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7.21

a) Neutral: some of the points are outside the control lines, so it is approximately normal. t values should be used because $n < 30$ and σ unknown

Sad: points inside control lines so it is normal. T should be used because $n < 30$ and σ unknown

b) ~~neutral~~

	n	mean	standard deviation
neutral	14	0.571	0.730
sad	17	2.118	1.244

c) null: H_0 : there is not a significant difference in the mean price of the waters

$$H_0: \mu_1 = \mu_2 \text{ or } \mu_1 - \mu_2 = 0$$

alt: H_A : there is a significant difference in the mean price of the waters

$$H_A: \mu_1 \neq \mu_2 \text{ or } \mu_1 - \mu_2 \neq 0$$

d)

$n_1 = 14$	$\alpha = 0.05$	$n_2 = 17$
$\bar{x}_1 = 0.571$		$\bar{x}_2 = 2.118$
$s_1 = 0.730$		$s_2 = 1.244$

$$t = \frac{0.571 - 2.118}{\sqrt{\frac{(0.730)^2}{14} - \frac{(1.244)^2}{17}}} = -4.306 = t \quad df = 13$$

$p\text{-value} = 0$

$p\text{-value} < \alpha$, so reject H_0

conclusion: There is sufficient sample evidence to warrant the conclusion that there is a significant difference between the means

$t = 2.16$ for df at $\alpha = 0.05$

$$\begin{aligned} c) \quad & (0.571 - 2.118) \pm (2.16) \sqrt{\frac{(0.730)^2}{14} + \frac{(1.244)^2}{17}} \\ & = -1.547 \pm 0.776 \\ & = -2.323 \leq \mu_1 - \mu_2 \leq -0.771 \end{aligned}$$

I am 95% confident The true difference in means for these two groups is between 2.323 and 0.771

7.89 a) $H_0: \mu_B = \mu_F$ hemoglobin in breast fed = formula

$H_A: \mu_B > \mu_F$ hemoglobin in breast fed > formula

$$t = \frac{13.3 - 12.4}{\sqrt{\frac{1.7^2}{23} + \frac{1.8^2}{19}}} = 1.654 \quad (p\text{-value} = 0.053)$$

$0.053 > 0.05$, so FTR H_0

conclusion: There is not significant evidence to support the claim the hemoglobin in breast fed is greater than formula.

$$\begin{aligned} b) \quad & t = 2.101 \text{ for } df = 18 \text{ at } 95\% \text{ conf.} \\ & (13.3 - 12.4) \pm 2.101 \sqrt{\frac{1.7^2}{23} + \frac{1.8^2}{19}} \end{aligned}$$

$$= -0.2434 \leq \mu_B - \mu_F \leq 2.0434$$

I am 95% confident The true difference in means for these two groups is between 0.2434 and 2.0434

c) The procedures are only valid when the samples are independent from the population

$$H_0: \sigma_1 = \sigma_2$$

$$H_A: \sigma_1 \neq \sigma_2$$

7.102

a)

TS

$$F = 0.38$$

$$b) F_{\text{critical}} = (n_1 - 1, n_2 - 1)$$

$$= (10, 15) =$$

$$2.54$$

c) F value is not within critical region, so fail to reject H_0

There is not sufficient evidence to suggest that the standard deviations are equal

7.122

a)

$$\bar{X}_1 = 49.69$$

$$S_1 = 12.32$$

$$S_1^2 = 5.38$$

$$\bar{X}_2 = 50.55$$

$$S_2 = 1.92$$

$$S_2^2 = 3.686$$

$$TS = t = -0.9$$

$$p\text{-val} = 0.383 \quad df = 9$$

b)

$$\text{mean} = -0.853$$

$$t = -2.13$$

$$S^2 = 1.611$$

$$p = 0.062$$

$$df = 9$$

c)

the results show no difference between the population means

8.7W a) girls: $p_g = \frac{48}{60} = 0.80$

standard error: $\sqrt{\frac{0.8(1-0.8)}{60}} = 0.05164$

boys: $p_b = \frac{52}{132} = 0.394$

standard error: $\sqrt{\frac{(0.394)(1-0.394)}{132}} = 0.0425$

b) $z = 1.96$

$$(0.8 - 0.394) \pm 1.96 \sqrt{\frac{(0.8)(1-0.8)}{60} + \frac{(0.394)(1-0.394)}{132}}$$

$$= 0.4061 \pm 0.131 = 0.275 \leq p_g - p_b \leq 0.5372$$

I am 90% confident the true difference between the proportions is between 0.275 and 0.5372

c) $H_0: p_1 = p_2$ $\hat{p} = \frac{x_1 + x_2}{n_1 + n_2} = 0.52$
 $H_A: p_1 \neq p_2$

$$z = \frac{(0.8 - 0.394) - 0}{0.52(1-0.52)\left(\frac{1}{60} + \frac{1}{132}\right)} \approx 5.22$$

5.22 is in rejection region so reject H_0

conclusion: there is a difference in the proportions of the two