

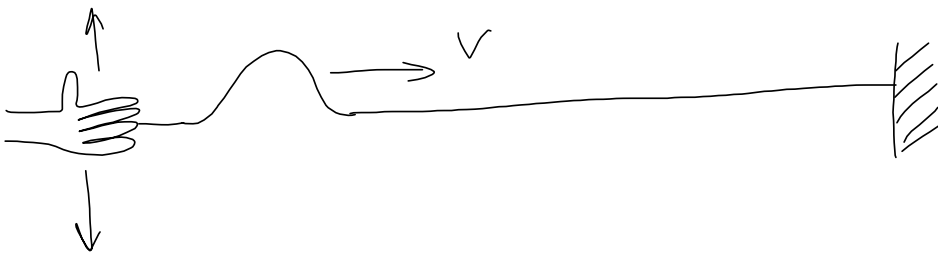
longitudinal wave

m_6 does not move immediately

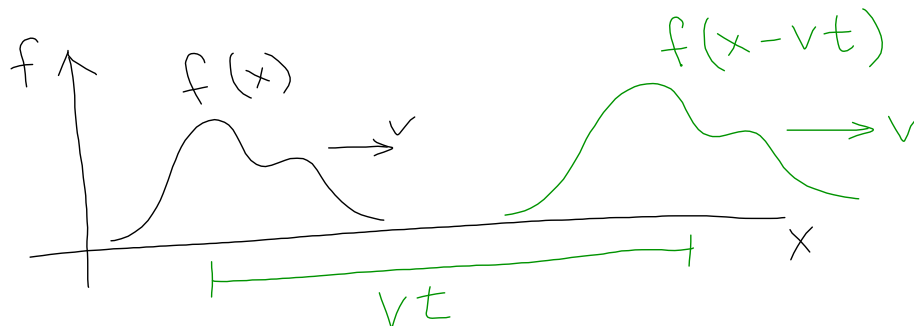
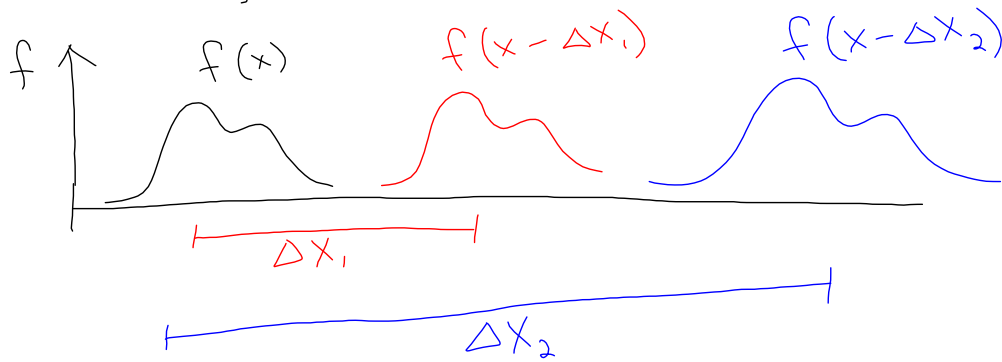
i.e. it takes time for the disturbance to propagate

$$\text{velocity of disturbance} = \frac{\text{distance between } m_1 \text{ \& } m_2}{\text{time before } m_6 \text{ starts moving}}$$

Another example: transverse wave



Traveling waves: (review)



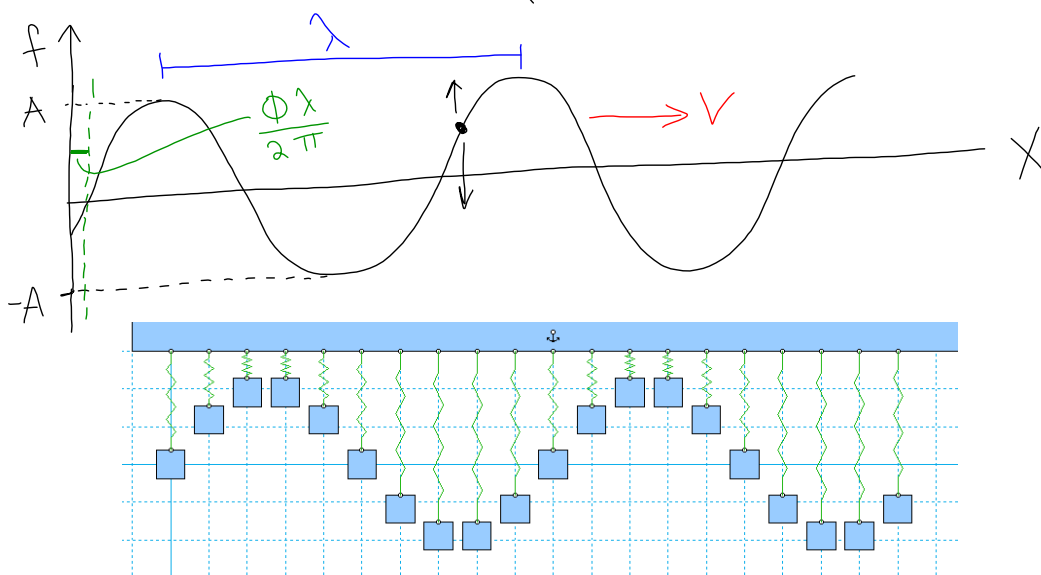
Waves are functions of space and time that can be written:

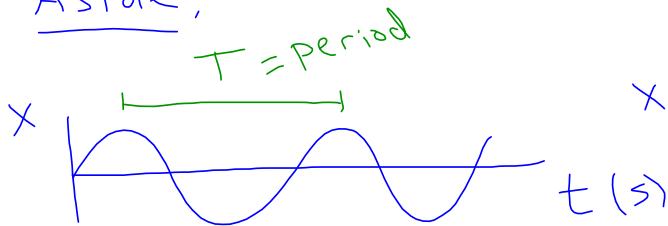
$$f(x \pm vt)$$

\uparrow
 $+$: propagating left
 $-$: propagating right

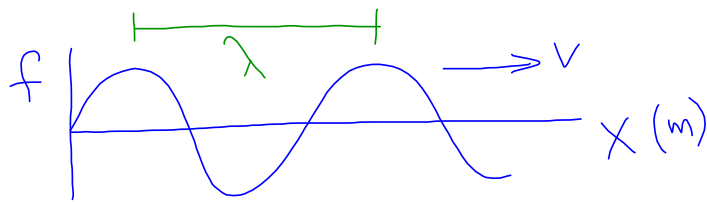
Most popular wave - sinusoidal wave

$$f(x, t) = A \sin\left(\frac{2\pi}{\lambda} (x - vt) + \Phi\right)$$



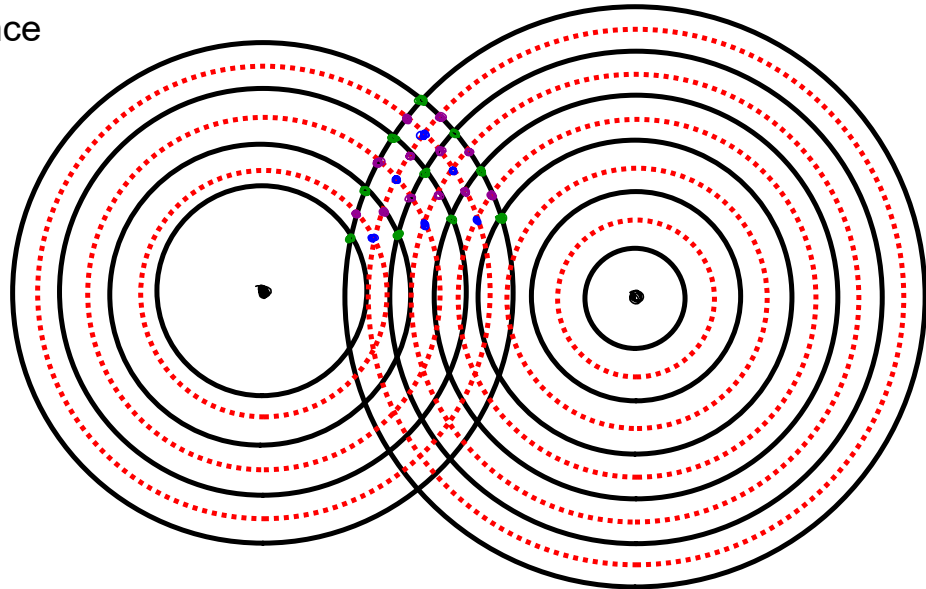
Aside:

$$x(t) = x_{\max} \sin\left(\frac{2\pi}{T} t\right)$$



$$f = f_{\max} \sin\left(\frac{2\pi}{\lambda} (x - vt)\right)$$

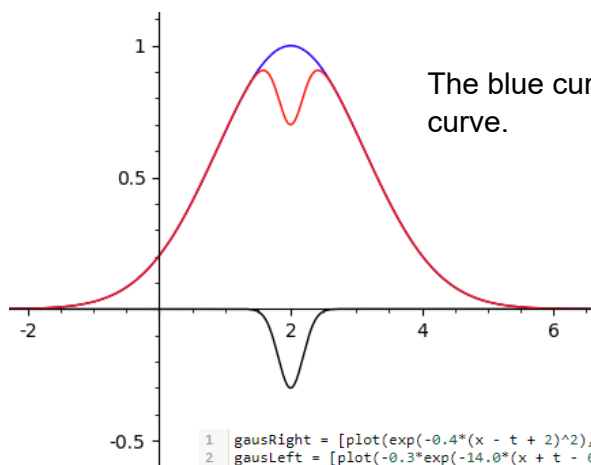
Wave interference



When a peak meets a peak: constructive interference - amplitudes combine
(green dots)

When a valley meets a valley: (negative) constructive interference -
(negative) amplitudes combine
(blue dots)

When a peak meets a valley: destructive interference - amplitudes (partially)
cancel out
(purple dots)



The blue curve and black curve interfere and you get the red curve.

```
1 gausRight = [plot(exp(-0.4*(x - t + 2)^2), (-4, 8), ymin=-1, ymax=1.2) for t in xrange(0, 8, 0.1)]
2 gausLeft = [plot(-0.3*exp(-14.0*(x + t - 6)^2), (-4, 8), color="black") for t in xrange(0, 8, 0.1)]
3 gausBoth = [plot(exp(-0.4*(x - t + 2)^2) - 0.3*exp(-14.0*(x + t - 6)^2), (-4, 8), color="red") for t in xrange(0, 8, 0.1)]
4 animation = animate(gausRight)
5 animation += animate(gausLeft)
6 animation += animate(gausBoth)
7 animation.show(delay=10)
```