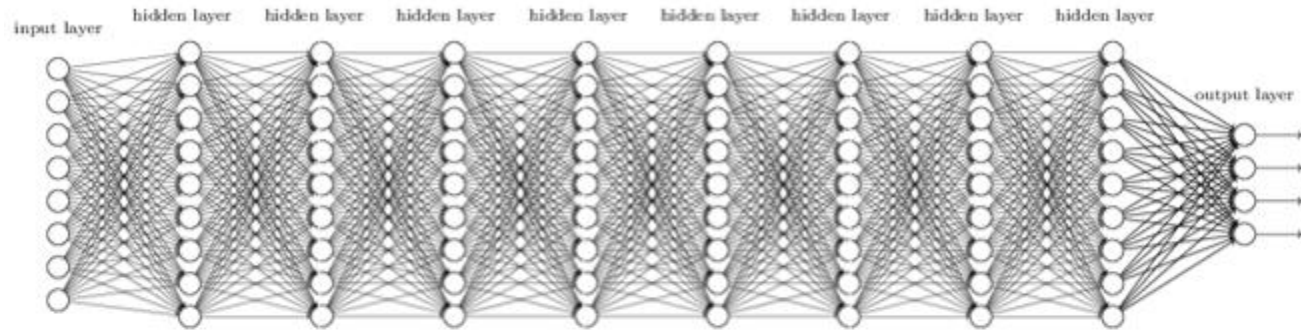
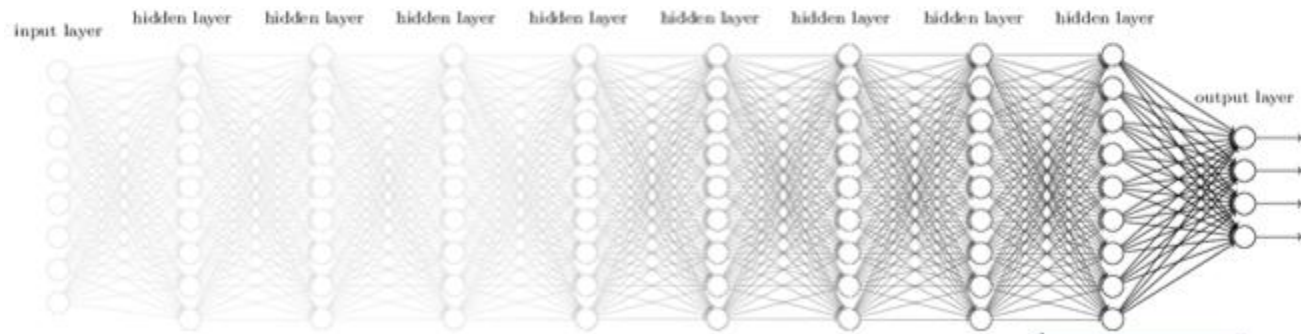


# VANISHING GRADIENT PROBLEM



Deep Neural Network



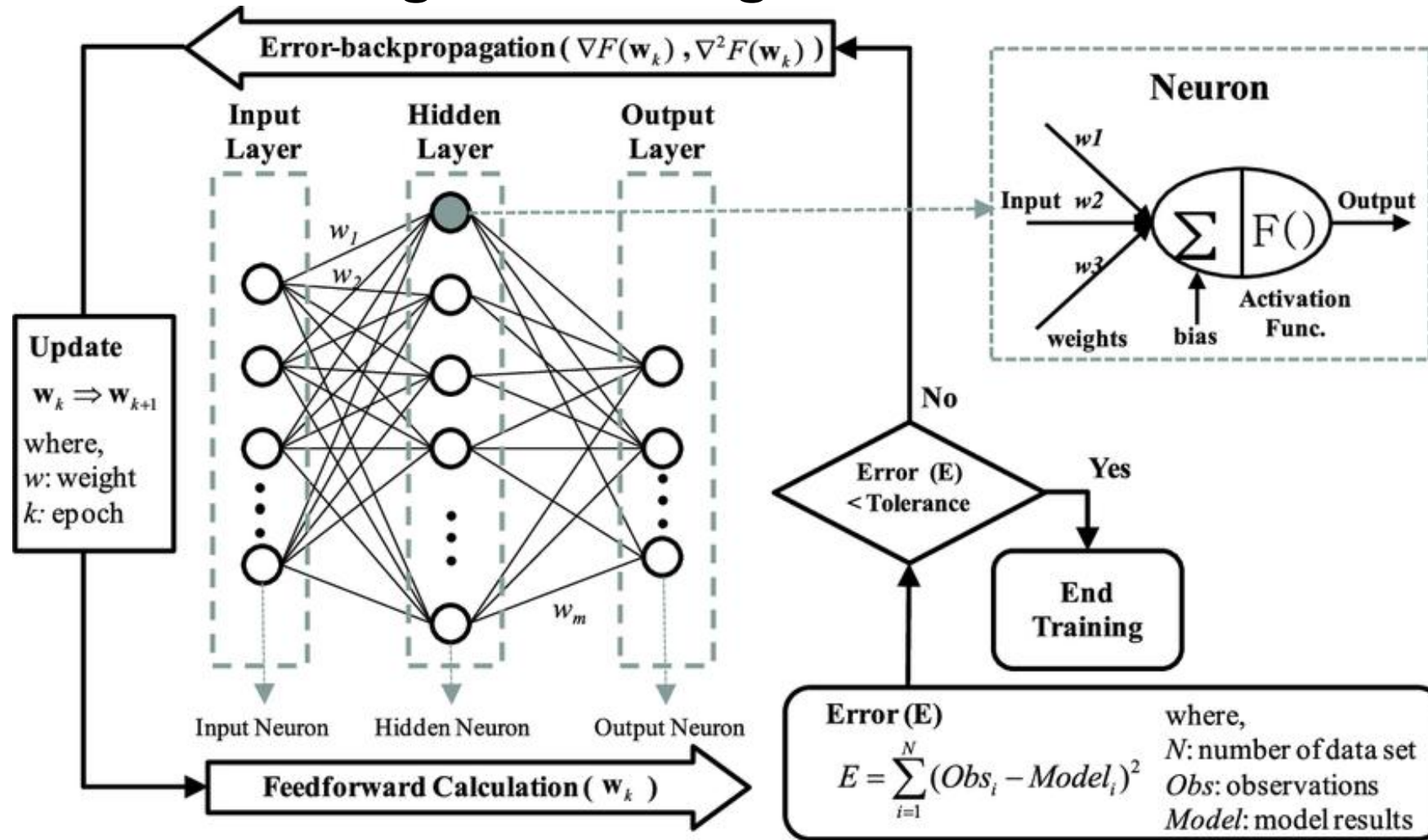
Vanishing Gradient

- **Giới thiệu Vanishing và Exploding Problem**
  - Vanishing Problem
  - Exploding Problem
- **Fashion MNIST Vanishing Problem**
  - Giới thiệu vấn đề
  - Solution1: Weight Increasing
  - Solution2: Better Activation
  - Solution3: Better Optimizer
  - Solution4: Normalize Inside Network
  - Solution5: Skip Connection
  - Solution6: Train Some Layer
- **Other Methods**

- **Giới thiệu Vanishing và Exploding Problem**
  - Vanishing Problem
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- **Fashion MNIST Vanishing Problem**
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- Other Methods

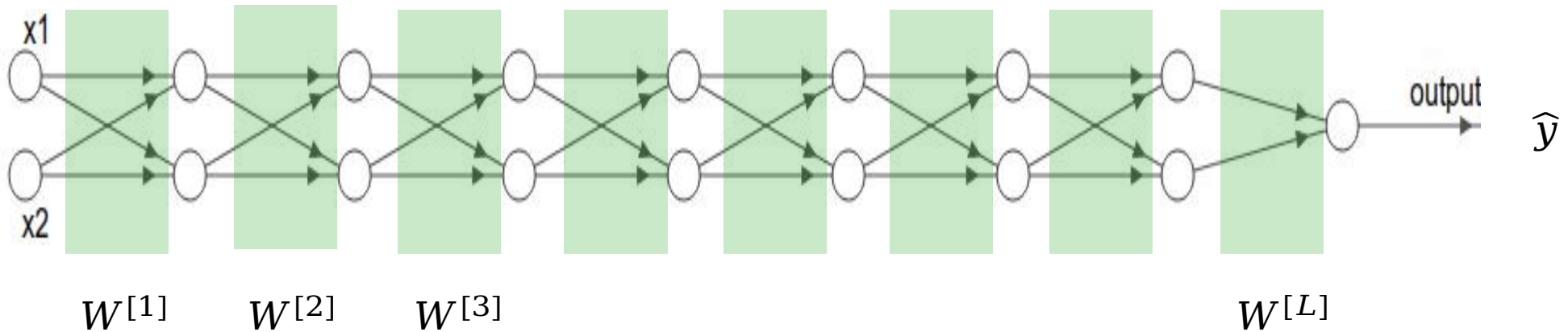
# Giới thiệu Vanishing và Exploding Problem

- General Learning Circle Diagram



# Giới thiệu Vanishing và Exploding Problem

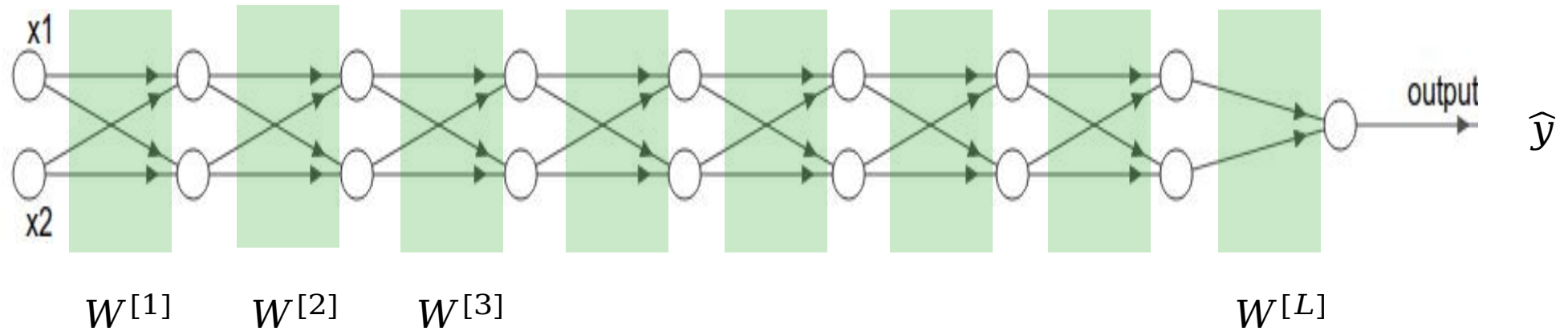
- Forwarding



- $a^0 = x$
- $z^{[l]} = W^{[l]T} * a^{[l-1]}$
- $a^{[l]} = g(z^{[l]})$
- $\hat{y} = a^{[L]} = g(z^{[L]}) = g(W^{[L]T} * g(W^{[L-1]T} * \dots g(W^{[2]T} * g(W^{[1]T} x))))$   
if  $g(\bullet)$  là linear (identity function )  
 $\Rightarrow \hat{y} = a^{[L]} = g(z^{[L]}) = W^{[L]T} * W^{[L-1]T} * \dots W^{[2]T} * W^{[1]T} x$

# Giới thiệu Vanishing và Exploding Problem

## • Backpropagation Algorithm



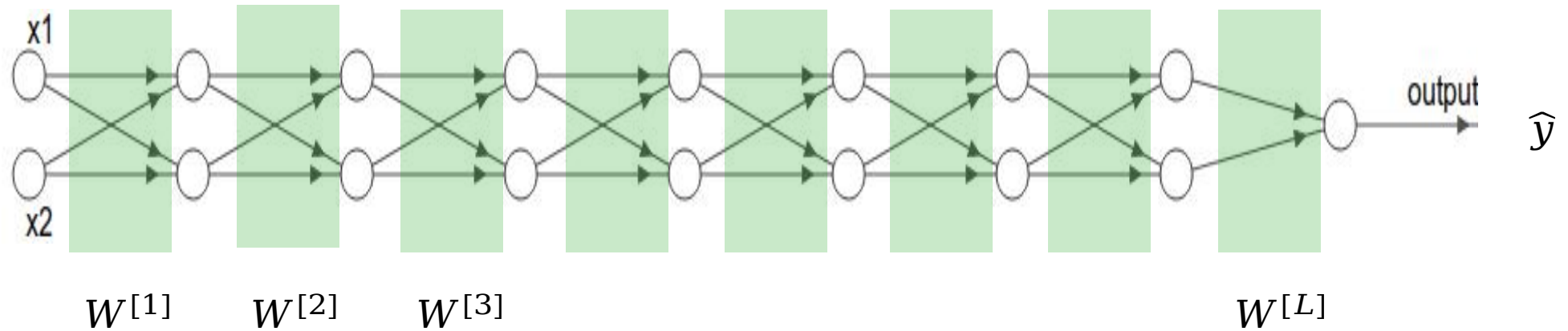
- $\frac{\partial L}{\partial w^{[L]}} = \frac{\partial L}{\partial a^{[L]}} * \frac{\partial a^{[L]}}{\partial z^{[L]}} * \frac{\partial z^{[L]}}{\partial w^{[L]}}$
- $\frac{\partial L}{\partial w^{[1]}} = \frac{\partial L}{\partial a^{[L]}} * \frac{\partial a^{[L]}}{\partial z^{[L]}} * \frac{\partial z^{[L]}}{\partial a^{[L-1]}} \dots * \frac{\partial a^{[2]}}{\partial z^{[2]}} * \frac{\partial z^{[2]}}{\partial a^{[1]}} * \frac{\partial a^{[1]}}{\partial z^{[1]}} * \frac{\partial z^{[1]}}{\partial w^{[1]}}$   
if  $g(\cdot)$  là linear (identity function)
- $\frac{\partial L}{\partial w^{[1]}} = \frac{\partial L}{\partial a^{[L]}} * \frac{\partial a^{[L]}}{\partial a^{[L-1]}} * \frac{\partial a^{[L-1]}}{\partial a^{[L-2]}} * \dots * \frac{\partial a^{[2]}}{\partial a^{[1]}} * \frac{\partial a^{[1]}}{\partial w^{[1]}}$

- $Loss = L(\hat{y}, y), \hat{y} = a^{[L]}$
- $a^{[l]} = g(z^{[l]})$

$$w^{[l]} = w^{[l]} - \eta \frac{\partial L}{\partial w^{[l]}}$$

# Giới thiệu Vanishing và Exploding Problem

- Exploding Problem

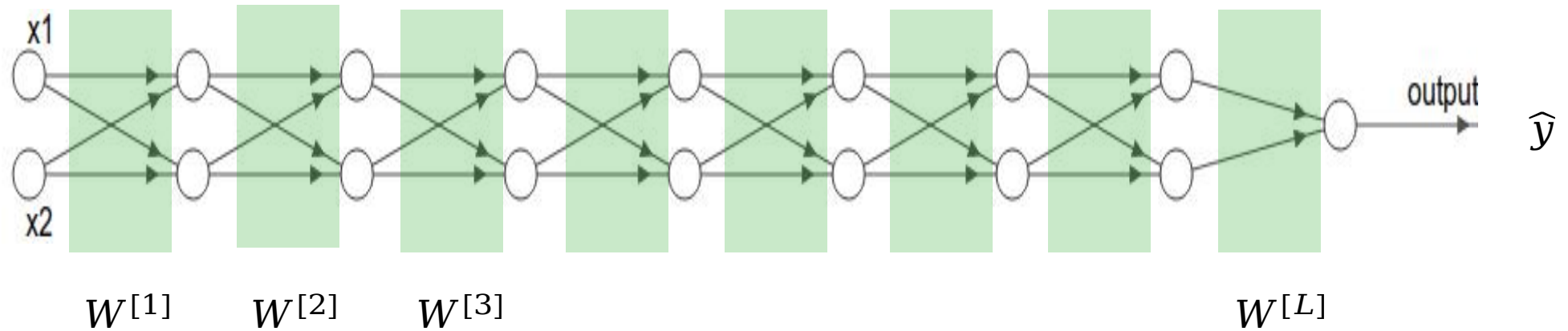


- $a^0 = x$
  - $z^{[l]} = W^{[l]T} * a^{[l-1]}$
  - $a^{[l]} = g(z^{[l]})$
  - $\hat{y} = a^{[L]} = g(z^{[L]}) = g(W^{[L]T} * g(W^{[L-1]T} * \dots * g(W^{[2]T} * g(W^{[1]T} x))))$
- if  $g(\cdot)$  là linear (identity function )
- Tất cả = 10** **=> chỉ 7 layers  $\hat{y} = 10^7$**
- $\Rightarrow \hat{y} = a^{[L]} = g(z^{[L]}) = W^{[L]T} * W^{[L-1]T} * \dots * W^{[2]T} * W^{[1]T} x$



# Giới thiệu Vanishing và Exploding Problem

## • Exploding Problem



**Tất cả = 10**  $\Rightarrow$  chỉ 7 layers =  $10^7$

$$\bullet \frac{\partial L}{\partial w^{[L]}} = \frac{\partial L}{\partial a^{[L]}} * \frac{\partial a^{[L]}}{\partial z^{[L]}} * \frac{\partial z^{[L]}}{\partial w^{[L]}}$$

$$\bullet \frac{\partial L}{\partial w^{[1]}} = \frac{\partial L}{\partial a^{[L]}} * \frac{\partial a^{[L]}}{\partial z^{[L]}} * \frac{\partial z^{[L]}}{\partial a^{[L-1]}} \dots * \frac{\partial a^{[2]}}{\partial z^{[2]}} * \frac{\partial z^{[2]}}{\partial a^{[1]}} * \frac{\partial a^{[1]}}{\partial z^{[1]}} * \frac{\partial z^{[1]}}{\partial w^{[1]}}$$

if  $g(\cdot)$  là linear (identity function)

$$\bullet \frac{\partial L}{\partial w^{[1]}} = \frac{\partial L}{\partial a^{[L]}} * \frac{\partial a^{[L]}}{\partial a^{[L-1]}} * \frac{\partial a^{[L-1]}}{\partial a^{[L-2]}} * \dots * \frac{\partial a^{[2]}}{\partial a^{[1]}} * \frac{\partial a^{[1]}}{\partial w^{[1]}}$$

$$\bullet \text{Loss} = L(\hat{y}, y), \quad \hat{y} = a^{[L]}$$

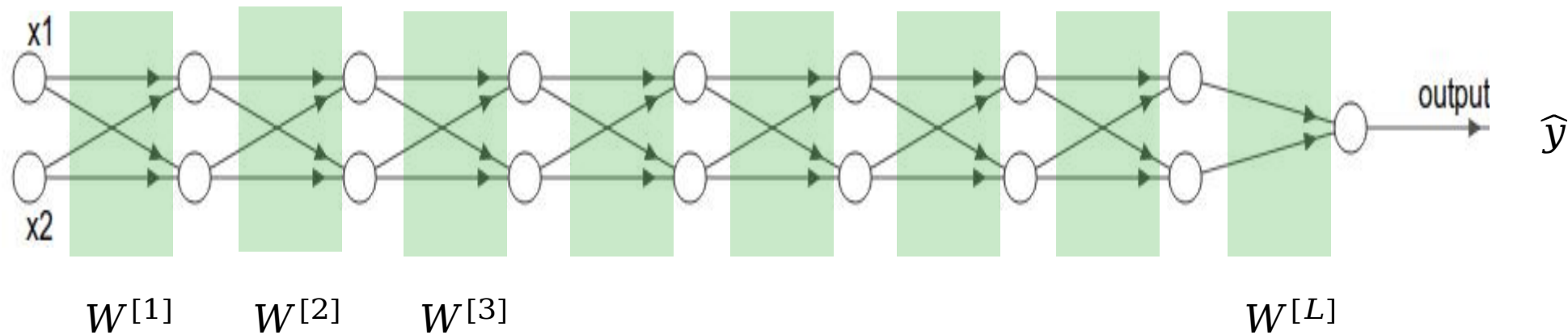
$$\bullet a^{[l]} = g(z^{[l]})$$

$$w^{[l]} = w^{[l]} - \eta \frac{\partial L}{\partial w^{[l]}}$$



# Giới thiệu Vanishing và Exploding Problem

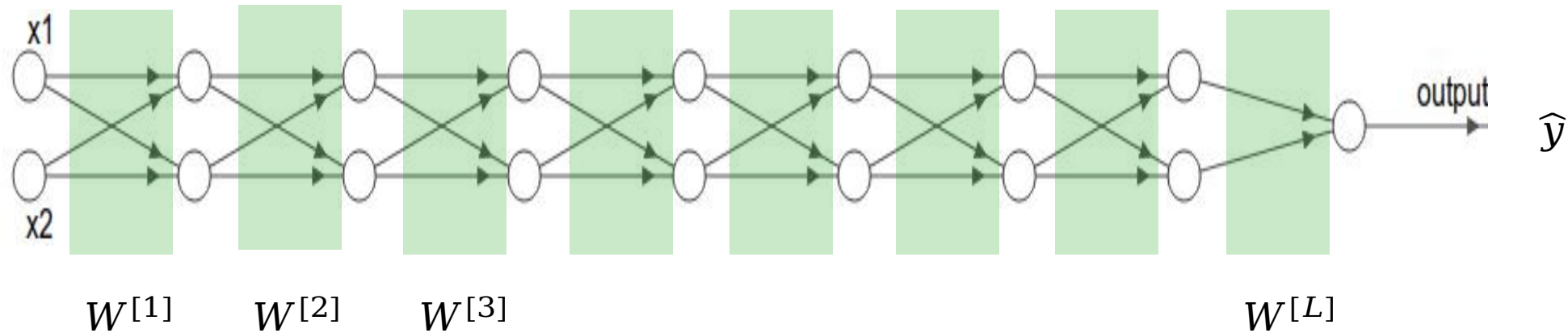
- **Exploding Problem**



- “*exploding gradients can make learning unstable*”. Page 282, Deep Learning (by Goodfellow, Yoshua Bengio, Aaron Courville), 2016
- **Exploding** trong trường hợp tốt nhất việc update weight một lượng lớn làm network học không ổn định và không thể hội tụ
- **Exploding** trong trường hợp xấu nhất NaN weight không thể update
- Một số dấu hiệu của exploding: loss là NaN, loss rất lớn và không có dấu hiệu giảm, model không ổn định loss tăng giảm không ổn định nhưng nhìn chung vẫn lớn

# Giới thiệu Vanishing và Exploding Problem

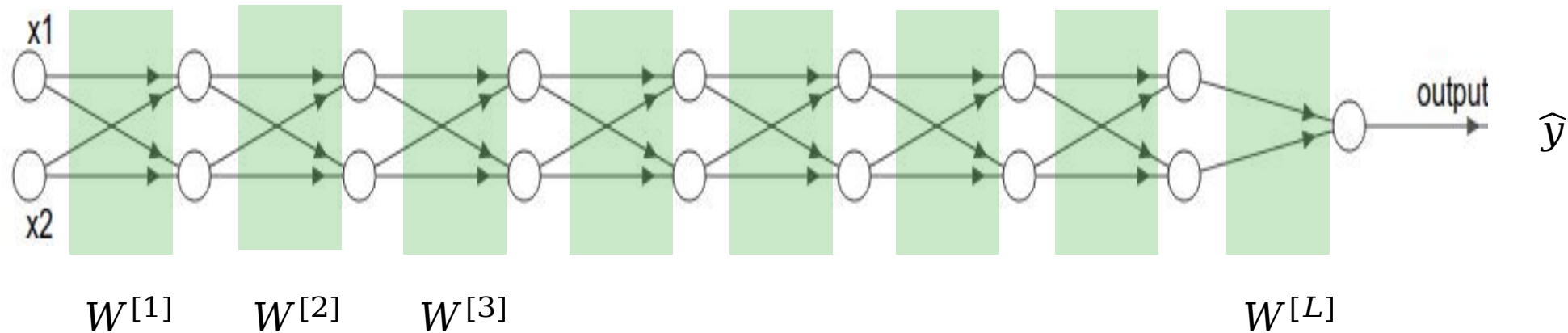
- **Vanishing Problem**



- $a^0 = x$
  - $z^{[l]} = W^{[l]T} * a^{[l-1]}$
  - $a^{[l]} = g(z^{[l]})$
  - $\hat{y} = a^{[L]} = g(z^{[L]}) = g(W^{[L]T} * g(W^{[L-1]T} * \dots * g(W^{[2]T} * g(W^{[1]T} x))))$
- if  $g(\cdot)$  là linear (identity function )
- Tất cả = 0.1** **=> chỉ 7 layers  $\hat{y} = 0.1^7$**
- =>  $\hat{y} = a^{[L]} = g(z^{[L]}) = W^{[L]T} * W^{[L-1]T} * \dots * W^{[2]T} * W^{[1]T} x$**

# Giới thiệu Vanishing và Exploding Problem

## • Vanishing Problem



Tất cả = 0.1  $\Rightarrow$  chỉ 7 layers =  $0.1^7$

$$\bullet \frac{\partial L}{\partial w^{[L]}} = \frac{\partial L}{\partial a^{[L]}} * \frac{\partial a^{[L]}}{\partial z^{[L]}} * \frac{\partial z^{[L]}}{\partial w^{[L]}}$$

$$\bullet \frac{\partial L}{\partial w^{[1]}} = \frac{\partial L}{\partial a^{[L]}} * \frac{\partial a^{[L]}}{\partial z^{[L]}} * \frac{\partial z^{[L]}}{\partial a^{[L-1]}} \dots * \frac{\partial a^{[2]}}{\partial z^{[2]}} * \frac{\partial z^{[2]}}{\partial a^{[1]}} * \frac{\partial a^{[1]}}{\partial z^{[1]}} * \frac{\partial z^{[1]}}{\partial w^{[1]}}$$

if  $g(\cdot)$  là linear (identity function)

$$\bullet \frac{\partial L}{\partial w^{[1]}} = \frac{\partial L}{\partial a^{[L]}} * \frac{\partial a^{[L]}}{\partial a^{[L-1]}} * \frac{\partial a^{[L-1]}}{\partial a^{[L-2]}} * \dots * \frac{\partial a^{[2]}}{\partial a^{[1]}} * \frac{\partial a^{[1]}}{\partial w^{[1]}}$$

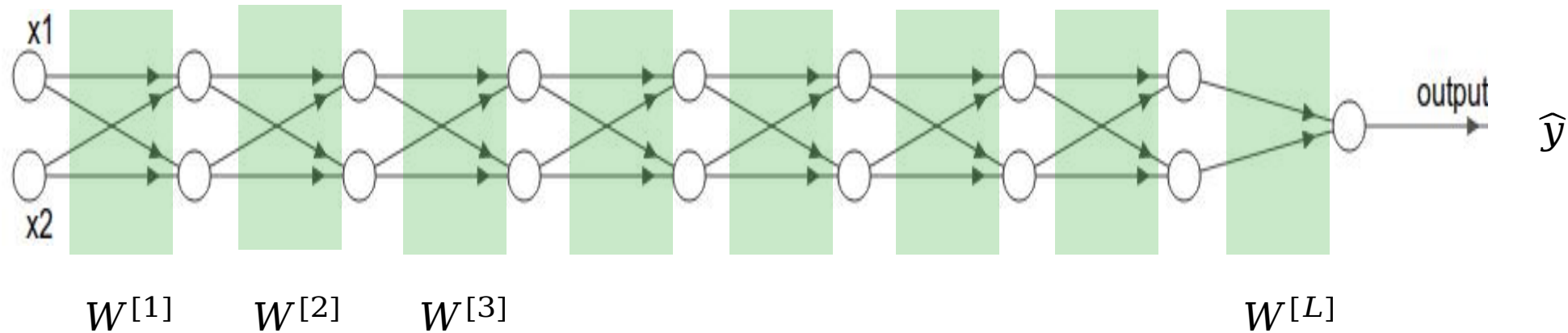
$$\bullet \text{Loss} = L(\hat{y}, y), \quad \hat{y} = a^{[L]}$$

$$\bullet a^{[l]} = g(z^{[l]})$$

$$w^{[l]} = w^{[l]} - \eta \frac{\partial L}{\partial w^{[l]}}$$

# Giới thiệu Vanishing và Exploding Problem

- **Vanishing Problem**



- **Backpropagation** dùng **chain rule**, khi tính **loss** sẽ là **tích của các gradient** trong **từng layer**
- Gradient càng nhỏ khi nhân lại với nhau sẽ càng tiến về 0
- Parameter ở các **layer gần input** sẽ **không đóng góp** vào việc học của model

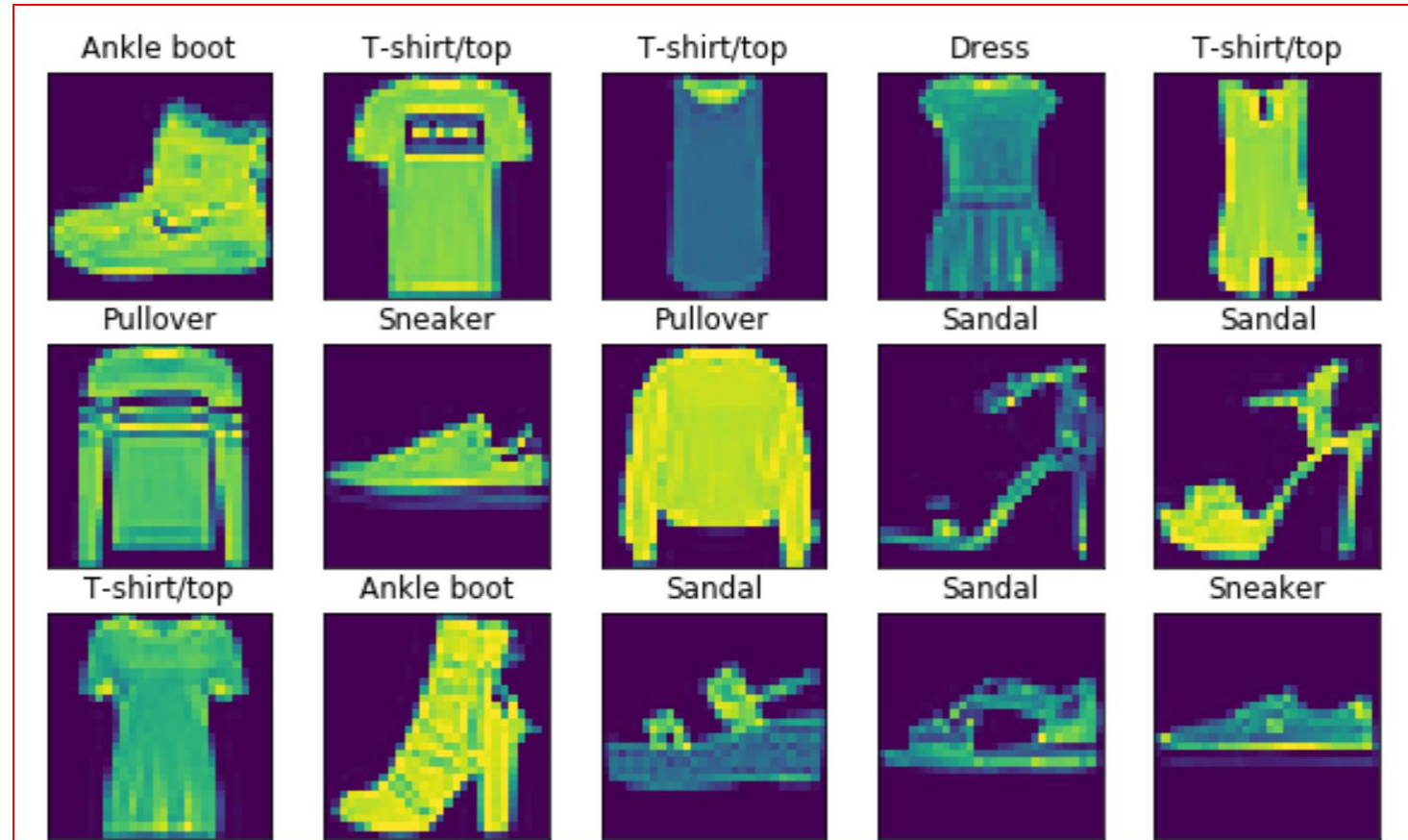
# Giới thiệu Vanishing và Exploding Problem

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- Giới thiệu Vanishing và Exploding Problem
  - Vanishing Problem
  - Exploding Problem
- **Fashion MNIST Vanishing Problem**
  - Giới thiệu vấn đề
  - Solution1: Weight Increasing
  - Solution2: Better Activation
  - Solution3: Better Optimizer
  - Solution4: Normalize Inside Network
  - Solution5: Skip Connection
  - Solution6: Train Some Layer

# Fashion MNIST Vanishing Problem

- Giới thiệu vấn đề
  - Fashion MNIS dataset
    - **Train:** 60,000 samples
    - **Test:** 10,000 samples
    - **Classes:** 10
    - **Size:** 28x28
    - **Image type:** grayscale



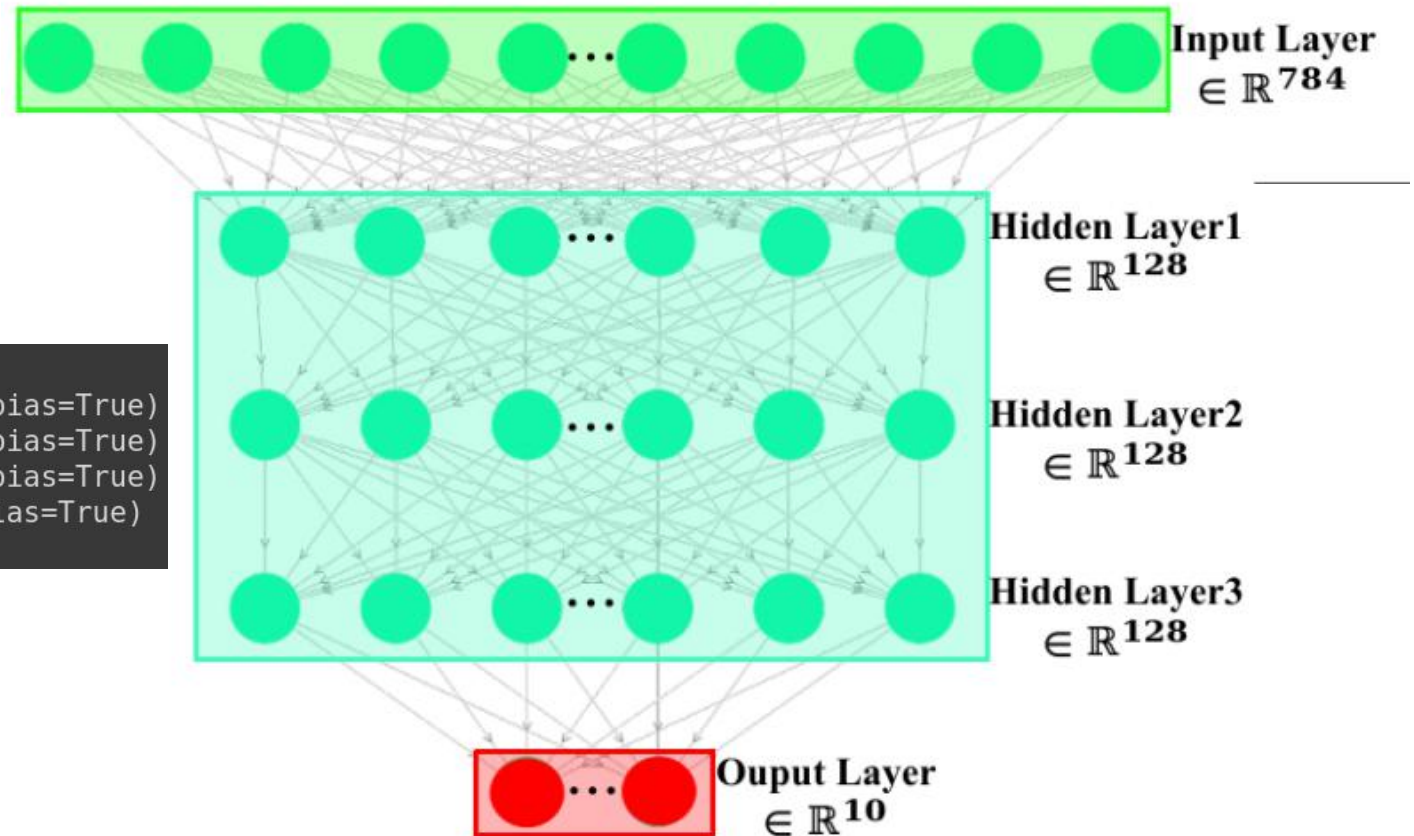


# Fashion MNIST Vanishing Problem

- **Giới thiệu vấn đề**

- Model1:

- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** 3 layers
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** CE
    - **Optimizer:** sgd



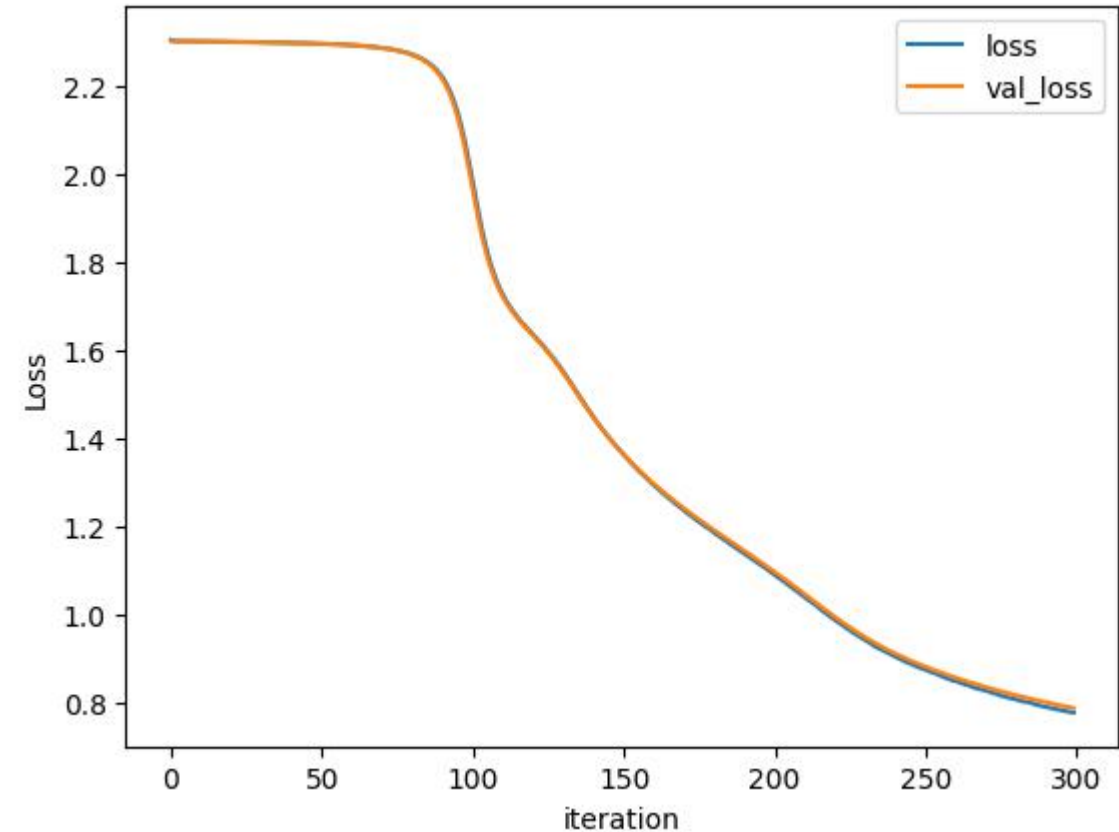
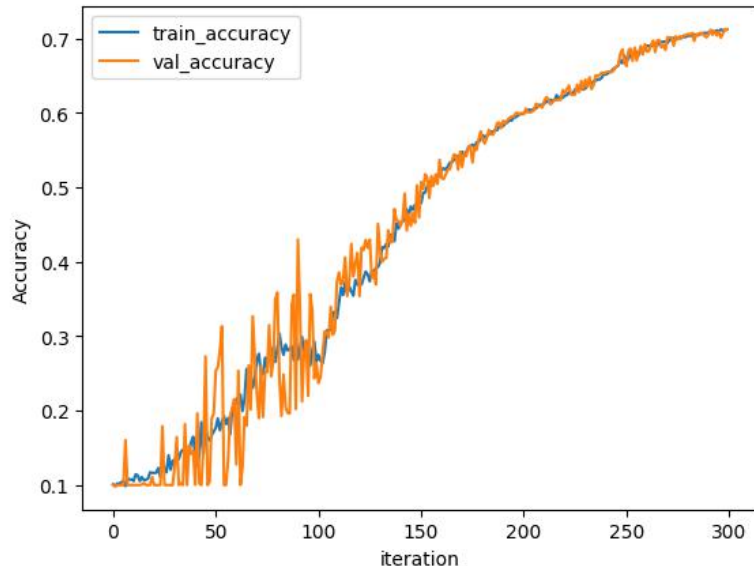
```
MLP(  
  (layer1): Linear(in_features=784, out_features=128, bias=True)  
  (layer2): Linear(in_features=128, out_features=128, bias=True)  
  (layer3): Linear(in_features=128, out_features=128, bias=True)  
  (output): Linear(in_features=128, out_features=10, bias=True)  
)
```

# Fashion MNIST Vanishing Problem

- **Giới thiệu vấn đề**

- Model1:

- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** 3 layers
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** CE
    - **Optimizer:** sgd



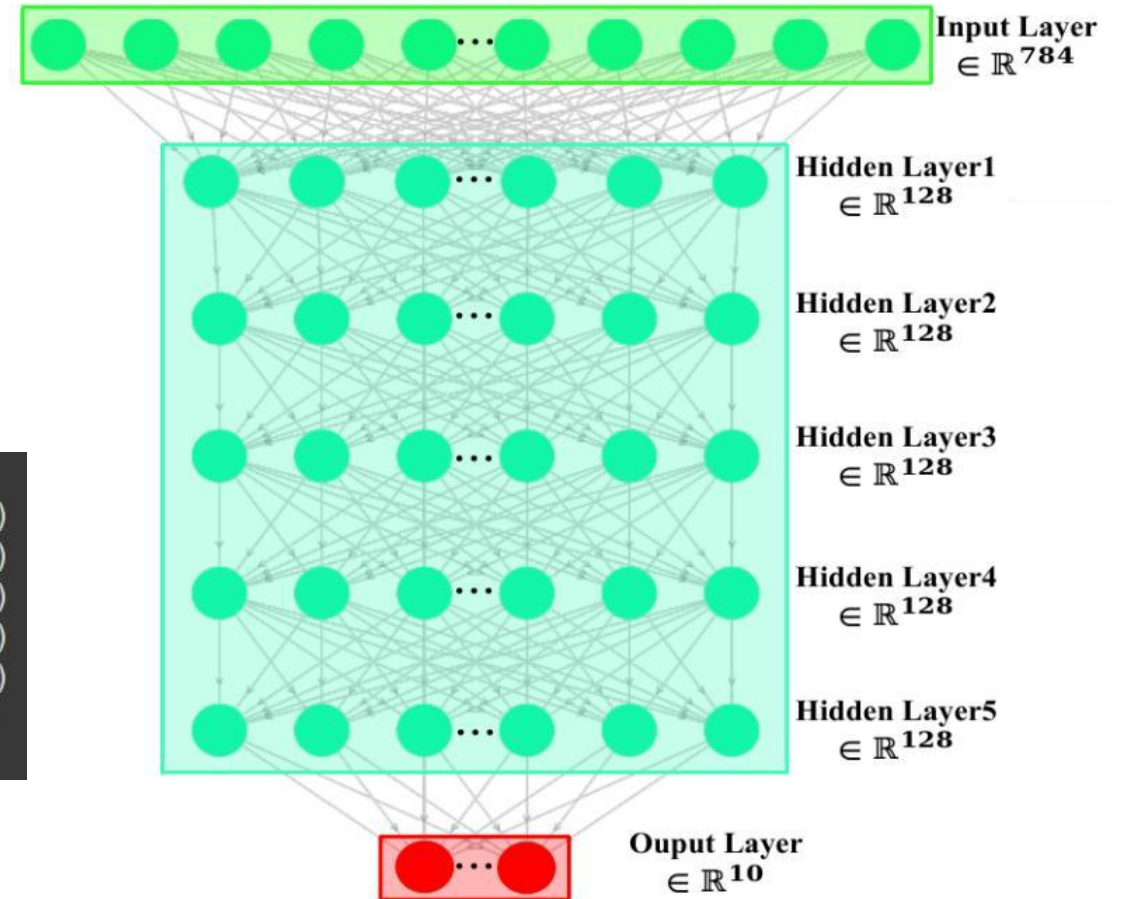
# Fashion MNIST Vanishing Problem

- Giới thiệu vấn đề

- Model2:

- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** 5 layers
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** CE
    - **Optimizer:** sgd

```
MLP(  
  (layer1): Linear(in_features=784, out_features=128, bias=True)  
  (layer2): Linear(in_features=128, out_features=128, bias=True)  
  (layer3): Linear(in_features=128, out_features=128, bias=True)  
  (layer4): Linear(in_features=128, out_features=128, bias=True)  
  (layer5): Linear(in_features=128, out_features=128, bias=True)  
  (output): Linear(in_features=128, out_features=10, bias=True)  
)
```

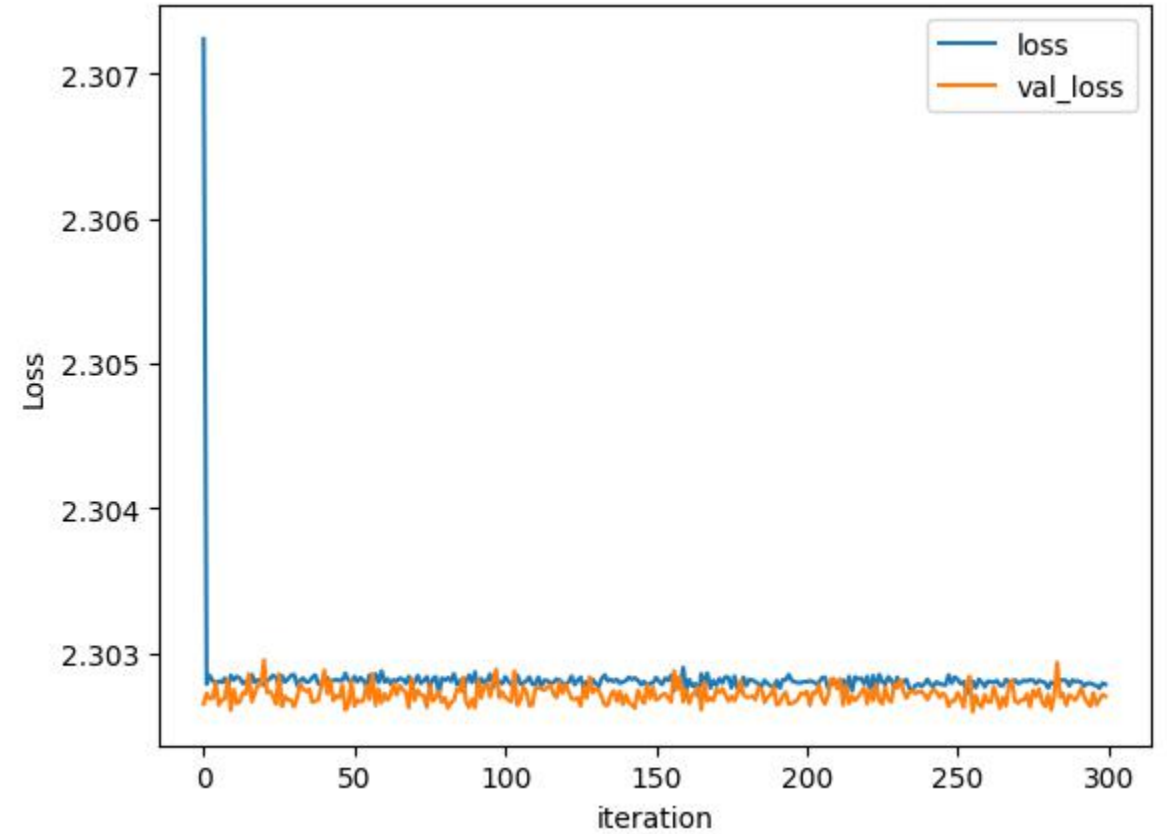
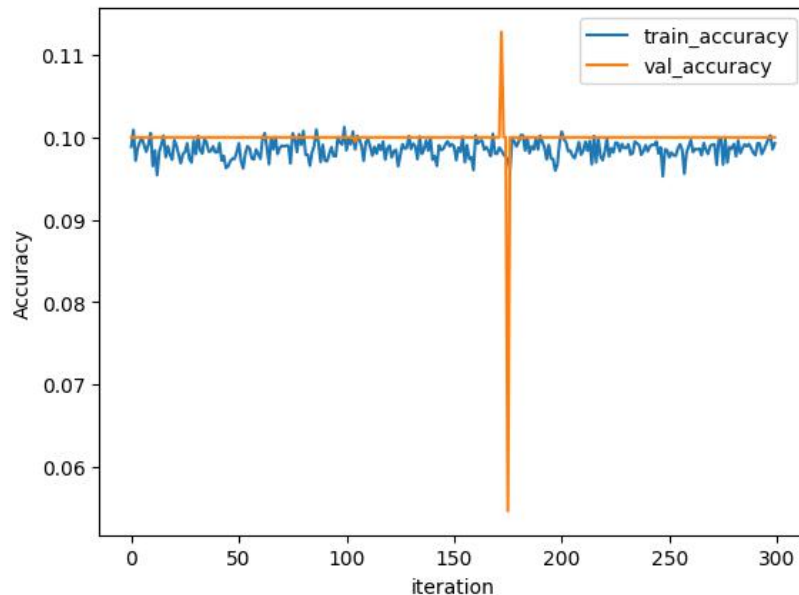


# Fashion MNIST Vanishing Problem

- **Giới thiệu vấn đề**

- Model2:

- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** 5 layers
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** CE
    - **Optimizer:** sgd





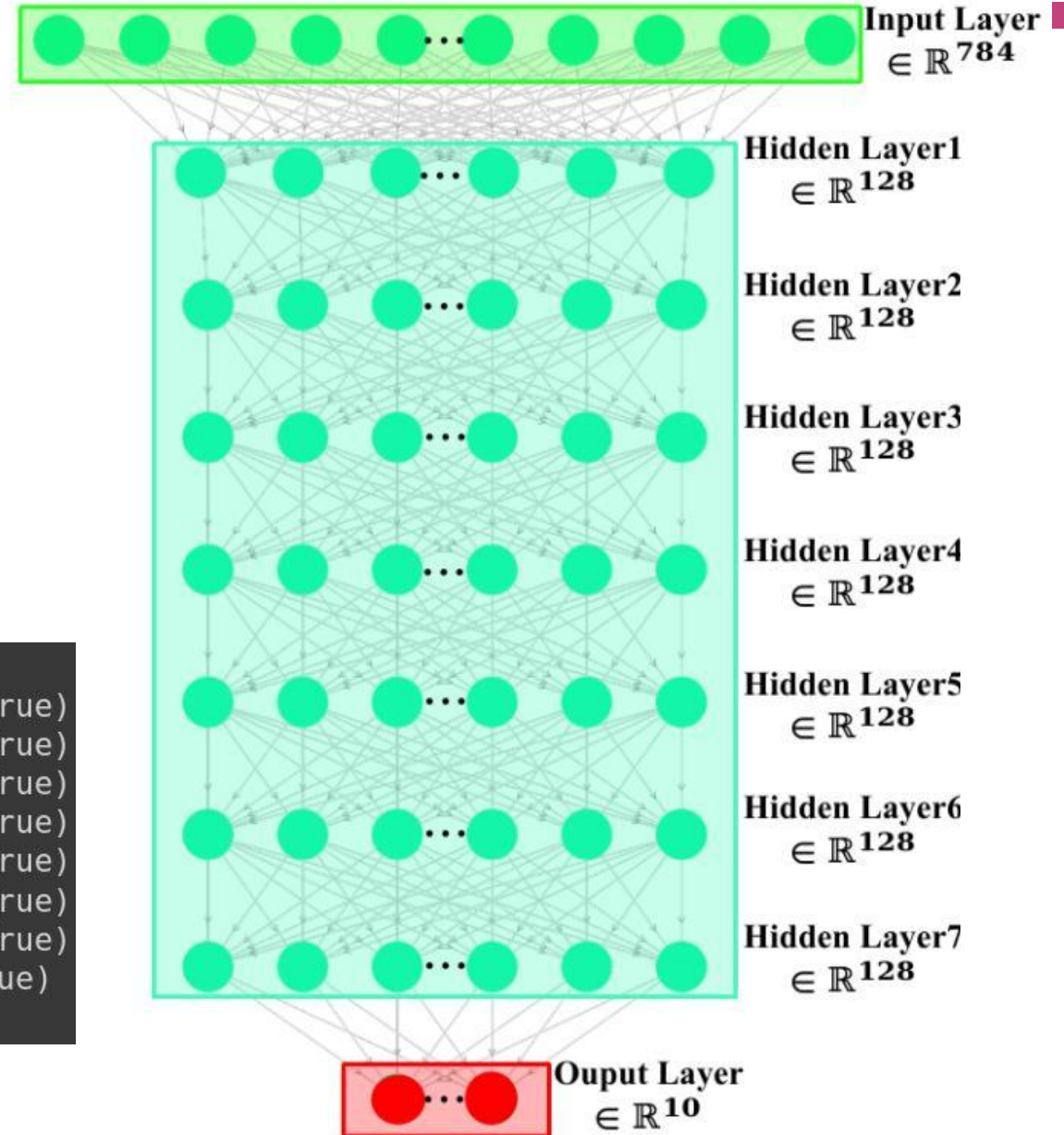
# Fashion MNIST Vanishing Problem

- **Giới thiệu vấn đề**

- Model3:

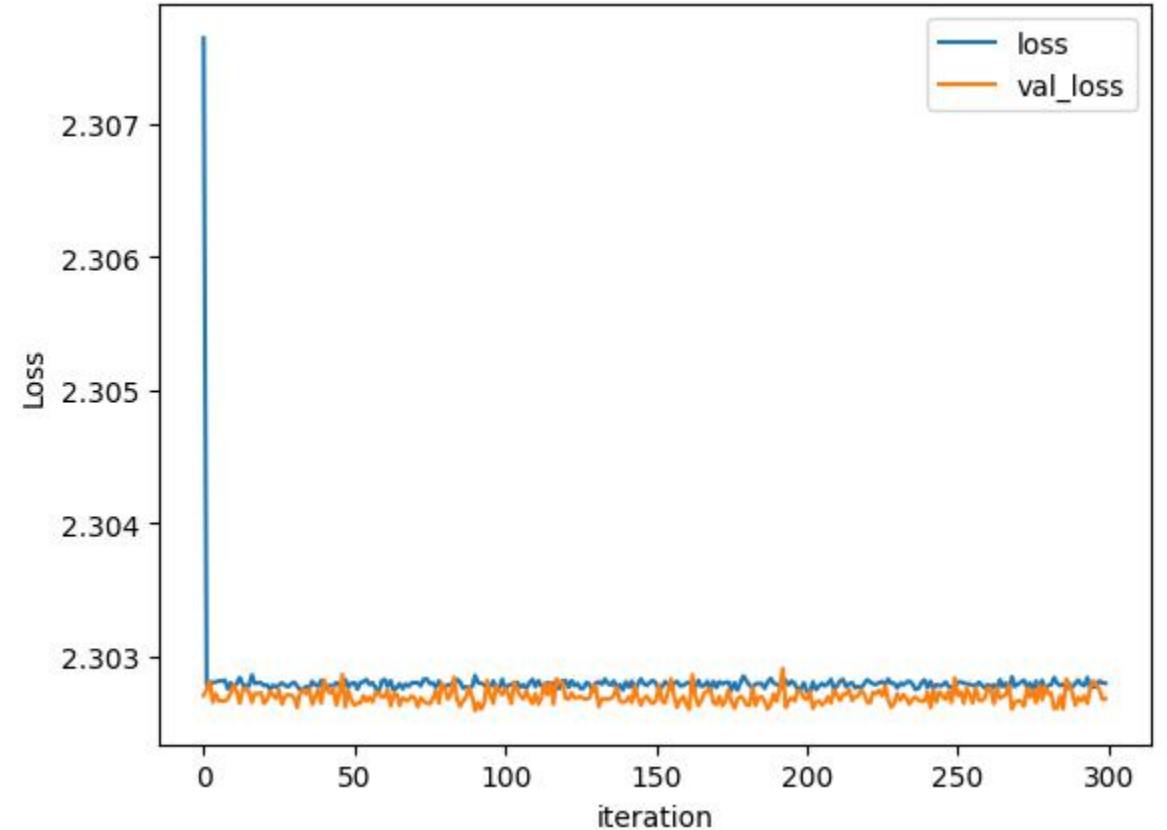
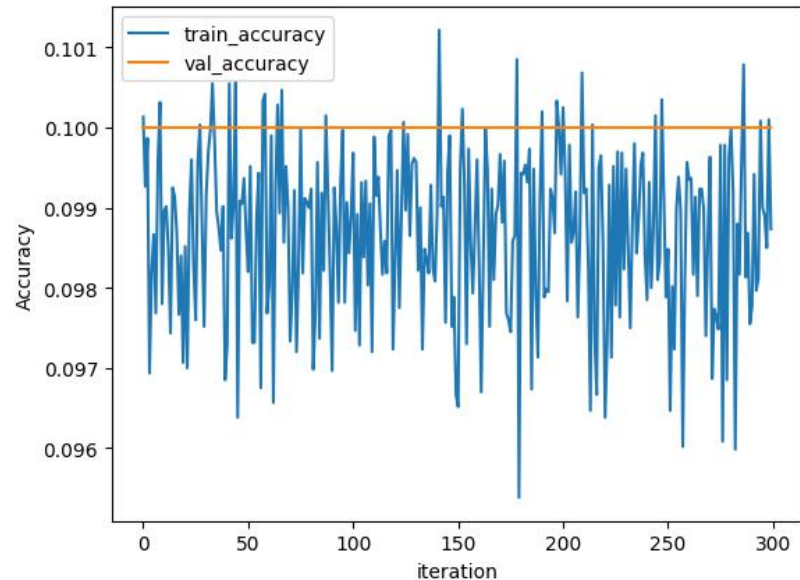
- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** 7 layers
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** CE
    - **Optimizer:** sgd

```
MLP(  
  (layer1): Linear(in_features=784, out_features=128, bias=True)  
  (layer2): Linear(in_features=128, out_features=128, bias=True)  
  (layer3): Linear(in_features=128, out_features=128, bias=True)  
  (layer4): Linear(in_features=128, out_features=128, bias=True)  
  (layer5): Linear(in_features=128, out_features=128, bias=True)  
  (layer6): Linear(in_features=128, out_features=128, bias=True)  
  (layer7): Linear(in_features=128, out_features=128, bias=True)  
  (output): Linear(in_features=128, out_features=10, bias=True)  
)
```



# Fashion MNIST Vanishing Problem

- Giới thiệu vấn đề
  - Model3:
    - Weight Initialization:  $\mu=0, \sigma=0.05$
    - Hidden Layers: 7 layers
    - Activation: sigmoid
    - Nodes: 128
    - Loss: CE
    - Optimizer: sgd



# Fashion MNIST Vanishing Problem

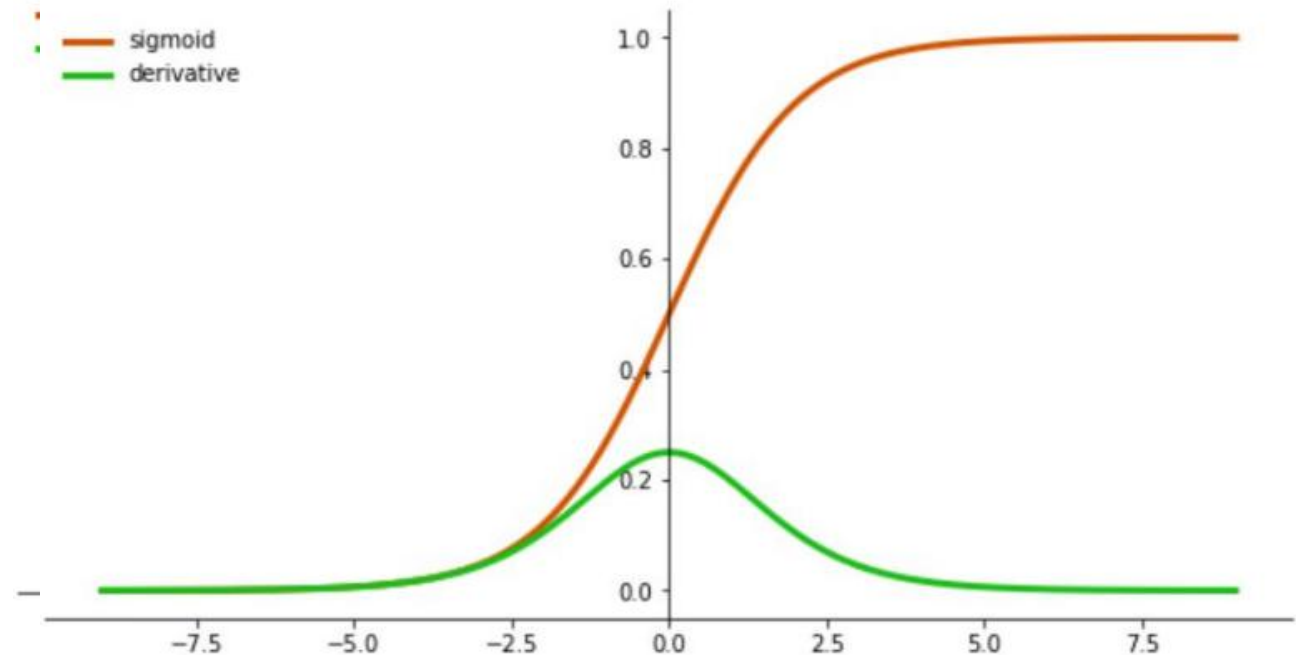
- **Giới thiệu vấn đề**
  - Các nguyên nhân có thể gây ra vanishing problem

$$\text{sigmoid}(x) = \frac{1}{1 + e^{-x}}$$

$$\sigma'(x) = \sigma(x)(1 - \sigma(x))$$

**Giá trị của đạo hàm:**

- min = 0
- max = 0.25

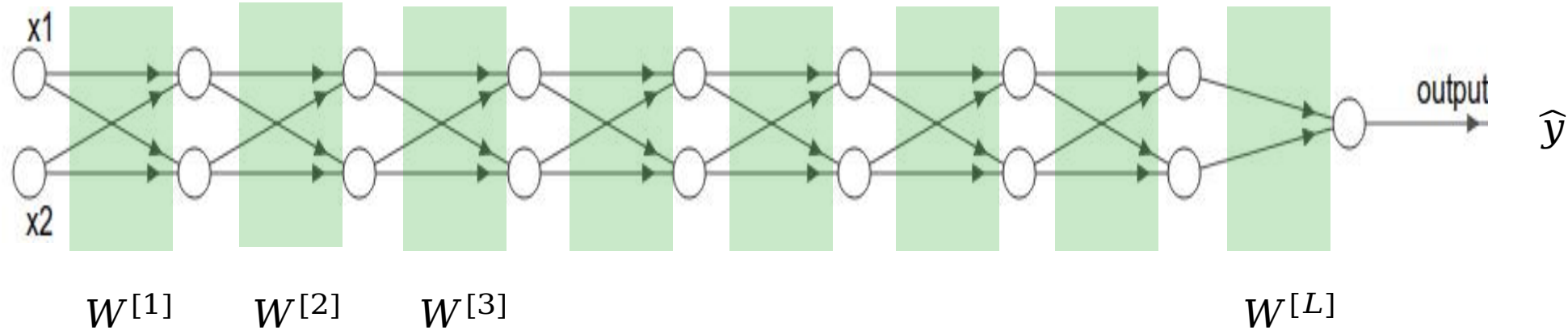




# Giới thiệu Vanishing và Exploding Problem

## • Giới thiệu vấn đề

- Các nguyên nhân có thể gây ra vanishing problem



$$\bullet \frac{\partial L}{\partial w^{[L]}} = \frac{\partial L}{\partial a^{[L]}} * \frac{\partial a^{[L]}}{\partial z^{[L]}} * \frac{\partial z^{[L]}}{\partial w^{[L]}}$$

=> chỉ 7 layers với giá trị đạo hàm đạt tối đa cho mỗi layer =  $0,25^7 \approx 6.10^{-5}$

if  $g(\cdot)$  là sigmoid function  $\sigma(x)$

$$\bullet \frac{\partial L}{\partial w^{[1]}} = \frac{\partial L}{\partial a^{[L]}} * \underbrace{\frac{\partial a^{[L]}}{\partial z^{[L]}}}_{[0; 0,25]} * \frac{\partial z^{[L]}}{\partial a^{[L-1]}} \dots * \underbrace{\frac{\partial a^{[2]}}{\partial z^{[2]}}}_{[0; 0,25]} * \frac{\partial z^{[2]}}{\partial a^{[1]}} * \underbrace{\frac{\partial a^{[1]}}{\partial z^{[1]}}}_{[0; 0,25]} * \frac{\partial z^{[1]}}{\partial w^{[1]}}$$

$$\bullet Loss = L(\hat{y}, y), \quad \hat{y} = a^{[L]}$$

$$\bullet a^{[l]} = g(z^{[l]})$$

$$w^{[l]} = w^{[l]} - \eta \frac{\partial L}{\partial w^{[l]}}$$

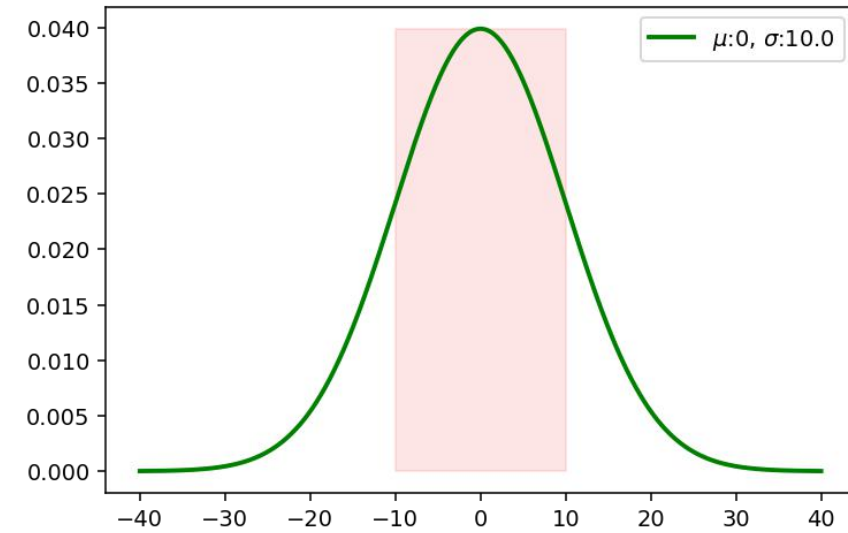
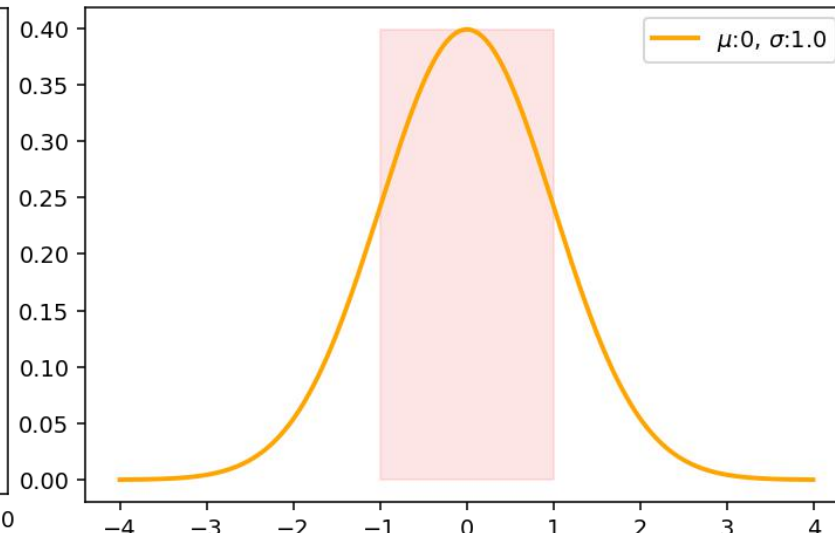
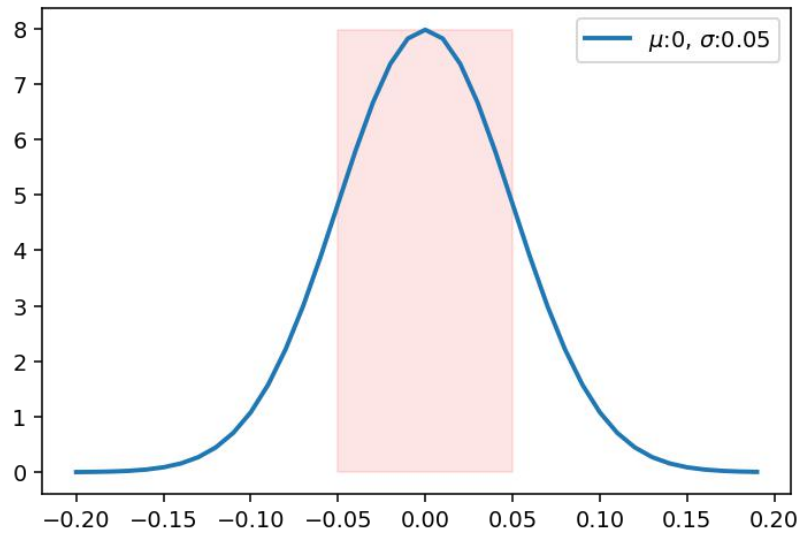
# Fashion MNIST Vanishing Problem

$$f(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}$$

$f(x)$  = probability density function

$\sigma$  = standard deviation

$\mu$  = mean



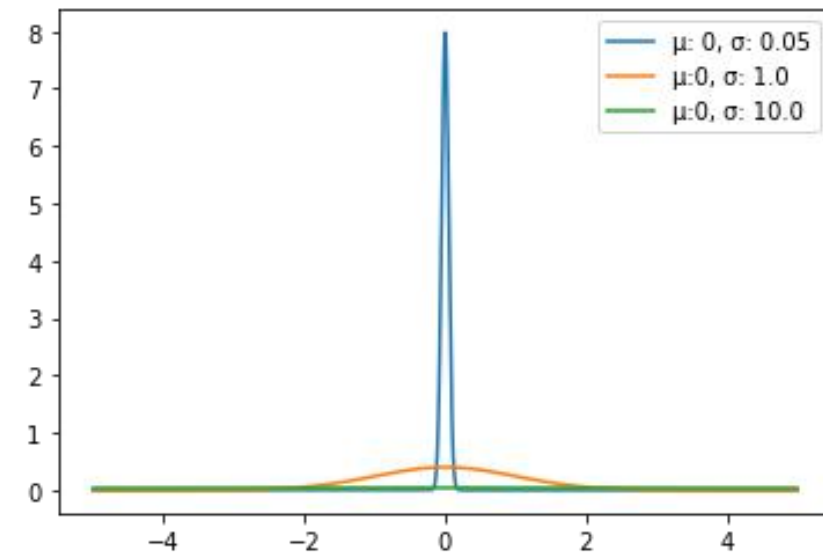
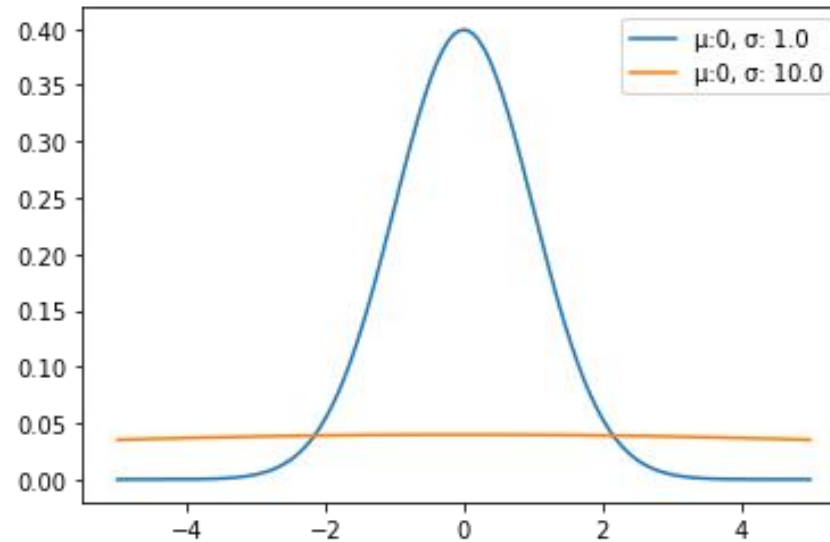
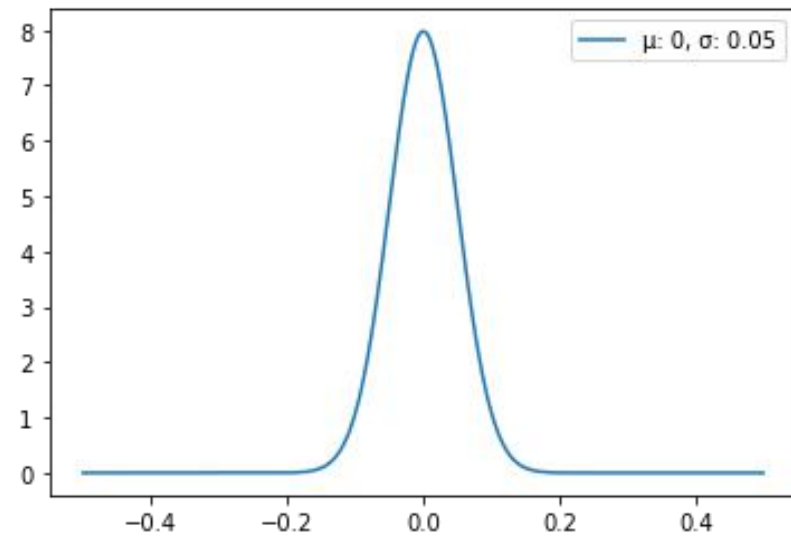
# Fashion MNIST Vanishing Problem

$$f(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}$$

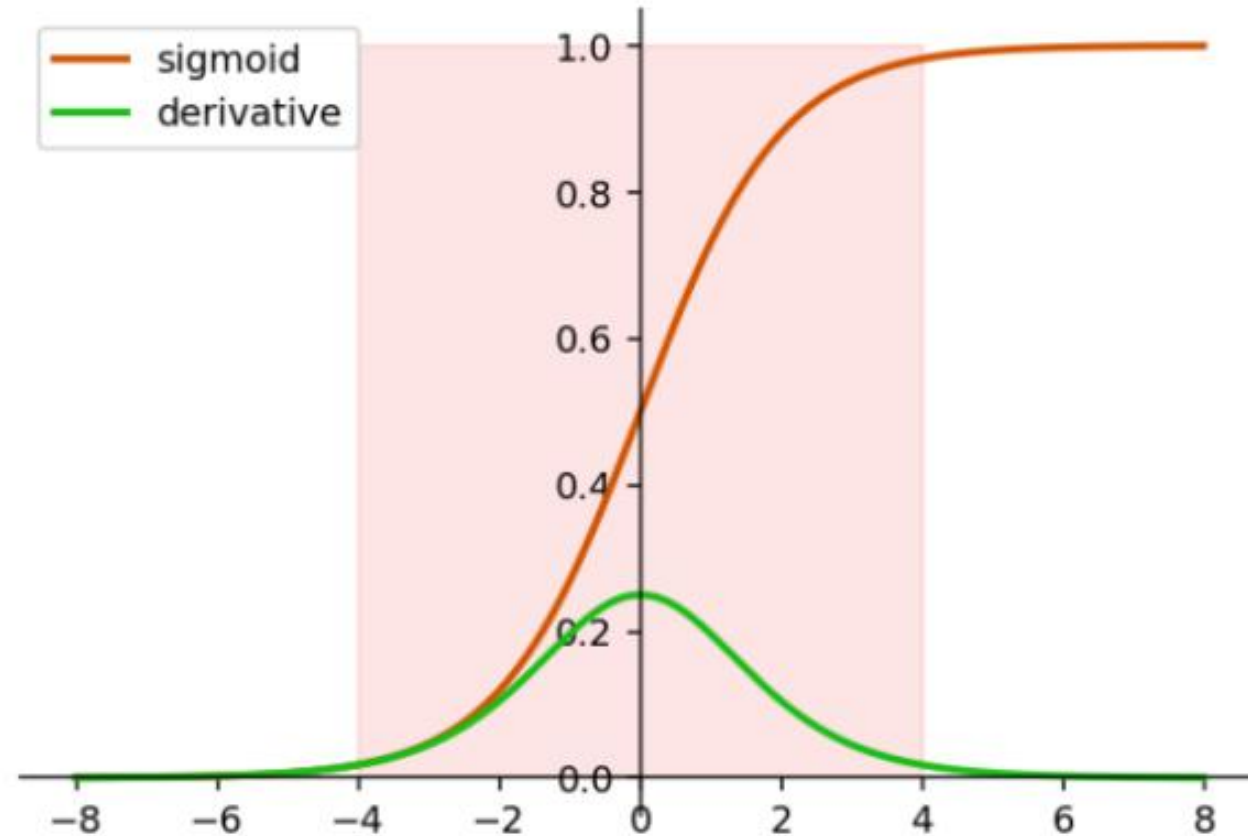
$f(x)$  = probability density function

$\sigma$  = standard deviation

$\mu$  = mean



# Fashion MNIST Vanishing Problem

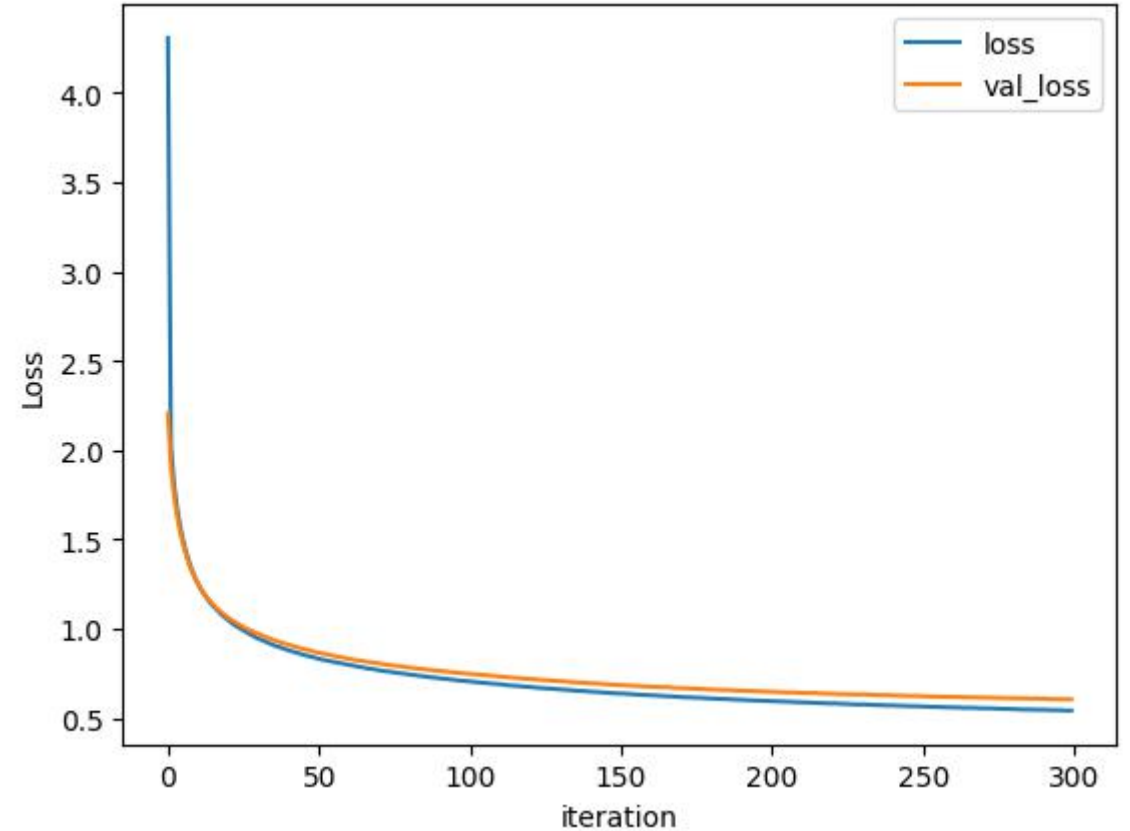
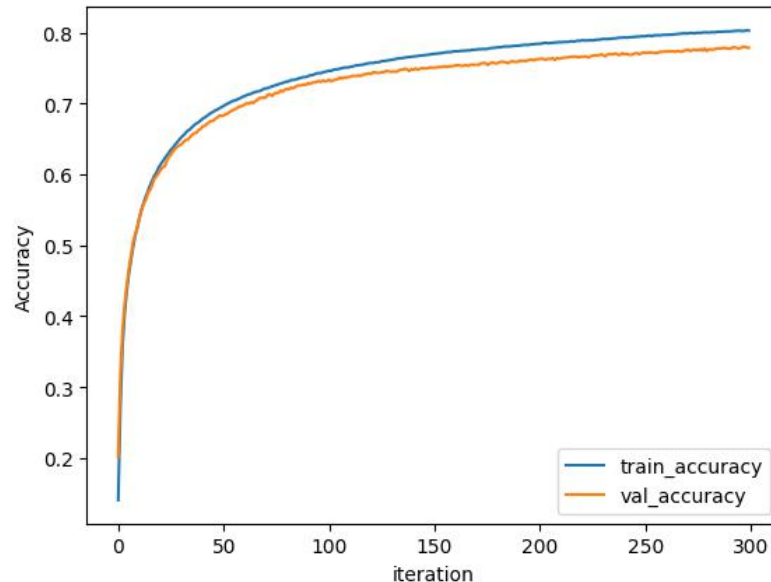


# Fashion MNIST Vanishing Problem

- **Weight Increasing**

- Model:

- **Weight Initialization:**  $\mu=0$ ,  $\sigma=1.0$
    - **Hidden Layers:** 7 layers
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** CE
    - **Optimizer:** sgd

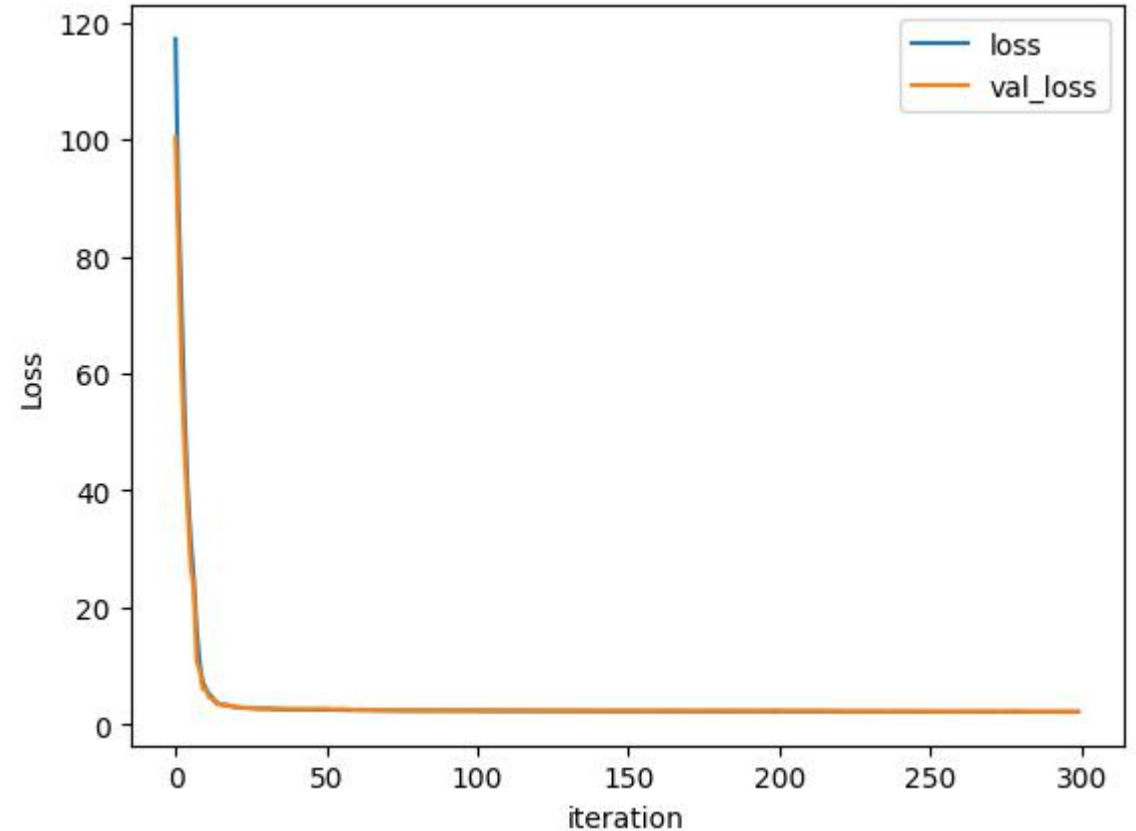
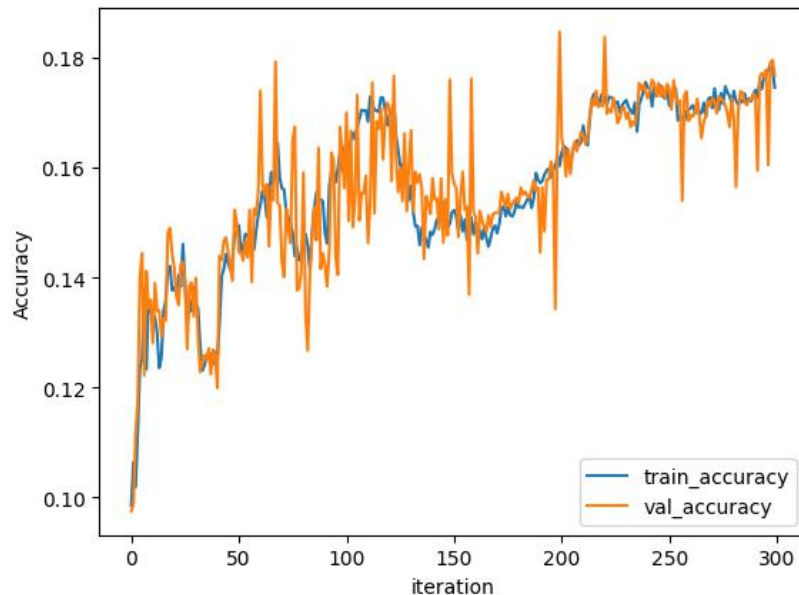


# Fashion MNIST Vanishing Problem

- **Weight Increasing**

- Model:

- **Weight Initialization:**  $\mu=0$ ,  $\sigma=10.0$
    - **Hidden Layers:** 7 layers
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** CE
    - **Optimizer:** sgd





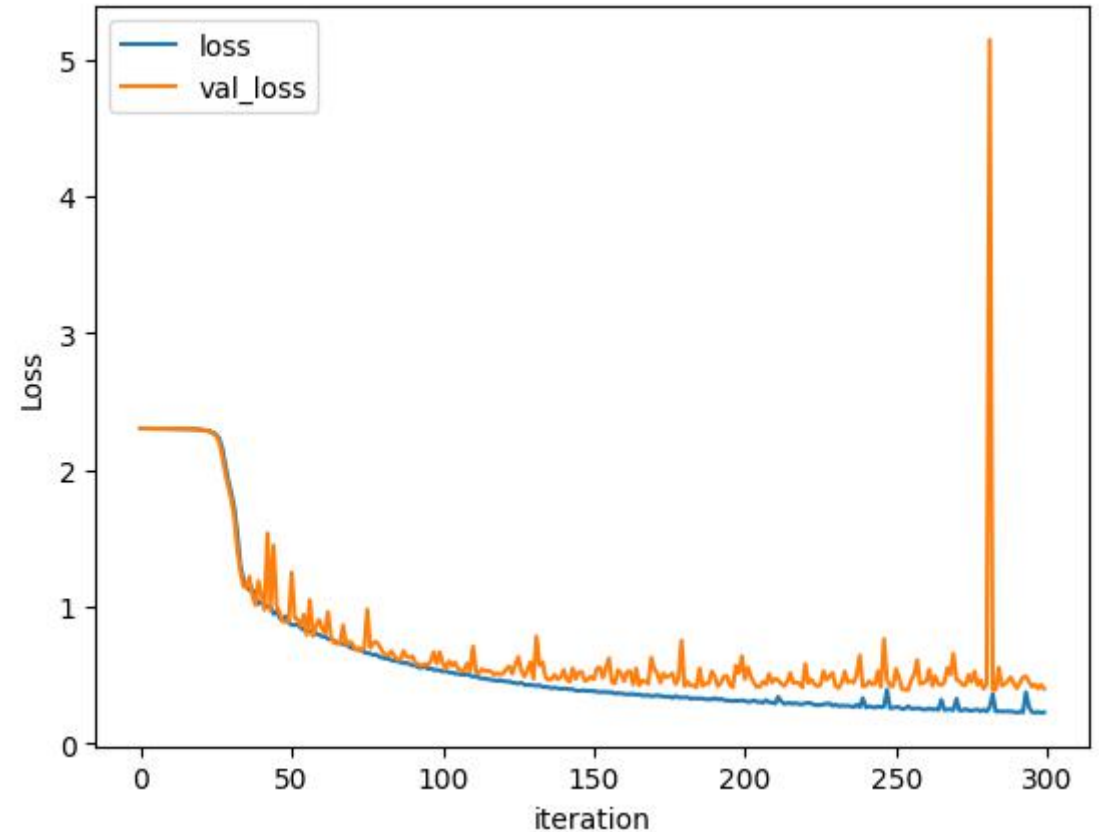
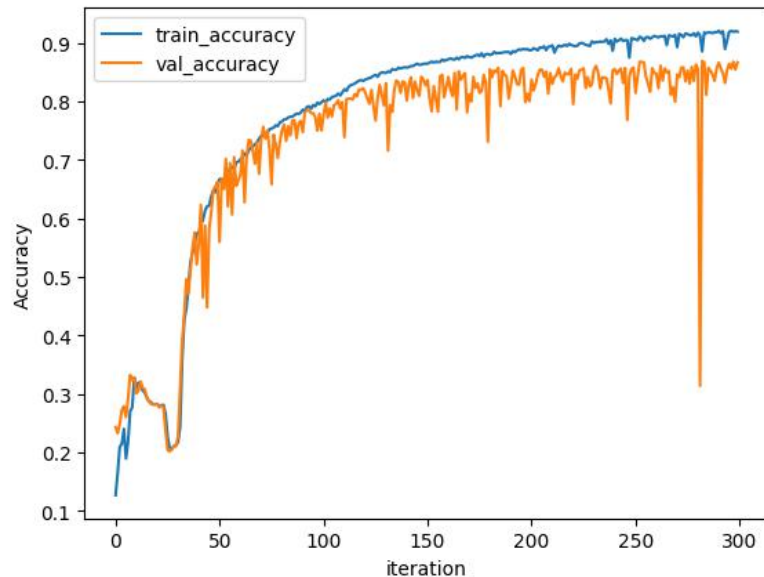


# Fashion MNIST Vanishing Problem

- **Better Activation**

- Model:

- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** 7 layers
    - **Activation:** **relu**
    - **Nodes:** 128
    - **Loss:** CE
    - **Optimizer:** sgd

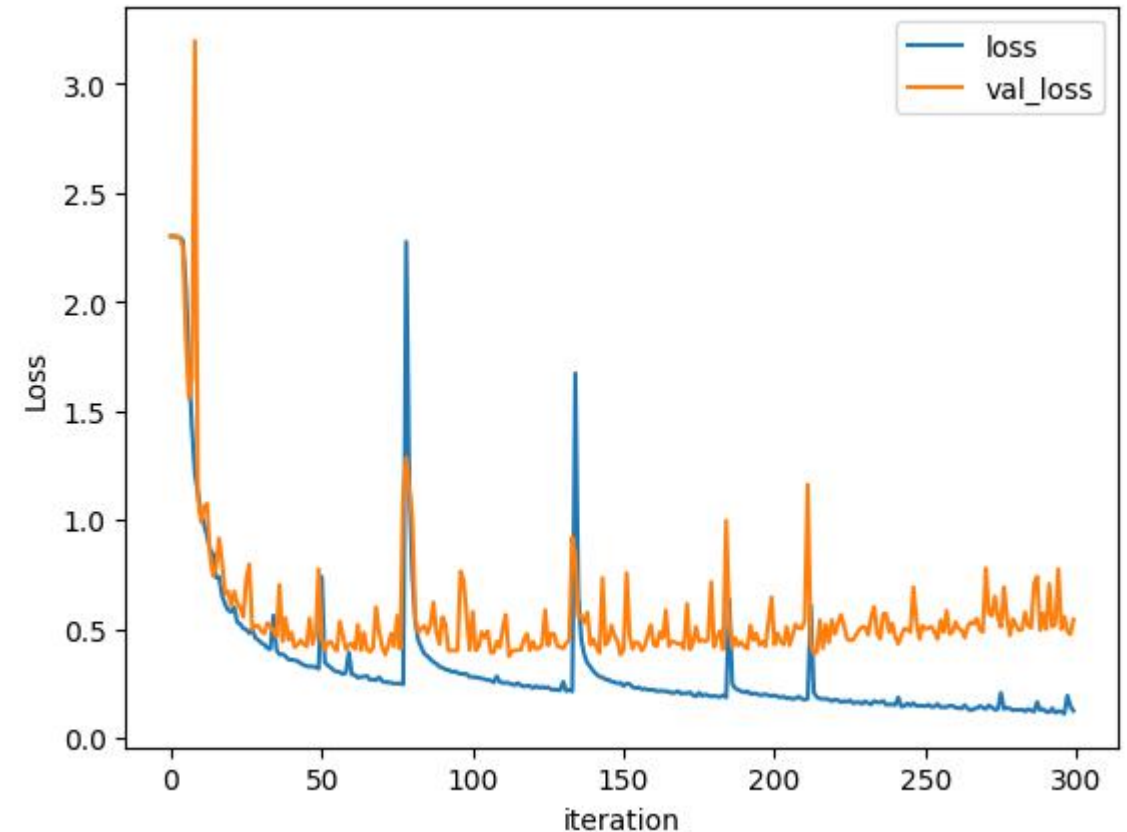
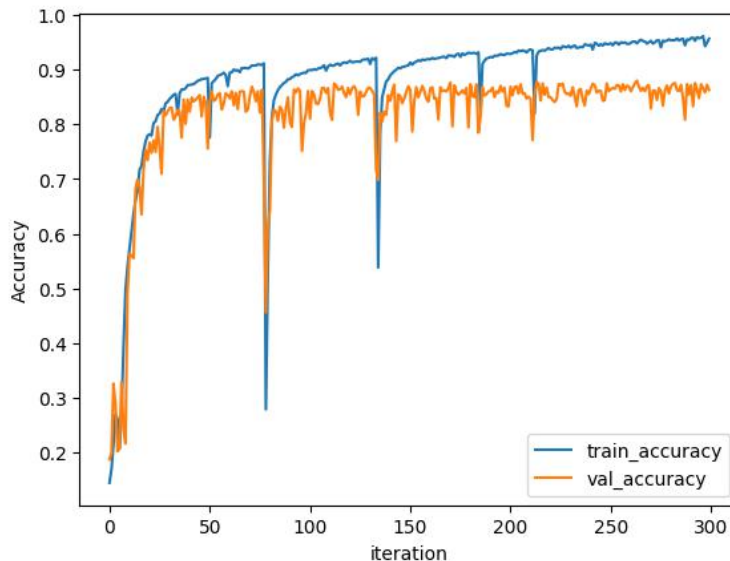


# Fashion MNIST Vanishing Problem

- **Better Activation**

- Model:

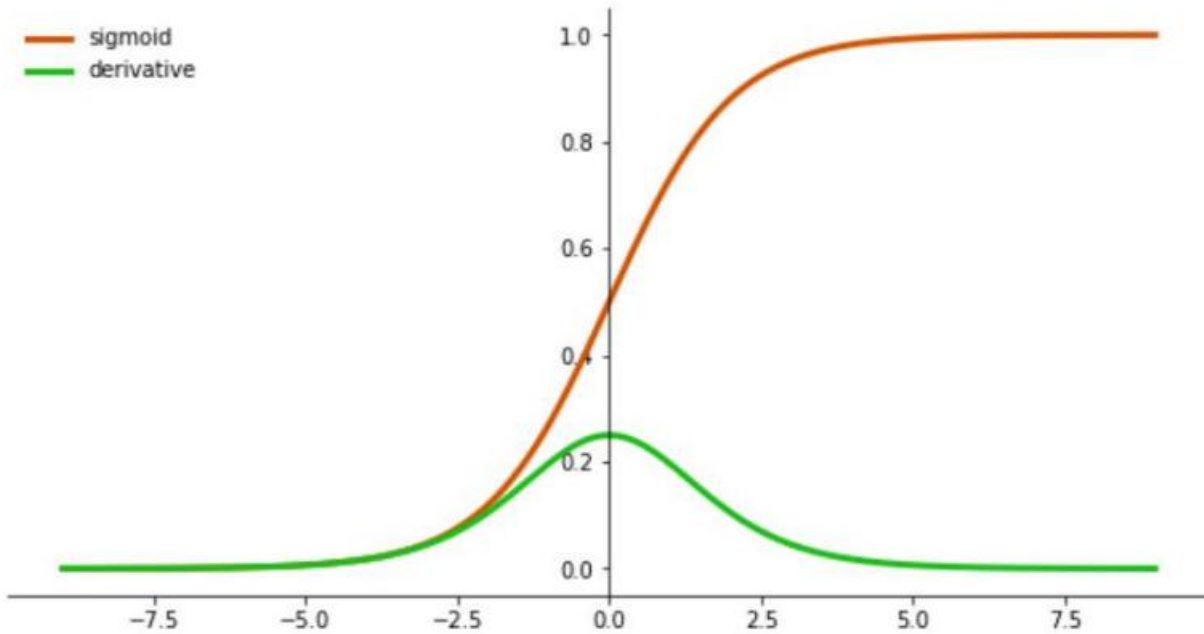
- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** 7 layers
    - **Activation:** **relu**
    - **Nodes:** 128
    - **Loss:** CE
    - **Optimizer:** sgd, **lr=0.05**



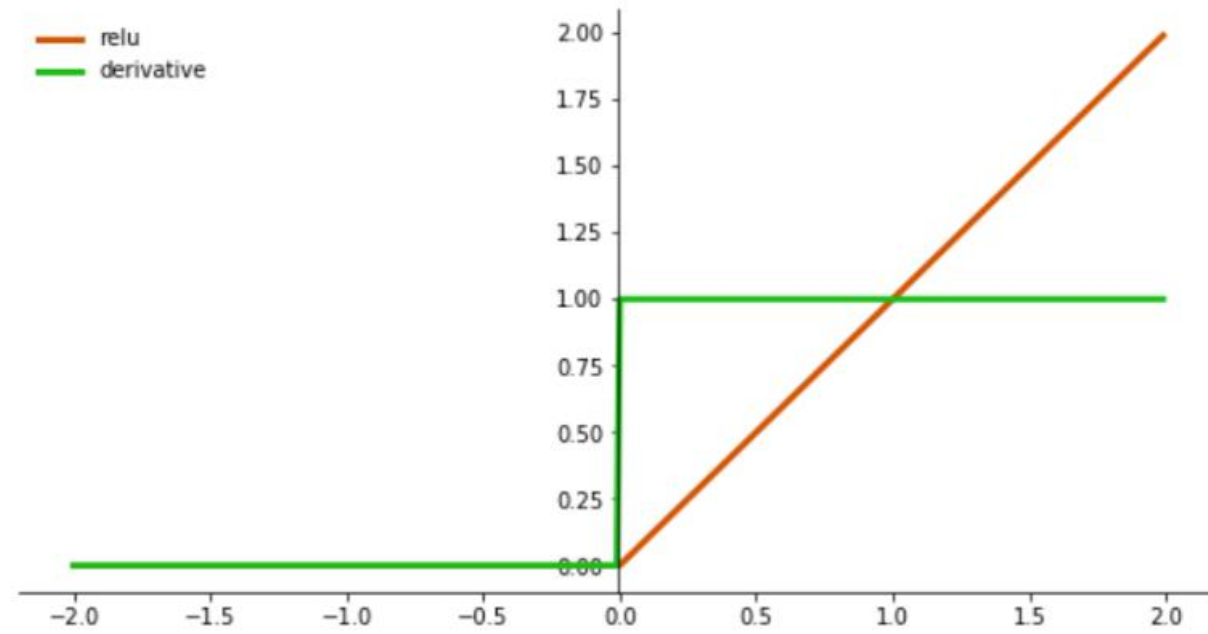
# Fashion MNIST Vanishing Problem

- Better Activation**

Sigmoid



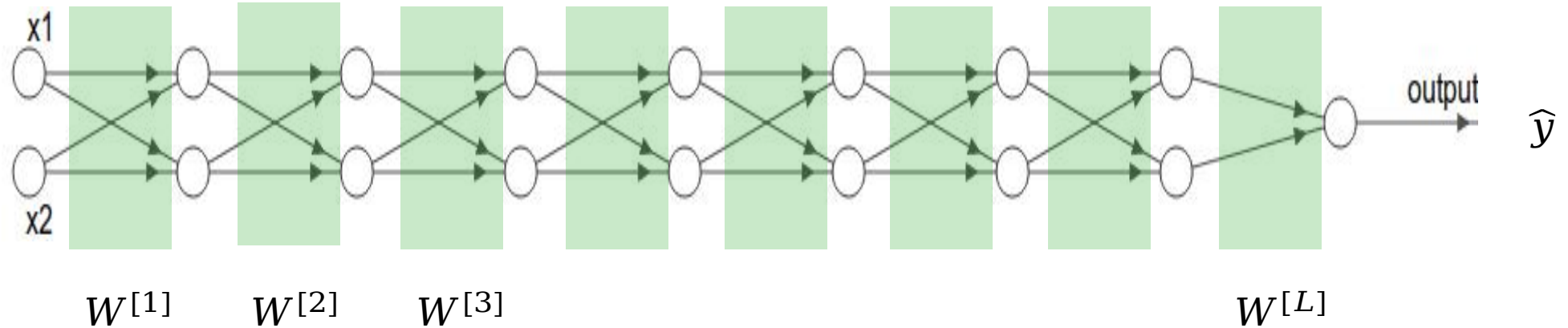
Relu



# Giới thiệu Vanishing và Exploding Problem

## • Better Activation

- Các nguyên nhân có thể gây ra vanishing problem



$$\bullet \frac{\partial L}{\partial w^{[L]}} = \frac{\partial L}{\partial a^{[L]}} * \frac{\partial a^{[L]}}{\partial z^{[L]}} * \frac{\partial z^{[L]}}{\partial w^{[L]}}$$

$$\bullet \text{Loss} = L(\hat{y}, y), \quad \hat{y} = a^{[L]}$$

$$\bullet a^{[l]} = g(z^{[l]})$$

if  $g(\cdot)$  là ReLu function  $\sigma(x)$

$$\bullet \frac{\partial L}{\partial w^{[1]}} = \frac{\partial L}{\partial a^{[L]}} * \underbrace{\frac{\partial a^{[L]}}{\partial z^{[L]}}}_{0 \text{ or } 1} * \frac{\partial z^{[L]}}{\partial a^{[L-1]}} \dots * \underbrace{\frac{\partial a^{[2]}}{\partial z^{[2]}}}_{0 \text{ or } 1} * \frac{\partial z^{[2]}}{\partial a^{[1]}} * \underbrace{\frac{\partial a^{[1]}}{\partial z^{[1]}}}_{0 \text{ or } 1} * \frac{\partial z^{[1]}}{\partial w^{[1]}}$$

$$w^{[l]} = w^{[l]} - \eta \frac{\partial L}{\partial w^{[l]}}$$

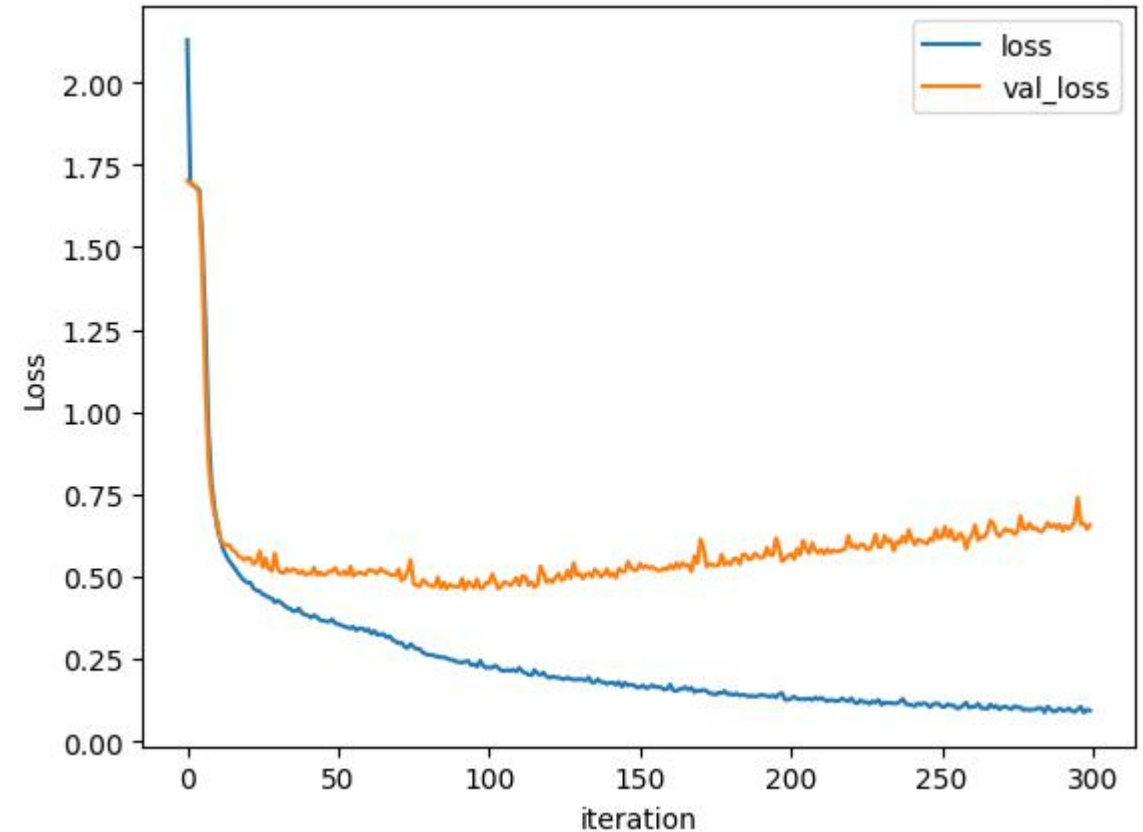
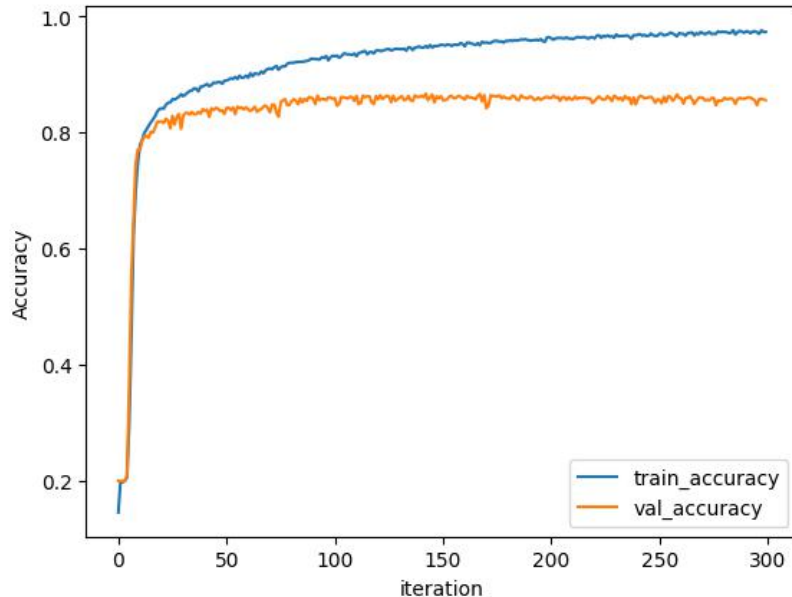


# Fashion MNIST Vanishing Problem

- **Better Optimizer**

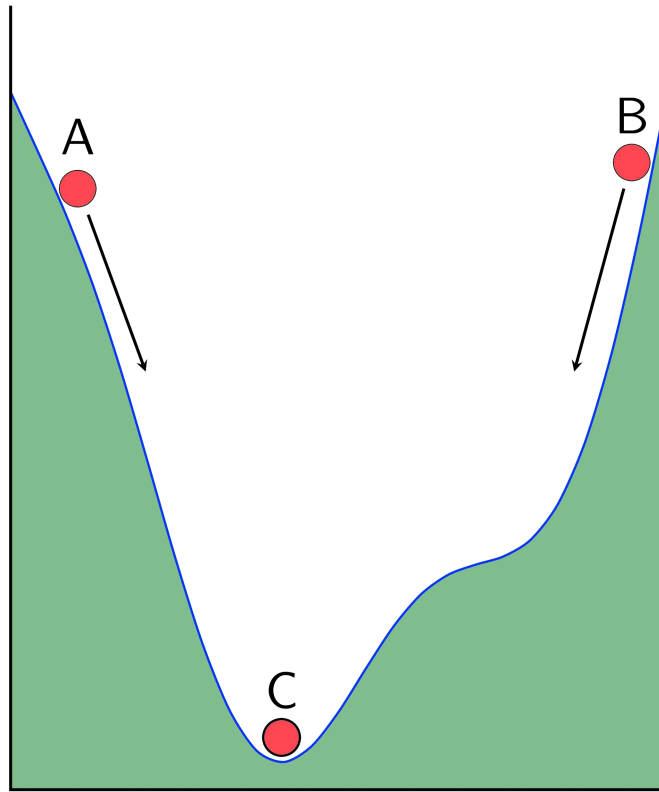
- Model:

- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** 7 layers
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** BCE
    - **Optimizer:** Adam

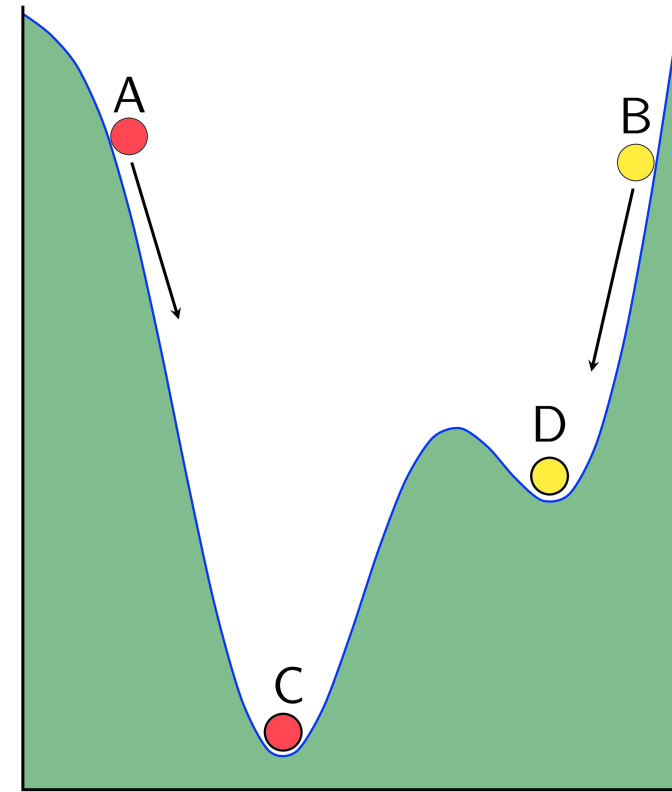


# Fashion MNIST Vanishing Problem

- **Better Optimizer**
  - SGD với momentum



a) GD

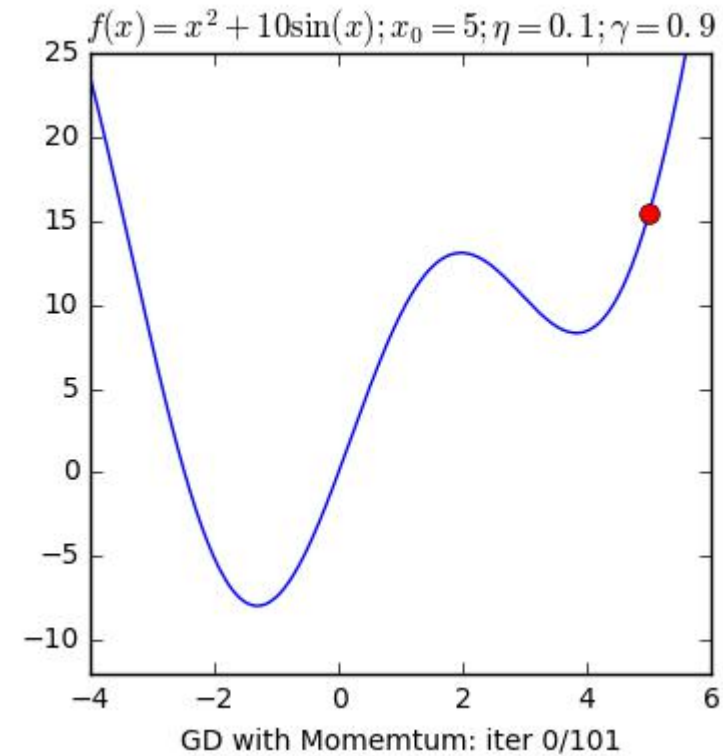
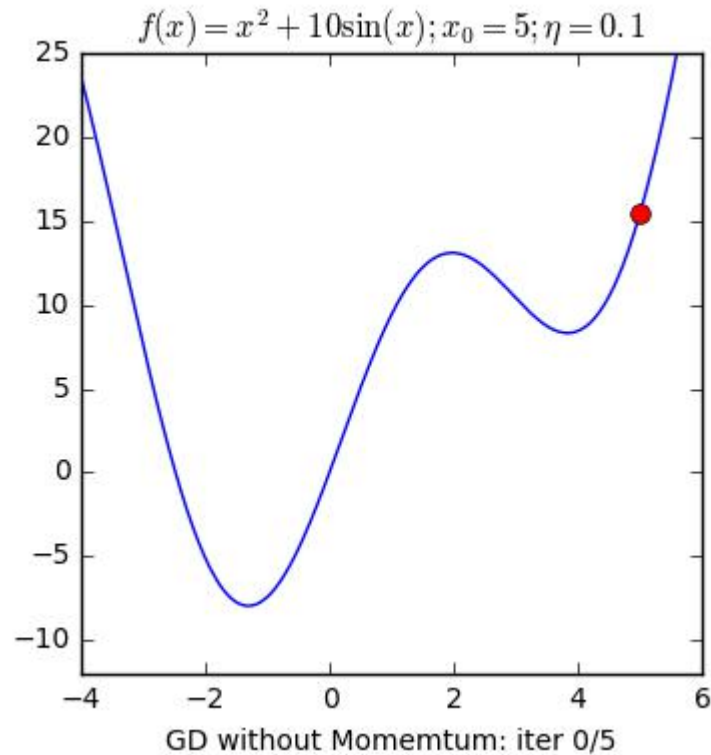


b) GD



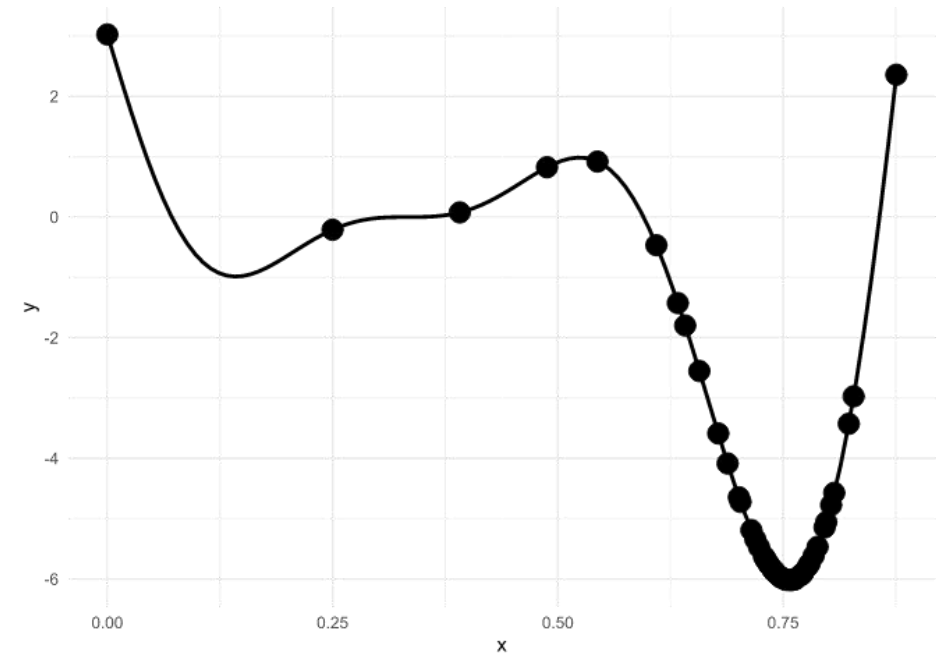
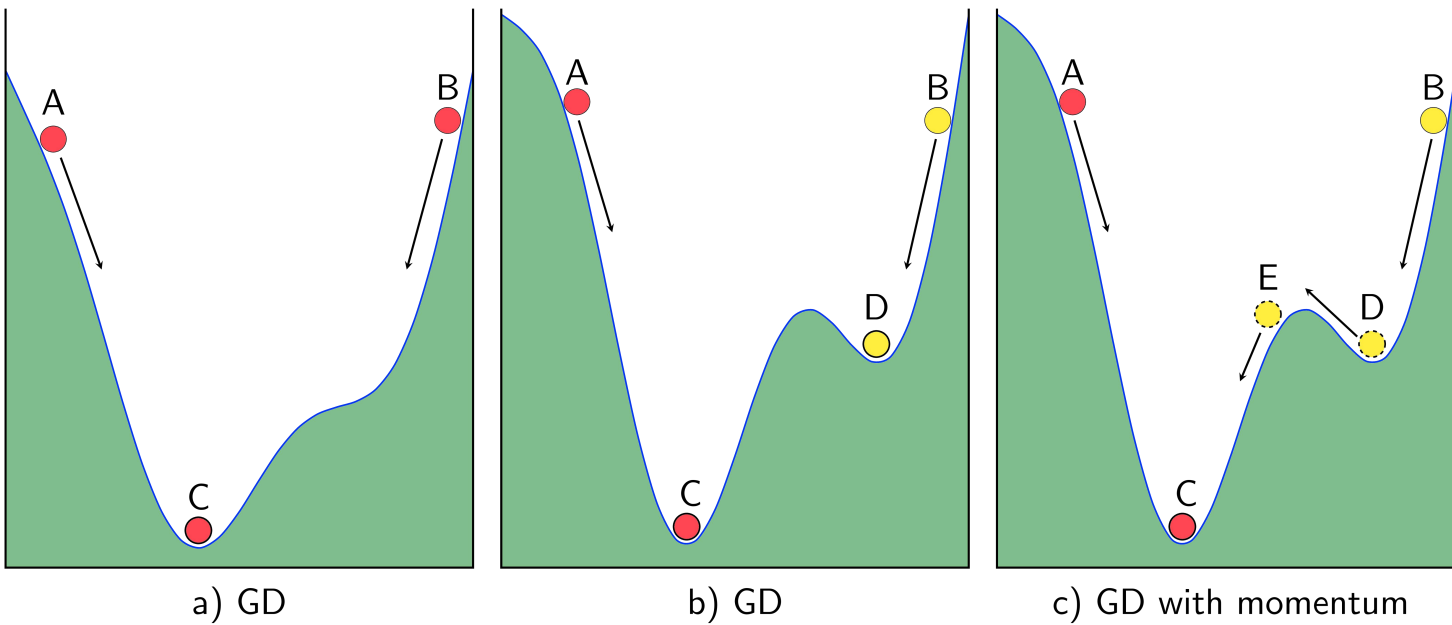
# Fashion MNIST Vanishing Problem

- **Better Optimizer**
  - SGD với momentum

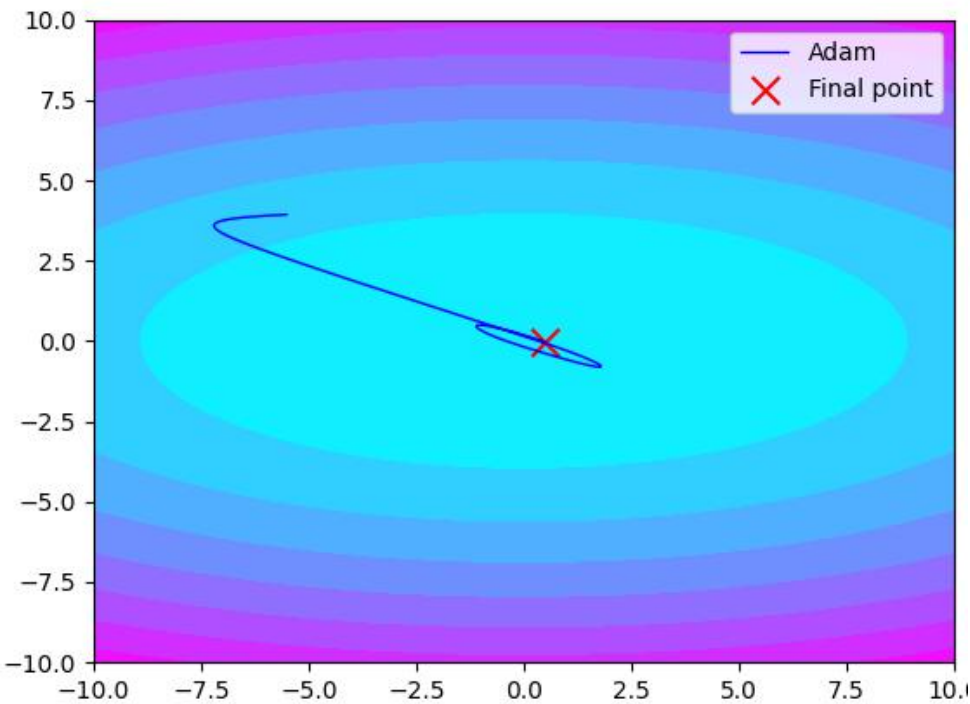


# Fashion MNIST Vanishing Problem

- **Better Optimizer**
  - Adam: momentum + ma sát



- **Better Optimizer**
  - Adam: momentum + ma sát



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**Algorithm 1:** *Adam*, our proposed algorithm for stochastic optimization. See section 2 for details, and for a slightly more efficient (but less clear) order of computation.  $g_t^2$  indicates the elementwise square  $g_t \odot g_t$ . Good default settings for the tested machine learning problems are  $\alpha = 0.001$ ,  $\beta_1 = 0.9$ ,  $\beta_2 = 0.999$  and  $\epsilon = 10^{-8}$ . All operations on vectors are element-wise. With  $\beta_1^t$  and  $\beta_2^t$  we denote  $\beta_1$  and  $\beta_2$  to the power  $t$ .

---

**Require:**  $\alpha$ : Stepsize

**Require:**  $\beta_1, \beta_2 \in [0, 1)$ : Exponential decay rates for the moment estimates

**Require:**  $f(\theta)$ : Stochastic objective function with parameters  $\theta$

**Require:**  $\theta_0$ : Initial parameter vector

$m_0 \leftarrow 0$  (Initialize 1<sup>st</sup> moment vector)

$v_0 \leftarrow 0$  (Initialize 2<sup>nd</sup> moment vector)

$t \leftarrow 0$  (Initialize timestep)

**while**  $\theta_t$  not converged **do**

$t \leftarrow t + 1$

$g_t \leftarrow \nabla_{\theta} f_t(\theta_{t-1})$  (Get gradients w.r.t. stochastic objective at timestep  $t$ )

$m_t \leftarrow \beta_1 \cdot m_{t-1} + (1 - \beta_1) \cdot g_t$  (Update biased first moment estimate)

$v_t \leftarrow \beta_2 \cdot v_{t-1} + (1 - \beta_2) \cdot g_t^2$  (Update biased second raw moment estimate)

$\hat{m}_t \leftarrow m_t / (1 - \beta_1^t)$  (Compute bias-corrected first moment estimate)

$\hat{v}_t \leftarrow v_t / (1 - \beta_2^t)$  (Compute bias-corrected second raw moment estimate)

$\theta_t \leftarrow \theta_{t-1} - \alpha \cdot \hat{m}_t / (\sqrt{\hat{v}_t} + \epsilon)$  (Update parameters)

**end while**

**return**  $\theta_t$  (Resulting parameters)

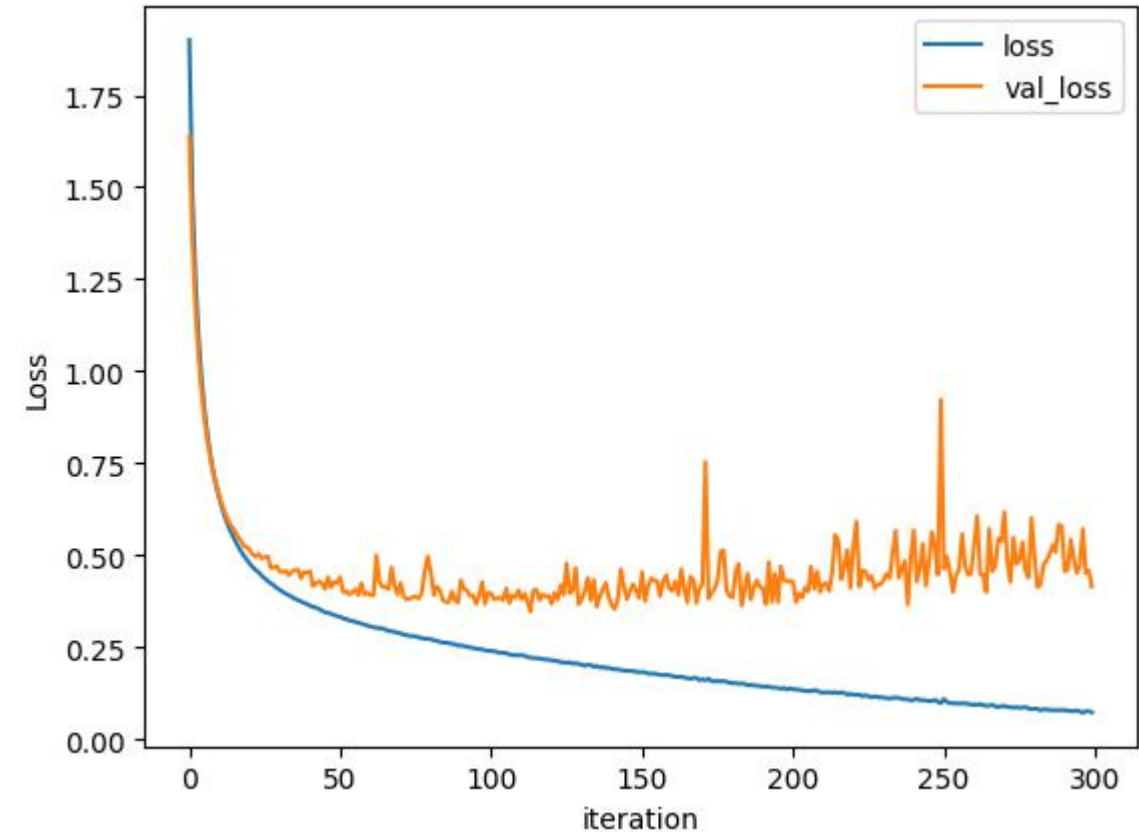
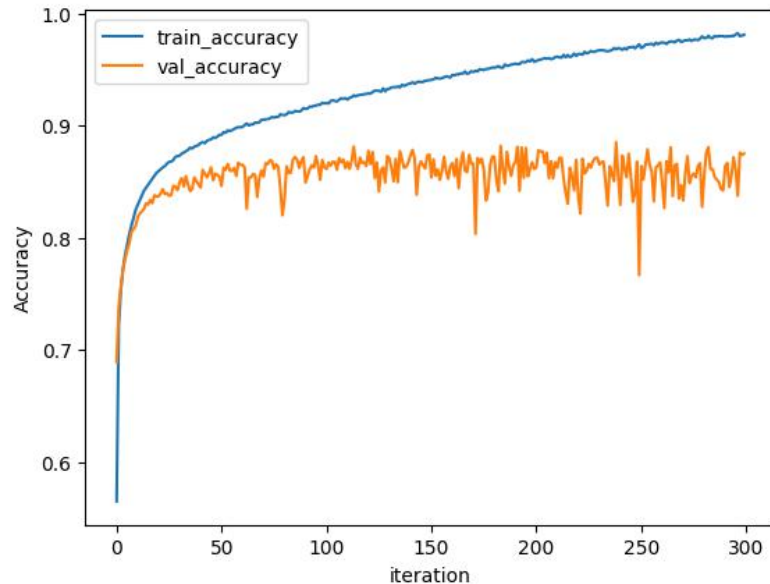
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# Fashion MNIST Vanishing Problem

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# Fashion MNIST Vanishing Problem

- **Normalize Inside Network**
  - Model:
    - **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** 7 layers + **BatchNorm**
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** BCE
    - **Optimizer:** sgd



# Fashion MNIST Vanishing Problem

- **Normalize Inside Network**

- BatchNormalization:

- Giúp việc **học nhanh** hơn và **ổn định** hơn
    - Train và Test phase hoạt động khác nhau

**Input:** Values of  $x$  over a mini-batch:  $\mathcal{B} = \{x_1 \dots x_m\}$ ;  
Parameters to be learned:  $\gamma, \beta$

**Output:**  $\{y_i = \text{BN}_{\gamma, \beta}(x_i)\}$

$$\mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^m x_i$$

// mini-batch mean

$$\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2$$

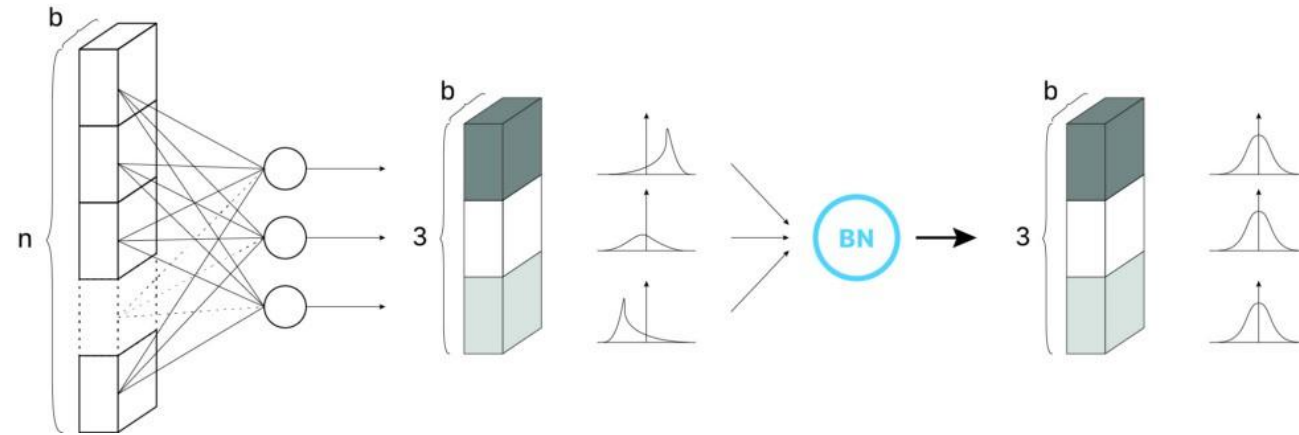
// mini-batch variance

$$\hat{x}_i \leftarrow \frac{x_i - \mu_{\mathcal{B}}}{\sqrt{\sigma_{\mathcal{B}}^2 + \epsilon}}$$

// normalize

$$y_i \leftarrow \gamma \hat{x}_i + \beta \equiv \text{BN}_{\gamma, \beta}(x_i)$$

// scale and shift



(1)(2) Tính mean và variance của 1 batch

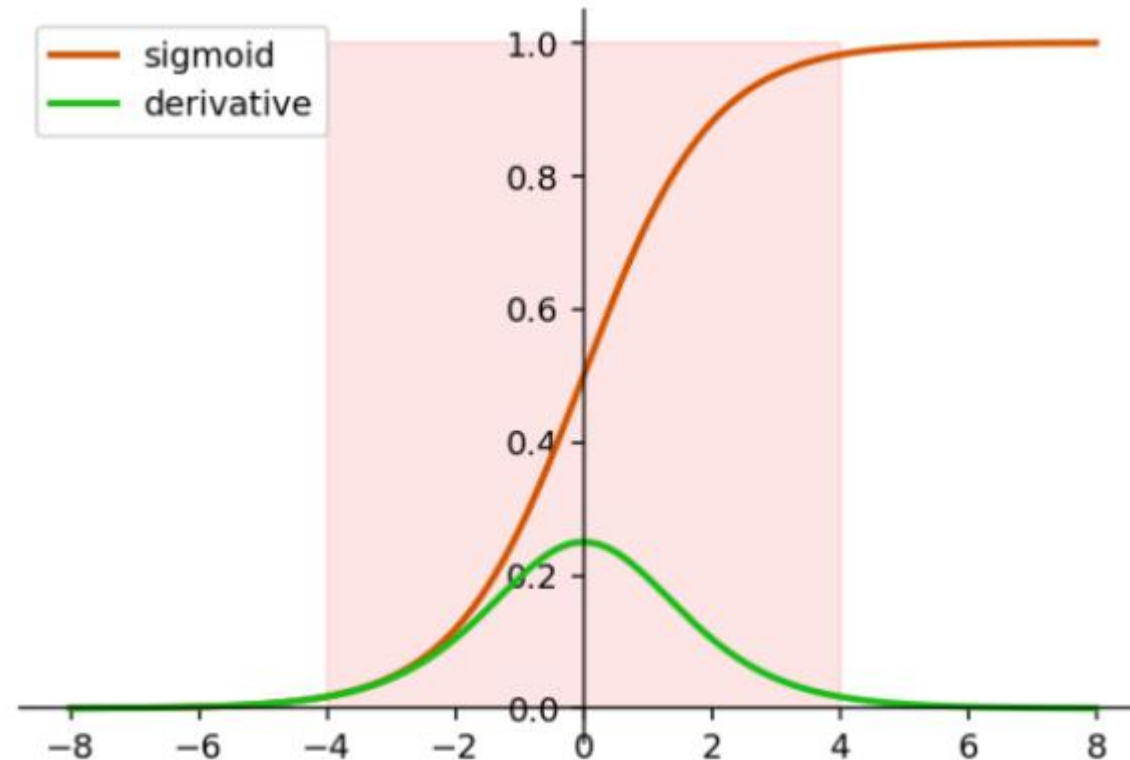
(3) normalize để mỗi node output theo 1 normal distribtuion

(4)  $\gamma$  và  $\beta$  là 2 tham số học trong train phase để scale và ship distribtuion

# Fashion MNIST Vanishing Problem

- **Normalize Inside Network**

- Problem: input có giá trị càng lớn sẽ càng bị giới hạn và tại vị trí đó dường như không có đạo hàm
- Sử dụng BatchNormalization giữ hoạt động trong range màu xanh  $[-4,4]$  nơi có đạo hàm mạnh



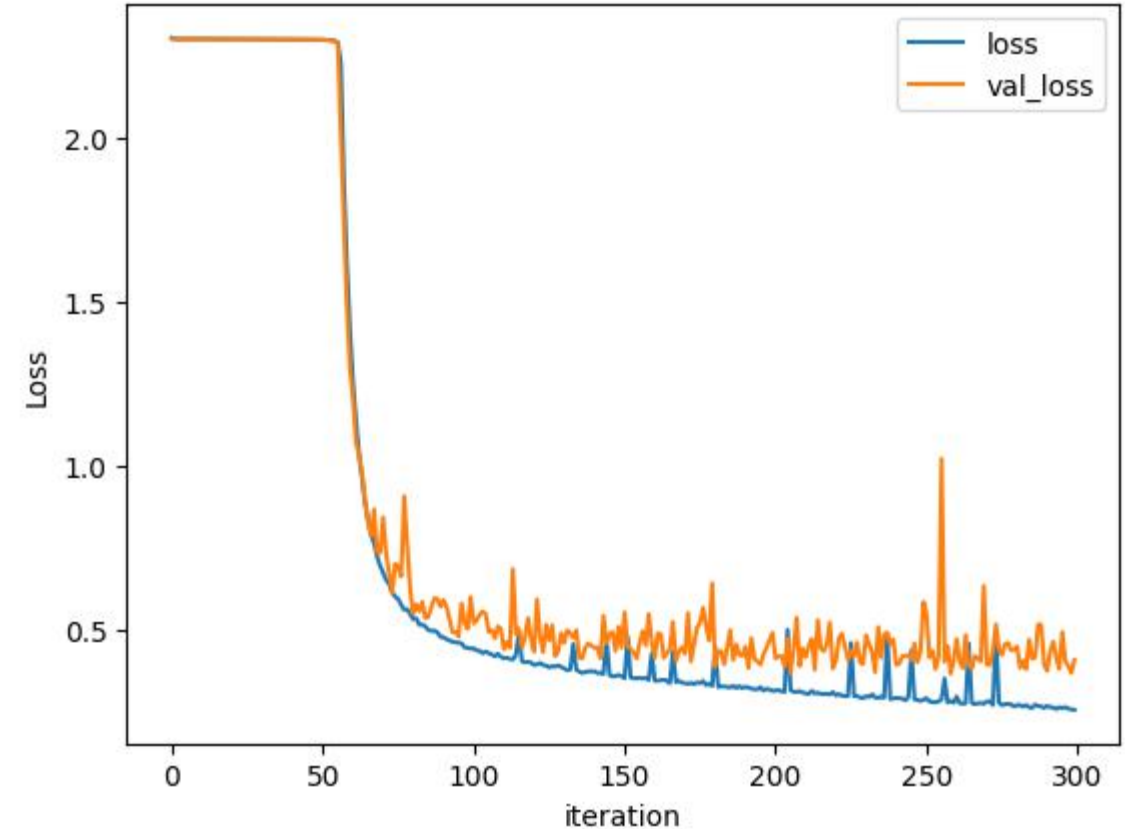
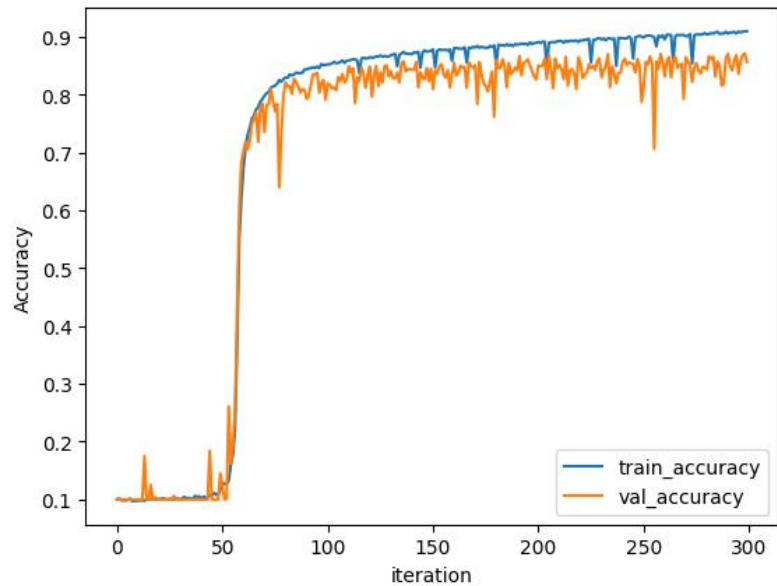


# Fashion MNIST Vanishing Problem

- **Normalize Inside Network**

- **Model:**

- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** 7 layers + CustomNorm
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** BCE
    - **Optimizer:** sgd

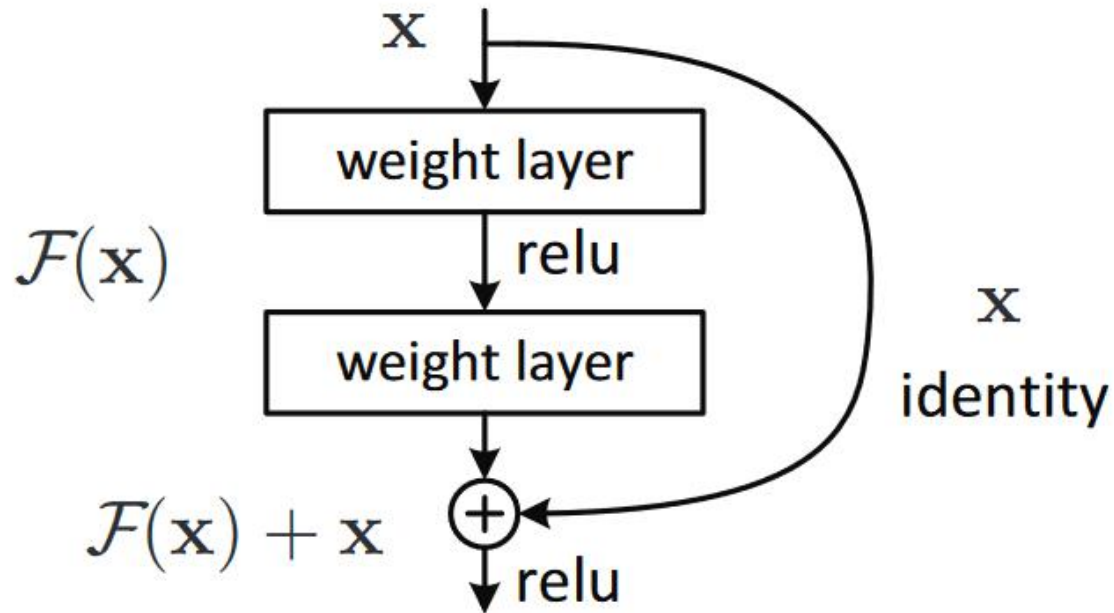






# Fashion MNIST Vanishing Problem

- Skip Connection



$$H(x) = F(x) + x$$

$$\frac{\partial L}{\partial x} = \frac{\partial L}{\partial H} \frac{\partial H}{\partial x} = \frac{\partial L}{\partial H} \left( \frac{\partial F}{\partial x} + 1 \right) = \frac{\partial L}{\partial H} \frac{\partial F}{\partial x} + \frac{\partial L}{\partial H}$$

- Khi không cần học ở nhóm layer này thì nó sẽ được điều hướng và học như identity function

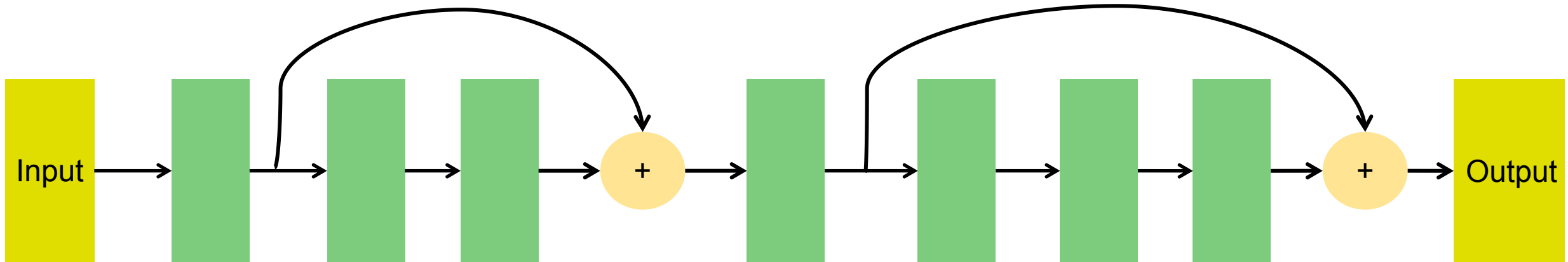
- Gradient qua các layer có thể sẽ nhỏ dần và bằng 0, do đó skip connection giúp thông tin truyền ngược lại dễ hơn

# Fashion MNIST Vanishing Problem

- **Skip Connection**

- Model1:

- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** 7 layers + **SkipConnection**
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** BCE
    - **Optimizer:** sgd

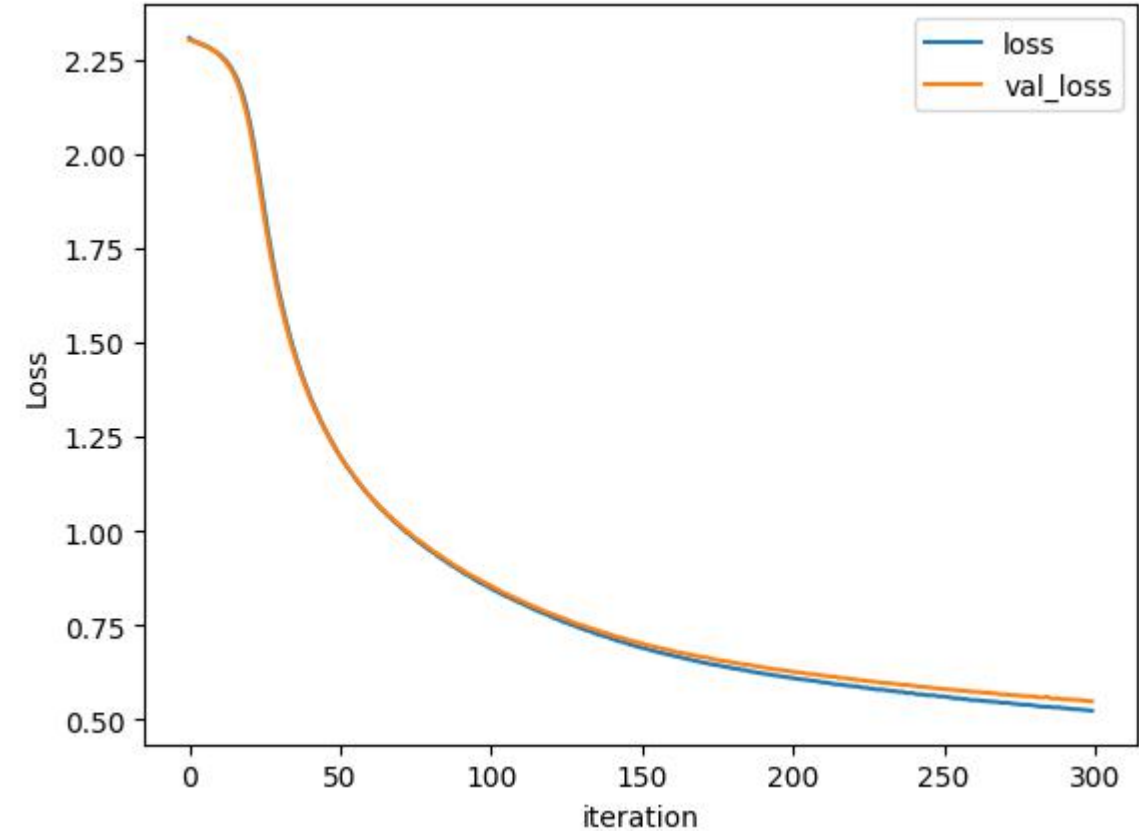
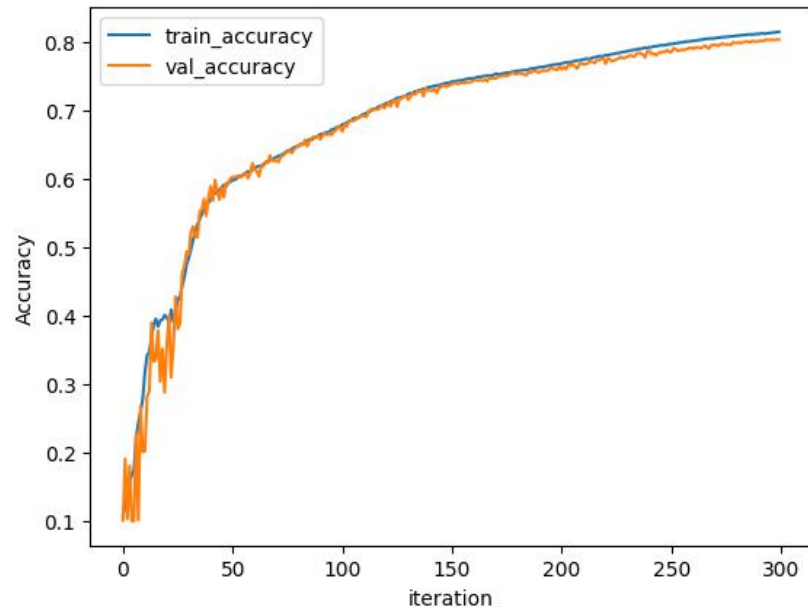


# Fashion MNIST Vanishing Problem

- **Skip Connection**

- Model:

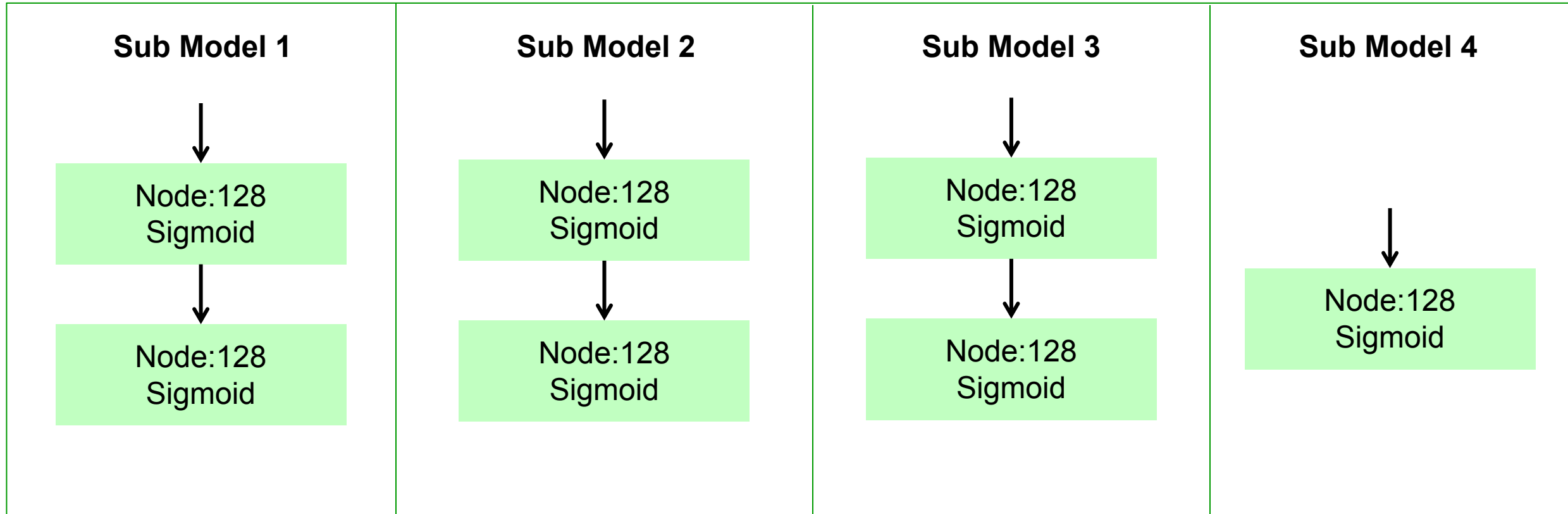
- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** 7 layers + **SkipConnection**
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** BCE
    - **Optimizer:** sqd





# Fashion MNIST Vanishing Problem

- **Train Some Layer**

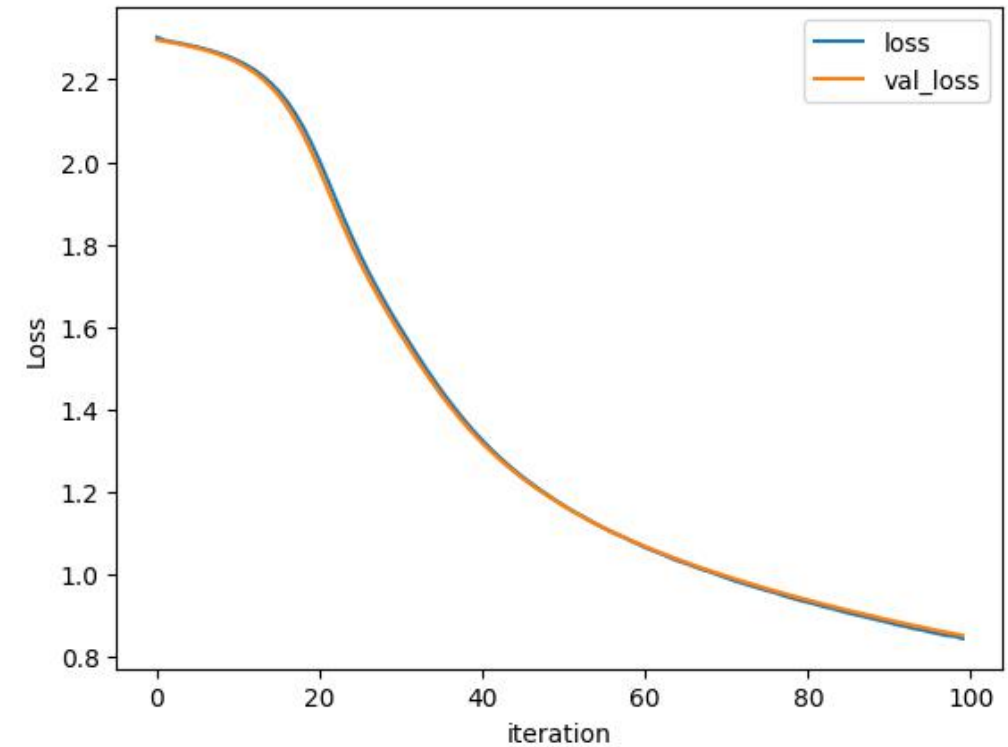
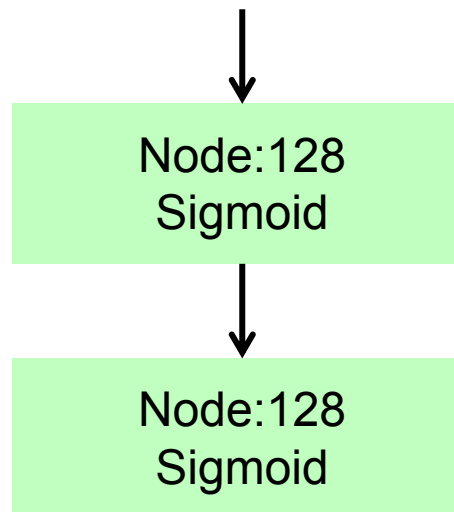
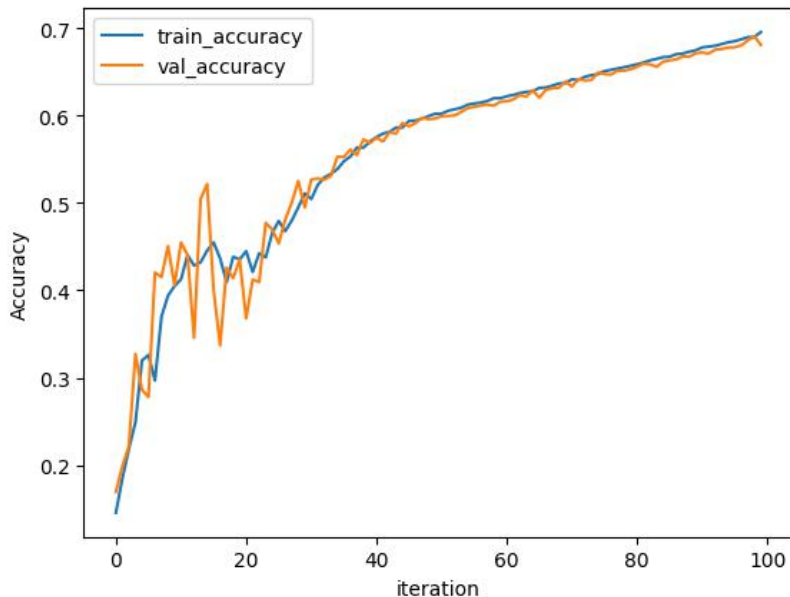


# Fashion MNIST Vanishing Problem

- **Train Some Layer**

- Train lần 1:

- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** sub model1 (2 layers)
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** BCE
    - **Optimizer:** sgd

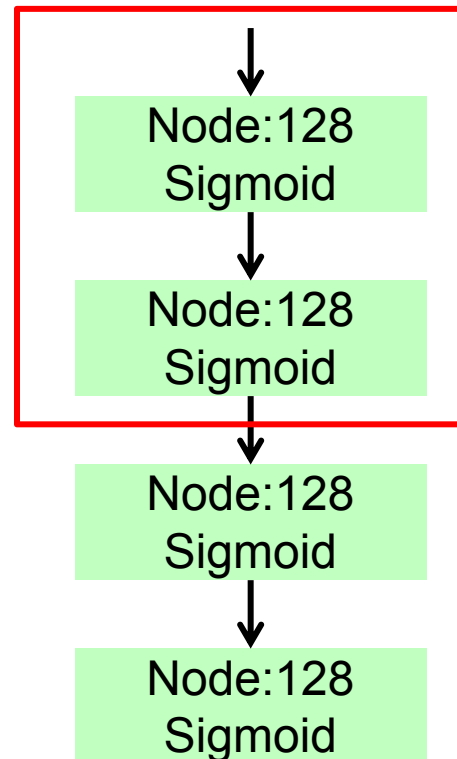
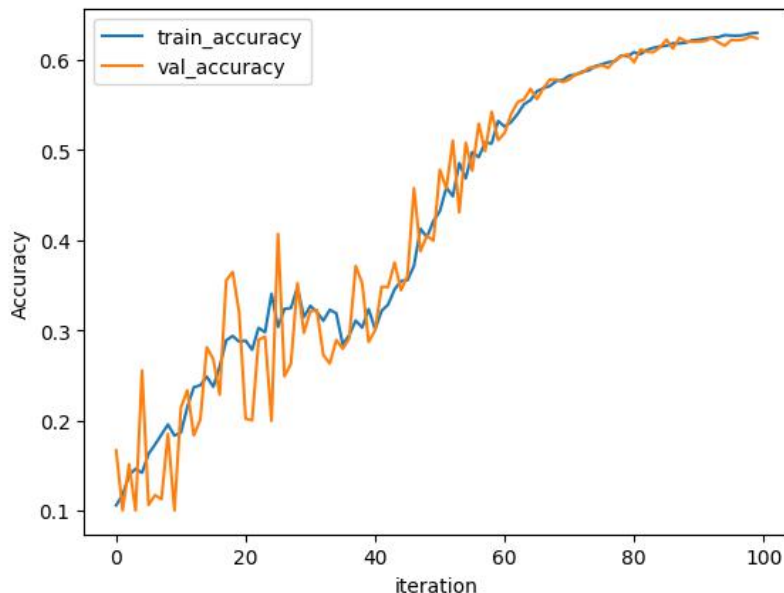


# Fashion MNIST Vanishing Problem

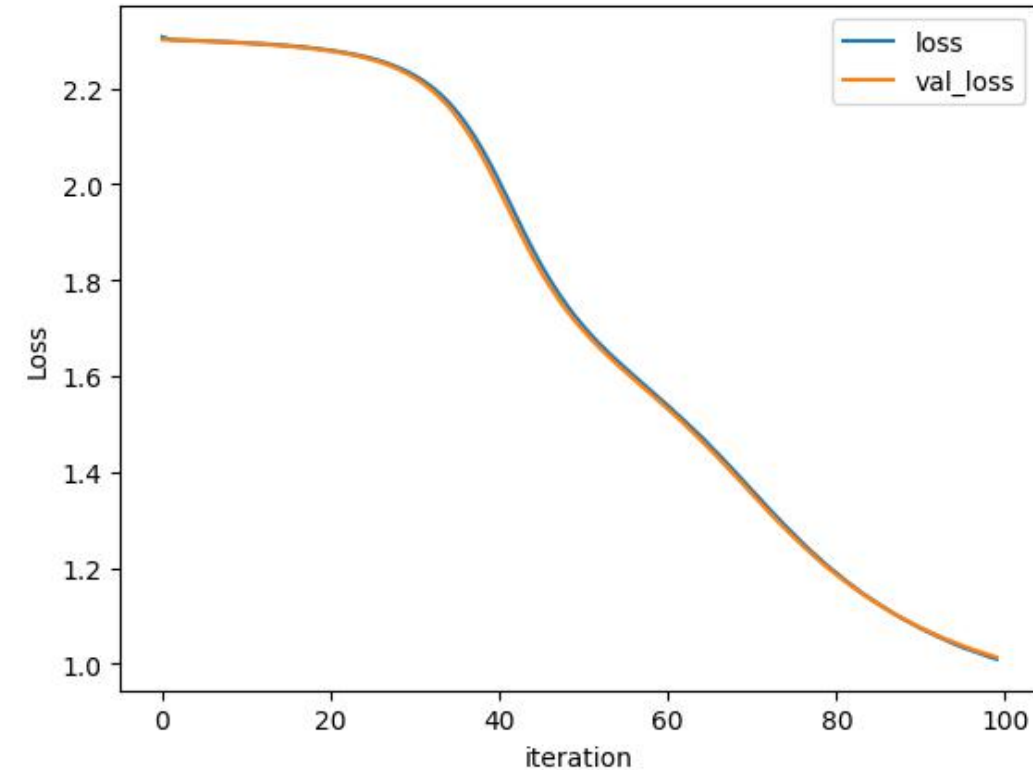
- **Train Some Layer**

- Train lần 2:

- **Weight Initialization:**  $\mu=0, \sigma=0.05$
    - **Hidden Layers:** sub model1(fix) + sub model2(train)
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** BCE
    - **Optimizer:** sgd



fix



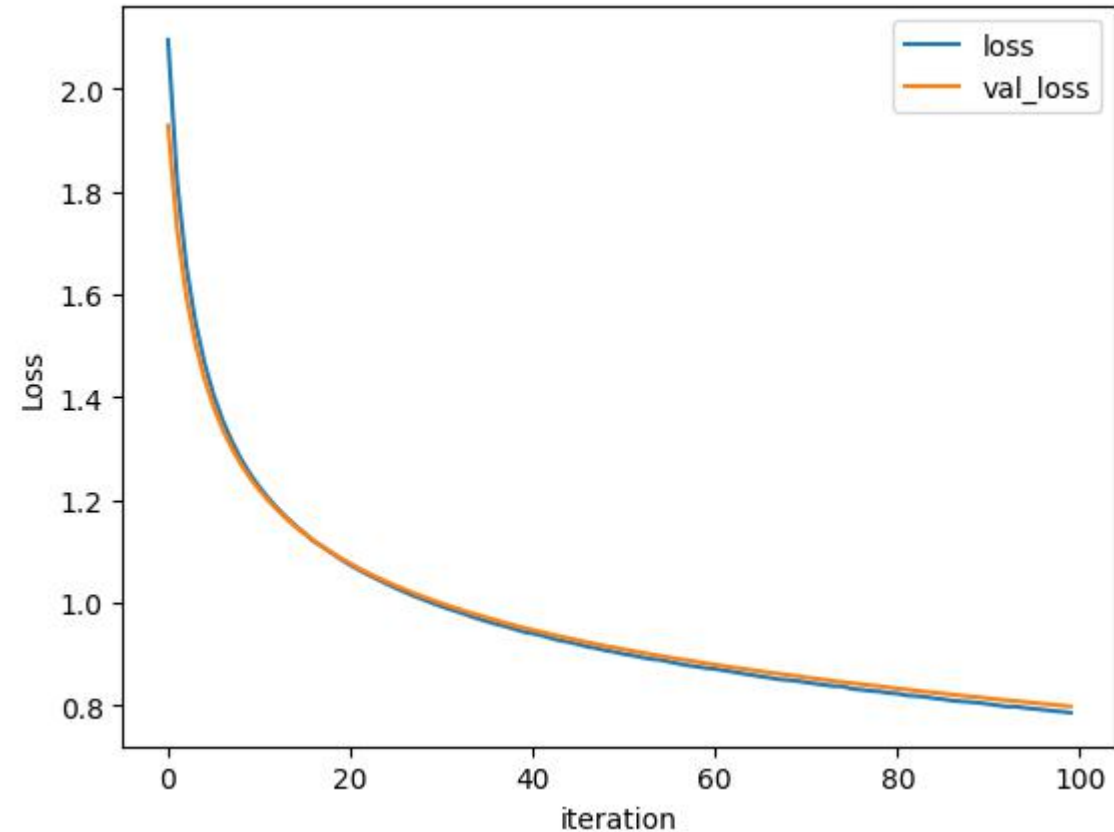
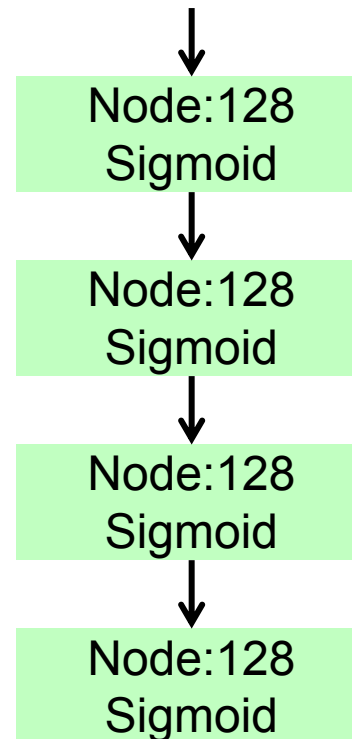
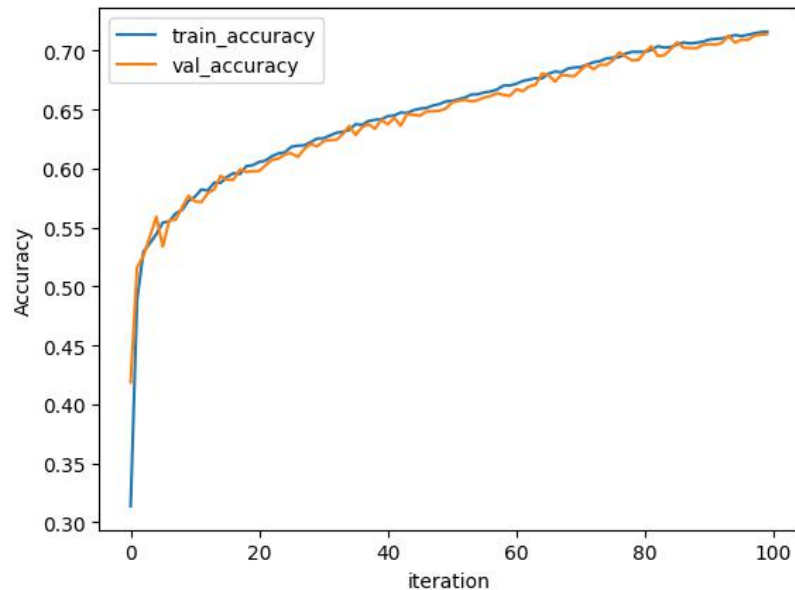


# Fashion MNIST Vanishing Problem

- **Train Some Layer**

- Train lần 3:

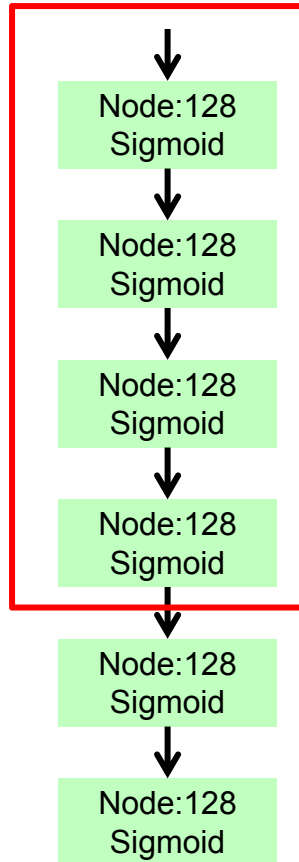
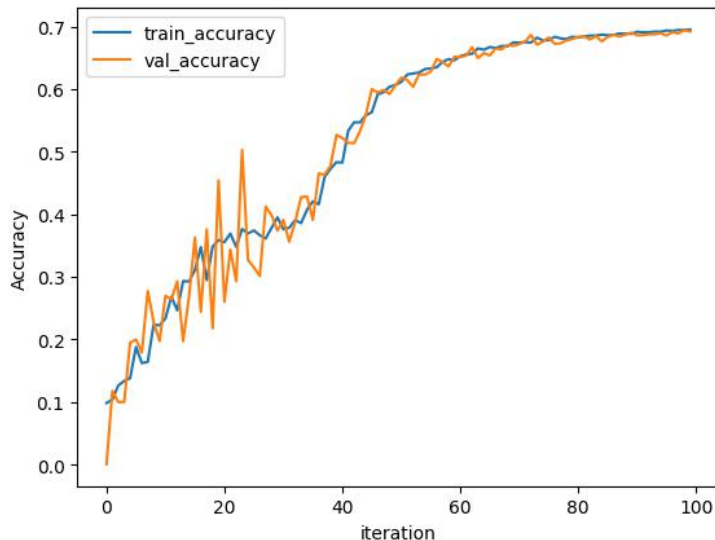
- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** sub model1(train) + sub model2(train)
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** BCE
    - **Optimizer:** sqd



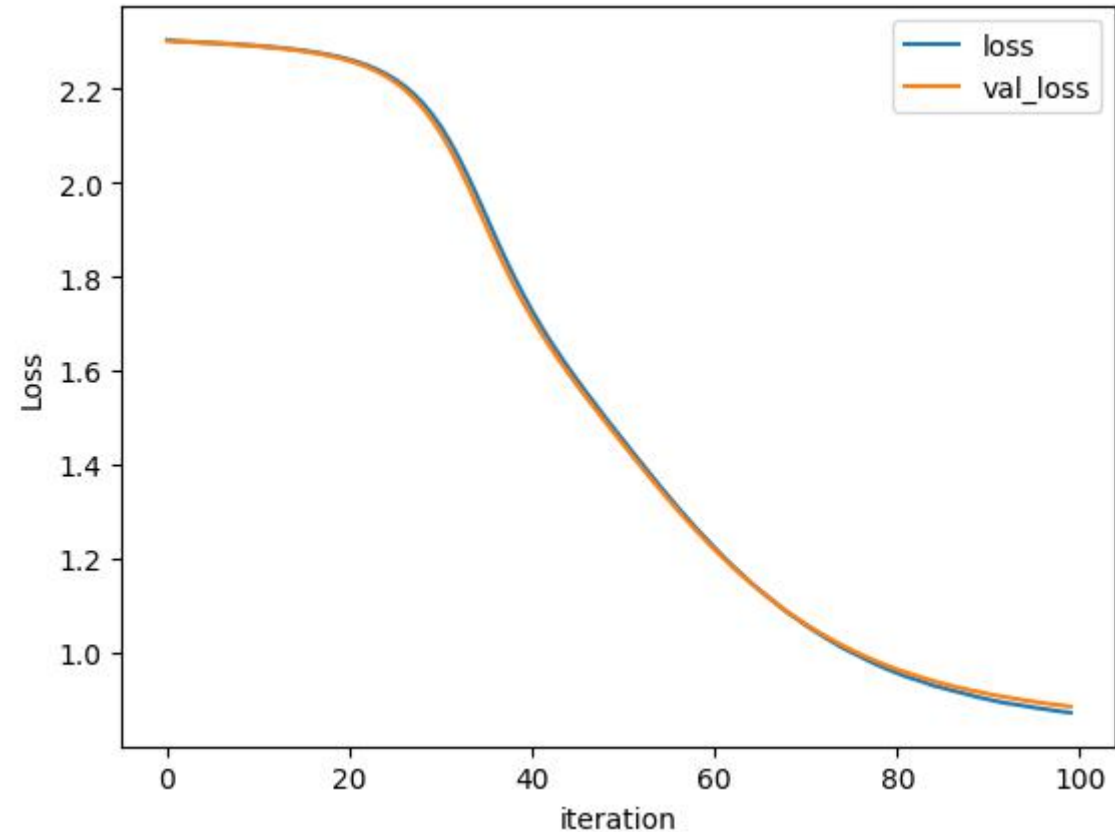
# Fashion MNIST Vanishing Problem

- **Train Some Layer**

- Train lần 4:
  - **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
  - **Hidden Layers:** sub model1(fix) + sub model2(fix) + sub model3(train)
  - **Activation:** sigmoid
  - **Nodes:** 128
  - **Loss:** BCE
  - **Optimizer:** sqd



fix

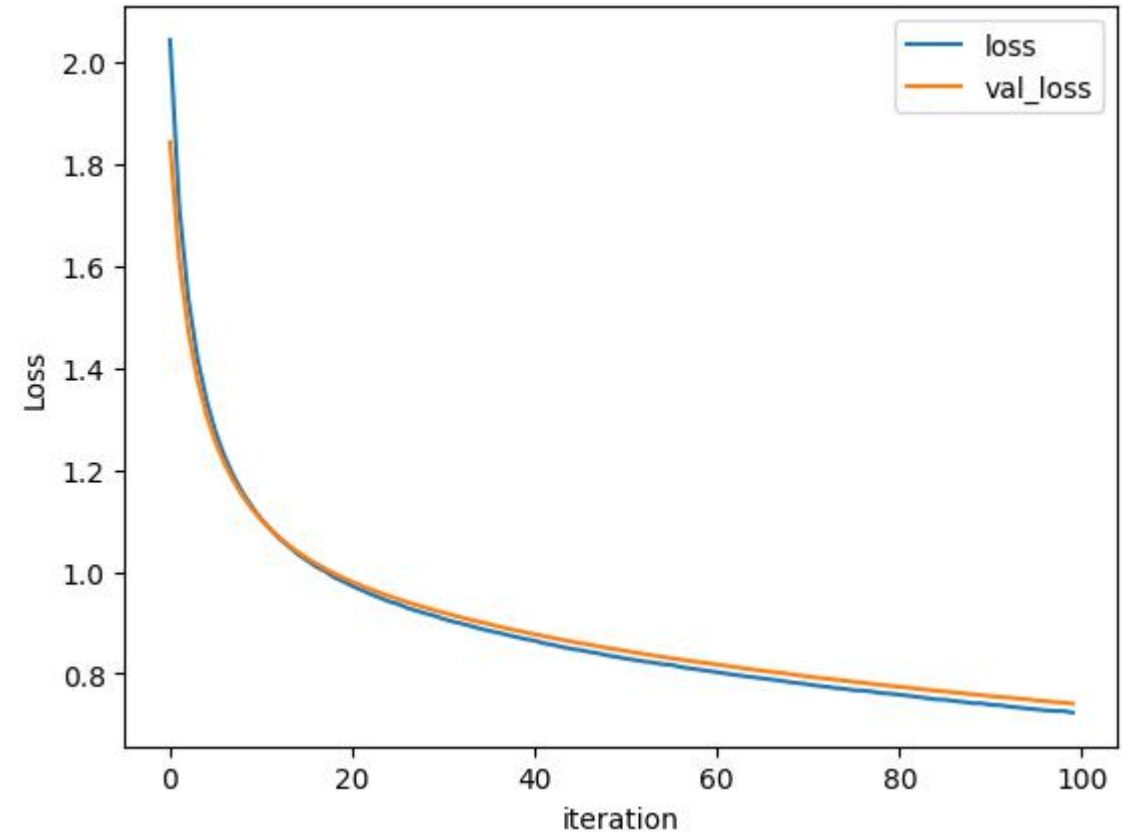
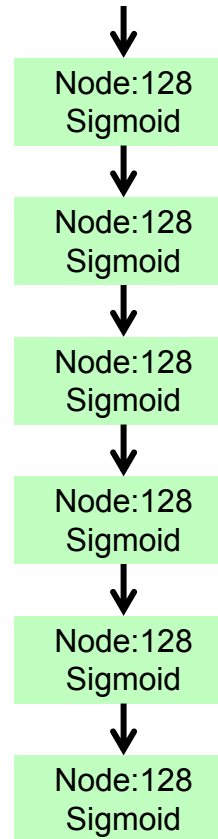
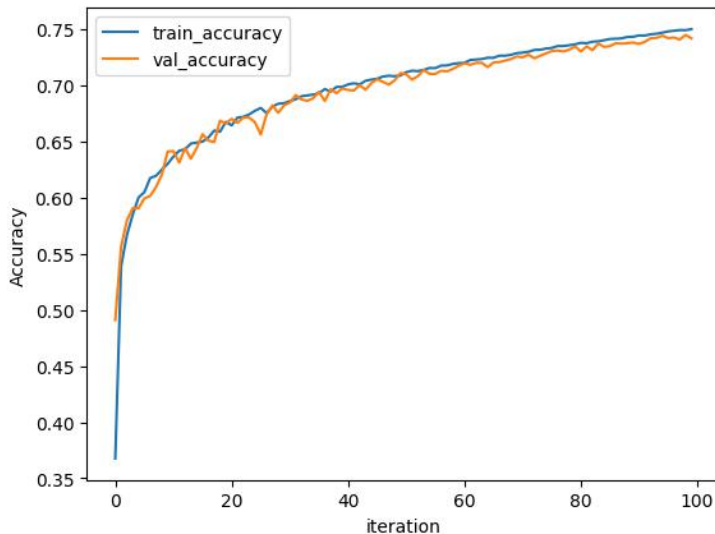


# Fashion MNIST Vanishing Problem

- **Train Some Layer**

- Train lần 5:

- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** sub model1(train) + sub model2(train) + sub model3(train)
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** BCE
    - **Optimizer:** sgd

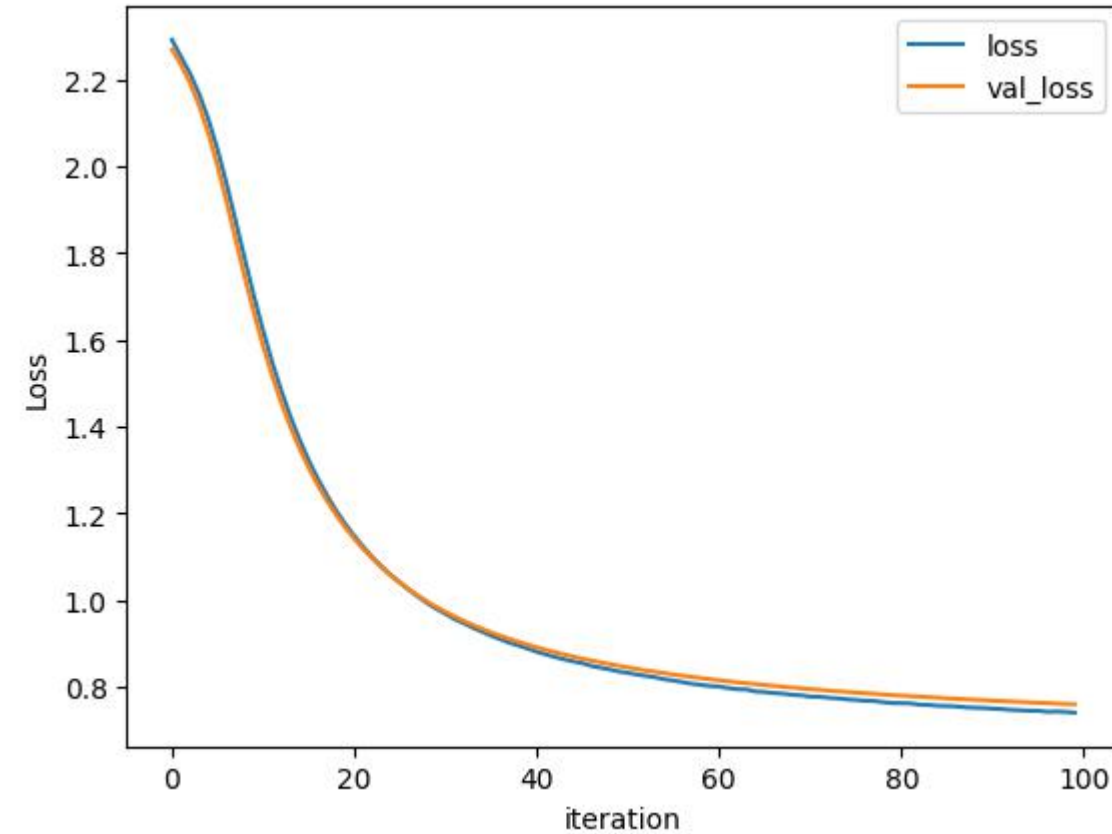
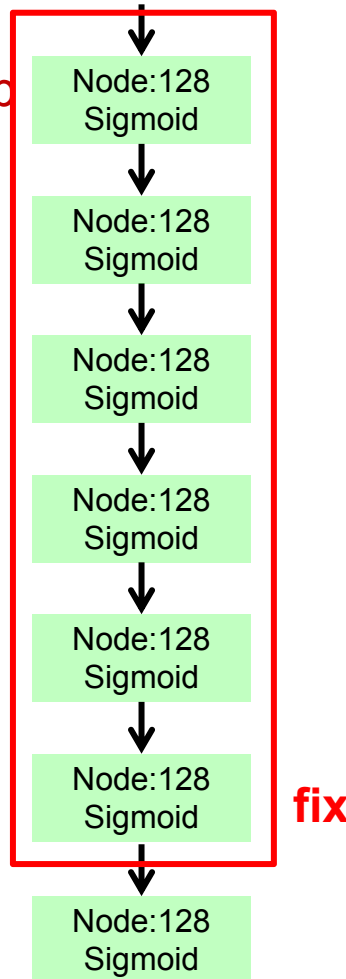
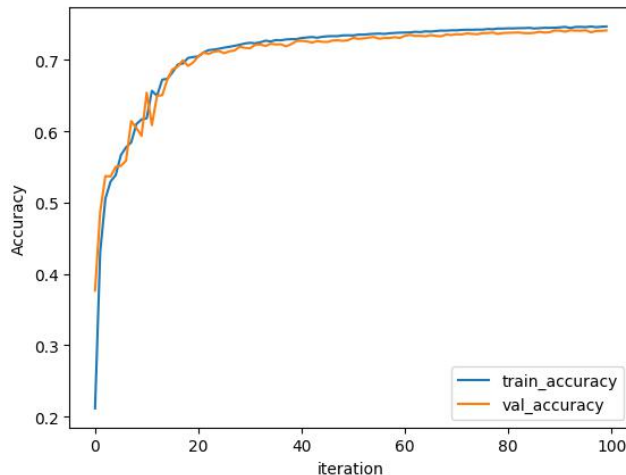


# Fashion MNIST Vanishing Problem

- **Train Some Layer**

- Train lần 6:

- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** sub model1(fix) + sub model2(fix) + sub model3(fix) + sub model4(train)
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** BCE
    - **Optimizer:** sgd

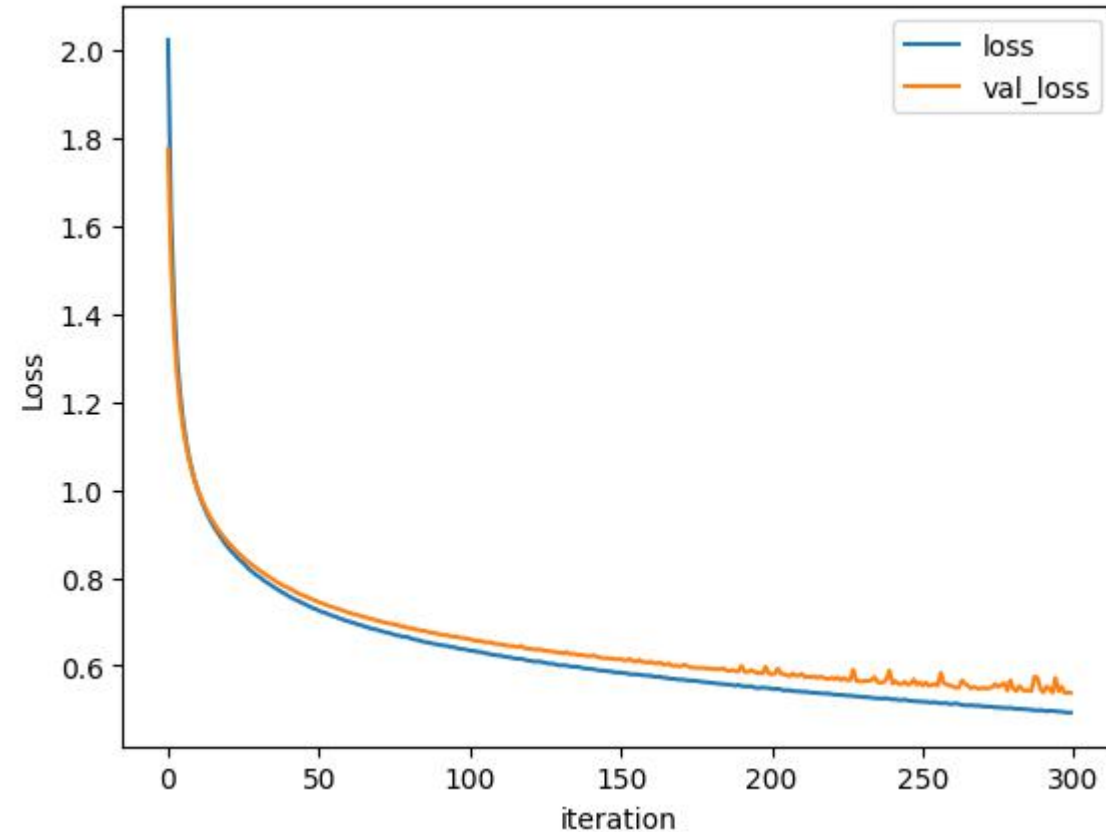
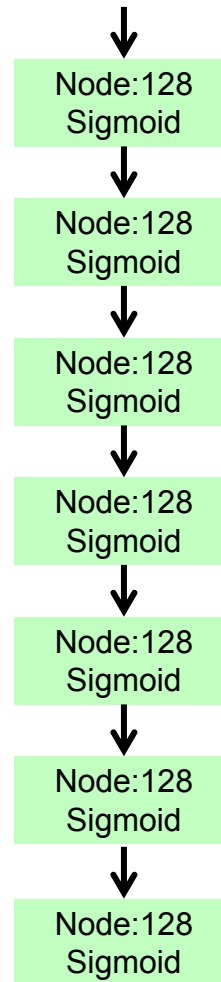
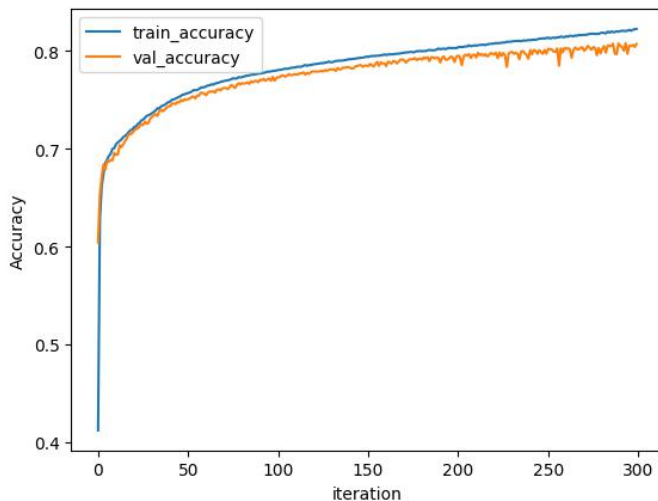


# Fashion MNIST Vanishing Problem

- **Train Some Layer**

- Train lần 7:

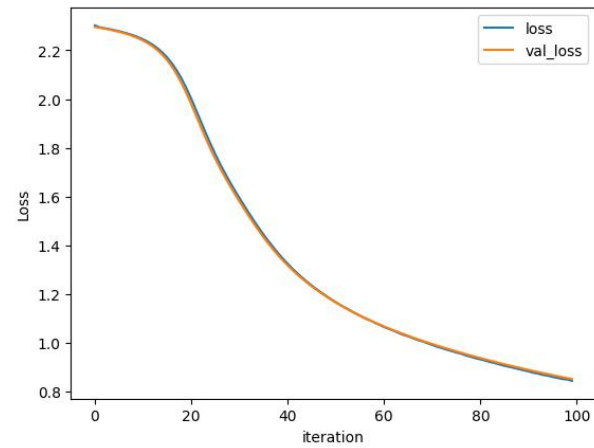
- **Weight Initialization:**  $\mu=0$ ,  $\sigma=0.05$
    - **Hidden Layers:** sub model1(train) + sub model2(train) + sub model3(train) + sub model4(train)
    - **Activation:** sigmoid
    - **Nodes:** 128
    - **Loss:** BCE
    - **Optimizer:** sqd



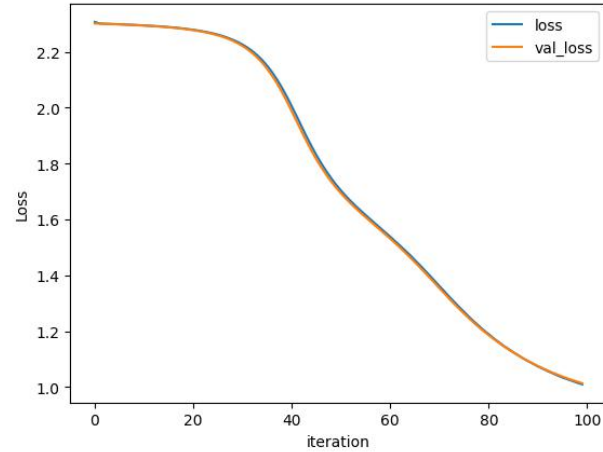
# Fashion MNIST Vanishing Problem

- Train Some Layer

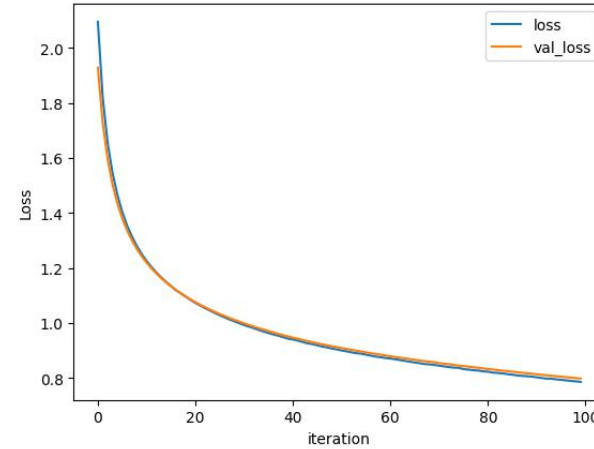
Train lần 1



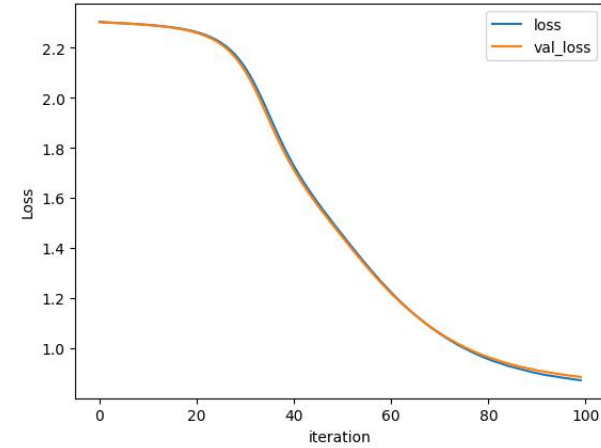
Train lần 2



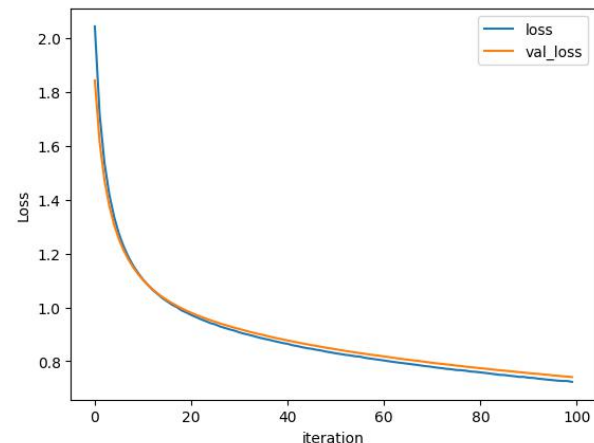
Train lần 3



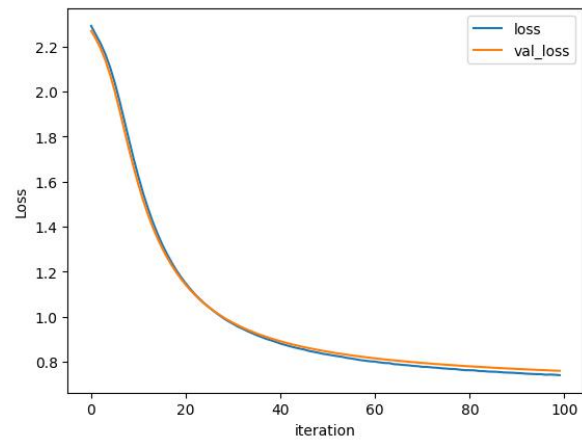
Train lần 4



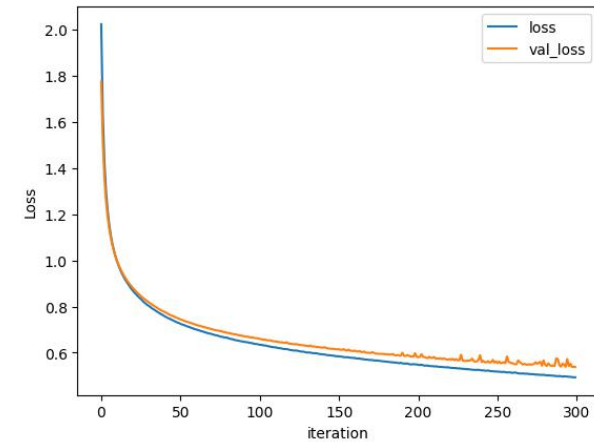
Train lần 5



Train lần 6



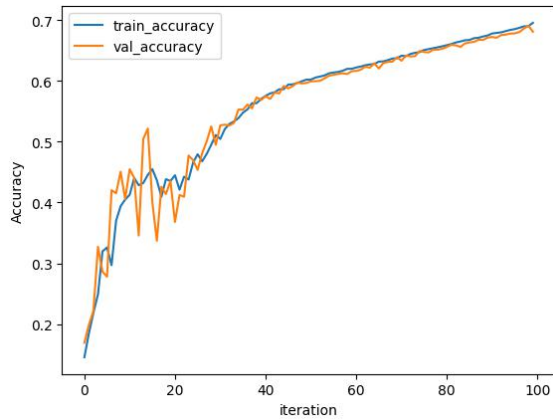
Train lần 7



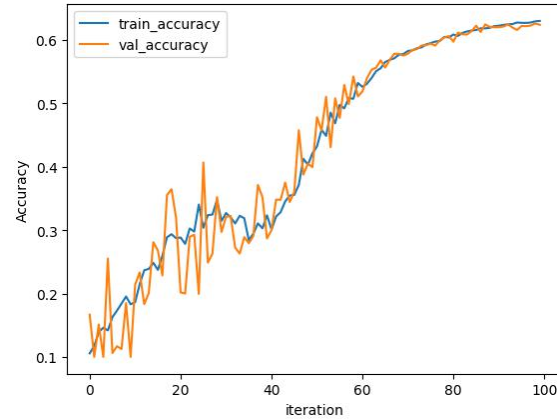
# Fashion MNIST Vanishing Problem

- Train Some Layer

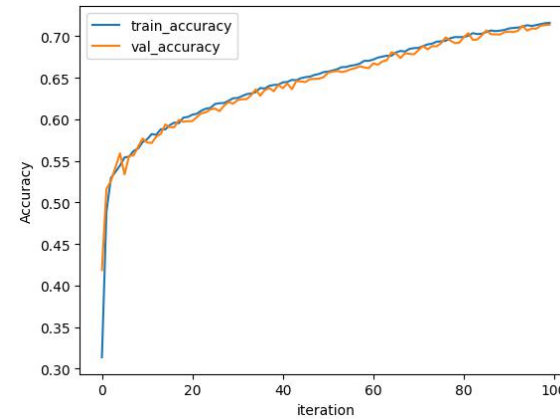
Train lần 1



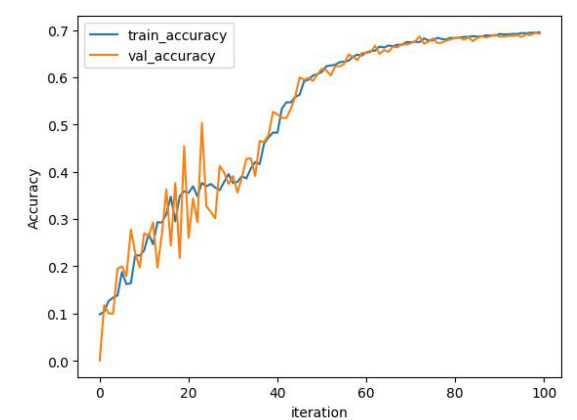
Train lần 2



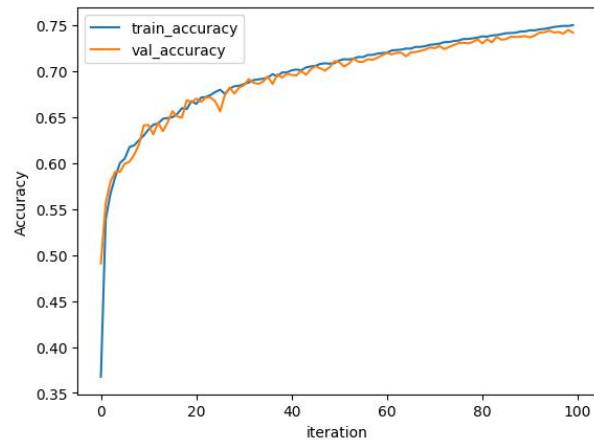
Train lần 3



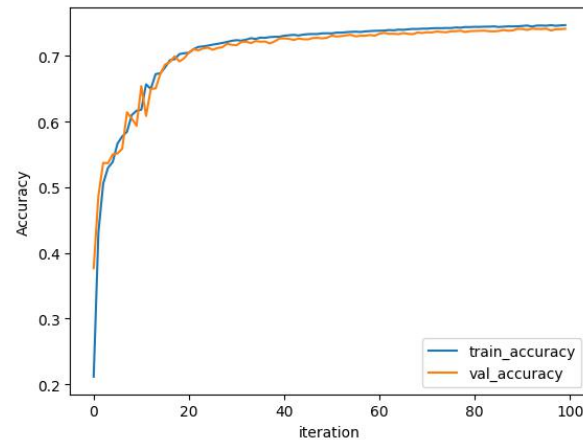
Train lần 4



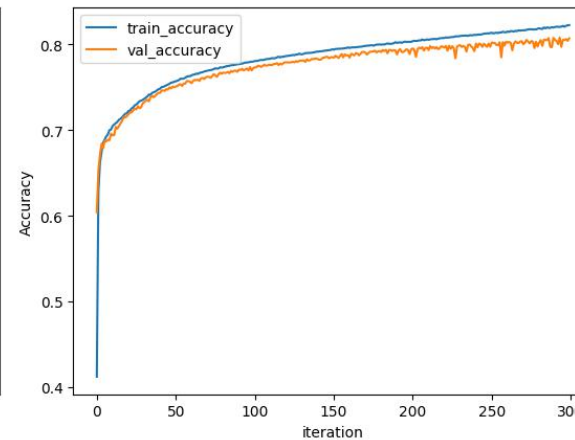
Train lần 5



Train lần 6



Train lần 7

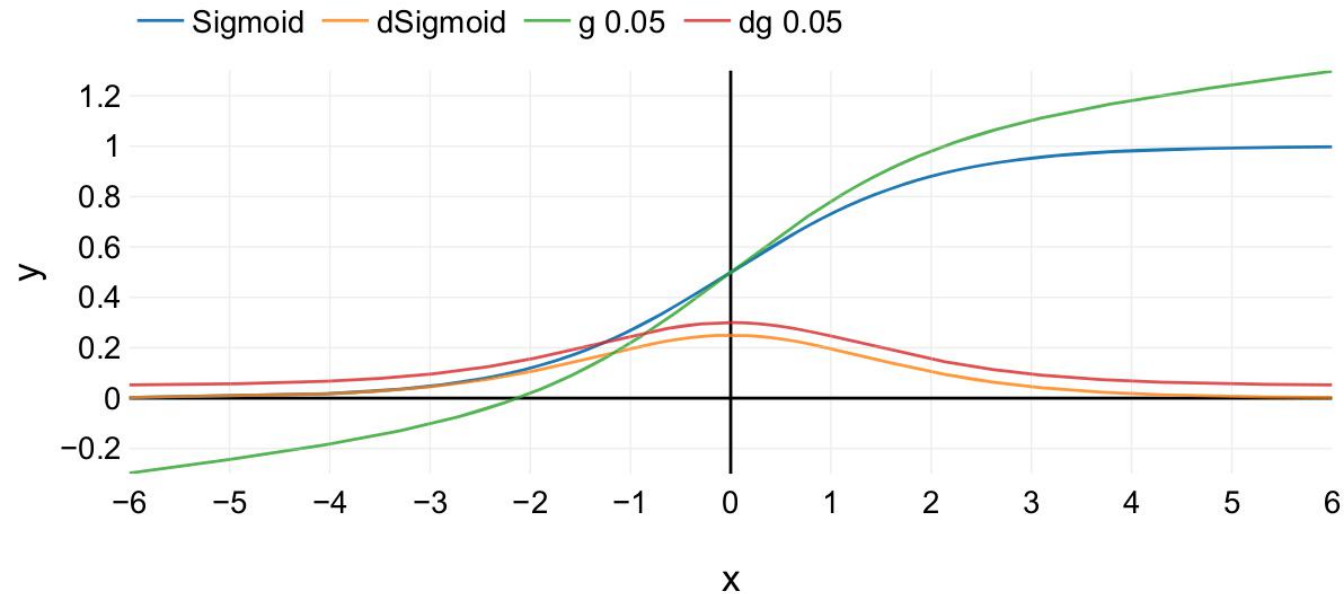


# Other Methods



# Other Methods

- **A new approach for the vanishing gradient problem on sigmoid activation**



Activation functions with  $\beta = 0.05$ , and their derivative functions

$$\text{Sigmoid}(z) = \frac{1}{1 + e^{-z}}$$
$$\frac{d}{dz} (\text{Sigmoid}(z)) = \text{Sigmoid}(z)(1 - \text{Sigmoid}(z))$$

$$g(z) = \text{Sigmoid}(z) + \beta z$$
$$g'(z) = \text{Sigmoid}(z)(1 + \text{Sigmoid}(z)) + \beta$$

- It is very close to the original sigmoid function in the range  $[-1, 1]$ .
- It is a differentiable and unbounded function.
- The derivative of both functions differs by a constant equal to  $\beta$ . That is, the derivative of  $g$  is larger than that of the sigmoid in all  $\mathbb{R}$ .
- When its argument tends to  $+\infty$  or  $-\infty$ , the derivative is asymptotic to  $\beta$ .

# Other Methods

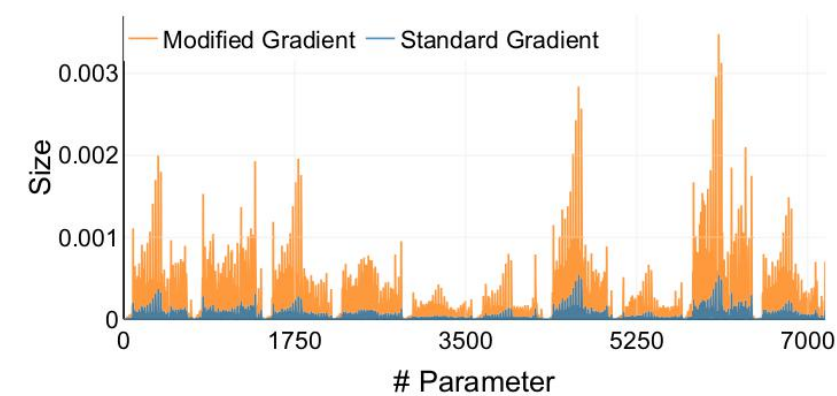
- A new approach for the vanishing gradient problem on sigmoid activation

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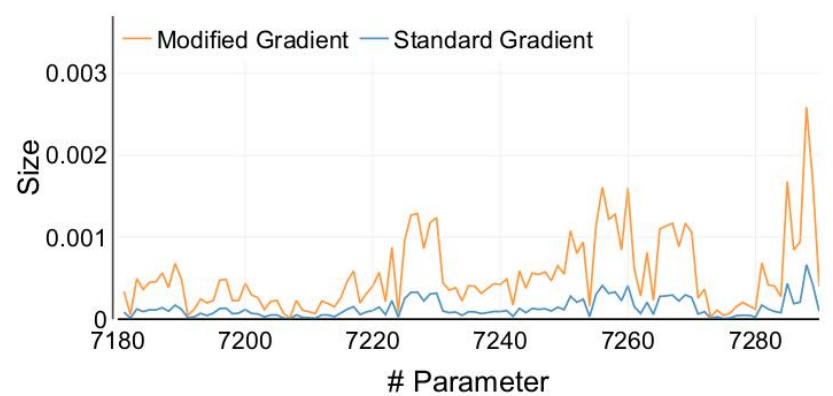
**Algorithm 1** Backpropagation with modified derivative for sigmoid function

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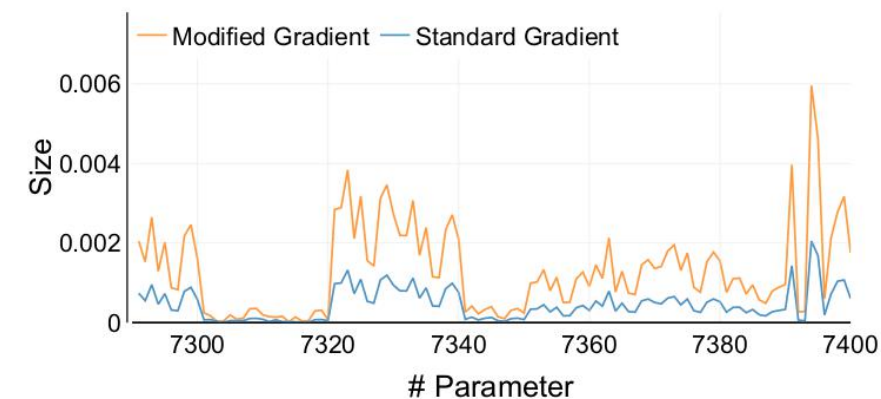
```
1: Input:  $x, y, \theta$ : weights and bias,  $\alpha$ : learning rate,  $\beta$ : modification parameter,  $f$ :  
   function,  $f'$ : derivative  
2: Output:  $\theta_{new}$   
3: Where:  $L$  is the number of layers,  
4: for  $epoch = 1, 2, \dots, N$  do  
5:   for  $l = 1, 2, \dots, L$  do (Compute Activations)  
6:     if  $l = 1$  then  
7:        $a^{(0)} = x$   
8:     end if  
9:      $z^{(l)} = \theta^{(l)} a^{(l-1)}$   
10:     $a^{(l)} = \text{Sigmoid}(z^{(l)})$   
11:  end for  
12:  for  $l = L, L - 1, \dots, 1$  do (Compute  $\delta$ )  
13:    if  $l = L$  then  
14:       $\delta_{out}^{(l)} = -(y - a^{(l)}) \bullet f'_{out}(z^{(l)})$   
15:    else  
16:       $\delta_{\beta}^{(l)} = ((\theta^{(l)})^T \delta_{\beta}^{(l+1)}) \bullet (\text{Sigmoid}'(z^{(l)}) + \beta)$   
17:    end if  
18:  end for  
19:  for  $l = L, L - 1, \dots, 1$  do (Compute gradient)  
20:     $\nabla_{\theta^{(l)}, \beta} J(\theta; x, y) = \delta_{\beta}^{(l)} (a^{(l-1)})^T$   
21:  end for  
22:  for  $l = L, L - 1, \dots, 1$  do (Update Parameters)  
23:     $\theta_{new}^{(l)} = \theta_{old}^{(l)} - \alpha \nabla_{\theta^{(l)}, \beta} J(\theta; x, y)$   
24:  end for  
25: end for
```



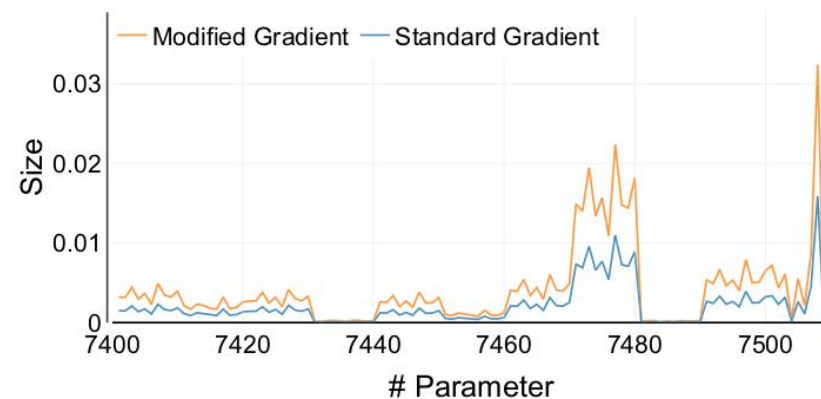
(a) Layer 1



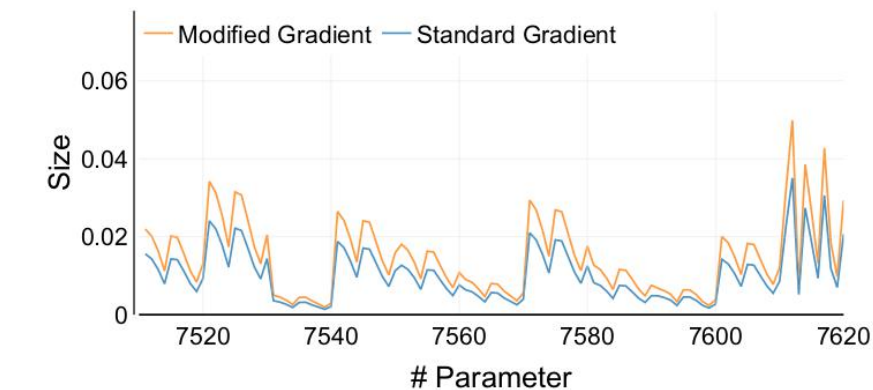
(b) Layer 2



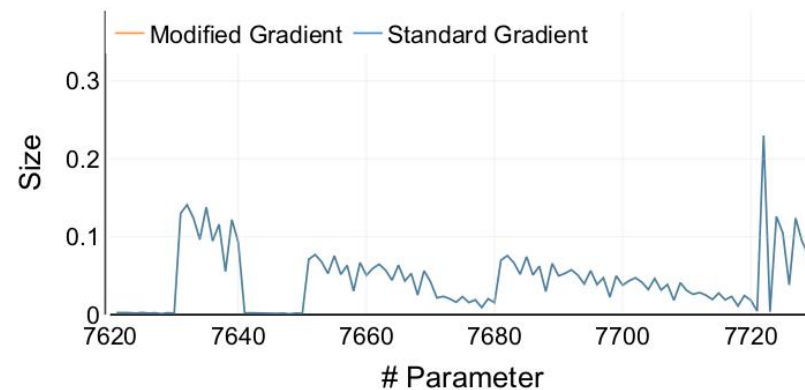
(c) Layer 3



(d) Layer 4



(e) Layer 5



(f) Layer 6

- **A new approach for the vanishing gradient problem on sigmoid activation**

# Other Methods

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- **Vanishing Gradient Analysis in Stochastic Diagonal Approximate Greatest Descent Optimization**

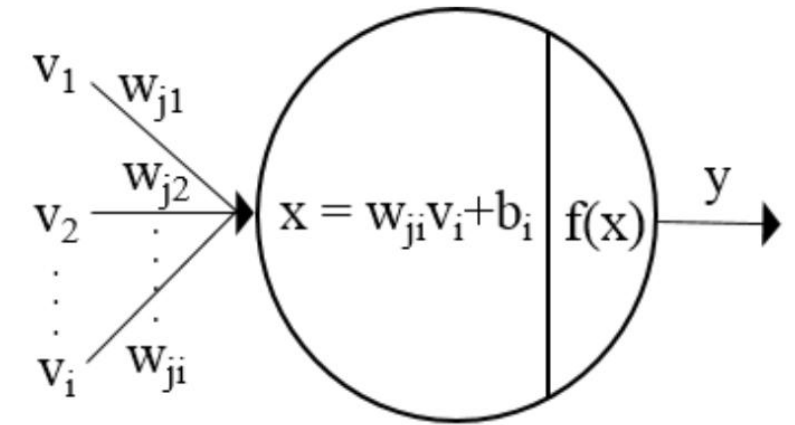
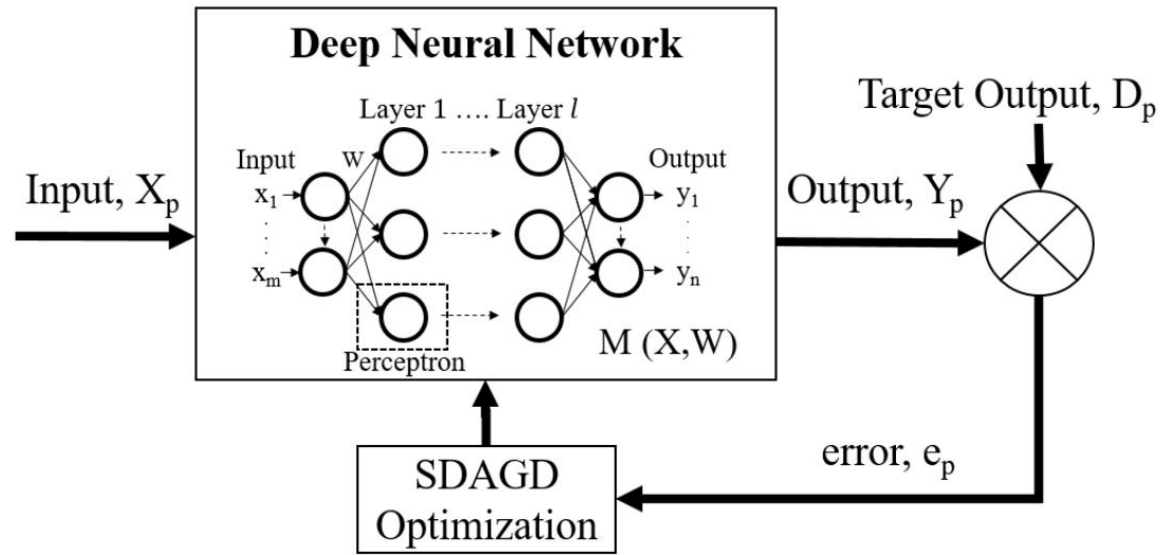


Fig. 2. Basic operation in a perceptron.

Fig. 1. Block diagram of deep learning neural networks with the proposed optimization method – Stochastic Diagonal Approximate Greatest Descent.

## Other Methods

- **Vanishing Gradient Analysis in Stochastic Diagonal Approximate Greatest Descent Optimization**

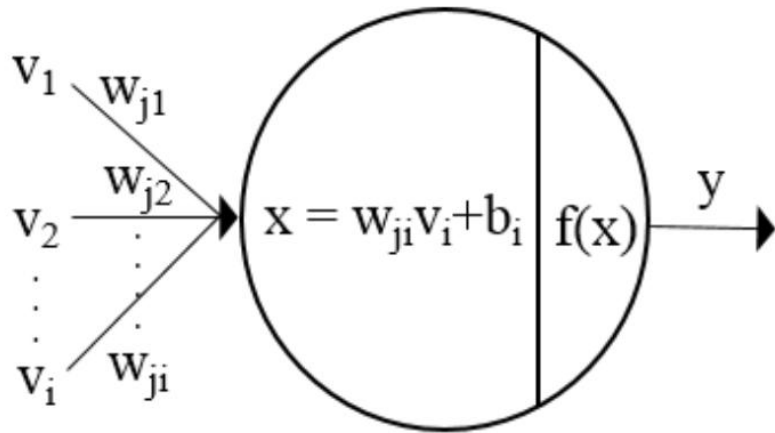


Fig. 2. Basic operation in a perceptron.

$$W_{k+1} = W_k + \eta g(W_k),$$

$$W_{k+1} = W_k + [\mu_k J + H(W_k)]^{-1} g(W_k)$$

where  $\mu_k = \frac{\|g(W_k)\|}{R_k}$  is the relative step length

$J$  is all-ones matrix,

$H(W_k)$  is the truncated Hessian matrix and  $R_k$

$R_k$  is the radius constant



# Other Methods

- **Vanishing Gradient Analysis in Stochastic Diagonal Approximate Greatest Descent Optimization**

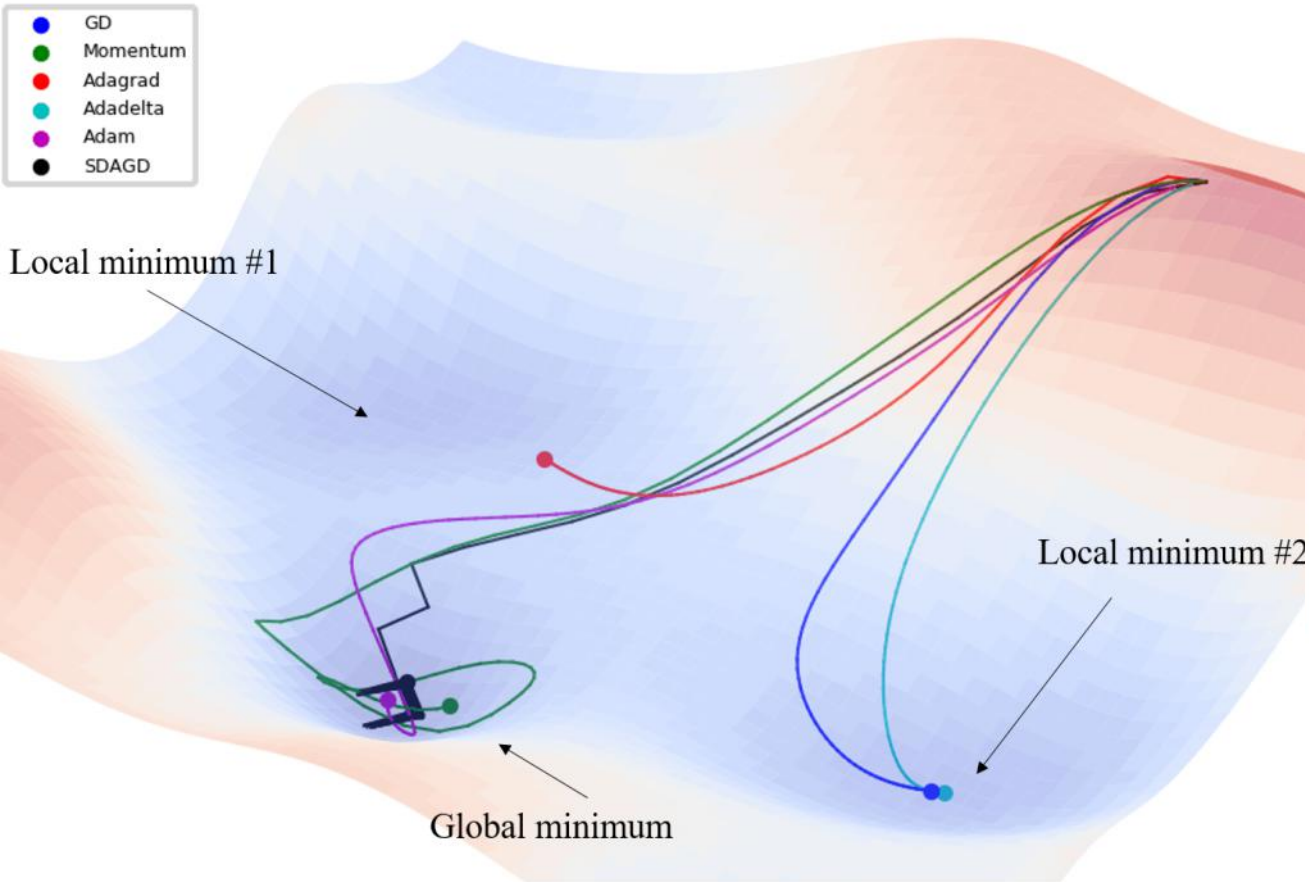


Fig. 3. A hilly error surface with two local minima and one global minimum.

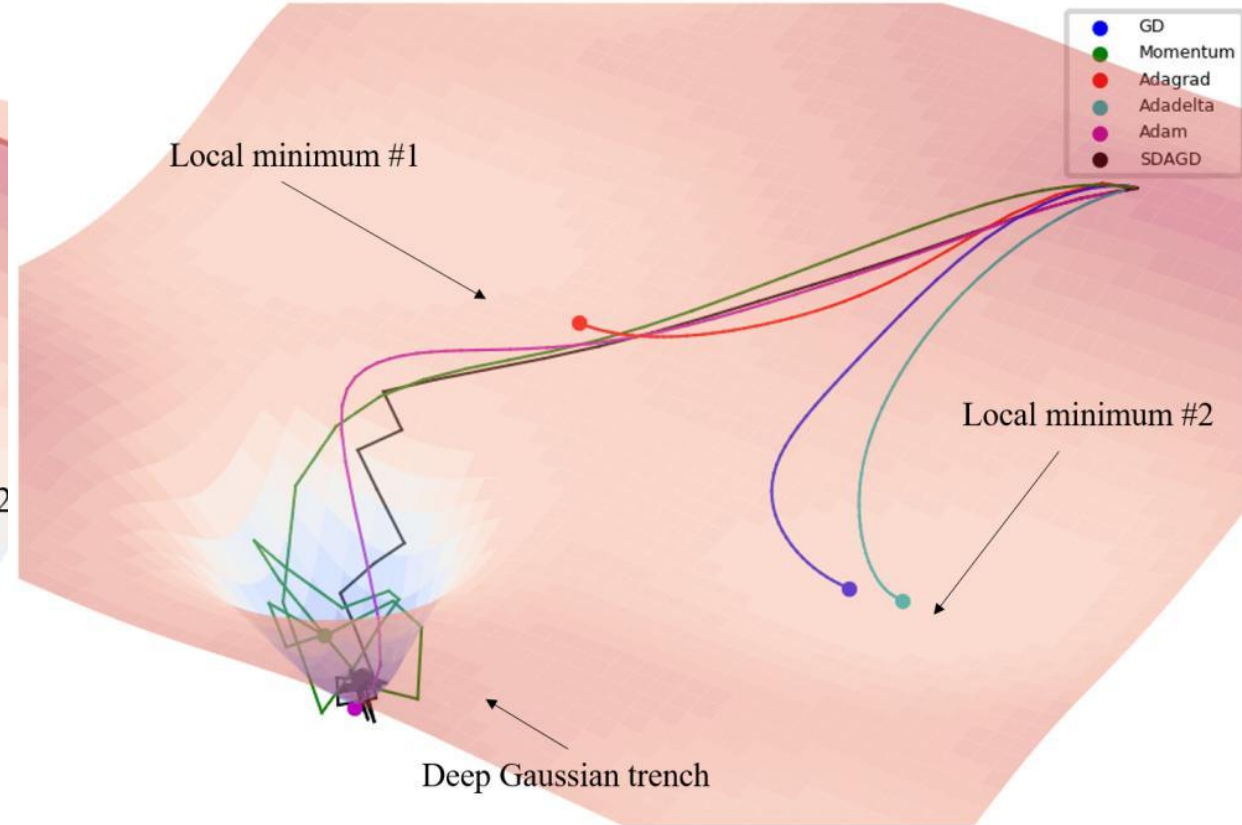


Fig. 4. A deep Gaussian trench to simulate drastic gradient changes.