

# TensorFlow

## Deep Learning Framework

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# Outline

- Introduction to Tensorflow
- Introduction to Tensorflow.Keras
- Model Construction
- Model Training and Inference
- Applying Softmax for Image Data

# Introduction



## TensorFlow

**Developer(s)** Google Brain Team<sup>[1]</sup>

**Initial release** November 9, 2015; 6 years ago

**Stable release** 2.6.1<sup>[2]</sup> (1 November 2021; 30 days ago) / May 14, 2021; 6 months ago

**Repository** [github.com/tensorflow/tensorflow](https://github.com/tensorflow/tensorflow)

**Written in** Python, C++, CUDA

**Platform** Linux, macOS, Windows, Android, JavaScript<sup>[3]</sup>

**Type** Machine learning library

**License** Apache License 2.0

**Website** [www.tensorflow.org](https://www.tensorflow.org)

## Installation

```
pip install tensorflow
```

## Package Declaration

```
import tensorflow as tf
```

## Example 1

```
1 import tensorflow as tf
2
3 print("TensorFlow version: ", tf.__version__)
4 print("Keras version: ", tf.keras.__version__)
```

TensorFlow version: 2.7.0

Keras version: 2.7.0

## Example 2

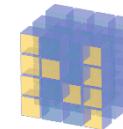
```
1 import tensorflow as tf
2
3 if tf.test.is_gpu_available():
4     print('Running on GPU')
5 else:
6     print('Running on CPU')
```

Running on CPU

# Introduction

## ❖ Tensor

- ❖ ~ ndarray in Numpy
- ❖ Run on both CPU and GPU
- ❖ All tensors are immutable
- ❖ Multi-dimensional arrays with a uniform type



NumPy

Important attributes

```
1 import tensorflow as tf
2 import numpy as np
3
4 # create a ndarray
5 an_array = np.array([1,3,5,7,11])
6 print(type(an_array), an_array)
7
8 # convert from ndarray to tensor
9 a_tensor = tf.convert_to_tensor(an_array)
10 print(a_tensor)
11
12 # convert from tensor to ndarray
13 array_2 = a_tensor.numpy()
14 print(type(array_2), array_2)
```

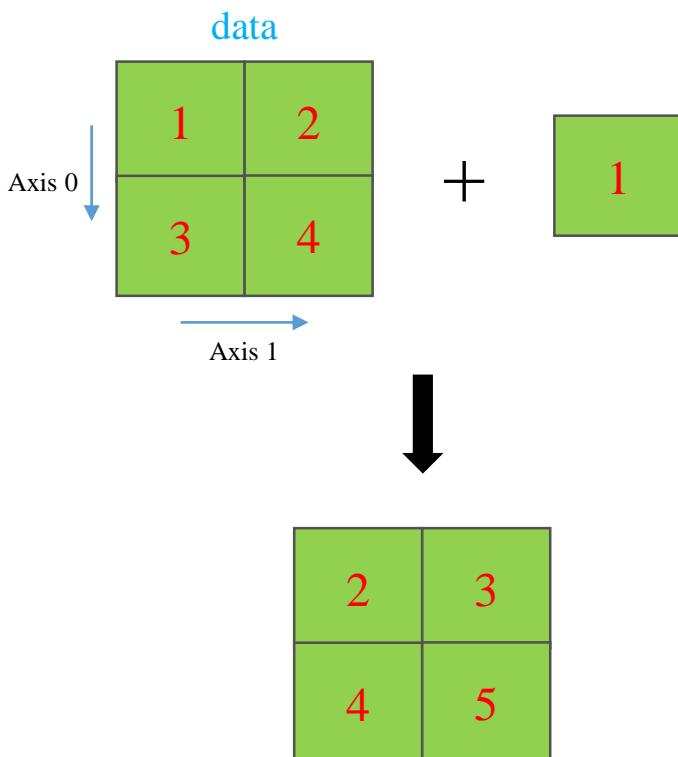
```
<class 'numpy.ndarray'> [ 1  3  5  7 11]
tf.Tensor([ 1  3  5  7 11], shape=(5,), dtype=int32)
<class 'numpy.ndarray'> [ 1  3  5  7 11]
```

```
1 import tensorflow as tf
2 import numpy as np
3
4 # create a 2x3 array
5 an_array = np.array([[1,2],
6                     [3,4],
7                     [5,6]])
8
9 # convert to tensor
10 a_tensor = tf.convert_to_tensor(an_array)
11
12 # no. of elements on each axis
13 print(a_tensor.shape)
14 # data type
15 print(a_tensor.dtype)
16
17 # no. of axes
18 print(a_tensor.ndim)
```

```
(3, 2)
<dtype: 'int32'>
2
```

# Introduction

- ❖ Tensor
- ❖ Broadcasting



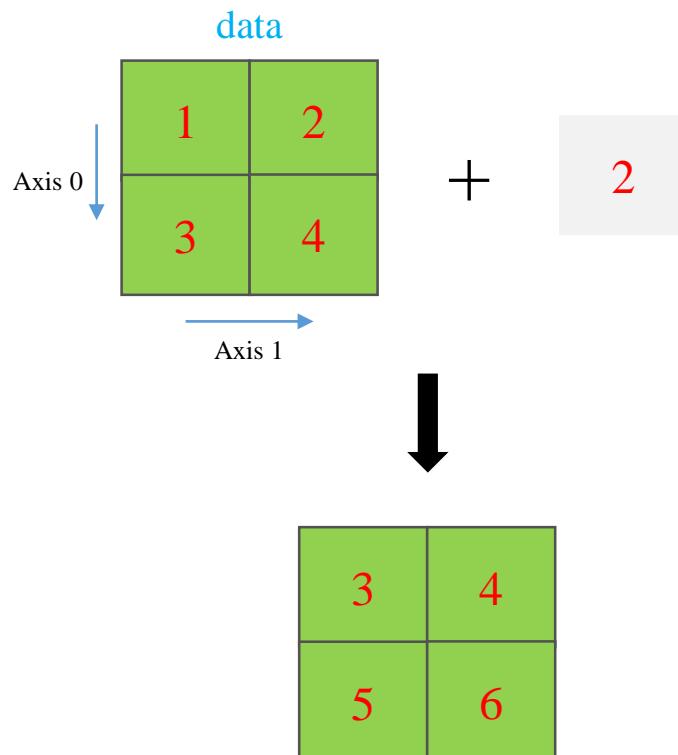
```
1 import tensorflow as tf
2 import numpy as np
3
4 # create two tensors
5 tensor_1 = tf.convert_to_tensor([[1,2],
6                                 [3,4]])
7 tensor_2 = tf.convert_to_tensor([1])
8
9 # add two tensors
10 tensor_3 = tensor_1 + tensor_2
11
12 print('tensor_1: \n', tensor_1)
13 print('tensor_2: \n', tensor_2)
14 print('tensor_3: \n', tensor_3)
```

```
tensor_1:
tf.Tensor(
[[1 2]
 [3 4]], shape=(2, 2), dtype=int32)
tensor_2:
tf.Tensor([1], shape=(1,), dtype=int32)
tensor_3:
tf.Tensor(
[[2 3]
 [4 5]], shape=(2, 2), dtype=int32)
```

# Introduction

## ❖ Tensor

### ❖ Broadcasting



```
1 import tensorflow as tf
2 import numpy as np
3
4 # create 2x2 tensor
5 tensor_1 = tf.convert_to_tensor([[1,2],
6                                 [3,4]])
7
8 # add a number to a tensor
9 tensor_2 = tensor_1 + 2
10
11 print('tensor_1: \n', tensor_1)
12 print('tensor_2: \n', tensor_2)
```

```
tensor_1:
tf.Tensor(
[[1 2]
 [3 4]], shape=(2, 2), dtype=int32)
tensor_2:
tf.Tensor(
[[3 4]
 [5 6]], shape=(2, 2), dtype=int32)
```

# Introduction

## ❖ Tensor

### ❖ Broadcasting

	0	1	2
0	1	2	3
1	4	5	6
2	7	8	9
3	10	11	12

+

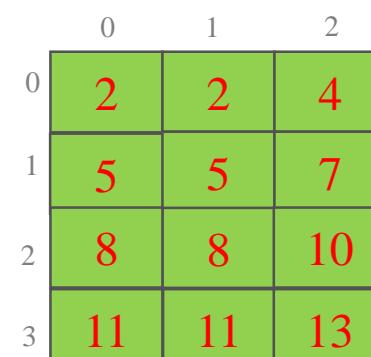


	0	1	2
0	1	2	3
1	4	5	6
2	7	8	9
3	10	11	12

+



=



```

1 import tensorflow as tf
2 import numpy as np
3
4 # create 4x3 tensor
5 np_data = np.array(range(1, 13)).reshape(4, 3)
6 tensor_1 = tf.convert_to_tensor(np_data)
7
8 # create the second tensor
9 tensor_2 = tf.convert_to_tensor([1, 0, 1])
10
11 # add a number to a tensor
12 tensor_3 = tensor_1 + tensor_2
13
14 print('tensor_1: \n', tensor_1)
15 print('tensor_2: \n', tensor_2)
16 print('tensor_3: \n', tensor_3)

```

```

tensor_1:
tf.Tensor(
[[ 1  2  3]
 [ 4  5  6]
 [ 7  8  9]
 [10 11 12]], shape=(4, 3), dtype=int32)
tensor_2:
tf.Tensor([1 0 1], shape=(3,), dtype=int32)
tensor_3:
tf.Tensor(
[[ 2  2  4]
 [ 5  5  7]
 [ 8  8 10]
 [11 11 13]], shape=(4, 3), dtype=int32)

```

# Introduction

## ❖ Tensor

### ❖ Important functions

Squared Difference

$$sd = (x - y)^2$$

x
1
2
3
4

sd
16
9
4
1

$$(x - y)^2 =$$

```
1 import tensorflow as tf
2
3 # create a list
4 x = [1,2, 3, 4]
5 y = 5
6
7 # compute squared difference
8 sd = tf.math.squared_difference(x,y)
9 print(sd)
```

tf.Tensor([16 9 4 1], shape=(4,), dtype=int32)

```
1 import tensorflow as tf
2
3 # create a tensor
4 x = tf.convert_to_tensor([1,2, 3, 4])
5 y = 5
6
7 # compute squared difference
8 sd = tf.math.squared_difference(x,y)
9 print(sd)
```

tf.Tensor([16 9 4 1], shape=(4,), dtype=int32)

```
1 import tensorflow as tf
2 import numpy as np
3
4 # create an ndarray
5 x = np.array([1,2, 3, 4])
6 y = 5
7
8 # compute squared difference
9 sd = tf.math.squared_difference(x,y)
10 print(sd)
```

tf.Tensor([16 9 4 1], shape=(4,), dtype=int32)

# Introduction

## ❖ Tensor

### ❖ Important functions

#### random.normal()

```
1 import tensorflow as tf
2
3 rand = tf.random.normal(shape = (3,2), mean=0, stddev=1)
4 print(rand)
```

```
tf.Tensor(
[[ 0.47103247 -0.12765862]
 [-0.26556632 -0.05912822]
 [ 1.0851953 -0.55289406]], shape=(3, 2), dtype=float32)
```

#### random.uniform()

```
1 import tensorflow as tf
2
3 rand = tf.random.uniform(shape=(3,2), minval=0,
                           maxval=9, dtype=tf.int32)
4
5 print(rand)
```

```
tf.Tensor(
[[4 0]
 [1 8]
 [0 2]], shape=(3, 2), dtype=int32)
```

# Introduction

## ❖ Tensor

### ❖ Important functions

tensor_1	
1	2
3	4

Axis 0 ↓

Axis 1 →

tensor_2	
3	4
5	6

tensor_3	
1	2
3	4
3	4
5	6

tensor_4			
1	2	3	4
3	4	5	6

concat()

```
1 import tensorflow as tf
2
3 tensor_1 = tf.random.normal(shape=(2, 2), mean=0, stddev=1)
4 tensor_2 = tf.random.normal(shape=(2, 2), mean=0, stddev=1)
5
6 # concat two tensors along axis_0
7 tensor_3 = tf.concat([tensor_1, tensor_1], axis=0)
8
9 # concat two tensors along axis_1
10 tensor_4 = tf.concat([tensor_1, tensor_1], axis=1)
11
12 print(tensor_1.shape)
13 print(tensor_2.shape)
14 print(tensor_3.shape)
15 print(tensor_4.shape)

(2, 2)
(2, 2)
(4, 2)
(2, 4)
```

# Introduction

## ❖ Tensor

### ❖ Important functions

1	2
7	9
8	6

.argmin(axis=0) = 

0	0
---	---

1	2
7	9
8	6

.argmin(axis=1) = 

0	0	1
---	---	---

### argmin()

```
1 import tensorflow as tf
2
3 # create a tensor
4 tensor = tf.random.uniform(shape=(3, 6), minval=0,
5                             maxval=20, dtype=tf.int32)
6
7 # find the index of the min value
8 min_position_1 = tf.argmin(tensor, axis=0)
9 min_position_2 = tf.argmin(tensor, axis=1)
10
11 print(tensor)
12 print('min_position_1: ', min_position_1)
13 print('min_position_2: ', min_position_2)
tf.Tensor(
[[ 5  0 13 11  4 10]
 [19  6  7  5 17  6]
 [18  9  9  2  1 11]], shape=(3, 6), dtype=int32)
min_position_1: tf.Tensor([0 0 1 2 2 1], shape=(6,), dtype=int64)
min_position_2: tf.Tensor([1 3 4], shape=(3,), dtype=int64)
```

# Introduction

## ❖ Tensor

### ❖ Important functions

1	2
7	9
8	6

.argmax(axis=0) = 

2	1
---	---

1	2
7	9
8	6

.argmax(axis=1) = 

1	1	0
---	---	---

### argmax()

```
1 import tensorflow as tf
2
3 # create a tensor
4 tensor = tf.random.uniform(shape=(3, 6), minval=0,
5                             maxval=20, dtype=tf.int32)
6
7 # find the index of the max value
8 max_position_1 = tf.argmax(tensor, axis=0)
9 max_position_2 = tf.argmax(tensor, axis=1)
10
11 print(tensor)
12 print('max_position_1: ', max_position_1)
13 print('max_position_2: ', max_position_2)

tf.Tensor(
[[ 8 10 13  1 12  1]
 [ 8 19  5  3 16 16]
 [ 2 16  7  1  4 17]], shape=(3, 6), dtype=int32)
max_position_1: tf.Tensor([0 1 0 1 1 2], shape=(6,), dtype=int64)
max_position_2: tf.Tensor([2 1 5], shape=(3,), dtype=int64)
```

# Introduction

## ❖ Tensor

### ❖ Important functions

$$\begin{matrix} \text{X} \\ \begin{array}{|c|c|} \hline 1 & 2 \\ \hline 3 & 4 \\ \hline \end{array} \end{matrix} \cdot \begin{matrix} \text{v} \\ \begin{array}{|c|} \hline 1 \\ \hline 2 \\ \hline \end{array} \end{matrix} = \begin{matrix} \text{result} \\ \begin{array}{|c|} \hline 5 \\ \hline 11 \\ \hline \end{array} \end{matrix}$$

$$\begin{matrix} \text{v} \\ \begin{array}{|c|c|} \hline 1 & 2 \\ \hline \end{array} \end{matrix} \cdot \begin{matrix} \text{X} \\ \begin{array}{|c|c|} \hline 1 & 2 \\ \hline 3 & 4 \\ \hline \end{array} \end{matrix} = \begin{matrix} \text{result} \\ \begin{array}{|c|} \hline 7 \\ \hline 10 \\ \hline \end{array} \end{matrix}$$

```

1 import tensorflow as tf
2 import numpy as np
3
4 matrix = tf.convert_to_tensor([[1, 2], [3, 4]])
5 vector = tf.convert_to_tensor([1, 2])
6
7 print('matrix shape \n', matrix.shape)
8 print('vector shape \n', vector.shape)
9
10 vector = tf.reshape(vector, (2, 1))
11 print('vector reshape \n', vector.shape)
12
13 result1 = tf.matmul(matrix, vector)
14 print(result1)
15
16 result2 = tf.matmul(tf.transpose(vector), matrix)
17 print(result2)

```

matrix shape  
 (2, 2)  
 vector shape  
 (2,)  
 vector reshape  
 (2, 1)  
 tf.Tensor(  
 [[ 5  
 [11]], shape=(2, 1), dtype=int32)  
 tf.Tensor([[ 7 10]], shape=(1, 2), dtype=int32)

# Introduction

## ❖ Tensor

### ❖ Important functions

$$\begin{array}{c} \text{X} \\ \begin{array}{|c|c|} \hline 1 & 2 \\ \hline 3 & 4 \\ \hline \end{array} \end{array} \bullet \begin{array}{c} \text{Y} \\ \begin{array}{|c|c|} \hline 2 & 3 \\ \hline 2 & 1 \\ \hline \end{array} \end{array} = \begin{array}{c} \text{result} \\ \begin{array}{|c|c|} \hline 6 & 5 \\ \hline 14 & 13 \\ \hline \end{array} \end{array}$$

$$\begin{array}{c} \text{Y} \\ \begin{array}{|c|c|} \hline 2 & 3 \\ \hline 2 & 1 \\ \hline \end{array} \end{array} \bullet \begin{array}{c} \text{X} \\ \begin{array}{|c|c|} \hline 1 & 2 \\ \hline 3 & 4 \\ \hline \end{array} \end{array} = \begin{array}{c} \text{result} \\ \begin{array}{|c|c|} \hline 11 & 16 \\ \hline 5 & 8 \\ \hline \end{array} \end{array}$$

```
1 import tensorflow as tf
2 import numpy as np
3
4 matrix1 = tf.convert_to_tensor([[1, 2], [3, 4]])
5 matrix2 = tf.convert_to_tensor([[2, 3], [2, 1]])
6
7 print('matrix1 shape \n', matrix1.shape)
8 print('matrix2 shape \n', matrix2.shape)
9
10 result1 = tf.matmul(matrix1, matrix2)
11 print(result1)
12
13 result2 = tf.matmul(matrix2, matrix1)
14 print(result2)
```

```
matrix1 shape
(2, 2)
matrix2 shape
(2, 2)
tf.Tensor(
[[ 6  5]
 [14 13]], shape=(2, 2), dtype=int32)
tf.Tensor(
[[11 16]
 [ 5  8]], shape=(2, 2), dtype=int32)
```

# Introduction

## ❖ Tensor

### ❖ Important functions

$$\begin{array}{c} \text{X} \\ \begin{array}{|c|c|} \hline 1 & 2 \\ \hline 3 & 4 \\ \hline \end{array} \end{array} \bullet \begin{array}{c} \text{Y} \\ \begin{array}{|c|c|} \hline 2 & 3 \\ \hline 2 & 1 \\ \hline \end{array} \end{array} = \begin{array}{c} \text{result} \\ \begin{array}{|c|c|} \hline 6 & 5 \\ \hline 14 & 13 \\ \hline \end{array} \end{array}$$

$$\begin{array}{c} \text{Y} \\ \begin{array}{|c|c|} \hline 2 & 3 \\ \hline 2 & 1 \\ \hline \end{array} \end{array} \bullet \begin{array}{c} \text{X} \\ \begin{array}{|c|c|} \hline 1 & 2 \\ \hline 3 & 4 \\ \hline \end{array} \end{array} = \begin{array}{c} \text{result} \\ \begin{array}{|c|c|} \hline 11 & 16 \\ \hline 5 & 8 \\ \hline \end{array} \end{array}$$

```
1 import tensorflow as tf
2 import numpy as np
3
4 matrix1 = tf.convert_to_tensor([[1, 2], [3, 4]])
5 matrix2 = tf.convert_to_tensor([[2, 3], [2, 1]])
6
7 print('matrix1 shape \n', matrix1.shape)
8 print('matrix2 shape \n', matrix2.shape)
9
10 result1 = matrix1@matrix2
11 print(result1)
12
13 result2 = matrix2@matrix1
14 print(result2)
```

```
matrix1 shape
(2, 2)
matrix2 shape
(2, 2)
tf.Tensor(
[[ 6  5]
 [14 13]], shape=(2, 2), dtype=int32)
tf.Tensor(
[[11 16]
 [ 5  8]], shape=(2, 2), dtype=int32)
```

# Introduction

## ❖ Variable: Represent a tensor whose values can be changed

```
1 # variable
2
3 var = tf.Variable([1.0, 2.0])
4 print(var.numpy())
5
6 var.assign([7, 9])
7 print(var.numpy())
```

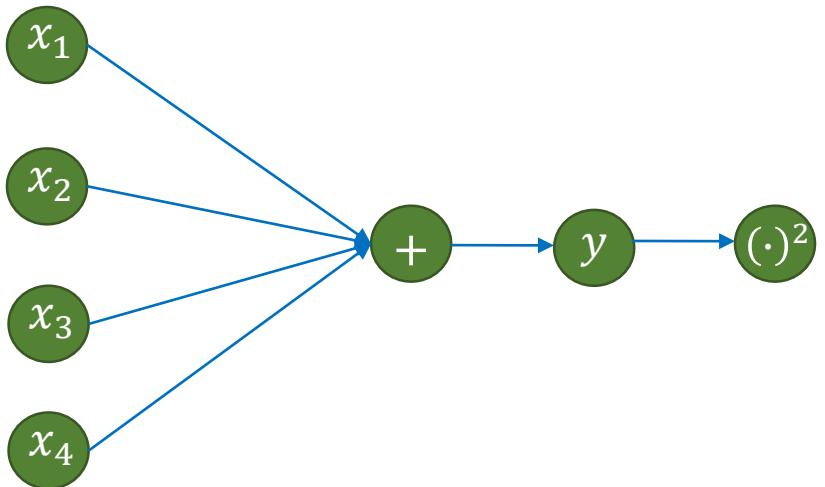
```
[1. 2.]
[7. 9.]
```

```
1 # variables
2
3 var = tf.Variable([1.0, 2.0])
4
5 var.assign_add([5, 3])
6 print(var.numpy())
7
8 var.assign_sub([2, 3])
9 print(var.numpy())
```

```
[6. 5.]
[4. 2.]
```

# Introduction

## ❖ Gradient computation



```
tf.Tensor(  
[[1. 1.]  
 [1. 1.]], shape=(2, 2), dtype=float32)  
tf.Tensor(  
[[8. 8.]  
 [8. 8.]], shape=(2, 2), dtype=float32)
```

```
1 import tensorflow as tf  
2  
3 # data  
4 x = tf.ones((2, 2))  
5  
6 with tf.GradientTape() as t:  
7     t.watch(x)  
8     y = tf.reduce_sum(x)  
9     z = tf.multiply(y, y)  
10  
11 # compute derivative  
12 dz_dx = t.gradient(z, x)  
13  
14 # print out  
15 print(x)  
16 print(dz_dx)
```

# Introduction

## ❖ Gradient computation

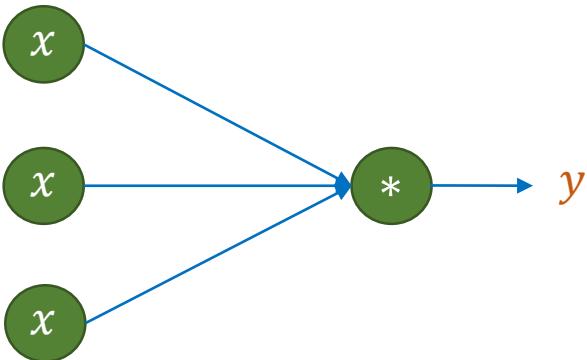


```
tf.Tensor(108.0, shape=(), dtype=float32)
tf.Tensor(6.0, shape=(), dtype=float32)
```

```
1 import tensorflow as tf
2
3 # data
4 x = tf.constant(3.0)
5
6 # trace
7 with tf.GradientTape(persistent=True) as t:
8     t.watch(x)
9     y = x * x
10    z = y * y
11
12 # compute derivative
13 dz_dx = t.gradient(z, x)
14 dy_dx = t.gradient(y, x)
15
16 # print out
17 print(dz_dx)
18 print(dy_dx)
```

# Introduction

## ❖ Gradient computation



```
tf.Tensor(3.0, shape=(), dtype=float32)
tf.Tensor(6.0, shape=(), dtype=float32)
```

```
1 # data
2 x = tf.Variable(1.0)
3
4 # trace
5 with tf.GradientTape() as t1:
6     with tf.GradientTape() as t2:
7         y = x*x*x
8
9     # compute derivative using t2
10    dy_dx = t2.gradient(y, x)
11
12    # compute derivative using t1
13    d2y_dx2 = t1.gradient(dy_dx, x)
14
15    # print out
16    print(dy_dx)
17    print(d2y_dx2)
```

# Introduction

## ❖ Gradient computation

$$g(x) = -3x + 4$$

$$h(g) = 2g + 1$$

```
tf.Tensor([-6.], shape=(1,), dtype=float32)
```

```
1 import tensorflow as tf
2
3 # variable
4 x = tf.ones((1))**2
5
6 # trace
7 with tf.GradientTape() as tape:
8     tape.watch(x)
9
10    # construct functions
11    g_x = -3*x + 4
12    h_g = 2*g_x + 1
13
14    # compute derivative
15    dh_dx = tape.gradient(h_g, x)
16
17    # print out
18    print(dh_dx)
```

# Introduction

## ❖ Gradient computation

$$g(x) = x^2 + 1$$

$$h(g) = e^g$$

```
tf.Tensor([14.778112], shape=(1,), dtype=float32)
```

```
1 import tensorflow as tf
2
3 # variable
4 x = tf.ones((1))
5
6 # trace
7 with tf.GradientTape() as tape:
8     tape.watch(x)
9
10    # construct functions
11    g_x = x*x + 1
12    h_g = tf.exp(g_x)
13
14    # compute derivative
15    dh_dx = tape.gradient(h_g, x)
16
17    # print out
18    print(dh_dx)
```

# Introduction

## ❖ Gradient computation

$$g(x) = \cos(x^2 e^x + 2x)$$

$$h(g) = e^g \sin(\sqrt{g})$$

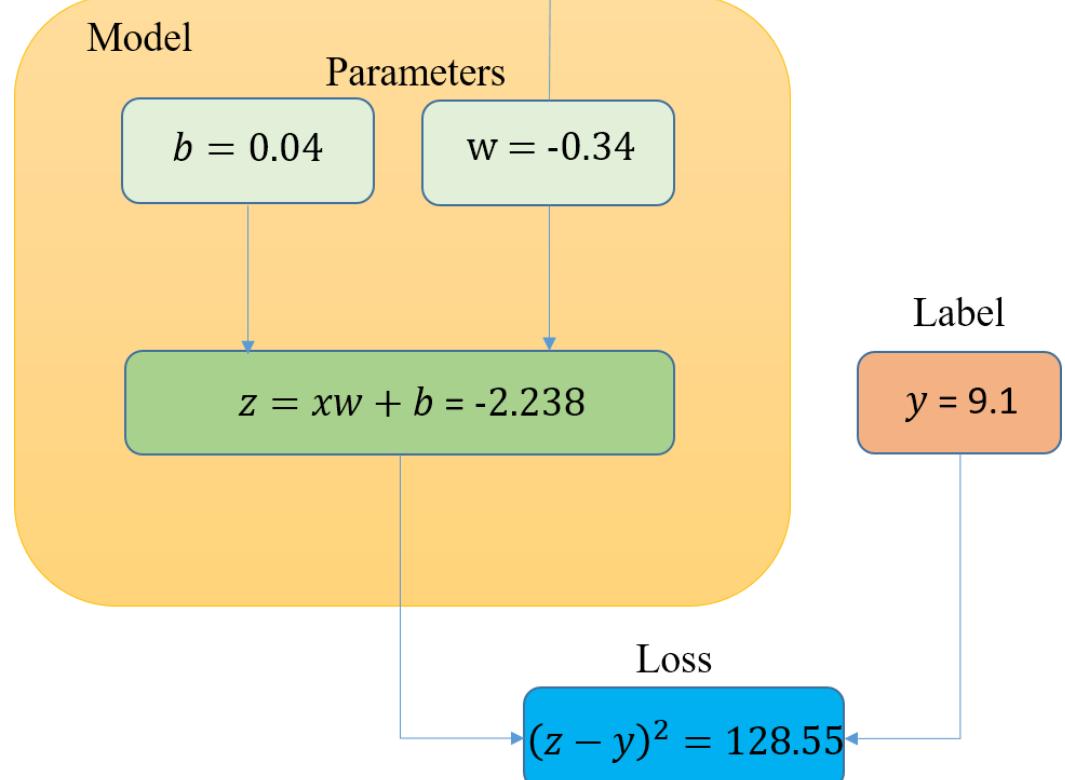
```
1 import tensorflow as tf
2
3 # variable
4 x = tf.ones((1))
5
6 # trace
7 with tf.GradientTape() as tape:
8     tape.watch(x)
9
10    # construct functions
11    g_x = tf.math.cos(x*x*tf.exp(x) + 2*x)
12    h_g = tf.exp(g_x)*tf.math.sin(tf.math.sqrt(g_x))
13
14    # compute derivative
15    dh_dx = tape.gradient(h_g, x)
16
17    # print out
18    print(dh_dx)
```

```
tf.Tensor([67.120346], shape=(1,), dtype=float32)
```

# Gradient computation

Initialize  
 $b=0.04$  and  
 $w=-0.34$

Input  
 $x = 6.7$



area	price
6.7	9.1
4.6	5.9
3.5	4.6
5.5	6.7

```
1 import tensorflow as tf
2
3 w = tf.Variable([-0.34])
4 b = tf.Variable([0.04])
5
6 x = [6.7, 4.6, 3.5, 5.5]
7 x = tf.convert_to_tensor(x)
8
9 print('b: \n', b.numpy())
10 print('w: \n', w.numpy())
11 print('x: \n', x.numpy())
12
13 with tf.GradientTape(persistent=True) as tape:
14     y = tf.math.multiply(x, w) + b
15     print('y: \n', y.numpy())
16
17 loss = tf.reduce_mean(y**2)
18 print('loss: \n', loss.numpy())
```

b:  
[0.04]  
w:  
[-0.34]  
x:  
[6.7 4.6 3.5 5.5]  
y:  
[-2.238 -1.524 -1.1500001 -1.83 ]  
loss:  
3.000655

# Gradient computation

Initialize  
 $b=0.04$  and  
 $w=-0.34$

Input  $x = 6.7$

Model

Parameters

$b = 0.0$

$w = 0.038$

$$z = xw + b = -2.238$$

Label  $y = 9.1$

Loss

$$(z - y)^2 = 128.55$$

area	price
6.7	9.1
4.6	5.9
3.5	4.6
5.5	6.7

```
1 import tensorflow as tf
2
3 w = tf.Variable(tf.random.normal((1,)))
4 b = tf.Variable(tf.zeros(1, dtype=tf.float32))
5
6 x = [6.7, 4.6, 3.5, 5.5]
7 x = tf.convert_to_tensor(x)
8
9 print('b: \n', b.numpy())
10 print('w: \n', w.numpy())
11 print('x: \n', x.numpy())
12
13 with tf.GradientTape(persistent=True) as tape:
14     y = tf.math.multiply(x, w) + b
15     print('y: \n', y.numpy())
16
17 loss = tf.reduce_mean(y**2)
18 print('loss: \n', loss.numpy())
```

b:

[0.]

w:

[0.03887156]

x:

[6.7 4.6 3.5 5.5]

y:

[0.2604395 0.1788092 0.13605048 0.2137936 ]

loss:

0.04100472

# Introduction

## ❖ Gradient computation

area	price
6.7	9.1
4.6	5.9
3.5	4.6
5.5	6.7

```
theta:  
[[ 0.04]  
[-0.34]]  
x:  
[[1.  6.7]  
[1.  4.6]  
[1.  3.5]  
[1.  5.5]]  
y:  
[[-2.238     ]  
[-1.524     ]  
[-1.1500001]  
[-1.83      ]]  
loss:  
3.000655
```

```
1 import tensorflow as tf  
2  
3 theta = tf.Variable([[0.04], [-0.34]])  
4  
5 x = [[1, 6.7],  
6 [1, 4.6],  
7 [1, 3.5],  
8 [1, 5.5]];  
9 x = tf.convert_to_tensor(x)  
10  
11 print('theta: \n', theta.numpy())  
12 print('x: \n', x.numpy())  
13  
14 with tf.GradientTape(persistent=True) as tape:  
15     y = x@theta  
16     print('y: \n', y.numpy())  
17  
18     loss = tf.reduce_mean(y**2)  
19     print('loss: \n', loss.numpy())
```

# Introduction

## ❖ Gradient computation

area	price
6.7	9.1
4.6	5.9
3.5	4.6
5.5	6.7

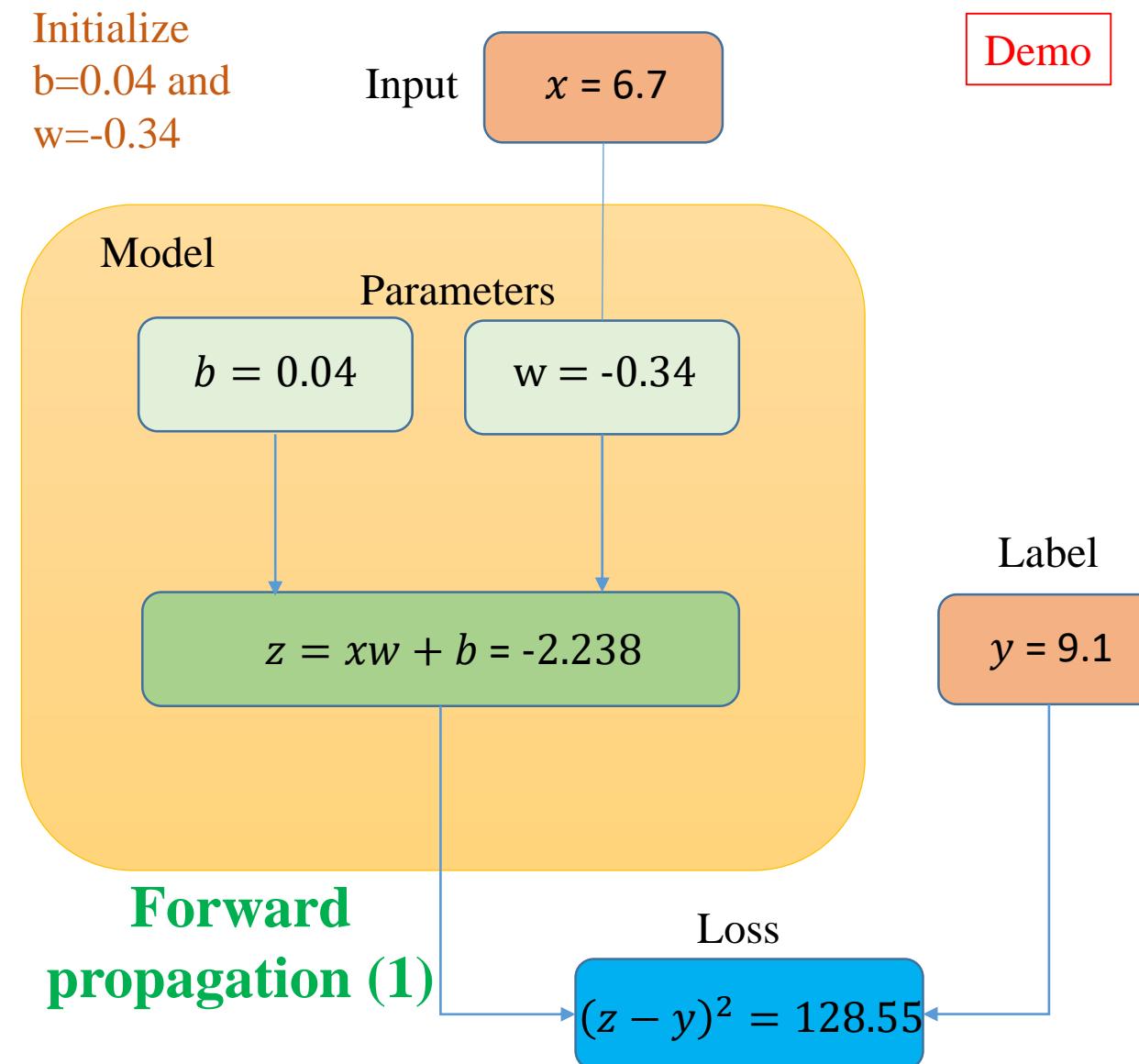
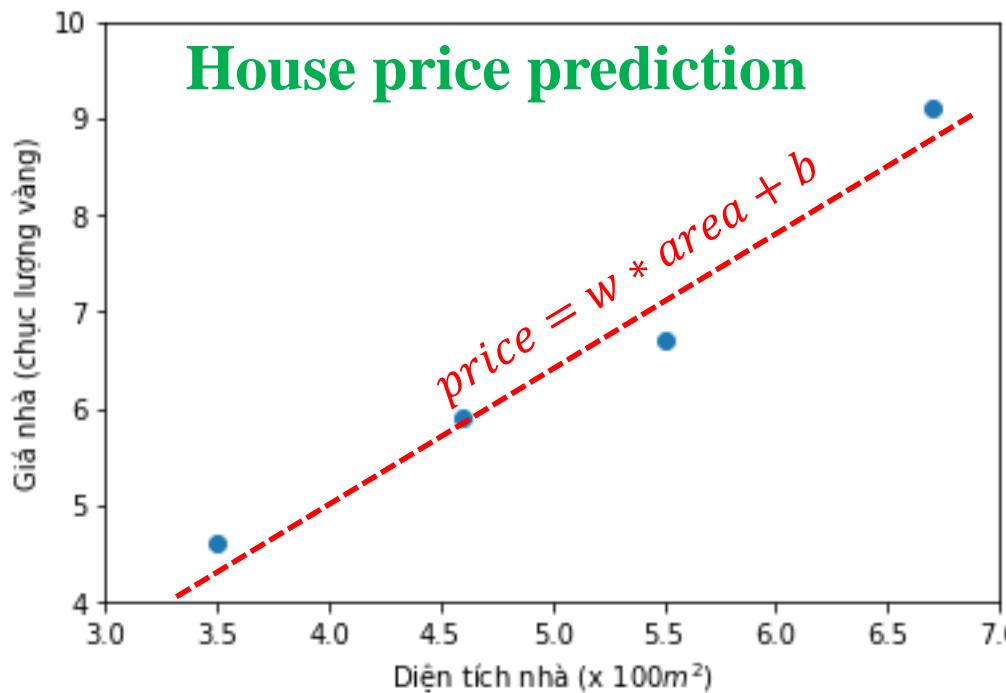
```
theta:  
[[0.28044993]  
[1.5637906 ]]  
x:  
[[1. 6.7]  
[1. 4.6]  
[1. 3.5]  
[1. 5.5]]  
y:  
[[10.757846 ]  
[ 7.4738865]  
[ 5.753717 ]  
[ 8.881298 ]]  
loss:  
70.893234
```

```
1 import tensorflow as tf  
2  
3 theta = tf.Variable(tf.random.normal((2,1)))  
4  
5 x = [[1, 6.7],  
6 [1, 4.6],  
7 [1, 3.5],  
8 [1, 5.5]];  
9 x = tf.convert_to_tensor(x)  
10  
11 print('theta: \n', theta.numpy())  
12 print('x: \n', x.numpy())  
13  
14 with tf.GradientTape(persistent=True) as tape:  
15     y = x@theta  
16     print('y: \n', y.numpy())  
17  
18     loss = tf.reduce_mean(y**2)  
19     print('loss: \n', loss.numpy())
```

# Linear Regression

Given sample data

area	price
6.7	9.1
4.6	5.9
3.5	4.6
5.5	6.7



# Linear Regression

Demo

Forward  
propagation

Input  
 $x = 0.67$

Model  
Parameters

$$b = 0.26676 \quad w = 1.17929$$

$$b = b - \eta L'_b \quad w = w - \eta L'_w$$

$$z = xw + b = -2.238$$

Label

$$y = 9.1$$

$$(z - y)^2 = 0.868$$

Giá trị  $w, b$  mới  
giúp loss giảm

Loss  
 $(z - y)^2 = 0.868$

Backpropagation

Model

$$b = 0.26676$$

Parameters

$$w = 1.17929$$

$$b = b - \eta L'_b$$

$$w = w - \eta L'_w$$

$$z = xw + b = -2.238$$

$$L'_w = 2x(z - y) \\ = -151.9292$$

$$L'_b = 2(z - y) \\ = -22.676$$

$$\eta = 0.01$$

Label

$$y = 9.1$$

$$128.55$$

# Introduction

## ❖ Gradient computation

```
theta:  
[[ 0.04]  
[-0.34]]  
  
x:  
[[1.  6.7]]  
  
y:  
[[-2.238]]  
  
loss:  
128.55025
```

```
tf.Tensor(  
[[ -22.676 ]  
[-151.9292]], shape=(2, 1), dtype=float32)
```

```
1 import tensorflow as tf  
2  
3 theta = tf.Variable([[0.04], [-0.34]])  
4  
5 x = [[1, 6.7]];  
6 x = tf.convert_to_tensor(x)  
7  
8 y = [9.1];  
9  
10 print('theta: \n', theta.numpy())  
11 print('x: \n', x.numpy())  
12  
13 with tf.GradientTape(persistent=True) as tape:  
14     y_hat = x@theta  
15     print('y: \n', y_hat.numpy())  
16  
17     loss = tf.reduce_mean((y_hat-y)**2)  
18     print('loss: \n', loss.numpy())  
19  
20 dtheta = tape.gradient(loss, theta)  
21 print(dtheta)
```

# Loss Functions

## ❖ Cross-entropy

$$\text{Loss} = \sum_i -y_i \log(\hat{y}_i)$$

```
1 import tensorflow as tf
2
3 y_true = [[0, 1, 0], [0, 0, 1]]
4 y_pred = [[0.05, 0.95, 0], [0.1, 0.8, 0.1]]
5 y_pred = tf.convert_to_tensor(y_pred)
6
7 # CategoricalCrossentropy
8 ce_function = tf.keras.losses.CategoricalCrossentropy()
9 loss = ce_function(y_true, y_pred)
10
11 print(loss.numpy())
```

1.1769392

# Loss Functions

## ❖ Cross-entropy

$$\text{Loss} = \sum_i -y_i \log(\hat{y}_i)$$

```
1 import tensorflow as tf
2
3 y_true = [1, 2]
4 y_pred = [[0.05, 0.95, 0], [0.1, 0.8, 0.1]]
5 y_pred = tf.convert_to_tensor(y_pred)
6
7 # SparseCategoricalCrossentropy
8 sce_function = tf.keras.losses.SparseCategoricalCrossentropy()
9 loss = sce_function(y_true, y_pred)
10 print(loss.numpy())
```

1.1769392

# Keras

- ❖ Run on top of Tensorflow
- ❖ Integrated into Tensorflow

## Package Declaration

```
1 import tensorflow as tf
2 import tensorflow.keras as keras
3
4 print("TensorFlow version: ", tf.__version__)
5 print("Keras version: ", keras.__version__)
```

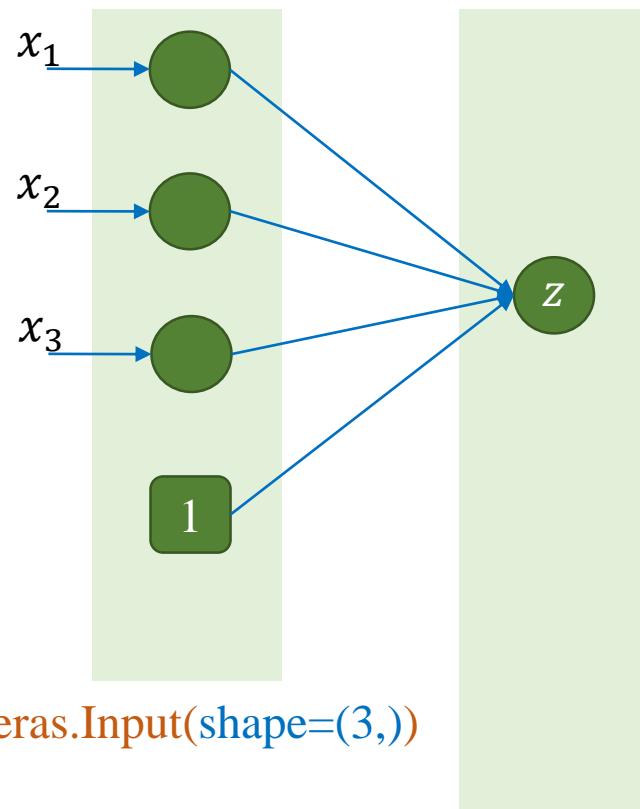
TensorFlow version: 2.7.0  
Keras version: 2.7.0



Original author(s)	François Chollet
Developer(s)	various
Initial release	27 March 2015; 6 years ago
Stable release	2.4.0 <sup>[1]</sup> / 17 June 2020; 17 months ago
Repository	<a href="https://github.com/keras-team/keras">github.com/keras-team/keras</a> 
Written in	Python
Platform	Cross-platform
Type	Neural networks
License	MIT
Website	<a href="https://keras.io">keras.io</a> 

# Keras

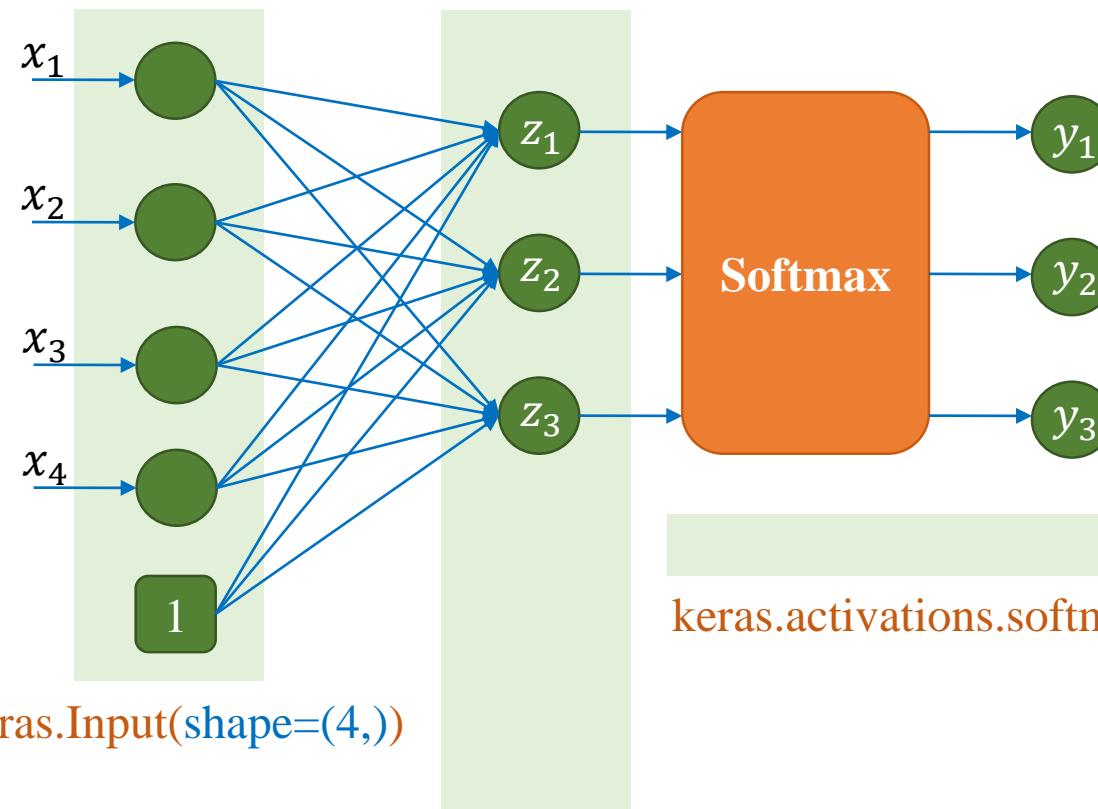
Model



`keras.Input(shape=(3,))`

`keras.layers.Dense(units=1)`

Model

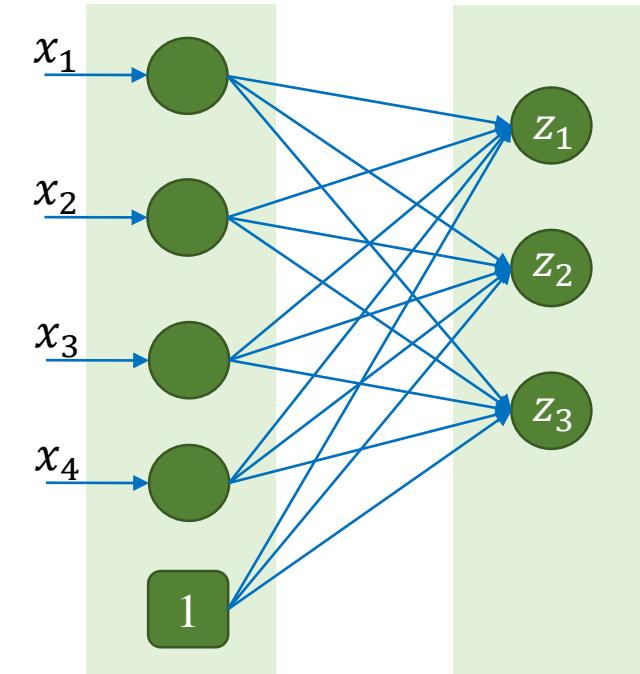
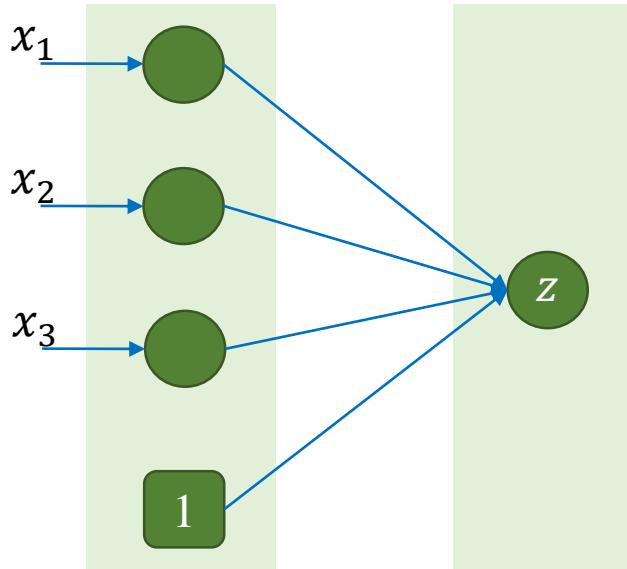
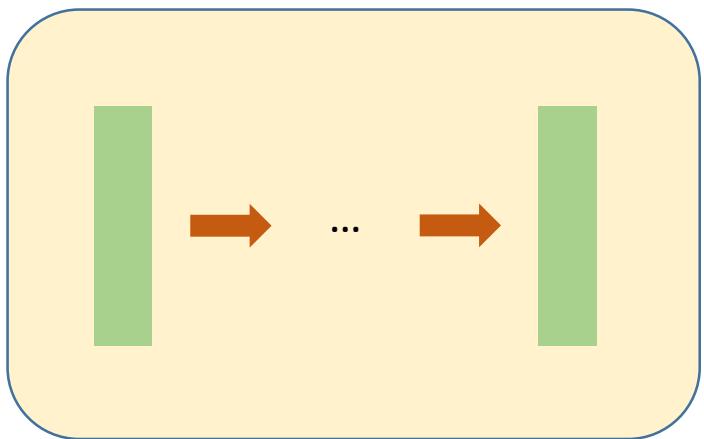


`keras.Input(shape=(4,))`

`keras.layers.Dense(units=3)`

# Keras

## Model



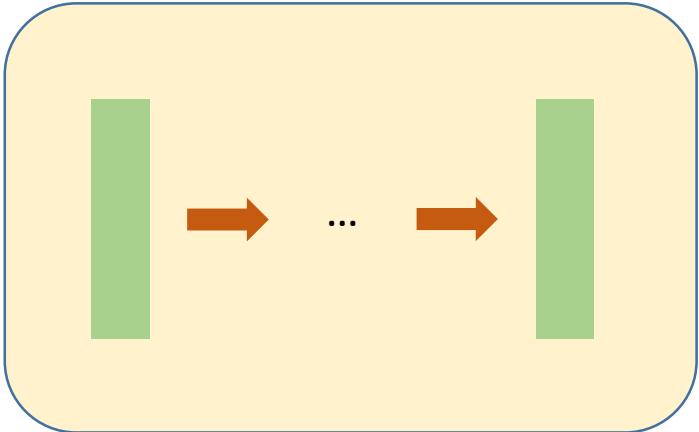
keras.Sequential()

```
1 import numpy as np
2 import tensorflow as tf
3 import tensorflow.keras as keras
4
5 # create model
6 model = keras.Sequential()
7 model.add(keras.Input(shape=(3,)))
8 model.add(keras.layers.Dense(1))
```

```
1 import numpy as np
2 import tensorflow as tf
3 import tensorflow.keras as keras
4
5 # create model
6 model = keras.Sequential()
7 model.add(keras.Input(shape=(4,)))
8 model.add(keras.layers.Dense(3))
```

# Keras

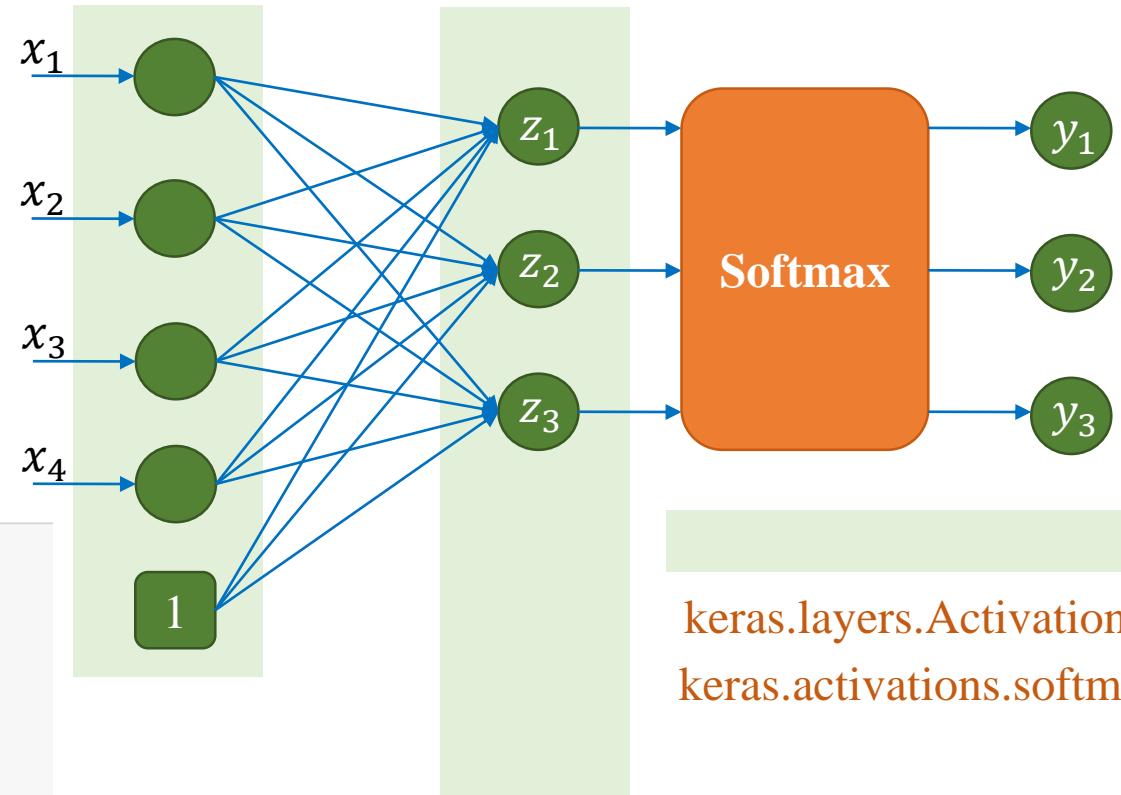
## Model



keras.Sequential()

```
1 import numpy as np
2 import tensorflow as tf
3 import tensorflow.keras as keras
4
5 # create model
6 model = keras.Sequential()
7 model.add(keras.Input(shape=(4,)))
8 model.add(keras.layers.Dense(3))
9 model.add(keras.layers.Activation(keras.activations.softmax))
```

keras.Input(shape=(4,))



keras.layers.Activation()  
keras.activations.softmax

keras.layers.Dense(units=3)

# Outline

- Introduction to Tensorflow
- Introduction to Tensorflow.Keras
- Model Construction
- Model Training and Inference
- Applying Softmax for Image Data

# Model Construction

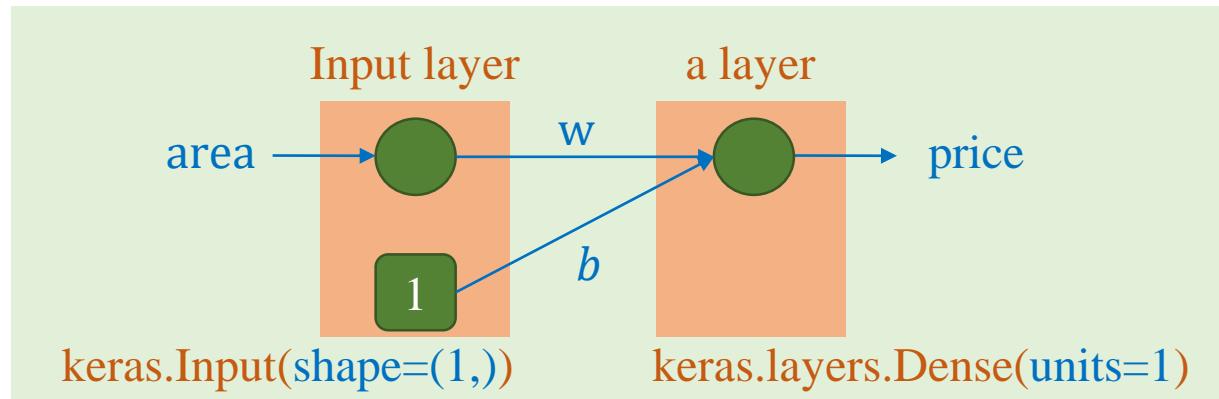
## ❖ Linear regression

Feature	Label
area	price
6.7	9.1
4.6	5.9
3.5	4.6
5.5	6.7

House price data

### Model

$$\text{price} = w * \text{area} + b$$
$$y = wx + b$$



```
1 import tensorflow as tf
2 import tensorflow.keras as keras
3
4 # create model
5 model = keras.Sequential()
6 model.add(keras.Input(shape=(1,)))
7 model.add(keras.layers.Dense(1))
8
9 model.summary()
```

Model: "sequential"

Layer (type)	Output Shape	Param #
dense (Dense)	(None, 1)	2

Total params: 2  
Trainable params: 2  
Non-trainable params: 0

# Model Construction

## ❖ Linear regression

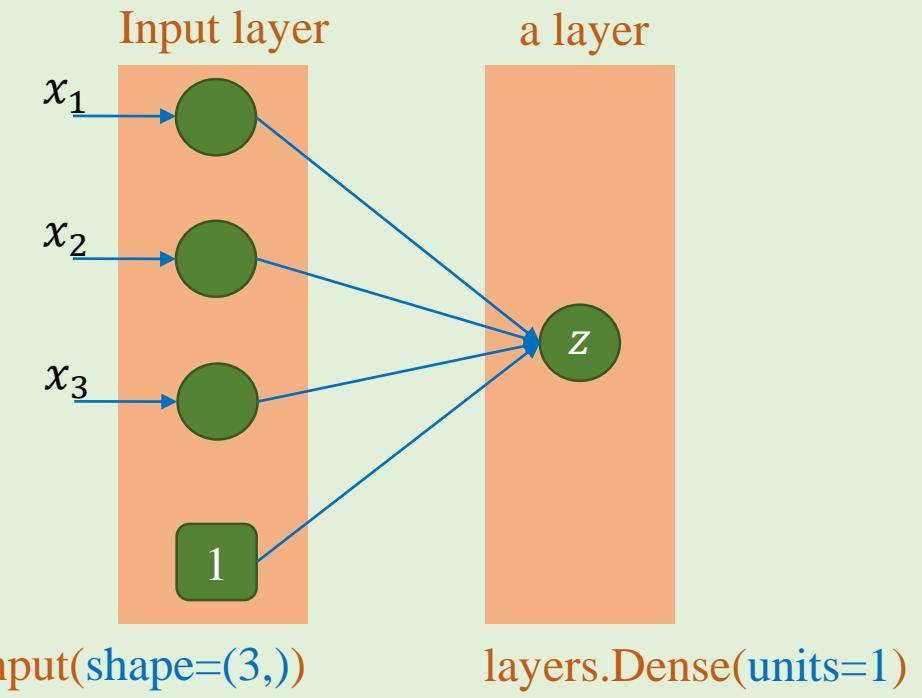
Features			Label
TV	Radio	Newspaper	Sales
230.1	37.8	69.2	22.1
44.5	39.3	45.1	10.4
17.2	45.9	69.3	12
151.5	41.3	58.5	16.5
180.8	10.8	58.4	17.9

Advertising-based sale data

## Model

$$\text{Sale} = w_1 * TV + w_2 * Radio + w_3 * Newspaper + b$$

$$y = w_1x_1 + w_2x_2 + w_3x_3 + b$$



```

1 import tensorflow as tf
2 import tensorflow.keras as keras
3
4 # create model
5 model = keras.Sequential()
6 model.add(keras.Input(shape=(3,)))
7 model.add(keras.layers.Dense(1))
8
9 model.summary()

```

# Model Construction

## ❖ Linear regression

Boston House  
Price Data

	Features														Label
	crim	zn	indus	chas	nox	rm	age	dis	rad	tax	ptratio	black	lstat	medv	
	0.00632	18	2.31	0	0.538	6.575	65.2	4.09	1	296	15.3	396.9	4.98	24	
	0.02731	0	7.07	0	0.469	6.421	78.9	4.9671	2	242	17.8	396.9	9.14	21.6	
	0.03237	0	2.18	0	0.458	6.998	45.8	6.0622	3	222	18.7	394.63	2.94	33.4	
	0.06905	0	2.18	0	0.458	7.147	54.2	6.0622	3	222	18.7	396.9	5.33	36.2	
	0.08829	12.5	7.87	0	0.524	6.012	66.6	5.5605	5	311	15.2	395.6	12.43	22.9	

### Model

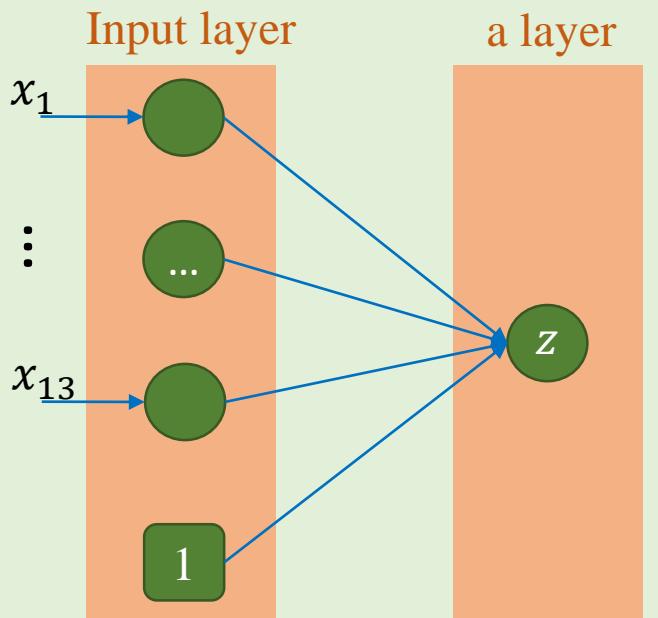
$$\text{medv} = w_1 * x_1 + \dots + w_{13} * x_{13} + b$$

# Model Construction

## ❖ Linear regression

### Model

$$\text{medv} = w_1 * x_1 + \dots + w_{13} * x_{13} + b$$



```
1 import tensorflow as tf
2 import tensorflow.keras as keras
3
4 # create model
5 model = keras.Sequential()
6 model.add(keras.Input(shape=(13,)))
7 model.add(keras.layers.Dense(1))
8
9 model.summary()
```

Model: "sequential\_1"

Layer (type)	Output Shape	Param #
dense_1 (Dense)	(None, 1)	14
Total params:	14	
Trainable params:	14	
Non-trainable params:	0	

# Model Construction

## Feature    Label

Petal_Length	Category
1.4	0
1	0
1.5	0
3	1
3.8	1
4.1	1

## Model

$$z = wx + b$$

$$\hat{y} = \frac{1}{1 + e^{-z}}$$

## ❖ Logistic regression

```

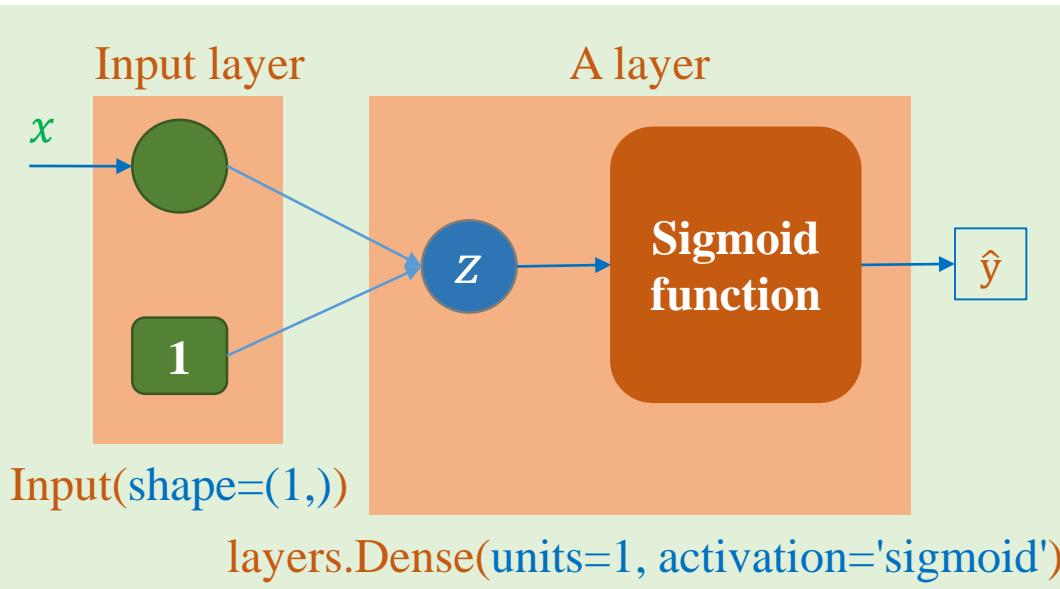
1 import tensorflow as tf
2 import tensorflow.keras as keras
3
4 # create model
5 model = keras.Sequential()
6 model.add(keras.Input(shape=(1,)))
7 model.add(keras.layers.Dense(1, activation='sigmoid'))
8
9 model.summary()

```

Model: "sequential"

Layer (type)	Output Shape	Param #
dense (Dense)	(None, 1)	2

Total params: 2  
Trainable params: 2  
Non-trainable params: 0



# Model Construction

## Feature      Label

Petal_Length	Petal_Width	Label
1.5	0.2	0
1.4	0.2	0
1.6	0.2	0
4.7	1.6	1
3.3	1.1	1
4.6	1.3	1

## Model

$$z = \theta^T x$$

$$\hat{y} = \frac{1}{1 + e^{-z}}$$

## ❖ Logistic regression

```

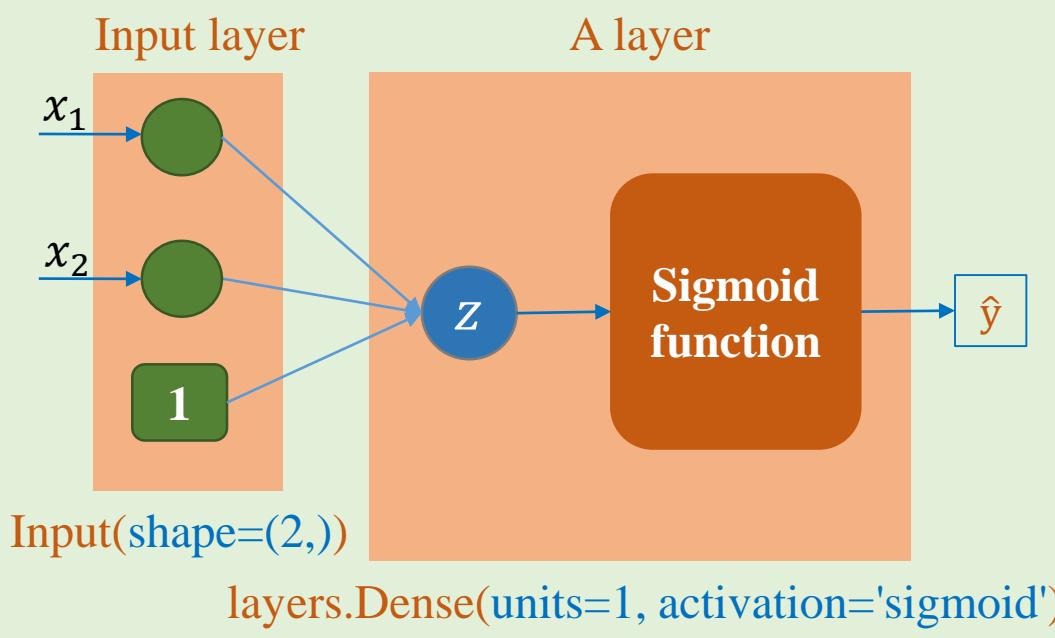
1 import tensorflow as tf
2 import tensorflow.keras as keras
3
4 # create model
5 model = keras.Sequential()
6 model.add(keras.Input(shape=(2,)))
7 model.add(keras.layers.Dense(1, activation='sigmoid'))
8
9 model.summary()

```

Model: "sequential"

Layer (type)	Output Shape	Param #
dense (Dense)	(None, 1)	3

Total params: 3  
Trainable params: 3  
Non-trainable params: 0



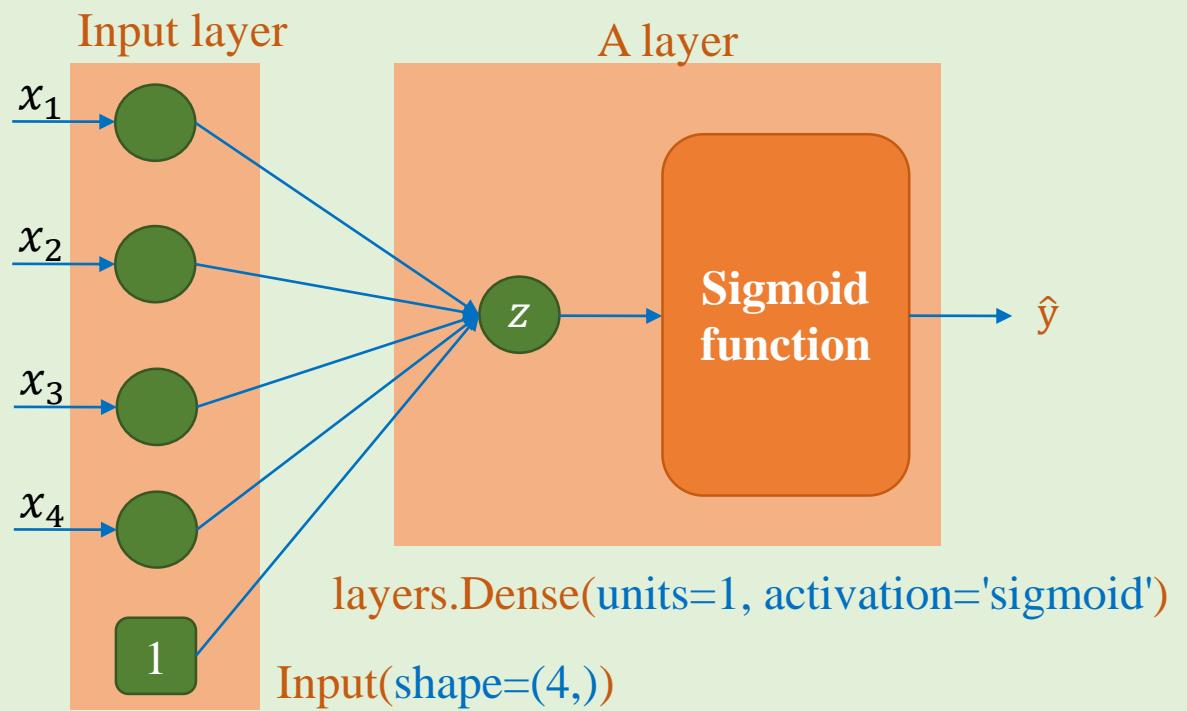
# Model Construction

Feature				Label
Sepal_Length	Sepal_Width	Petal_Length	Petal_Width	Label
5.2	3.5	1.5	0.2	0
5.2	3.4	1.4	0.2	0
4.7	3.2	1.6	0.2	0
6.3	3.3	4.7	1.6	1
4.9	2.4	3.3	1.1	1
6.6	2.9	4.6	1.3	1

Model

$$z = \theta^T x$$

$$\hat{y} = \frac{1}{1 + e^{-z}}$$



## ❖ Logistic regression

```

1 import tensorflow as tf
2 import tensorflow.keras as keras
3
4 # create model
5 model = keras.Sequential()
6 model.add(keras.Input(shape=(4,)))
7 model.add(keras.layers.Dense(1, activation='sigmoid'))
8
9 model.summary()

```

Model: "sequential"

Layer (type)	Output Shape	Params
dense (Dense)	(None, 1)	5
Total params:	5	
Trainable params:	5	
Non-trainable params:	0	

# Model Construction

## Feature Label

Petal_Length	Label
1.4	1
1.3	1
1.5	1
4.5	2
4.1	2
4.6	2

Iris Classification Data

$$z_1 = xw_1 + b_1$$

$$z_2 = xw_2 + b_2$$

$$\hat{y}_1 = \frac{e^{z_1}}{\sum_{j=1}^2 e^{z_j}}$$

$$\hat{y}_2 = \frac{e^{z_2}}{\sum_{j=1}^2 e^{z_j}}$$

## ❖ Softmax regression

```

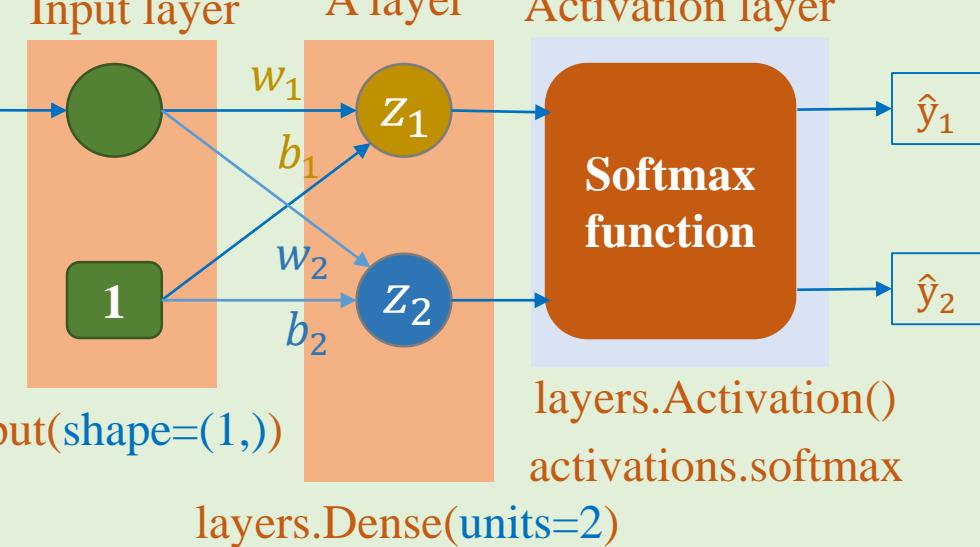
1 import tensorflow as tf
2 import tensorflow.keras as keras
3
4 # create model
5 model = keras.Sequential()
6 model.add(keras.Input(shape=(1,)))
7 model.add(keras.layers.Dense(2))
8 model.add(keras.layers.Activation(keras.activations.softmax))
9
10 model.summary()

```

Model: "sequential"

Layer (type)	Output Shape	Param #
dense (Dense)	(None, 2)	4
activation (Activation)	(None, 2)	0

Total params: 4  
Trainable params: 4  
Non-trainable params: 0



# Model Construction

## Feature Label

Petal_Length	Label
1.4	1
1.3	1
1.5	1
4.5	2
4.1	2
4.6	2

Iris Classification Data

$$z_1 = xw_1 + b_1$$

$$z_2 = xw_2 + b_2$$

$$\hat{y}_1 = \frac{e^{z_1}}{\sum_{j=1}^2 e^{z_j}}$$

$$\hat{y}_2 = \frac{e^{z_2}}{\sum_{j=1}^2 e^{z_j}}$$

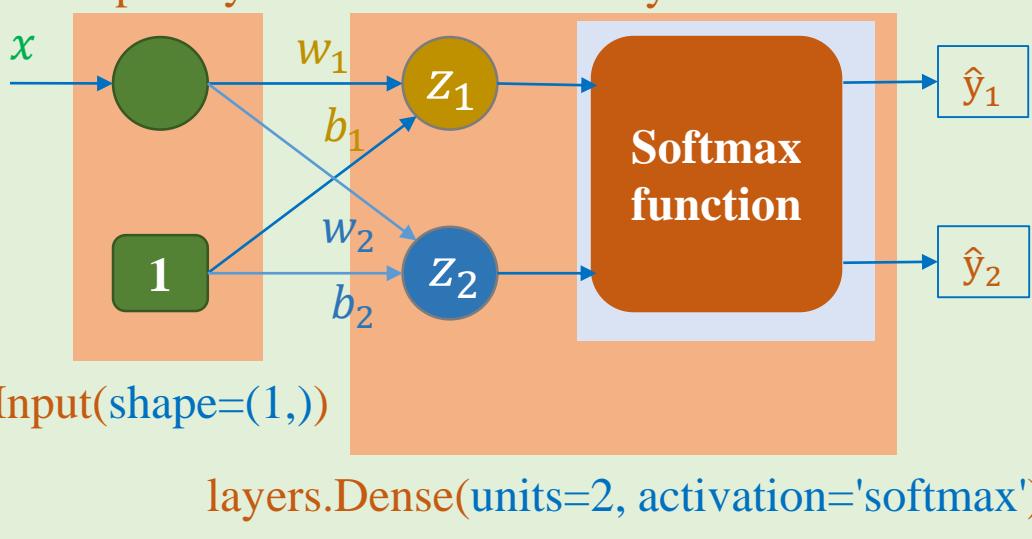
## ❖ Softmax regression

```

1 import tensorflow as tf
2 import tensorflow.keras as keras
3
4 # create model
5 model = keras.Sequential()
6 model.add(keras.Input(shape=(1,)))
7 model.add(keras.layers.Dense(2, activation='softmax'))
8
9 model.summary()

```

## Input layer



## A layer

Model: "sequential"

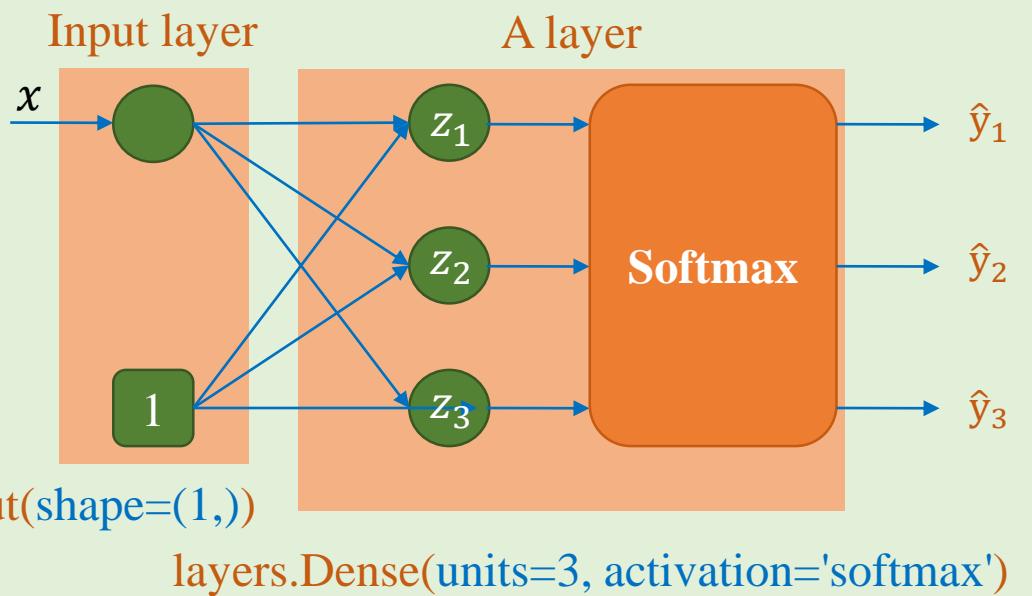
Layer (type)	Output Shape	Param #
dense (Dense)	(None, 2)	4

Total params: 4  
Trainable params: 4  
Non-trainable params: 0

# Model Construction

## ❖ Softmax regression

Petal_Length	Label
1.4	1
1.3	1
1.5	1
4.5	2
4.1	2
4.6	2
5.2	3
5.6	3
5.9	3



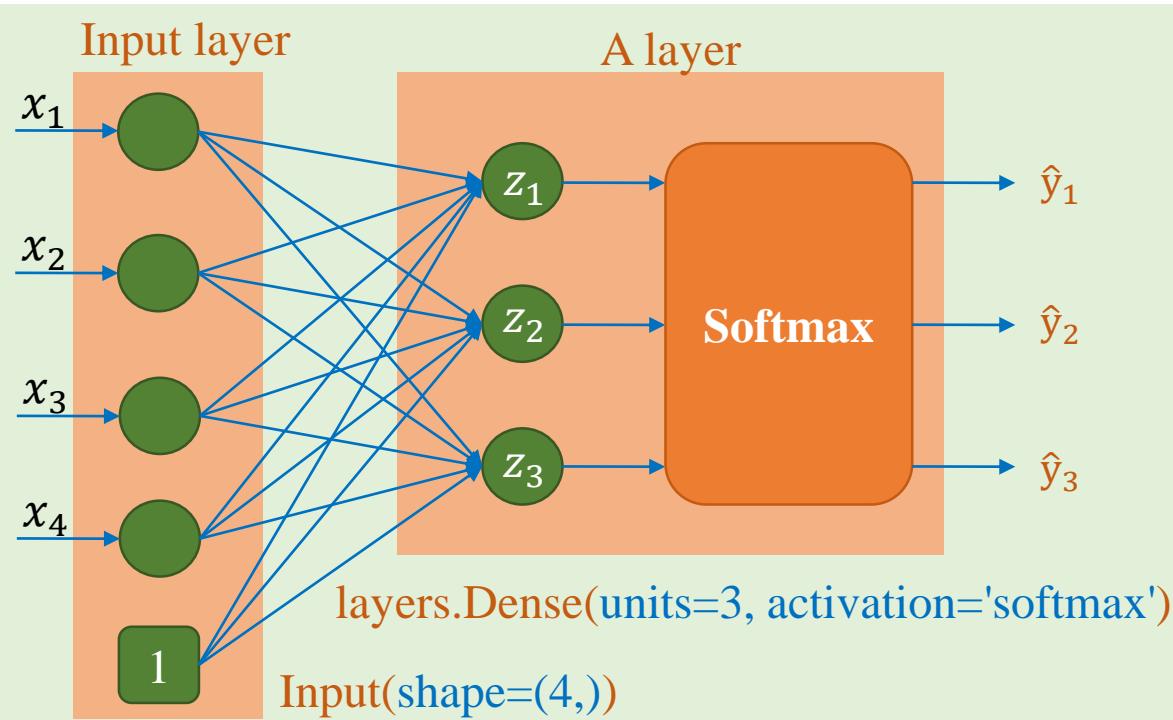
```
1 import tensorflow as tf  
2 import tensorflow.keras as keras  
3  
4 # create model  
5 model = keras.Sequential()  
6 model.add(keras.Input(shape=(1,)))  
7 model.add(keras.layers.Dense(3, activation='softmax'))  
8  
9 model.summary()
```

Model: "sequential"

Layer (type)	Output Shape	Param #
dense (Dense)	(None, 3)	6
Total params:	6	
Trainable params:	6	
Non-trainable params:	0	

# Model Construction

Sepal_Length	Sepal_Width	Petal_Length	Petal_Width	Label
5.2	3.5	1.5	0.2	1
5.2	3.4	1.4	0.2	1
4.7	3.2	1.6	0.2	1
6.3	3.3	4.7	1.6	2
4.9	2.4	3.3	1.1	2
6.6	2.9	4.6	1.3	2
6.4	2.8	5.6	2.2	3
6.3	2.8	5.1	1.5	3
6.1	2.6	5.6	1.4	3



## ❖ Softmax regression

### Forward computation

$$\mathbf{z} = \boldsymbol{\theta}^T \mathbf{x} \quad \hat{\mathbf{y}} = \frac{e^{\mathbf{z}}}{\sum_{i=1}^k e^{z_i}}$$

```
1 import tensorflow as tf
2 import tensorflow.keras as keras
3
4 # create model
5 model = keras.Sequential()
6 model.add(keras.Input(shape=(4,)))
7 model.add(keras.layers.Dense(3, activation='softmax'))
8
9 model.summary()
```

Model: "sequential"

Layer (type)	Output Shape	Param #
dense (Dense)	(None, 3)	15
Total params:	15	
Trainable params:	15	
Non-trainable params:	0	

# Outline

- Introduction to Tensorflow
- Introduction to Tensorflow.Keras
- Model Construction
- Model Training and Inference
- Applying Softmax for Image Data

# Training

## ❖ Logistic regression

→ Tính output  $\hat{y}$

$$\begin{aligned} z &= \theta^T x \\ \hat{y} &= \sigma(z) = \frac{1}{1 + e^{-z}} \end{aligned}$$

→ Tính loss (binary cross-entropy)

$$L(\theta) = (-\mathbf{y}^T \log \hat{\mathbf{y}} - (1-\mathbf{y})^T \log(1-\hat{\mathbf{y}}))$$

→ Tính đạo hàm

$$L'_{\theta} = \mathbf{x}^T (\hat{\mathbf{y}} - \mathbf{y})$$

→ Cập nhật tham số (Stochastic gradient descent)

$$\theta = \theta - \eta L'_{\theta}$$

Computed automatically

Declare optimizer and loss function

```
model.compile(optimizer='sgd',
               loss='binary_crossentropy')
```

Start training

```
model.fit(x-data, y-data, batch-size, epochs)
```

If batch-size=1 → Stochastic training

If batch-size=N → Batch training

If 1<batch-size<N → Mini-batch training

# Training

## ❖ Softmax regression

→ Tính output  $\hat{y}$

$$\mathbf{z} = \boldsymbol{\theta}^T \mathbf{x} \quad \hat{y} = \frac{e^{\mathbf{z}}}{\sum_{i=1}^k e^{z_i}}$$

→ Tính loss (cross-entropy)

$$L(\boldsymbol{\theta}) = - \sum_{i=1}^k y_i \log \hat{y}_i$$

→ Tính đạo hàm

$$\frac{\partial L}{\partial \boldsymbol{\theta}_i} = \mathbf{x} (\hat{y}_i - y_i)$$

→ Cập nhật tham số (Stochastic gradient descent)

$$\boldsymbol{\theta} = \boldsymbol{\theta} - \eta L'_{\boldsymbol{\theta}}$$

Computed automatically

**Declare optimizer and loss function**

```
model.compile(optimizer='sgd',
               loss='categorical_crossentropy')
```

**Start training**

```
model.fit(x-data, y-data, batch-size, epochs)
```

If batch-size=1 → Stochastic training

If batch-size=m → Batch training

If 1<batch-size<m → Mini-batch training

# Training

## ❖ Linear regression

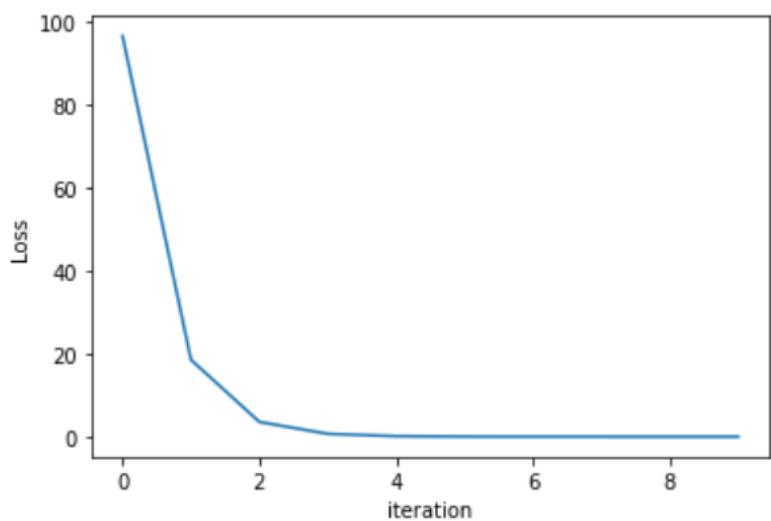
Feature      Label

area	price
6.7	9.1
4.6	5.9
3.5	4.6
5.5	6.7

Model

$$\begin{aligned} \text{price} &= w * \text{area} + b \\ y &= wx + b \end{aligned}$$

House price data



```

1 import numpy as np
2 import tensorflow as tf
3 import tensorflow.keras as keras
4
5 batch_size = 4
6 epochs = 10
7
8 # Data Preparation
9 data = np.genfromtxt('data.csv', delimiter=',')
10 X = data[:,0:1]
11 y = data[:,1:]
12
13 # create model
14 model = tf.keras.Sequential(
15     [tf.keras.layers.Dense(units=1, input_shape=[1])])
16
17 # declare optimization method and loss function
18 opt = keras.optimizers.SGD(learning_rate=0.01)
19 model.compile(optimizer=opt, loss='mse')
20
21 # training
22 history = model.fit(X, y, batch_size, epochs)

```

Train on 4 samples  
Epoch 1/10  
4/4 [=====] - 0s 28ms/sample - loss: 96.6016  
Epoch 2/10  
4/4 [=====] - 0s 247us/sample - loss: 18.6414  
Epoch 3/10  
4/4 [=====] - 0s 499us/sample - loss: 3.6692  
Epoch 4/10  
4/4 [=====] - 0s 245us/sample - loss: 0.7937  
Epoch 5/10  
4/4 [=====] - 0s 499us/sample - loss: 0.2415  
Epoch 6/10  
4/4 [=====] - 0s 499us/sample - loss: 0.1353

# Training

## ❖ Logistic regression

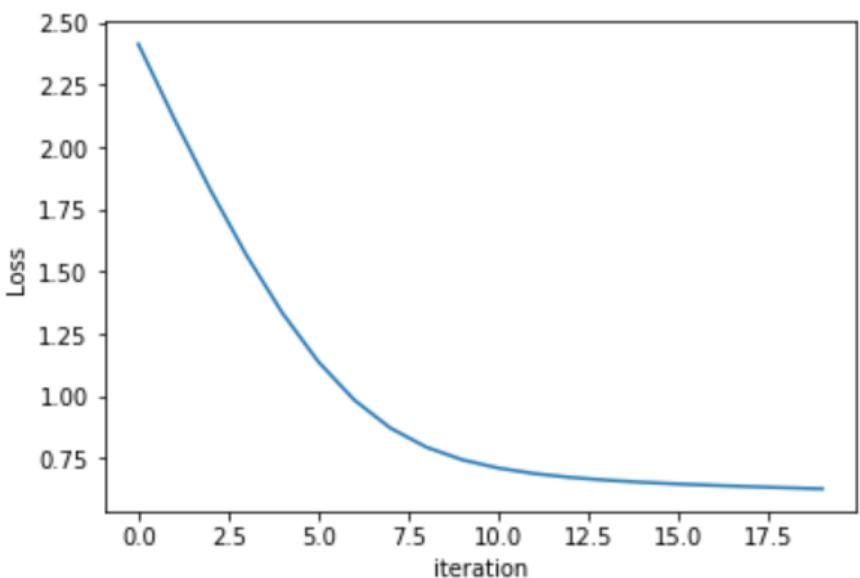
Feature    Label

Petal_Length	Category
1.4	0
1	0
1.5	0
3	1
3.8	1
4.1	1

Model

$$z = w\mathbf{x} + b$$

$$\hat{y} = \frac{1}{1 + e^{-z}}$$



```

1 import numpy as np
2 import tensorflow as tf
3 import tensorflow.keras as keras
4
5 batch_size = 6
6 epochs = 20
7
8 # Data Preparation
9 data = np.genfromtxt('iris_1D.csv', delimiter=',', skip_header=1)
10 X = data[:,0:1]
11 y = data[:,1]
12
13 # create model
14 model = tf.keras.Sequential(
15     [tf.keras.layers.Dense(units=1, activation='sigmoid', input_shape=[1])])
16
17 # declare optimization method and loss function
18 opt = keras.optimizers.SGD(learning_rate=0.1)
19 model.compile(optimizer=opt, loss='binary_crossentropy')
20
21 # training
22 history = model.fit(X, y, batch_size, epochs)

```

Train on 6 samples  
Epoch 1/20  
6/6 [=====] - 0s 20ms/sample - loss: 2.4125  
Epoch 2/20  
6/6 [=====] - 0s 339us/sample - loss: 2.1118  
Epoch 3/20  
6/6 [=====] - 0s 326us/sample - loss: 1.8278  
Epoch 4/20  
6/6 [=====] - 0s 161us/sample - loss: 1.5661  
Epoch 5/20  
6/6 [=====] - 0s 333us/sample - loss: 1.3337  
Epoch 6/20  
6/6 [=====] - 0s 166us/sample - loss: 1.1381  
Epoch 7/20  
6/6 [=====] - 0s 160us/sample - loss: 0.9842

# Training

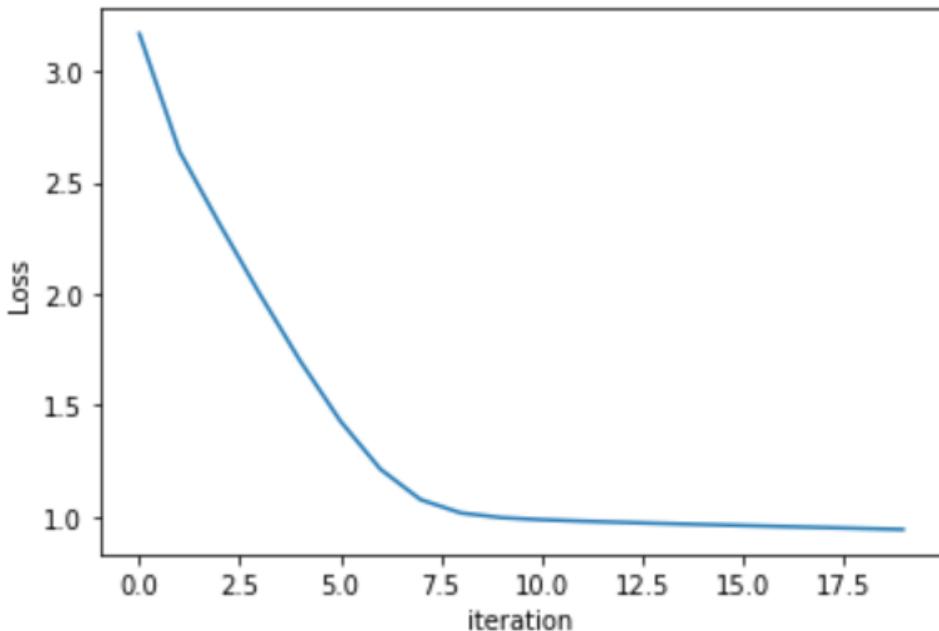
Petal_Length	Label
1.4	1
1.3	1
1.5	1
4.5	2
4.1	2
4.6	2
5.2	3
5.6	3
5.9	3

## ❖ Softmax regression

Model

$$\mathbf{z} = \boldsymbol{\theta}^T \mathbf{x}$$

$$\hat{\mathbf{y}} = \frac{e^{\mathbf{z}}}{\sum_{i=1}^k e^{z_i}}$$



```

1 import numpy as np
2 import tensorflow as tf
3 import tensorflow.keras as keras
4
5 batch_size = 9
6 epochs = 20
7
8 # Data Preparation
9 data = np.genfromtxt('iris_1D_3c.csv', delimiter=',', skip_header=1)
10 x = data[:,0:1]
11 y = data[:,1]
12
13 # create model
14 model = tf.keras.Sequential(
15     [tf.keras.layers.Dense(units=3, activation='softmax', input_shape=[1])])
16
17 # declare optimization method and loss function
18 opt = keras.optimizers.SGD(learning_rate=0.1)
19 model.compile(optimizer=opt, loss='sparse_categorical_crossentropy')
20
21 # training
22 history = model.fit(x, y, batch_size, epochs)

```

Train on 9 samples

Epoch 1/20  
9/9 [=====] - 0s 19ms/sample - loss: 3.1676  
Epoch 2/20  
9/9 [=====] - 0s 221us/sample - loss: 2.6389  
Epoch 3/20  
9/9 [=====] - 0s 110us/sample - loss: 2.3121  
Epoch 4/20  
9/9 [=====] - 0s 221us/sample - loss: 1.9978  
Epoch 5/20  
9/9 [=====] - 0s 111us/sample - loss: 1.6993  
Epoch 6/20  
9/9 [=====] - 0s 220us/sample - loss: 1.4296  
Epoch 7/20  
9/9 [=====] - 0s 222us/sample - loss: 1.2127  
Epoch 8/20  
9/9 [=====] - 0s 221us/sample - loss: 1.0761  
Epoch 9/20  
9/9 [=====] - 0s 222us/sample - loss: 1.0165  
Epoch 10/20  
9/9 [=====] - 0s 222us/sample - loss: 0.9956

# Compile Function

Configures the model for training

```
compile(  
    optimizer='rmsprop',  
    loss=None,  
    metrics=None,  
    loss_weights=None,  
    weighted_metrics=None,  
    run_eagerly=None,  
    steps_per_execution=None  
)
```

```
1 # metrics  
2  
3 # compile  
4 model.compile(optimizer='sgd',  
5                 loss='sparse_categorical_crossentropy',  
6                 metrics=[keras.metrics.SparseCategoricalAccuracy()])  
7  
8 # training  
9 batch_size = 32  
10 epochs = 5  
11 history = model.fit(x, y, batch_size,  
12                       epochs=epochs, verbose=2)
```

```
Epoch 1/5  
5/5 - 0s - loss: 0.4602 - sparse_categorical_accuracy: 0.9467 - 373ms/epoch - 75ms/step  
Epoch 2/5  
5/5 - 0s - loss: 0.4608 - sparse_categorical_accuracy: 0.8133 - 9ms/epoch - 2ms/step
```

# Evaluate Function

Returns the loss value & metrics values for the model in test mode

evaluate(  
x=None,  
y=None,  
batch\_size=None,  
verbose=1,  
)

```
1 # compile
2 model.compile(optimizer='sgd',
3                 loss='sparse_categorical_crossentropy',
4                 metrics=[keras.metrics.SparseCategoricalAccuracy()])
5
6 # training
7 batch_size = 32
8 epochs = 500
9 history = model.fit(x_train, y_train, batch_size,
10                      validation_data=(x_val, y_val),
11                      epochs=epochs, verbose=0)
12
13 model.evaluate(x_val, y_val, batch_size, verbose=2)
```

1/1 - 0s - loss: 0.2789 - sparse\_categorical\_accuracy: 0.9333 - 29ms/epoch  
[0.2789105176925659, 0.9333333373069763]

# Fit Function

```
# training
batch_size = 32
epochs = 500
history = model.fit(x, y, batch_size, epochs)
```

fit(  
x=None,  
y=None,  
batch\_size=None,  
epochs=1,  
verbose='auto',  
callbacks=None,  
validation\_split=0.0,  
validation\_data=None,  
shuffle=True,  
class\_weight=None,  
sample\_weight=None,  
initial\_epoch=0,  
steps\_per\_epoch=None,  
validation\_steps=None,  
validation\_batch\_size=None,  
validation\_freq=1,  
max\_queue\_size=10,  
workers=1,  
use\_multiprocessing=False  
)

# Fit Function

```
1 # compile
2 model.compile(optimizer='sgd',
3                 loss='sparse_categorical_crossentropy')
4
5 # training
6 batch_size = 32
7 epochs = 10
8 history = model.fit(X, y, batch_size,
9                       epochs=epochs, initial_epoch=5)
```

```
Epoch 6/10
5/5 [=====] - 0s 2ms/step - loss: 1.3554
Epoch 7/10
5/5 [=====] - 0s 1ms/step - loss: 1.1875
Epoch 8/10
5/5 [=====] - 0s 2ms/step - loss: 1.1136
Epoch 9/10
5/5 [=====] - 0s 2ms/step - loss: 1.0656
Epoch 10/10
5/5 [=====] - 0s 1ms/step - loss: 1.0340
```

fit(  
x=None,  
y=None,  
batch\_size=None,  
epochs=1,  
verbose='auto',  
callbacks=None,  
validation\_split=0.0,  
validation\_data=None,  
shuffle=True,  
class\_weight=None,  
sample\_weight=None,  
initial\_epoch=0,  
steps\_per\_epoch=None,  
validation\_steps=None,  
validation\_batch\_size=None,  
validation\_freq=1,  
max\_queue\_size=10,  
workers=1,  
use\_multiprocessing=False  
)

# Fit Function

verbose = 0	Silent
verbose = 1	Progress bar
verbose = 2	One line per epoch

```

1 # compile
2 model.compile(optimizer='sgd',
3                 loss='sparse_categorical_crossentropy')
4
5 # training
6 batch_size = 32
7 epochs = 6
8 history = model.fit(x, y, batch_size,
9                      epochs=epochs, verbose=1)

```

```

Epoch 1/6
5/5 [=====] - 0s 2ms/step - loss: 3.3299
Epoch 2/6
5/5 [=====] - 0s 2ms/step - loss: 2.2940
Epoch 3/6
5/5 [=====] - 0s 2ms/step - loss: 1.6176
Epoch 4/6
5/5 [=====] - 0s 2ms/step - loss: 1.1914
Epoch 5/6
5/5 [=====] - 0s 2ms/step - loss: 1.0308
Epoch 6/6
5/5 [=====] - 0s 1ms/step - loss: 0.9764

```

fit(  
x=None,  
y=None,  
batch\_size=None,  
epochs=1,  
verbose='auto',  
)

```

1 # compile
2 model.compile(optimizer='sgd',
3                 loss='sparse_categorical_crossentropy')
4
5 # training
6 batch_size = 32
7 epochs = 6
8 history = model.fit(X, y, batch_size,
9                      epochs=epochs, verbose=2)

```

```

Epoch 1/6
5/5 - 0s - loss: 0.8153 - 297ms/epoch - 59ms/step
Epoch 2/6
5/5 - 0s - loss: 0.7971 - 7ms/epoch - 1ms/step
Epoch 3/6
5/5 - 0s - loss: 0.7824 - 7ms/epoch - 1ms/step
Epoch 4/6
5/5 - 0s - loss: 0.7672 - 11ms/epoch - 2ms/step
Epoch 5/6
5/5 - 0s - loss: 0.7551 - 11ms/epoch - 2ms/step
Epoch 6/6
5/5 - 0s - loss: 0.7447 - 6ms/epoch - 1ms/step

```

# Fit Function

```
1 # compile
2 model.compile(optimizer='sgd',
3                 loss='sparse_categorical_crossentropy')
4
5 # training
6 batch_size = 32
7 epochs = 6
8 history = model.fit(X, y, batch_size,
9                       epochs=epochs, verbose=2,
10                      validation_split=0.2)
```

```
Epoch 1/6
4/4 - 1s - loss: 0.8714 - val_loss: 0.7968 - 521ms/epoch - 130ms/step
Epoch 2/6
4/4 - 0s - loss: 0.8324 - val_loss: 0.8786 - 40ms/epoch - 10ms/step
Epoch 3/6
4/4 - 0s - loss: 0.8058 - val_loss: 0.9249 - 53ms/epoch - 13ms/step
Epoch 4/6
4/4 - 0s - loss: 0.7857 - val_loss: 0.9224 - 48ms/epoch - 12ms/step
Epoch 5/6
4/4 - 0s - loss: 0.7647 - val_loss: 0.9255 - 48ms/epoch - 12ms/step
Epoch 6/6
4/4 - 0s - loss: 0.7473 - val_loss: 0.9454 - 48ms/epoch - 12ms/step
```

fit(  
x=None,  
y=None,  
batch\_size=None,  
epochs=1,  
verbose='auto',  
callbacks=None,  
validation\_split=0.0,  
validation\_data=None,  
shuffle=True,  
class\_weight=None,  
sample\_weight=None,  
initial\_epoch=0,  
steps\_per\_epoch=None,  
validation\_steps=None,  
validation\_batch\_size=None,  
validation\_freq=1,  
max\_queue\_size=10,  
workers=1,  
use\_multiprocessing=False  
)

# Fit Function

```
1 import numpy as np
2
3 # Load data
4 data = np.genfromtxt('iris_full.csv',
5                      delimiter=',',
6                      skip_header=1)
7 x = data[:,0:4]
8 y = data[:,4:]
9 N = x.shape[0]
10
11 # shuffle
12 inds = np.arange(N)
13 np.random.shuffle(inds)
14
15 x = x[inds]
16 y = y[inds]
17
18 # prepare train and val data
19 N_train = 120
20 x_train = x[:N_train]
21 y_train = y[:N_train]
22
23 x_val = x[N_train:]
24 y_val = y[N_train:]
```

fit(  
    x=None,  
    y=None,  
    batch\_size=None,  
    epochs=1,  
    verbose='auto',  
    callbacks=None,  
    validation\_split=0.0,  
    validation\_data=None,  
    shuffle=True,  
    class\_weight=None,  
    sample\_weight=None,  
    initial\_epoch=0,  
    steps\_per\_epoch=None,  
    validation\_steps=None,  
    validation\_batch\_size=None,  
    validation\_freq=1,  
    max\_queue\_size=10,  
    workers=1,  
    use\_multiprocessing=False  
)

# Fit Function

```
1 # compile
2 model.compile(optimizer='sgd',
3                 loss='sparse_categorical_crossentropy')
4
5 # training
6 batch_size = 32
7 epochs = 6
8 history = model.fit(x_train, y_train, batch_size,
9                      validation_data=(x_val, y_val),
10                     epochs=epochs, verbose=2)
```

```
Epoch 1/6
4/4 - 1s - loss: 1.3266 - val_loss: 1.0424 - 512ms/epoch - 128ms/step
Epoch 2/6
4/4 - 0s - loss: 0.9921 - val_loss: 0.7892 - 36ms/epoch - 9ms/step
Epoch 3/6
4/4 - 0s - loss: 0.7719 - val_loss: 0.6777 - 41ms/epoch - 10ms/step
Epoch 4/6
4/4 - 0s - loss: 0.6949 - val_loss: 0.6468 - 41ms/epoch - 10ms/step
Epoch 5/6
4/4 - 0s - loss: 0.6648 - val_loss: 0.6351 - 42ms/epoch - 10ms/step
Epoch 6/6
4/4 - 0s - loss: 0.6501 - val_loss: 0.6252 - 40ms/epoch - 10ms/step
```

fit(  
 x=None,  
 y=None,  
 batch\_size=None,  
 epochs=1,  
 verbose='auto',  
 callbacks=None,  
 validation\_split=0.0,  
 validation\_data=None,  
 shuffle=True,  
 class\_weight=None,  
 sample\_weight=None,  
 initial\_epoch=0,  
 steps\_per\_epoch=None,  
 validation\_steps=None,  
 validation\_batch\_size=None,  
 validation\_freq=1,  
 max\_queue\_size=10,  
 workers=1,  
 use\_multiprocessing=False  
)

# Fit Function

```
1 # callbacks
2
3 # compile
4 model.compile(optimizer='sgd',
5                 loss='sparse_categorical_crossentropy')
6
7 # training
8 callbacks = [
9     keras.callbacks.ModelCheckpoint(
10         filepath="models/model_{epoch}",
11         save_best_only=True,
12         monitor="val_loss",
13         verbose=1
14     )
15 ]
16
17 batch_size = 32
18 epochs = 5
19 history = model.fit(x_train, y_train, batch_size,
20                      validation_data=(x_val, y_val),
21                      epochs=epochs, verbose=2,
22                      callbacks=callbacks)
```

fit(  
    x=None,  
    y=None,  
    batch\_size=None,  
    epochs=1,  
    verbose='auto',  
    callbacks=None,  
    validation\_split=0.0,  
    validation\_data=None,  
    shuffle=True,  
    class\_weight=None,  
    sample\_weight=None,  
    initial\_epoch=0,  
    steps\_per\_epoch=None,  
    validation\_steps=None,  
    validation\_batch\_size=None,  
    validation\_freq=1,  
    max\_queue\_size=10,  
    workers=1,  
    use\_multiprocessing=False  
)

# Predict Function

Generates output predictions  
for the input samples

predict(  
    x=None,  
    y=None,  
    batch\_size=None,  
    verbose=1,  
)

```
1 # compile
2 model.compile(optimizer='sgd',
3                 loss='sparse_categorical_crossentropy',
4                 metrics=[keras.metrics.SparseCategoricalAccuracy()])
5
6 # training
7 batch_size = 32
8 epochs = 500
9 history = model.fit(x_train, y_train, batch_size,
10                      validation_data=(x_val, y_val),
11                      epochs=epochs, verbose=0)
12
13 model.evaluate(x_val, y_val, batch_size, verbose=2)
```

```
1/1 - 0s - loss: 0.2789 - sparse_categorical_accuracy: 0.9333 - 29ms/epoch
[0.2789105176925659, 0.9333333373069763]
```

```
1 output = model.predict(x_val)
2 print(output.shape)
```

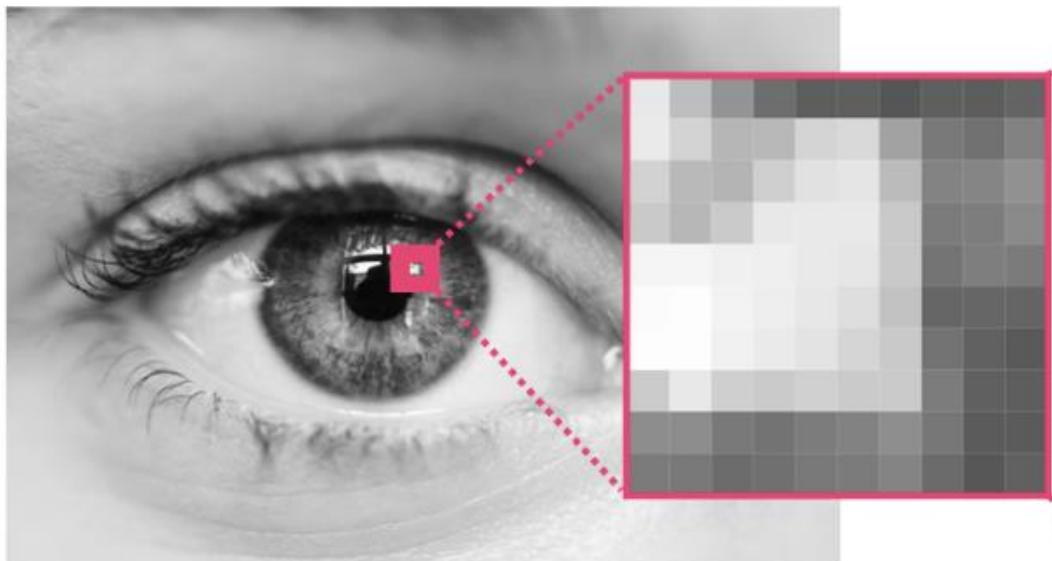
(30, 3)

# Outline

- Introduction to Tensorflow
- Introduction to Tensorflow.Keras
- Model Construction
- Model Training and Inference
- Applying Softmax for Image Data

# Image Classification: Image Data

## ❖ Grayscale images



(Height, Width)

Pixel  $p$  = scalar

$0 \leq p \leq 255$

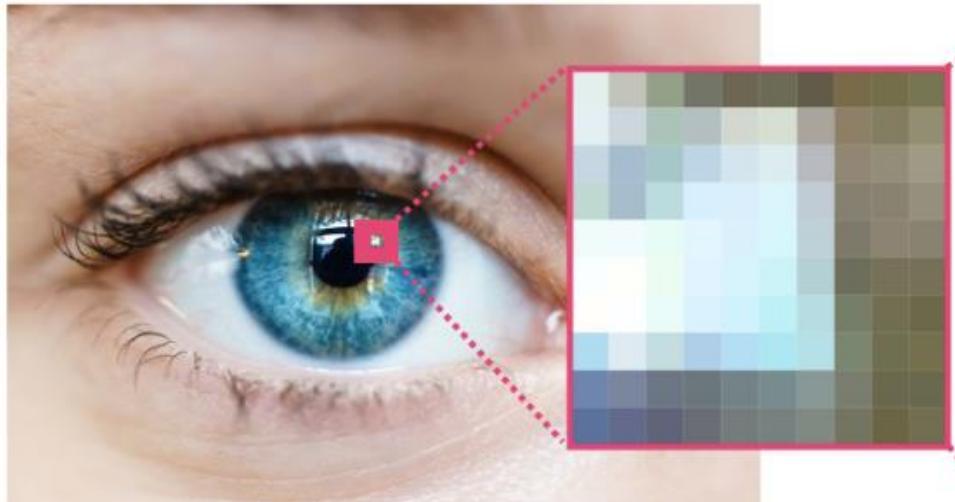
230	194	147	108	90	98	84	96	91	101
237	206	188	195	207	213	163	123	116	128
210	183	180	205	224	234	188	122	134	147
198	189	201	227	229	232	200	125	127	135
249	241	237	244	232	226	202	116	125	126
251	254	241	239	230	217	196	102	103	99
243	255	240	231	227	214	203	116	95	91
204	231	208	200	207	201	200	121	95	95
144	140	120	115	125	127	143	118	92	91
121	121	108	109	122	121	134	106	86	97

Resolution: #pixels

Resolution = Height x Width

# Image Classification: Image Data

## ❖ Color images



(Height, Width, channel)

RGB color image

$$\text{Pixel } p = \begin{bmatrix} r \\ g \\ b \end{bmatrix}$$

$$0 \leq r,g,b \leq 255$$

233	188	137	96	90	95	63	73	73	82	
237	202	159	120	105	110	88	107	112	121	109
226	191	147	110	101	112	98	123	110	119	142
221	191	176	182	203	214	169	144	133	145	131
185	160	161	184	205	223	186	137	147	161	122
181	174	189	207	206	215	194	136	142	151	140
246	237	237	231	208	206	192	122	143	144	87
254	254	241	224	199	192	181	99	122	117	133
239	248	232	207	187	182	184	110	114	110	74
193	215	193	167	158	164	181	114	112	111	74
113	119	110	111	113	123	135	120	108	106	113
93	97	91	103	107	111	122	112	104	114	105
										82
										113

Resolution: #pixels  
Resolution = Height x Width

# Important Packages

## ❖ Some functions

### To download a file

```
import urllib.request as req  
req.urlretrieve(url, name)
```

### To open an image

```
from PIL import Image  
img = Image.open(name)
```

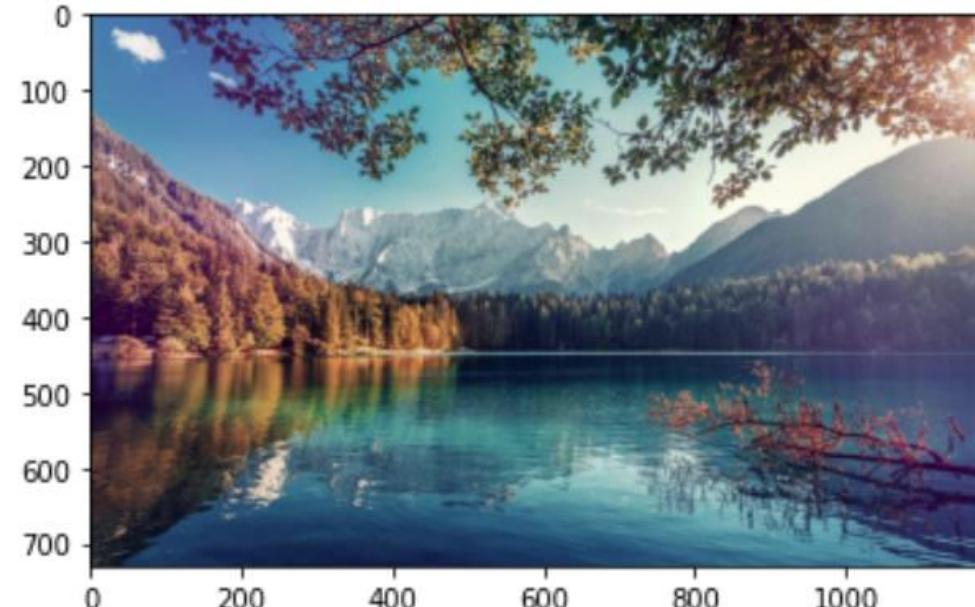
### To show an image

```
import matplotlib.pyplot as plt  
plt.imshow(img)
```

```
import urllib.request as req  
from PIL import Image  
import matplotlib.pyplot as plt  
  
# download an image  
req.urlretrieve('https://www.dropbox.com/s/zwy8ddkdm3thatr/nature.jpg?dl=1',  
                 'image.jpg')
```

```
# show the image  
img = Image.open('image.jpg')  
plt.imshow(img)
```

```
<matplotlib.image.AxesImage at 0x7f5088018b90>
```



# Image Data

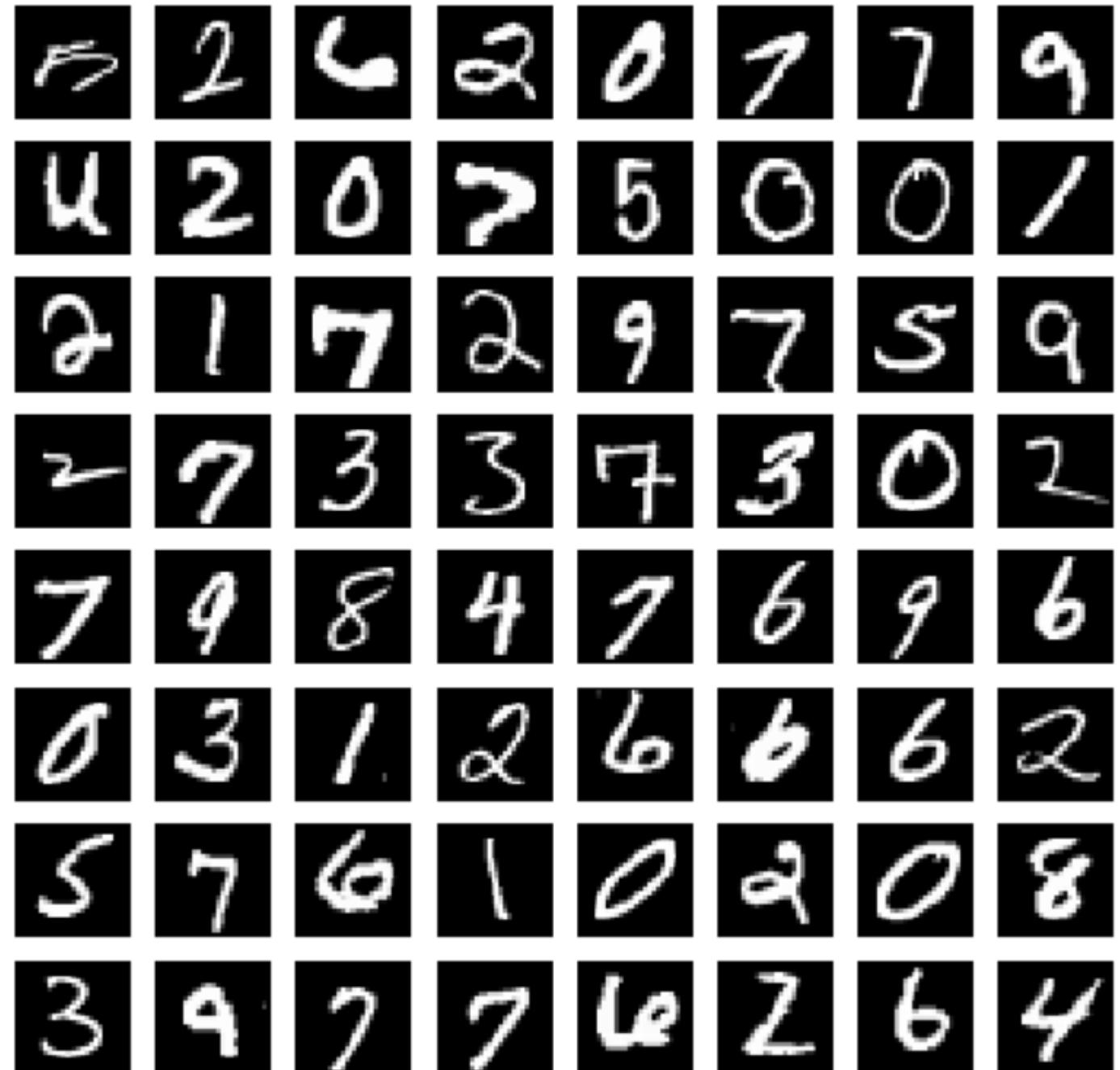
MNIST dataset

Grayscale images

Resolution=28x28

Training set: 60000 samples

Testing set: 10000 samples



# Image Data

MNIST dataset

Grayscale images

Resolution=28x28

Training set: 60000 samples

Testing set: 10000 samples

## TRAINING SET LABEL FILE (train-labels-idx1-ubyte):

[offset]	[type]	[value]	[description]
0000	32 bit integer	0x00000801(2049)	magic number (MSB first)
0004	32 bit integer	60000	number of items
0008	unsigned byte	??	label
0009	unsigned byte	??	label
.....			
xxxx	unsigned byte	??	label

The labels values are 0 to 9.

## TRAINING SET IMAGE FILE (train-images-idx3-ubyte):

[offset]	[type]	[value]	[description]
0000	32 bit integer	0x00000803(2051)	magic number
0004	32 bit integer	60000	number of images
0008	32 bit integer	28	number of rows
0012	32 bit integer	28	number of columns
0016	unsigned byte	??	pixel
0017	unsigned byte	??	pixel
.....			
xxxx	unsigned byte	??	pixel

<http://yann.lecun.com/exdb/mnist/>

# Image Data

```
1 def load_mnist():
2     mnist = {}
3     for name in filename[:2]:
4         with gzip.open(folder+name[1], 'rb') as f:
5             mnist[name[0]] = np.frombuffer(f.read(), np.uint8, offset=16).reshape(-1,28*28)
6
7     for name in filename[-2:]:
8         with gzip.open(folder+name[1], 'rb') as f:
9             mnist[name[0]] = np.frombuffer(f.read(), np.uint8, offset=8)
10
11    return mnist["training_images"], mnist["training_labels"], mnist["test_images"], mnist["test_labels"]
12
13 X_train, y_train, X_test, y_test = load_mnist()
14
15 #kiểm tra dữ liệu
16 print(X_train.shape)
17 print(y_train.shape)
18 print(X_test.shape)
19 print(y_test.shape)
```

```
(60000, 784)
(60000,)
(10000, 784)
(10000,)
```

MNIST dataset



784

# Image Data

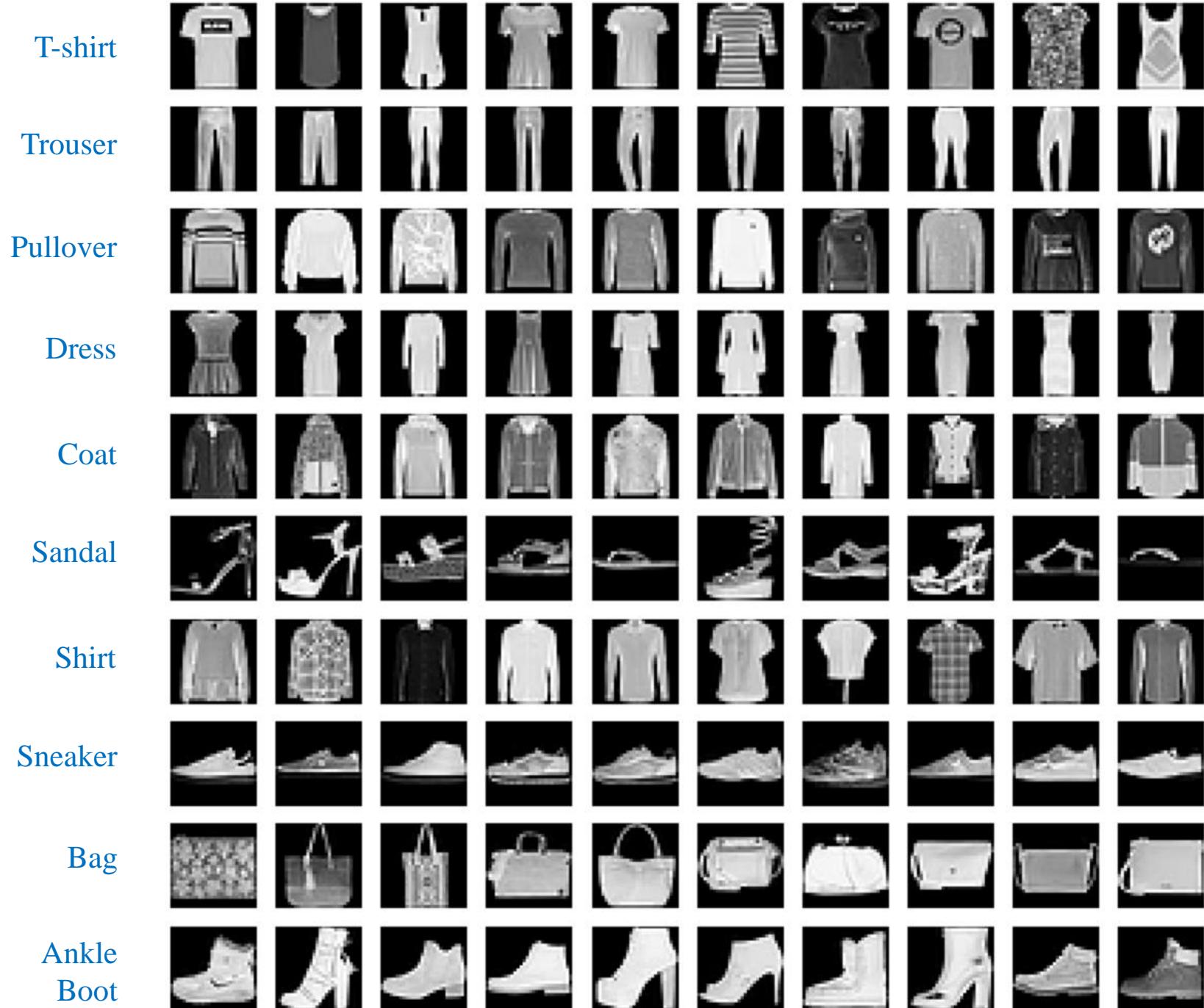
## Fashion-MNIST dataset

Grayscale images

Resolution=28x28

Training set: 60000 samples

Testing set: 10000 samples



# Image Classification

## ❖ Fashion-MNIST data

### Download data

Name	Size
t10k-images-idx3-ubyte.gz	4.4 MB
t10k-labels-idx1-ubyte.gz	5.1 kB
train-images-idx3-ubyte.gz	26.4 MB
train-labels-idx1-ubyte.gz	29.5 kB

```
1 import numpy as np
2 from urllib import request
3 import gzip
4 import pickle
5
6 filename = [["training_images","train-images-idx3-ubyte.gz"],
7             ["test_images","train-labels-idx1-ubyte.gz"],
8             ["training_labels","t10k-images-idx3-ubyte.gz"],
9             ["test_labels","t10k-labels-idx1-ubyte.gz"]]
10
11 # function to download data
12 def download_fashion_mnist(folder):
13     base_url = "http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/"
14     for name in filename:
15         print("Downloading " + name[1] + "...")
16
17         # luu vao folder data_fashion_mnist
18         request.urlretrieve(base_url + name[1], folder + name[1])
19         print("Download complete.")
20
21 # download dataset và save to folder 'data_fashion_mnist/'
22 folder = 'data_fashion_mnist/'
23 download_fashion_mnist(folder)
```

# Image Classification

## Fashion-MNIST data

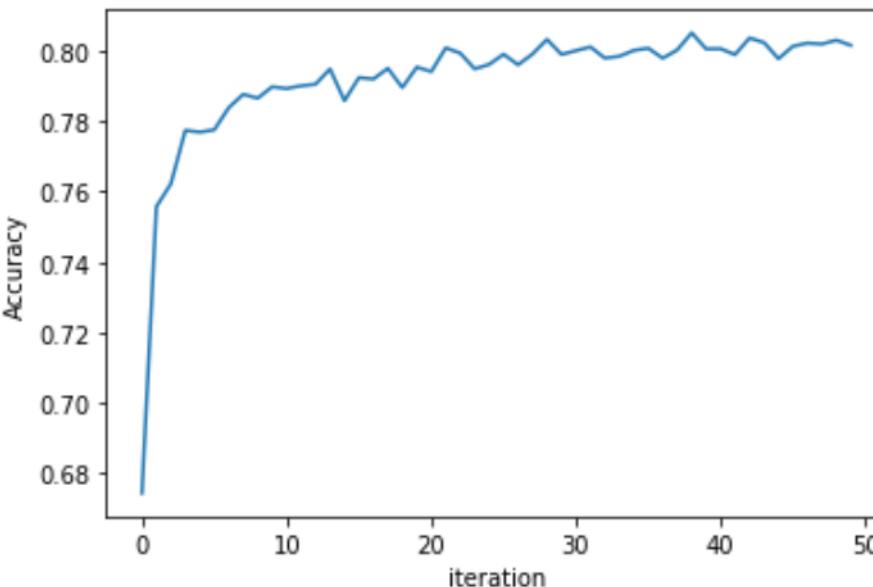
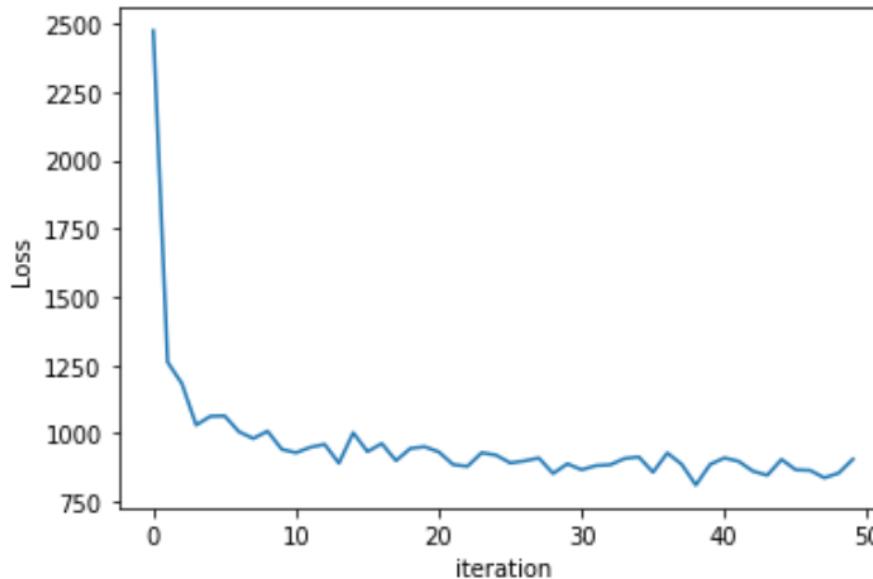
```
X_train: (60000, 784)
y_train: (60000,)
X_test: (10000, 784)
y_test: (10000,)
```



```
1 import os
2 import gzip
3 import numpy as np
4
5 def load_fashion_mnist(path, kind='train'):
6     """Load fashion_MNIST data from `path`"""
7     labels_path = os.path.join(path, '%s-labels-idx1-ubyte.gz' % kind)
8     images_path = os.path.join(path, '%s-images-idx3-ubyte.gz' % kind)
9
10    with gzip.open(labels_path, 'rb') as lbpath:
11        labels = np.frombuffer(lbpath.read(), dtype=np.uint8, offset=8)
12    with gzip.open(images_path, 'rb') as imgpath:
13        images = np.frombuffer(imgpath.read(),
14                               dtype=np.uint8, offset=16).reshape(len(labels), 784)
15
16    return images, labels
17
18
19 X_train, y_train = load_fashion_mnist('C:/Data/data_fashion_mnist/')
20 print('X_train:', X_train.shape)
21 print('y_train:', y_train.shape)
22
23 X_test, y_test = load_fashion_mnist('C:/Data/data_fashion_mnist/', kind='t10k')
24 print('X_test:', X_test.shape)
25 print('y_test:', y_test.shape)
```

Read data

# Demo



```
import tensorflow as tf
import tensorflow.keras as keras

# create model
model = keras.Sequential()
model.add(keras.Input(shape=(784,)))
model.add(keras.layers.Dense(10, activation='softmax'))
model.summary()

# optimizer and loss
model.compile(optimizer='sgd',
              loss='sparse_categorical_crossentropy',
              metrics=['accuracy'])

# training
history = model.fit(X_train, y_train, 256,
                     epochs=50, verbose=2)

# testing
test_loss, test_acc = model.evaluate(X_test, y_test)
print('Test accuracy:', test_acc)
```

# Demo

```
import tensorflow as tf
import tensorflow.keras as keras

# predict
def predict(x, w, b):
    return tf.math.softmax(tf.matmul(x, w) + b)

# weights
w = tf.Variable(tf.random.normal((784, 10),
                                 mean=0,
                                 stddev=0.01,
                                 dtype=tf.float64))
b = tf.Variable(tf.zeros((10,)),
               dtype=tf.float64)

# loss function
loss_fn = keras.losses.SparseCategoricalCrossentropy()

# training
lr = 0.01
num_epochs = 50
losses = [] # for debug

for epoch in range(num_epochs):
    with tf.GradientTape() as t:
        # output
        output = predict(X_train, w, b)

        # loss
        loss = loss_fn(y_train, output)
        losses.append(loss.numpy())

        # gradient
        dw, db = t.gradient(loss, [w, b])

        # update
        w.assign_sub(lr*dw)
        b.assign_sub(lr*db)
```

## GradientTape

# Model Saving and Loading

## Model Saving

```
1 import numpy as np
2 import tensorflow as tf
3 import tensorflow.keras as keras
4
5 batch_size = 4
6 epochs = 10
7
8 # Data Preparation
9 data = np.genfromtxt('data.csv', delimiter=',')
10 X = data[:,0:1]
11 y = data[:,1:]
12
13 # create model
14 model = tf.keras.Sequential(
15     [tf.keras.layers.Dense(units=1, input_shape=[1])])
16
17 # declare optimization method and loss function
18 opt = keras.optimizers.SGD(learning_rate=0.01)
19 model.compile(optimizer=opt, loss='mse')
20
21 # training
22 history = model.fit(X, y, batch_size, epochs)
23
24 # save entire model
25 model.save('my_model/model.h5')
```

## Model Loading

```
1 import tensorflow as tf
2 import tensorflow.keras as keras
3
4 # load model
5 model = tf.keras.models.load_model('my_model/model.h5')
6
7 # testing
8 X_testing = [[5.0]]
9 y_hat = model.predict(X_testing)
10 print(y_hat)
```

[[6.5115185]]

# Tensorflow

## ❖ Demo

```
Python 3.7.3 (default, Apr 24 2019, 15:29:51) [MSC v.1915 64 bit (AMD64)] ::  
Type "help", "copyright", "credits" or "license" for more information.  
>>>  
>>>  
>>>  
>>>  
>>>  
>>>  
>>>  
>>>  
>>> for epoch in range(n_epochs):  
...     sum_of_losses = 0  
...     gradients = np.zeros((2,1))  
...  
...     for index in range(4):  
...         xi = X_b[index:index+1]  
...         yi = y[index:index+1]
```

# Reference

## Tensor

<https://www.tensorflow.org/guide/tensor>

## TensorFlow 2 quickstart for beginners

<https://www.tensorflow.org/tutorials/quickstart/beginner>

## Save and load models

[https://www.tensorflow.org/tutorials/keras/save\\_and\\_load](https://www.tensorflow.org/tutorials/keras/save_and_load)

## Gradient tape

<https://www.tensorflow.org/guide/autodiff>

