

#### DUKE UNIVERSITY, PRATT SCHOOL OF ENGINEERING

## ME321 - Group Project 2

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Both arms BF and AE will experience compressive stress and no other stresses. The pins at C and D will experience direct shear from the platform and wall. The pins at A and B will have direct shear from the arms and the wall. The pins at E and F will experience direct shear from the arms and platform. The platform will have compressive and tensile stress on the top and bottom respectively as well as bending stress, direct shear stress, torsion, and transverse shear stress.

There will be stress concentrations at the transverse holes for the pins in the support arms, at the transverse holes in the wall connections for the pins, and at the through holes in the platform for the bolts to secure the pulley.

The pins are most likely to have the maximum stress due to loading because of their relatively small cross sectional areas compared to other components. The pins would fail at the location where the two parts they are connecting are adjacent, i.e. where the arm is flush against the wall or platform. The forces change direction at this location, which would cause a sharp change in shear and stress build up. The platform would be most likely to fail at the pin locations due to stress concentrations or at the midpoint between points E and F on the bottom side of the platform because the bending stress is maximized there. For the arms, the key locations would be the pin holes because of stress concentration.

2.

--

20.

MS DT:

Compressive stress in BF: 
$$\sigma_0 = \frac{F_{BF}}{A}$$

Pins:

Direct shear stress in Pin B: 
$$\frac{4}{8} \frac{V}{A}$$

Where  $V = \sqrt{\frac{1}{8} \frac{2}{4} + \frac{2}{8}}$ 

Force in Force in x-direction z-direction

Platform:

Max bending stress: 
$$\sigma_B = \frac{M_{max} y_{max}}{I}$$

Where  $y_{max} = \frac{h}{12}$ ,  $M_{max} = M_{oment}$  at support  $arms$ 

Direct shear stress in pin holes: 
$$\tau = \frac{V}{A}$$

where 
$$V=\sqrt{R_{x_i}^2 + R_{z_i}^2}$$
  
for each different pin

Torsion in platform: T= (F,-Fz)R~Pulley radius

Rectangular cross-section Shear in platform:

> Maximum shoar could be due to pulley or support arms, numeric analysis required

Transverse shear =  $\frac{\sqrt{Q}}{Ib}$ 

Will vary heavily in I,Q, and b based on weight reduction techniques. Shear will be based on pulley and support arm forces.

Zb.

For support arms:

Stress concentration factor is a function of  $\frac{d}{\omega}$  Bar width



where A=h(w-d)

For platform:

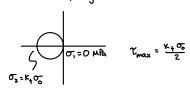
Again, stress concentration factor is a function of  $\frac{d}{w}$ 

This time we have shear stress, so  $\sigma = k_{\uparrow}, \frac{VQ}{Th}$ 

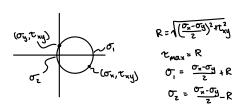
These concentrations arise at pin hole locations with support arms and wall

For support arms:

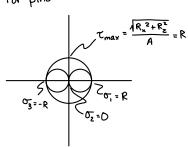
Stress is purely axial



For platform:



For pins:



Ductile materials:

From Max Shear Stress Theory:

$$T_{\text{max}} = \frac{\frac{1}{2} S_{\text{y}}}{\gamma}$$

$$N = \frac{S_{\text{y}}}{2T_{\text{max}}}$$

Distortion Energy Theory:

Brittle Materials:

$$\frac{\sigma_A}{s_{ult}} - \frac{\sigma_B}{s_{uc}} < \frac{1}{n}$$

$$\sigma_B < -\frac{s_{vc}}{s_{ul}}$$

$$\sigma' = \frac{1}{4z} \left[ (\sigma_{x} - \sigma_{y})^{2} + (\sigma_{y} - \sigma_{z})^{2} + (\sigma_{x} - \sigma_{z})^{2} + 6(\tau_{xy}^{2} + \tau_{yz}^{2} + \tau_{xz}^{2}) \right]^{1/2}$$

$$\Omega = \frac{S_{y}}{\sigma'},$$

Since Distortion Energy theorem is more conservative, we will use that safety factor.

e.

Based on the Euler buckling formula (slender arms),

$$b_{cl}^{cl} = \frac{\Gamma_s}{\mu_s EI}$$

f. For maximum deflection, use superposition for pump force and arm forces

From table A-9:

2. Cantilever with intermediate bad:

$$y_{AB} = \frac{F_{\kappa}^{2}(x-3a)}{6EI}$$

$$y_{BC} = \frac{F_{\alpha}^{2}(a-3\kappa)}{6EI}$$

$$y_{MAX} = \frac{F_{\alpha}^{2}(a-3\kappa)}{6EI}$$

For platform:  

$$y_{max} = \frac{F_{.a.}^{2}}{6EI}(a_{1}-3L) - \frac{F_{2}a_{2}^{2}}{6EI}(a_{2}-3L)$$

where F., a, belong to the pulley and Fz, az belong to the support arms

#### **Dimensions and Approximate K Values**

Component	Dimension	Loading	d/w Ratio	Approximate K
Support Arm (Bar with Hole)	W = 1 in, d = 0.25 in, l = 22 in	Axial (Compression)	0.25	2.2
Pin (Clevis Pin)	D = 0.25 in, I = 1 in	Pure Shear	N/A	1.0
Platform (Large Plate with Small Holes)	w = 12 in, d = 0.25 in, I = 18 in	Shear Around Hole	0.02	1.9

A Aluminum assumed for all muterials

Loads! 
$$T_{shaft} = \frac{\rho_{over}}{w} = \frac{2600W}{2\pi \cdot (1800/60)} = 13.85 \text{ N·m} = 10.2 \text{ At·IL}$$

$$\Delta F_{belt} = \frac{T_{shaft}}{r} = \frac{13.85}{0.127} = 109N = 24.5 \text{ IS}$$

$$F_{heriz} = \frac{13.85}{0.471} = 29.4 \text{ N} = 6.6 \text{ IS}$$

Arm Calculations: 1 in x.25 in x22 in , 6,=2.2

again assuming aluminum > E=10.106 psi

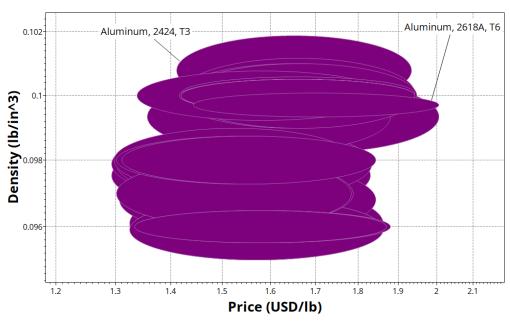
$$P_{cr} = \frac{\pi^2 EI}{L^2} = \frac{19.8696 \times 10.10^6 \times 10.001302}{(22)^2} = 266 15 (critical load)$$

## Pin Calculations:

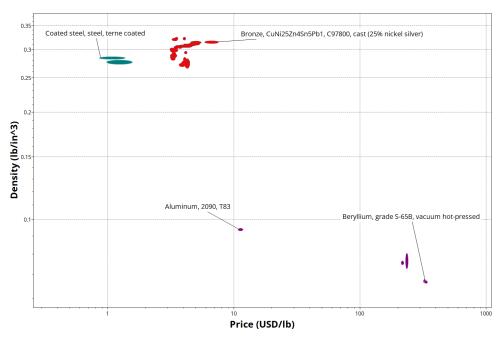
Shear Stress: 
$$A = \frac{\pi d^2}{4} = \frac{\pi . 0.25^2}{4} = 0.049 \text{ in}^2$$
  
again assuming 22515 shear  $\Rightarrow T_{\text{pin}} = \frac{2515}{0.049 \text{ in}^2} = 510 \text{ ps};$   
 $T_{\text{max}} = \frac{\xi_y}{\sqrt{3}} \approx \frac{40,000}{\sqrt{3}} = 23,000 \text{ ps};$   
 $FOS = \frac{23000}{610} = 45 > 7 = 1.5 \text{ }$ 

### Platform Pelleution;

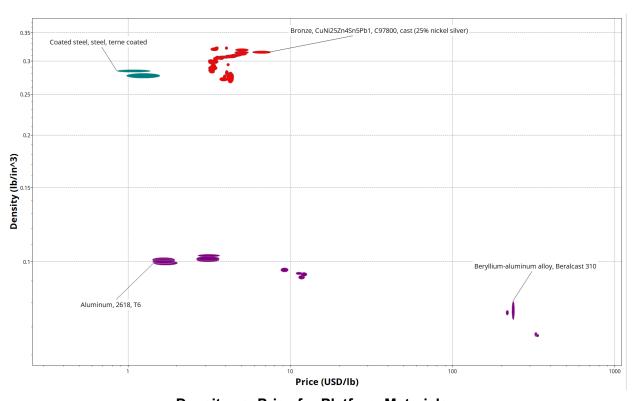
$$F = \frac{6h^3}{12} = \frac{12 \cdot 0.5^3}{12} = \frac{12 \cdot .125}{12} = 0.125in^4$$
  
 $S_{max} = \frac{FL^3}{3ET}$  A. Assume material is steeld  
 $E = 29 \cdot 10^6 \text{ psi}$ 



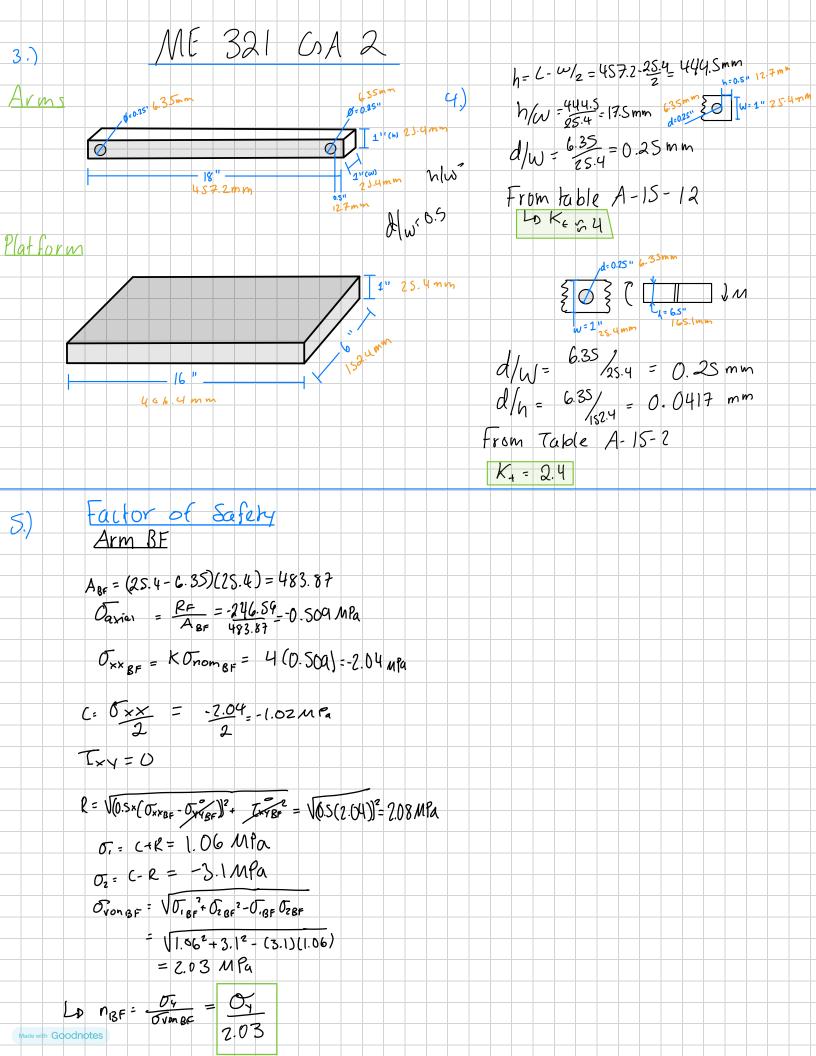
**Density vs. Price for Support Arm Materials** 

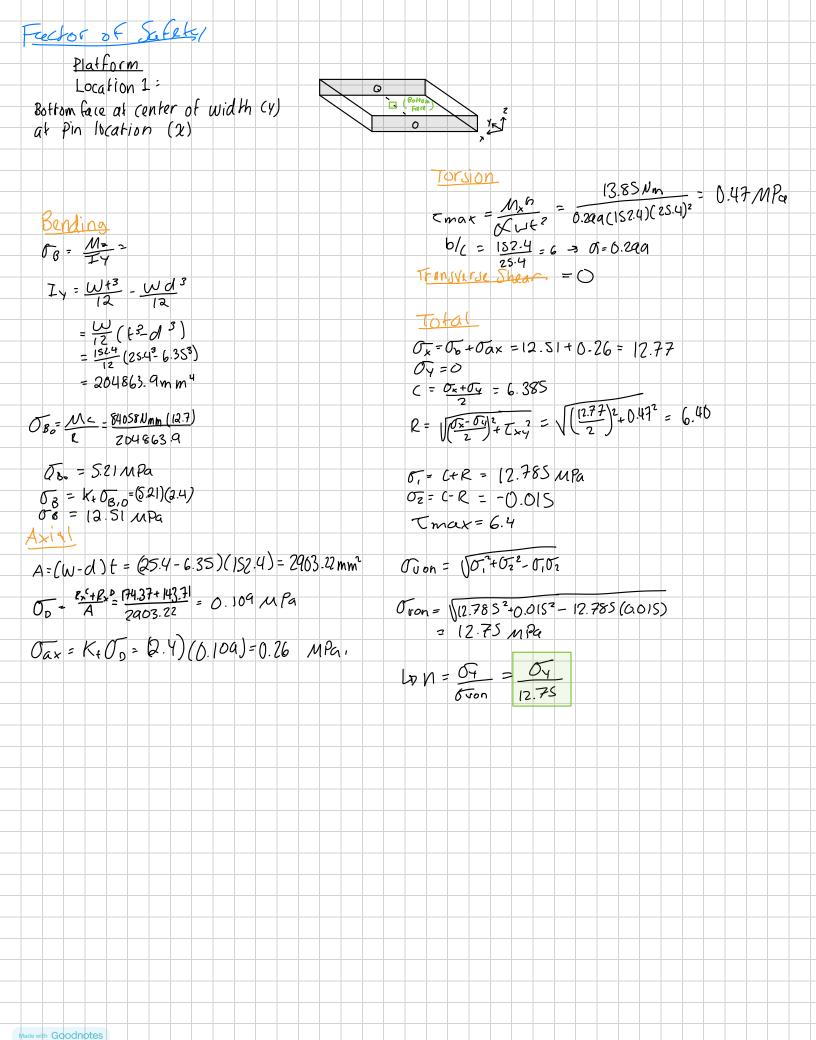


**Density vs. Price for Pin Materials** 



**Density vs. Price for Platform Materials** 





Location 2 Cross section where pin hole (10 lies. T= VQ/IB Bending None Torsion-Countered by arms (hone) axial For (0.0: d/z) OO = F = Rxc+RxP W-a)t = [74.37+143.7] = 0.109 MPa d/w=6.33 = 0.25, 2 = 12.7 = 0.5; EDT (+d(2,0,0): K+ 53.8 Tax= K+00 = 3.8 (0.109) Jax = 0.414 MPa For (+0(2,0,0) A= lxw=182.4 x 25.4 = 3870.96 mm2 (= 0.21 MPa Jax = F = 174.37+143.71 = 0.082 MPa (otal For (o, o, tal) Ouon = (10,2+022-0,02 5v=0082MPa (2) + (0.148)2 r= 6.154 C=0.041 h= 04 0.417 0,= C+r = 0.195 MPa Oz=C-r=0.113 MPG Tron = 10-1952+0.1132- 0.19580.113 Nron = 0.170 n= Oy 0.170

Transverse For (0,0,0,0/2)  $0 = \frac{\omega}{2} \left( \left( \frac{2}{2} - \frac{4}{7} \right) \right) = \frac{\omega}{2} \left( \left( \frac{d+1}{4} \right)^2 - \left( \frac{d}{2} \right)^2 \right) = 21685.9 \, \text{mm}^2$ I = (13- (13) = 204863.9mm4 T = 318.08 (216859) = 0.27 MPa 2048639 (152.4) For ( d (2,0,0) Tmax = 41 = 4618.08) 0-148 MP4 0 = B.4/4MPa  $r = (0.4/4)^2 + (0.022)^2$ C= 0.414 = 0.207 MPa 0,= (+r = 0.417 MPa 52 = C-r = -0.003 MPa Ovon = \ 8.4172+0.0032-0.00320.417) Ovon= 0.417 MPa

Location 3 At pin hole EF Axial None Bending None Transverse

Transverse

Transverse

3A 3CWE) 3(182.4-25.4) Thax = O. IIMPa Torsion Torsion = 0.47 MPa Tmax = 0.47 x K = 0.47 x 3 = 1.41 MPa GVm = V3(Transfort Transverse) n = Sy = Sy = Sy = Sy = S(0.11+0.472) Made with Goodnotes

We were initially opting to select aluminum 2424 or 2618 for use with the support arms, however, they are not readily available for purchase. We conducted our analysis using aluminum 2024, which was also recommended by Ansys and has similar performance characteristics with more availability.

The final selected dimensions for the arms are:

```
arm_w = 0.5"
arm_t = 0.145"
arm_l = 18"
```

This gives us a projected factor of safety just above 1.5 for both deflection and buckling when using 6061 Aluminum with minimal deflection.

```
Arm Calculations
hw 1.0 dw 0.5
Area: 0.02125
Sigma_D_arm: -11603.764705882353
Sigma_axial_arm: -29009.41176470588
Sigma_principal_arm_1: 0.0
Sigma_principal_arm_2: -29009.41176470588
sigma_von_arm: 29009.41176470588
Arm FOS: S_y / 29009.41176470588
Arm FOS: 1.5512206991645714
```

```
Arm Buckling Calculations
0.4921875
P_cr: 40.242118860547684
Buckling FOS: 1.6096847544219073
```

Given that the dimension of 0.085" is not commonly available, we will need to machine the face down to that size or elect to go with the next available size.

For the platform we selected the following dimensions and elected to go with aluminum 6061-T6 to alleviate costs and maintain lightweight characteristics:

```
p_w = 6"

p_t = 0.35"

p_l = 16"
```

This allows for very high deflection FOS of over 15 and satisfies the 1.5 FOS for all other categories. We could accomplish a more efficient design with increased weight reduction by reducing the thickness of the aluminum (and still meeting performance criteria), however, we need to be able to comfortably situate the 0.25" clevis pins into the side of the platform. Reducing the thickness more than this may not leave for a lot of room for the pin to rest on the side of the platform. We may attempt a workaround by constructing an alternative mounting point (angle bracket or hollow out the inside of the aluminum using a mill) in order to maximize the potential for weight reductions while maintaining optimal deflection characteristics.

```
Platform Case 1 Calculations
dh 0.0416666666666664 dw 0.7142857142857143
Moment of Inertia (y): 0.0136249999999995
Sigma_b_1: 9530.275229357801
Sigma_b: 20013.577981651382
Platform axial area: 0.599999999999999999
Sigma_D: 530.1333333333334
Sigma_axial: 1113.2800000000002
T_max: 10449.798648556412
Mohr's radius: 14858.813002376337
Sigma_von: 27819.759229062012
Platform Case 1 (bottom face along hole axis) FOS: S_y / 27819.759229062012
Platform Case 1 FOS: 1.6175553364599426
```

Appendix A: Code for calculating buckling, deflection, and factors of safety import math

```
import math
#Arm FOS
print("Arm Calculations")
arm w = 0.5
arm_t = 0.145
arm 1 = 18
k arm = 2.5
arm E = 1.04*10**7
sy_arm = 45000
hw = 0.5/arm w
dw = 0.25/arm w
print(f"hw {hw} dw {dw}")
A arm = (arm w-0.25)*arm t
print(f"Area: {A arm}")
sigma_arm_axial = -246.58/A_arm #-1096N
print(f"Sigma D arm: {sigma arm axial}")
sigma_arm_xx = k_arm*sigma_arm_axial
print(f"Sigma axial arm: {sigma arm xx}")
```

```
mohrs_arm_center = sigma_arm_xx/2
mohrs_arm_radius = math.sqrt((0.5*sigma_arm_xx) ** 2)
sigma_arm_1 = mohrs_arm_center + mohrs_arm_radius
print(f"Sigma_principal_arm_1: {sigma_arm_1}")
sigma arm 2 = mohrs arm center - mohrs arm radius
print(f"Sigma principal arm 2: {sigma_arm_2}")
sigma von arm = math.sqrt(sigma arm 1 ** 2 + sigma arm 2 ** 2 -
sigma_arm_1*sigma_arm_2)
print(f"sigma_von_arm: {sigma_von_arm}")
print(f"Arm FOS: S_y / {sigma_von_arm}")
sf = sy_arm / sigma_von_arm
print(f"Arm FOS: {sf}")
print()
print("----")
print()
#Platform FOS Case 1
print("Platform Case 1 Calculations")
p_w = 6 \#width (mm)
p t = 0.35 #thickness (mm)
p l = 16 \#length (mm)
k p = 2.1
alpha = 0.299
sy_p = 45000
E = 7*10**10
F1 = 25
F2 = 448.9435
a1 = 1.5
a2 = p_1 - 3.75 - a1
dh = 0.25/p w
dw = 0.25/p t
print(f"dh {dh} dw {dw}")
I_y = p_w/12 * (p_t**3 - 0.25**3)
print(f"Moment of Inertia (y): {I_y}")
sigma_b_0 = 742*(p_t/2)/I_y
print(f"Sigma b 1: {sigma b 0}")
```

```
sigma_b = sigma_b_0 * k_p
print(f"Sigma b: {sigma b}")
#axial calculatios:
A p = (p t-0.25) * p w
print(f"Platform axial area: {A_p}")
sigma d = 318.08/A p
print(f"Sigma D: {sigma d}")
sigma_axial = k_p * sigma_d
print(f"Sigma axial: {sigma axial}")
#torsion
t_max = 2296.5/(alpha * p_w * p_t**2)
print(f"T_max: {t_max}")
#total
sigma_x = sigma_b + sigma_axial
c = sigma_x / 2
r = math.sqrt((sigma_x/2)**2+t_max ** 2)
print(f"Mohr's radius: {r}")
sigma1 = c+r
sigma2 = c-r
sigma von = math.sqrt(sigma1**2 + sigma2**2 -sigma1*sigma2)
print(f"Sigma von: {sigma von}")
print(f"Platform Case 1 (bottom face along hole axis) FOS: S_y / {sigma_von}")
sf = sy_p / sigma_von
print(f"Platform Case 1 FOS: {sf}")
print()
print("----")
print()
#platform case 2 calculations 1
print("Platform case 2 (cross section where pin holes c/d lies) calculations")
print("for (0, 0, +-d/2)")
k p = 3.8
sigma_axial = k_p * sigma_d
print(f"Sigma axial: {sigma axial}")
```

```
q = p_w/2*(((0.25+p_t)/4)**2-(0.25/2)**2)
transverse= 318.08*q/(I_y * p_w)
sigma x = sigma axial
r = math.sqrt((sigma_x/2)**2+transverse**2)
c = sigma x / 2
sigma 1 = c + r
sigma 2 = c - r
sigma_von = math.sqrt(sigma1**2 + sigma2**2 -sigma1*sigma2)
print(f"Sigma_von: {sigma_von}")
print(f"Platform Case 2 FOS: S y / {sigma von}")
sf = sy p / sigma von
print(f"Platform Case 1 FOS: {sf}")
#platform case 2 calculations 2
print()
print("Platform case 2 calculations II")
print("for (+-d/2, 0, 0)")
k p = 3.8
sigma_d = (174.37+143.71)/(p_t*p_w)
sigma axial = k p * sigma d
print(f"Sigma axial: {sigma axial}")
#transverse
transverse = 4*318.08/(3*p_t*p_w)
sigma_x = sigma_axial
r = math.sqrt((sigma_x/2)**2+transverse**2)
c = sigma x / 2
sigma 1 = c + r
sigma 2 = c - r
sigma_von = math.sqrt(sigma1**2 + sigma2**2 -sigma1*sigma2)
print(f"Sigma_von: {sigma_von}")
print(f"Platform Case 2 FOS (+- d/2, 0, 0): S y / {sigma von}")
print()
print("-----")
print()
print("Platform case 3 (at pinhole EF) calculations")
tmax = 4*318.08/(3*p_w*p_t)
print(f"tmax: {tmax}")
k = 3
```

```
torsion = 0.47*k
print(f"Torsion: {torsion}")
sigma_vm = math.sqrt(3*(torsion+tmax**2))
print(f"Platform Case 3 FOS: S y / {sigma vm}")
sf = sy_p / sigma_vm
print(f"Platform Case 1 FOS: {sf}")
print()
print("-----")
print()
#deflection
print("Platform Deflection Calculations")
y_{max} = F1*a1**2 * (a1 - 3*p_1) / (6*E*I_y) - F2*a2**2 * (a2 - 3*p_1)/(6*E*I_y)
print(f"deflection max: {y_max}")
fs = 0.01 / y_max
print(f"deflection FOS {fs}")
print()
print("-----")
print()
print("Arm Buckling Calculations")
print(f"{I y}")
arm_I = (arm_t) **3*(arm_w)/12
P cr = math.pi**2 * arm E * arm I / ((arm 1)**2)
print(f"P_cr: {P_cr}")
FOS = P_cr / F1
print(f"Buckling FOS: {FOS}")
#buckling
```