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In [1]: import numpy as np

g=9.81 # m/s^2
pendulum_length = 1 # meters
theta_0 = 40 # degrees
t_final = 18.5 # seconds
dt=0.005 # seconds
n_steps=int(t_final/dt)

def pendulum_rk4(dt, n_steps, initial_theta_degrees, l):
    ''' RK4 integrator to solve the Simple Pendulum ODE system:
        d^2 theta / d theta ^2 = -(g/l)sin(theta)
        returns the x,y position, time, theta and d theta/ dt arrays with n_
    ...
    theta_old = initial_theta_degrees*(np.pi/180)

    theta_dot_old = 0

    pos_x = np.zeros(n_steps+1)
    pos_y = np.zeros(n_steps+1)
    times = np.zeros(n_steps+1)
    thetas = np.zeros(n_steps+1)
    theta_dots = np.zeros(n_steps+1)

    ## initial conditions
    pos_x[0] = np.sin(theta_old)*l
    pos_y[0] = -np.cos(theta_old)*l
    times[0] = 0
    thetas[0] = theta_old

    t_new = 0
    for i in range(n_steps):
        t_new += dt

        k1_theta = theta_dot_old
        k1_theta_dot = -(g/l)*np.sin(theta_old) ## use ODE equation for k_theta

        k2_theta = theta_dot_old + k1_theta_dot*dt/2
        k2_theta_dot = -(g/l)*np.sin(theta_old + k1_theta*dt/2)

        k3_theta = theta_dot_old + k2_theta_dot*dt/2
        k3_theta_dot = -(g/l)*np.sin(theta_old + k2_theta*dt/2)

        k4_theta = theta_dot_old + k3_theta_dot*dt
        k4_theta_dot = -(g/l)*np.sin(theta_old + k3_theta*dt)

        ## use k1,k2,k3,k4 to update theta and dtheta/ dt
        theta_new = theta_old + dt * (k1_theta + 2*k2_theta + 2*k3_theta + k4_theta)/6
        theta_dot_new = theta_dot_old + dt * (k1_theta_dot + 2*k2_theta_dot + 2*k3_theta_dot + k4_theta_dot)/6
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### update arrays
pos_x[i+1] = np.sin(theta_new)*l
pos_y[i+1] = -np.cos(theta_new)*l
times[i+1] = times[i]+dt
thetas[i+1] = theta_new
theta_dots[i+1] = theta_dot_new
###

theta_old = theta_new
theta_dot_old = theta_dot_new

return pos_x, pos_y, times, thetas, theta_dots

pos_x, pos_y, times, thetas, theta_dots = pendulum_rk4(dt, n_steps, theta_0,
print(f"After {round(times[-1], 2)} seconds, the pedulum bob has height {rou
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After 18.5 seconds, the pedulum bob has height 4.21 meters