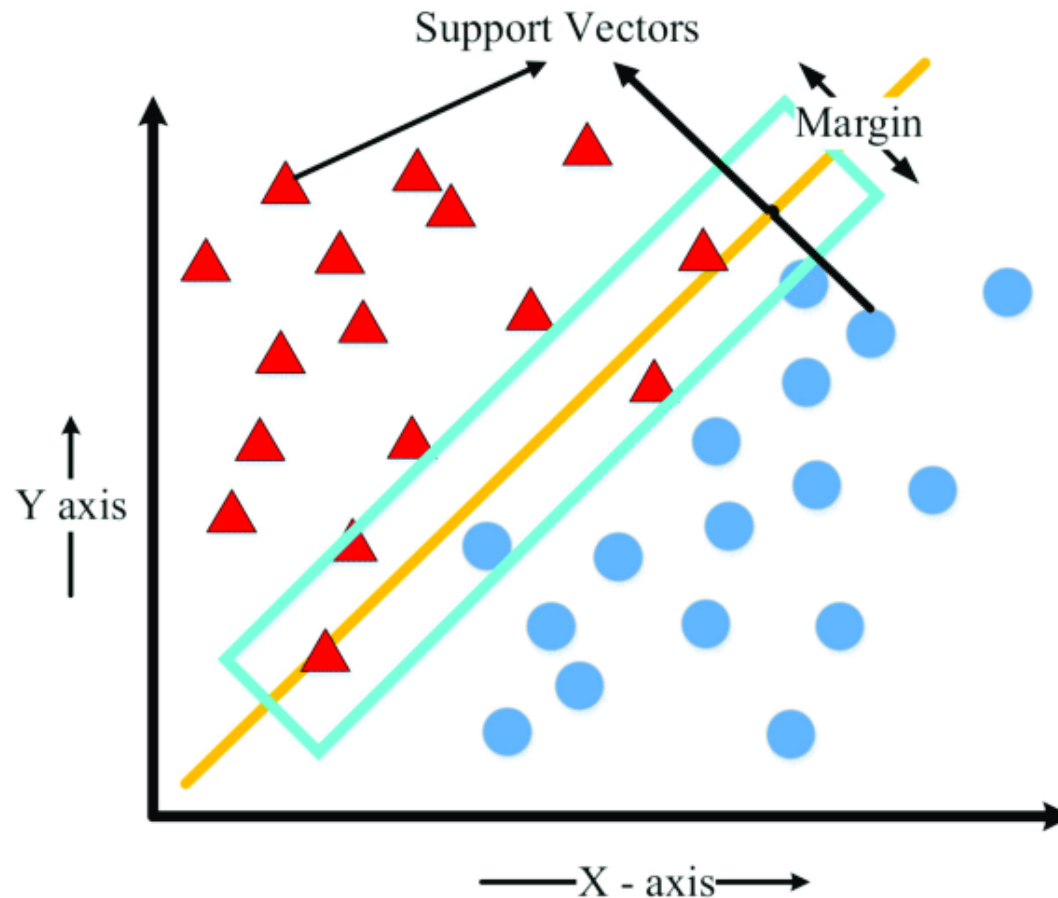
- Linear
- Polynomial
- Radial Basis Function (RBF)
- Sigmoid

Different results from different kernels using sklearn

Code Examples

❖ Introduction

Description: Build a binary classifier with SVM using scikit-learn library.



Code Examples

❖ Step 1: Import libraries

```
1 import numpy as np
2 import pandas as pd
3 import matplotlib.pyplot as plt
4
5 from sklearn.svm import SVC
6 from sklearn.preprocessing import StandardScaler
7 from sklearn.model_selection import train_test_split
8 from sklearn.metrics import accuracy_score
```



Code Examples

❖ Step 2: Download and load dataset

1. Download the dataset [here](#).
2. Using `pandas.read_csv()` to read the dataset.

```
1 dataset_path = './linear_separable_bin_clf.csv'
2 df = pd.read_csv(
3     dataset_path,
4     names=['label', 'features_1', 'features_2']
5 )
6 df
```

	label	features_1	features_2
0	1.0	2.6487	4.5192
1	1.0	1.5438	2.4443
2	1.0	1.8990	4.2409
3	1.0	2.4711	5.8097
4	1.0	3.3590	6.4423
...
95	-1.0	7.3641	5.9868
96	-1.0	6.2592	4.6711
97	-1.0	8.3703	7.5810
98	-1.0	8.5676	4.6457
99	-1.0	8.1676	4.6457

100 rows x 3 columns

Code Examples

❖ Step 3: Get some detail information

```
1 df.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 100 entries, 0 to 99
Data columns (total 3 columns):
#   Column      Non-Null Count  Dtype  
---  -
0   label       100 non-null   float64
1   features_1  100 non-null   float64
2   features_2  100 non-null   float64
dtypes: float64(3)
memory usage: 2.5 KB
```

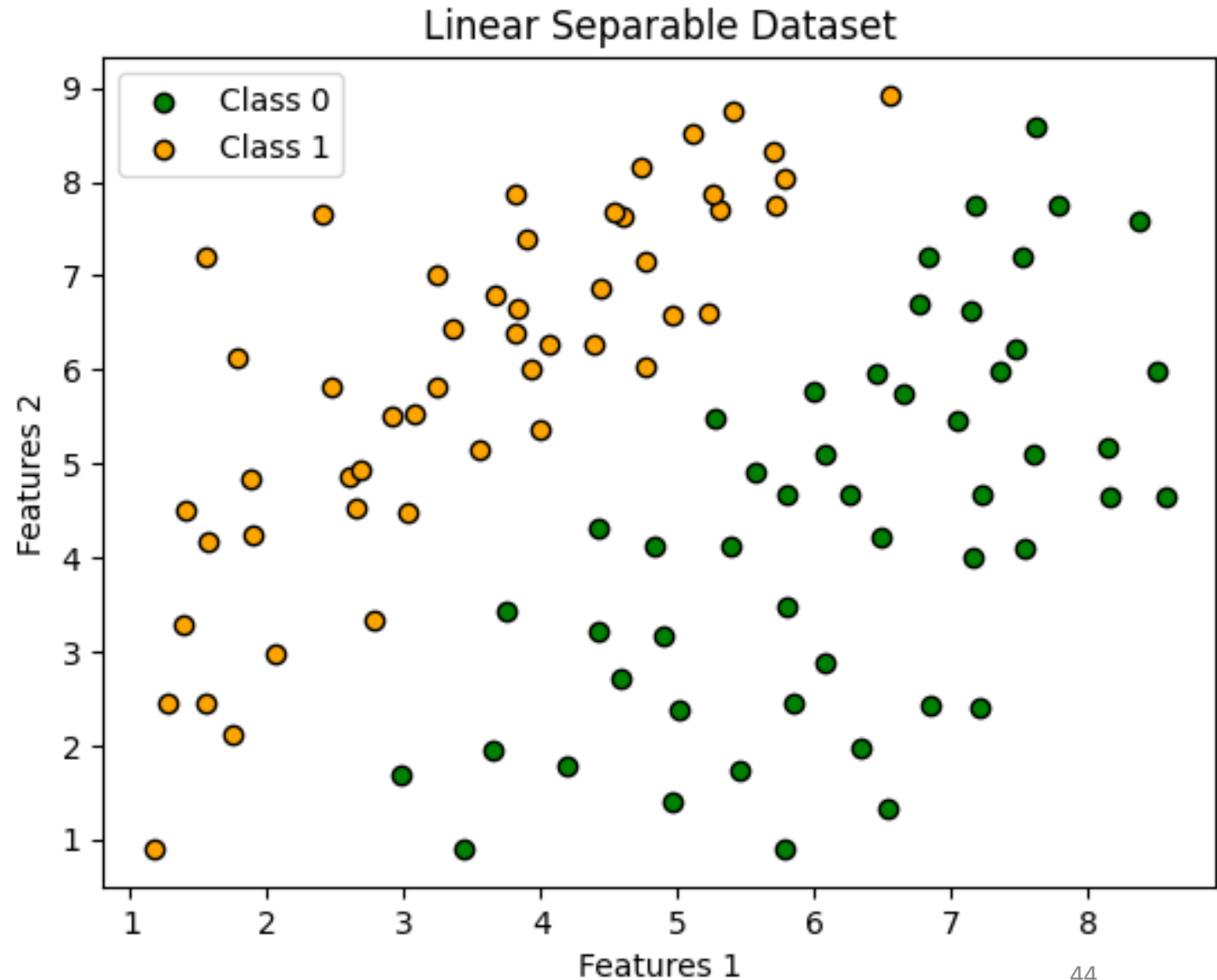
```
1 df.describe()
```

	label	features_1	features_2
count	100.000000	100.000000	100.000000
mean	0.000000	4.866669	5.144230
std	1.005038	1.964860	2.103965
min	-1.000000	1.169000	0.900800
25%	-1.000000	3.418175	3.469150
50%	0.000000	4.927500	5.265700
75%	1.000000	6.466375	6.720625
max	1.000000	8.567600	8.922100

Code Examples

❖ Step 4: Plot the dataset

```
1 class_0 = df[df['label'] == -1]
2 class_1 = df[df['label'] == 1]
3 plt.scatter(
4     class_0['features_1'],
5     class_0['features_2'],
6     edgecolor="black",
7     marker='o',
8     color='green',
9     label='Class 0'
10 )
11 plt.scatter(
12     class_1['features_1'],
13     class_1['features_2'],
14     edgecolor="black",
15     marker='o',
16     color='orange',
17     label='Class 1'
18 )
19 plt.xlabel('Features 1')
20 plt.ylabel('Features 2')
21 plt.title('Linear Separable Dataset')
22 plt.legend()
23 plt.show()
```



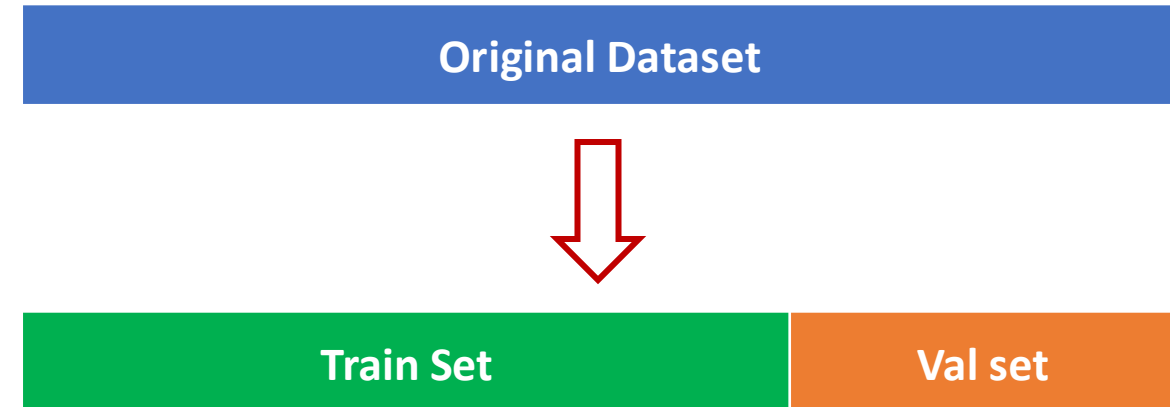
Code Examples

❖ Step 5: Split train val dataset

```
1 dataset_arr = df.to_numpy()
2 X, y = dataset_arr[:, 1:], dataset_arr[:, 0]
3
4 test_size = 0.3
5 random_state = 1
6 is_shuffle = True
7 X_train, X_val, y_train, y_val = train_test_split(
8     X, y,
9     test_size=test_size,
10    random_state=random_state,
11    shuffle=is_shuffle
12 )
```

```
1 print(f'Number of training samples: {X_train.shape[0]}')
2 print(f'Number of val samples: {X_val.shape[0]}')
```

```
Number of training samples: 70
Number of val samples: 30
```



Code Examples

❖ Step 6: Train SVM

In this problem, we do classification, so we will use SVC module.

```
1 classifier = SVC(  
2     kernel='linear',  
3     random_state=random_state  
4 )  
5 classifier.fit(X_train, y_train)
```

▼ SVC

```
SVC(kernel='linear', random_state=1)
```

sklearn.svm.SVC

```
class sklearn.svm.SVC(*, C=1.0, kernel='rbf', degree=3, gamma='scale', coef0=0.0, shrinking=True, probability=False,  
tol=0.001, cache_size=200, class_weight=None, verbose=False, max_iter=-1, decision_function_shape='ovr', break_ties=False,  
random_state=None)
```

[\[source\]](#)

C-Support Vector Classification.

The implementation is based on libsvm. The fit time scales at least quadratically with the number of samples and may be impractical beyond tens of thousands of samples. For large datasets consider using [LinearSVC](#) or [SGDClassifier](#) instead, possibly after a [Nyström](#) transformer or other [Kernel Approximation](#).

The multiclass support is handled according to a one-vs-one scheme.

For details on the precise mathematical formulation of the provided kernel functions and how `gamma`, `coef0` and `degree` affect each other, see the corresponding section in the narrative documentation: [Kernel functions](#).

Read more in the [User Guide](#).

Read more about SVC [here](#)

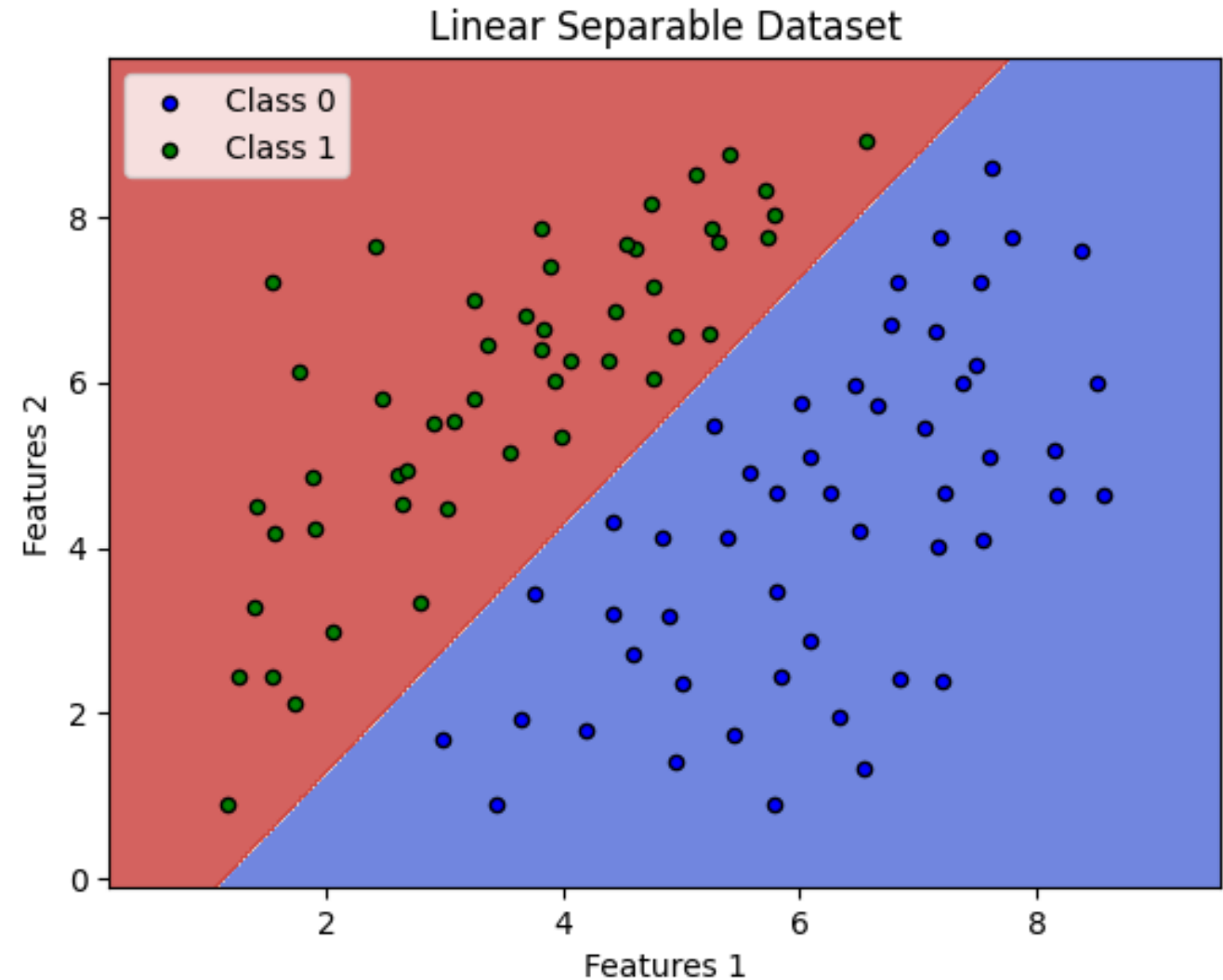
Code Examples

❖ Step 7: Evaluation

Evaluate trained SVM on val set:

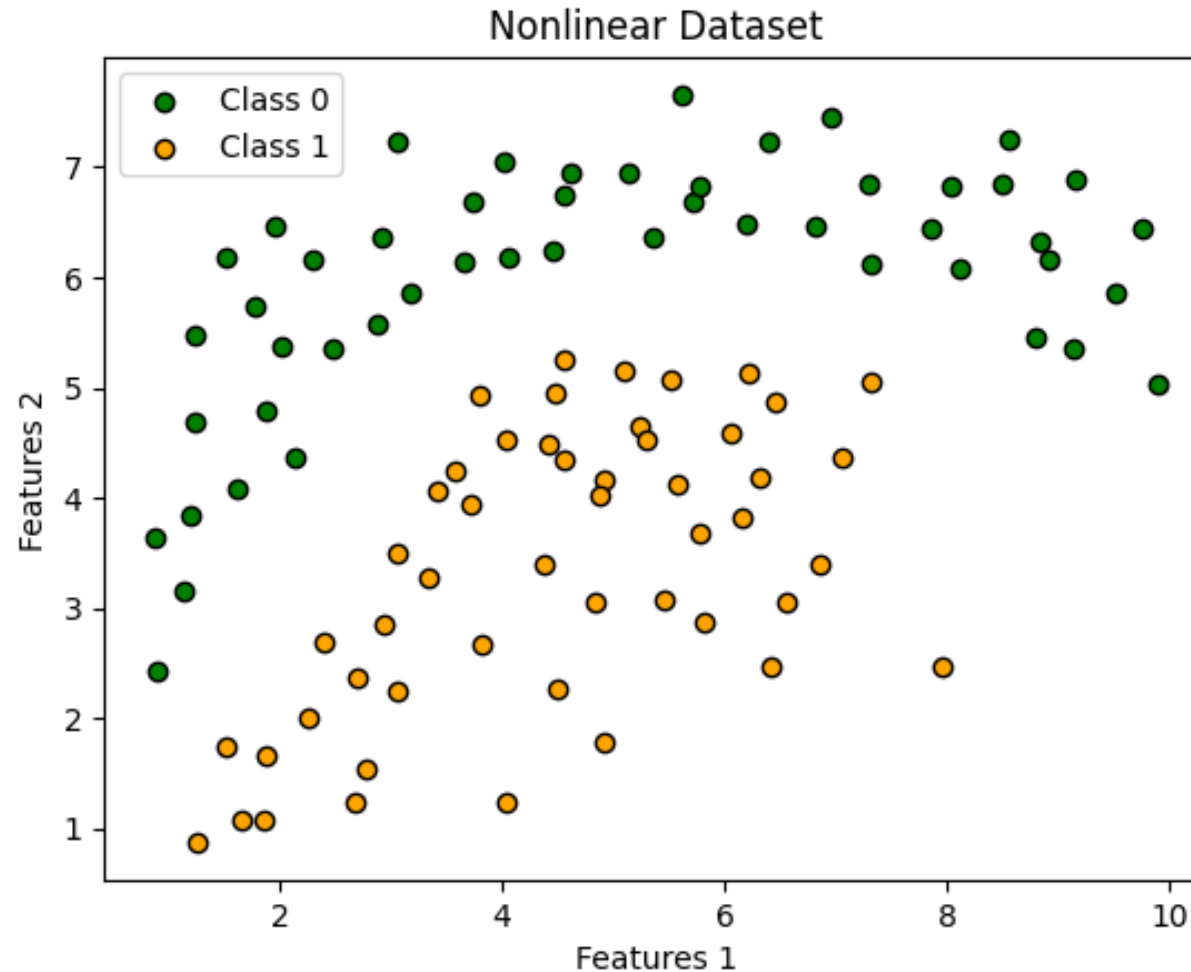
```
1 y_pred = classifier.predict(X_val)
2 scores = accuracy_score(y_pred, y_val)
3
4 print('Evaluation results on validation set:')
5 print(f'Accuracy: {scores}')
```

Evaluation results on validation set:
Accuracy: 1.0



Code Examples

❖ Linear kernel with non-linear dataset ? (Download [here](#))

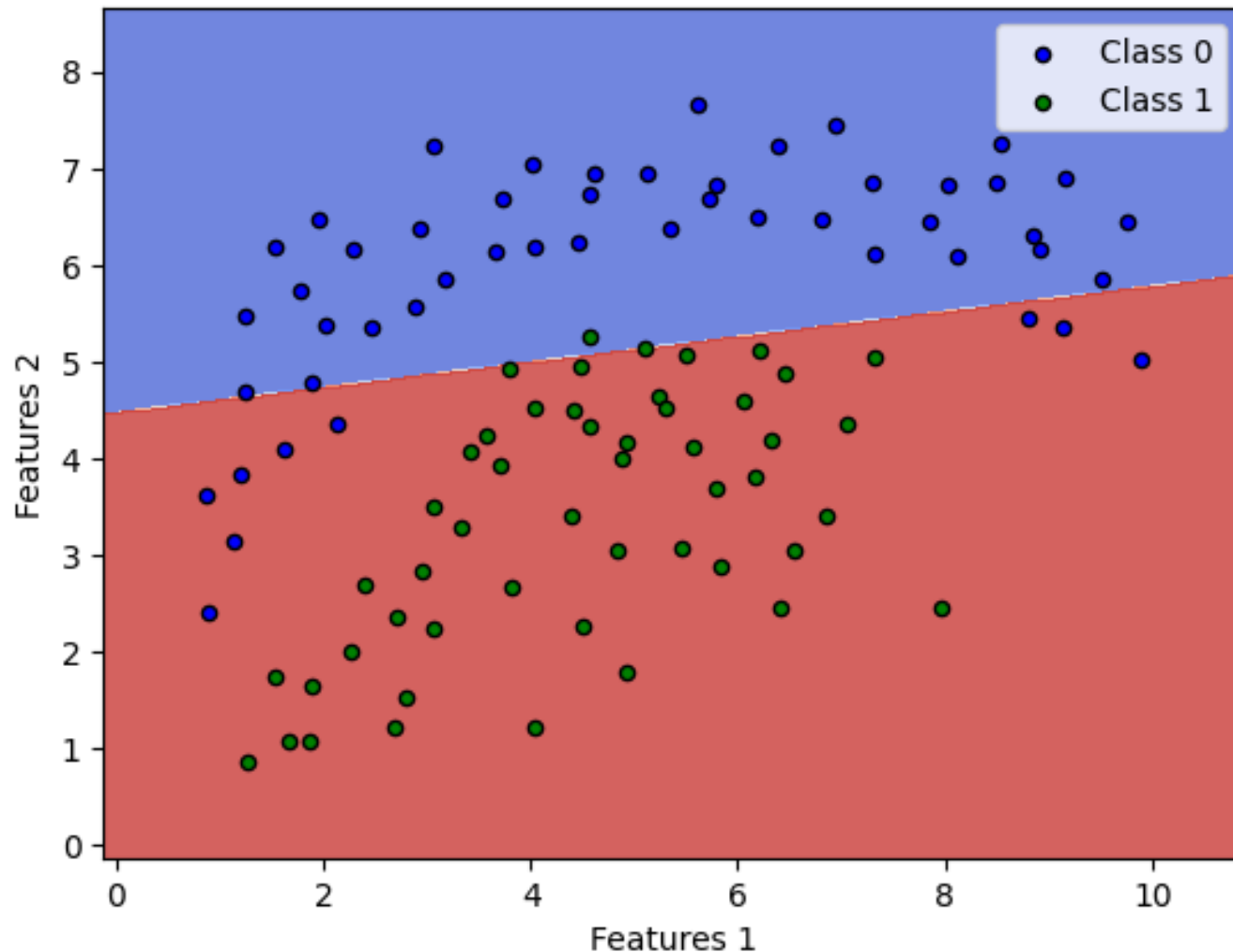


If we apply the same previous SVC code, will it still work?

Code Examples

❖ Linear kernel with non-linear dataset ?

Classification Results (Linear Kernel)



```
1 linear_clf = SVC(  
2     kernel='linear',  
3     random_state=random_state  
4 )  
5 linear_clf.fit(X_train, y_train)
```

▼ SVC

```
SVC(kernel='linear', random_state=1)
```

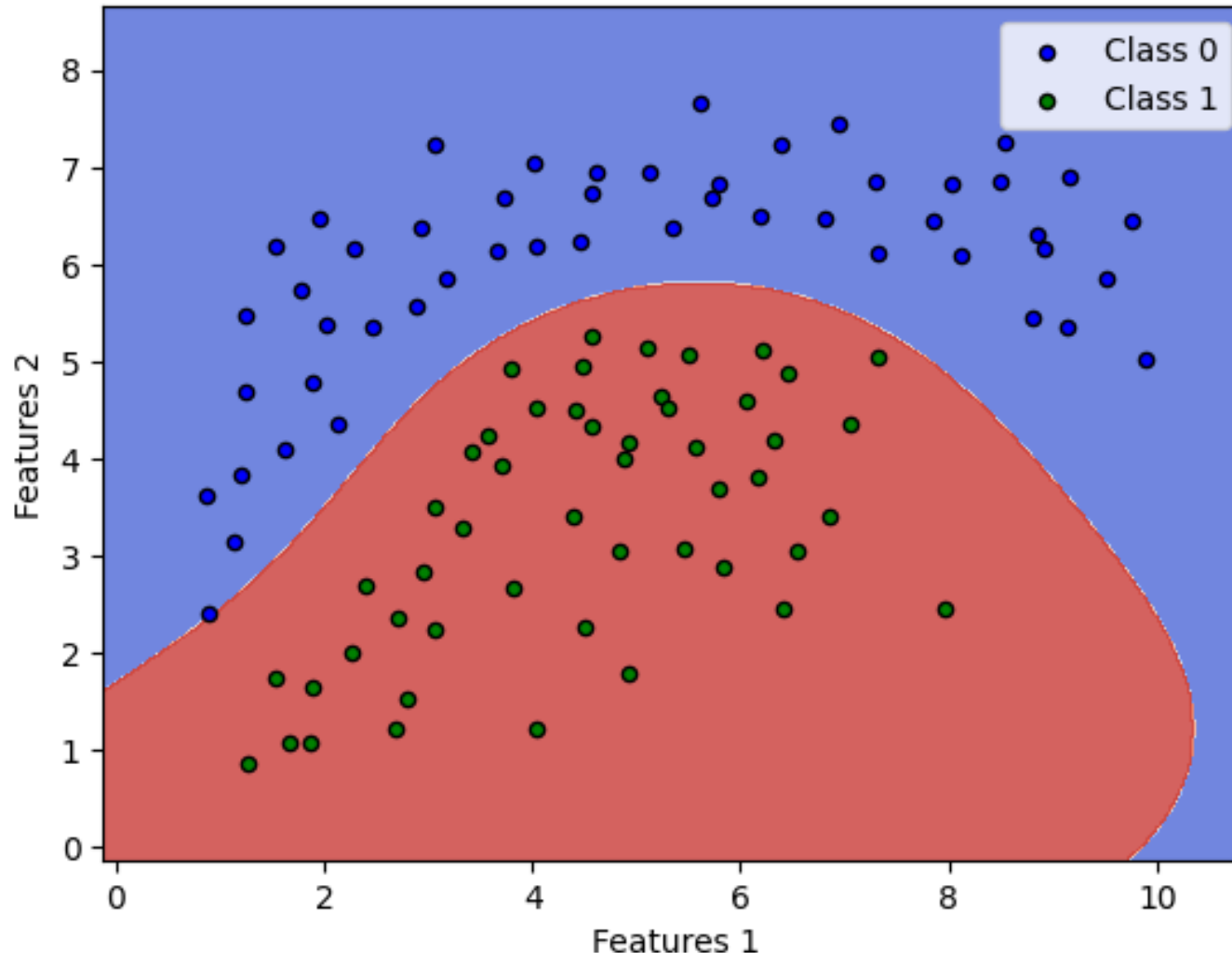
```
1 linear_scores = accuracy_score(y_pred_linear, y_val)  
2 print('Evaluation results on validation set:')  
3 print(f'Linear kernel accuracy: {linear_scores}')
```

Evaluation results on validation set:
Linear kernel accuracy: 0.8666666666666667

Code Examples

❖ How about other kernels ?

Classification Results (RBF Kernel)



```
1 rbf_clf = SVC(  
2     kernel='rbf',  
3     random_state=random_state  
4 )  
5 rbf_clf.fit(X_train, y_train)
```

▼ SVC
SVC(random_state=1)

```
1 rbf_scores = accuracy_score(y_pred_rbf, y_val)  
2 print('Evaluation results on validation set:')  
3 print(f'RBF kernel accuracy: {rbf_scores}')
```

Evaluation results on validation set:
RBF kernel accuracy: 1.0

It is important to tune proper hyperparameters of SVM for the best result.

Question

