

Unified Socio-Mythic Calculus (USMC) Specification

1 Universe and State

Definition 1 (Nodes, types, qualities, energies). *Let $\Omega = \{N_i\}$ be a finite set of nodes with*

$$N_i = (\text{Name}_i, T_i, Q_i, E_i),$$

where T_i tags domain (e.g. mythic character/place/idea or social object/config), $Q_i \in \{-1, +1\}$ encodes wound/gift or stress/content polarity, and $E_i \in \mathbb{R}$ encodes magnitude or salience.

Definition 2 (Story/experience graph with suspended set). *At discrete time t , define*

$$G_t = (\Omega, E_t, S_t),$$

where $E_t \subseteq \Omega \times \Omega$ are active bonds (edges), and $S_t \subseteq \Omega \times \Omega$ are suspended ties captured by the naught operator $\widehat{0}$. A pair may be active, suspended, or absent.

2 Primitive Operators

Definition 3 (Pointwise operators on pairs (i, j)). *For each ordered pair (i, j) , define*

$$\hat{A}_{ij} \in \{\widehat{+}, \widehat{-}, \widehat{0}\} :$$

- **Connect** $\widehat{+}_{ij}$: *add (i, j) to E_t ; remove from S_t .*
- **Disconnect** $\widehat{-}_{ij}$: *remove (i, j) from both E_t and S_t .*
- **Naught** $\widehat{0}_{ij}$: *move (i, j) to S_t (deliberate non-action that preserves potential).*

3 Composite Transform as Guarded Naught

Definition 4 (Motif and boundary). *Let $M \subseteq G_t$ be a motif (subgraph). Let ∂M denote the set of pairs on the boundary of M relevant for suspension.*

Definition 5 (Guarded transform). *Define the transform operator on motif M by*

$$\hat{\tau}_M := \underbrace{\prod_{(i,j) \in \partial M} \widehat{0}_{ij}}_{\text{create conserved gap}} \circ \underbrace{\text{Wait}[g_M(G)]}_{\text{fire at threshold}} \circ \underbrace{\text{Rewire}_M}_{\text{relabel nodes/edges}} .$$

Here, the guard function $g_M(G)$ encodes a phase threshold; when satisfied, Rewire_M may add/remove edges and relabel qualities/energies within M .

4 Effects, Value, and Objective

Definition 6 (Pair effect and totals). *For any prospective or active pair (i, j) , define pair effect*

$$\Phi_{ij} = (Q_i E_i) + (Q_j E_j).$$

Define total realized effect

$$\Phi_{\text{total}}(G_t) = \sum_{e_{ij} \in E_t} \Phi_{ij}.$$

Definition 7 (Order and Freewill). *Let*

$$O(G_t) = \Phi_{\text{total}}(G_t) - \lambda \cdot \text{Complexity}(G_t), \quad F(G_t) = \sum_{e_{ij} \notin E_t} |\Phi_{ij}|.$$

Optionally decompose $F = F_{\text{susp}} + F_{\text{abs}}$ with F_{susp} summing pairs in S_t .

Definition 8 (Target objective (singularity)). *With weights $\alpha, \beta > 0$, define*

$$G^* = \arg \max_{G_t} [\alpha O(G_t) + \beta F(G_t)].$$

5 Threshold Guards

Two families of guards are common; either can be used alone or in concert.

- **Counting/structure guard (mythic):** fire when an event count or structural criterion reaches a narrative threshold $k = T_n$.
- **Value/ratio guard (social):** fire when a criterion indicates readiness or safety, e.g. a tension-content ratio crossing an ε -band, or a prescribed gain condition $\Delta O \geq 0$.

6 Dynamics and Policy

Definition 9 (Step dynamics). *At each step,*

$$G_{t+1} = \hat{A} G_t, \quad \hat{A} \in \{\hat{+}, \hat{-}, \hat{0}, \hat{\tau}\}.$$

A policy selects \hat{A} to ascend the objective $\alpha O + \beta F$, while any use of $\hat{\tau}$ must satisfy its guard.

Definition 10 (Operator statistics). *Track operator rates r_+, r_-, r_0, r_τ and guard triggers to localize phase changes in the process.*

7 Minimal Worked Example

Consider nodes

$$N_h = (\text{Hero}, \text{Char}, +1, E_h), \quad N_s = (\text{Sword}, \text{Artifact}, -1, E_s),$$

and motif $M = \{h, s\}$.

(1) **Naught.** Apply $\hat{0}_{hs}$: move pair (h, s) to S_t (tension held, potential conserved).

(2) **Guard.** After thresholds/ratios satisfy $g_M(G)$, the transform may fire.

(3) **Transform.** Apply $\hat{\tau}_M$ with relabeling $Q_s : -1 \rightarrow +1$ and bond $\hat{+}_{hs}$. The change in pair effect is

$$\Delta\Phi = [(+1 \cdot E_h) + (+1 \cdot E_s)] - [(+1 \cdot E_h) + (-1 \cdot E_s)] = 2E_s.$$

Thus O increases (modulo the complexity term), and F decreases for that pair as potential becomes realized.

8 Assumptions and Notes

- $Q \in \{-1, +1\}$ is a coarse polarity; refinements (e.g. continuous valence or multi-axes qualities) are admissible with minor algebraic changes.
- $\text{Complexity}(G)$ penalizes gratuitous structure; any monotone measure (e.g. description length or sparsity loss) can be used.
- Guards can be domain-tuned (ritual time windows, consensus thresholds, safety checks) without altering the operator algebra.

Appendix A: Symbol \leftrightarrow Term Map

Symbol	Interpretation
Ω	Entities (mythic roles, social objects)
E_t	Active bonds / realized ties
S_t	Suspended ties via naught (held potential)
Q_i	Polarity: wound/gift or stress/content
E_i	Salience/strength/charge
$\hat{+}, \hat{-}, \hat{0}$	Connect, Disconnect, Naught
$\hat{\tau}$	Guarded transform (naught \rightarrow threshold \rightarrow rewire)
Φ_{ij}	Pair effect contribution
O, F	Order (realized, minus complexity) and Freewill (unrealized potential)
$g_M(G)$	Threshold function (counting/structure or value/ratio)
G^*	Target configuration maximizing $\alpha O + \beta F$

Appendix B: Operator Table

Op	Name	Precondition	Effect on (E_t, S_t)
$\hat{+}_{ij}$	Connect	pair (i, j) exists	$(i, j) : S_t \setminus \{(i, j)\}, E_t \cup \{(i, j)\}$
$\hat{-}_{ij}$	Disconnect	pair (i, j) exists	$(i, j) : E_t \setminus \{(i, j)\}, S_t \setminus \{(i, j)\}$
$\hat{0}_{ij}$	Naught (Suspend)	pair (i, j) exists	$(i, j) : E_t \setminus \{(i, j)\}, S_t \cup \{(i, j)\}$
$\hat{\tau}_M$	Transform (Guarded)	$g_M(G)$ true	Rewire edges/labels within M