Statistical Inference using RevBayes

A very short introduction to RevBayes & Rev

Mike May and Sebastian Höhna

1 Basic Rev Commands

1.1 Introduction

This tutorial demonstrates the very basic syntactical features of RevBayes and Rev. A more elaborate introduction into Rev and probabilistic graphical models is provided. A good reference for probabilistic graphical models for Bayesian phylogenetic inference is given in Höhna et al. (2014). The statistical examples are borrowed from a fourth year statistics course taught in the fall term 2011 at Stockholm University.

The first section of this tutorial involves

- 1. Creating different types of variables.
- 2. Learning about functions.

Then we will see how to perform statistical inference using RevBayes and Rev by implementing a Monte Carlo algorithm. Finally, we will see how RevBayes's built-in functions vastly simplify this inference task.

Let's start with the basic concepts for the interactive use of RevBayes with Rev (the language of RevBayes). You should try to execute the statements step by step, look at the output and try to understand what and why things are happening. We start with some simple concepts to get familiar and used to RevBayes. By now you should have executed RevBayes and you should see the command prompt waiting for input. The best exercise is to write these statements exactly in RevBayes.

1.2 Starting RevBayes

This tutorial demonstrates the basic syntactical features of RevBayes and the Rev scripting language. Let's start with the basic concepts for the interactive use of RevBayes with Rev (the language of RevBayes). You should try to execute the statements step by step, look at the output and try to understand what and why things are happening.

First, open up your terminal and type RevBayes. This should launch RevBayes and give you a command prompt (the > character). This means RevBayes is waiting for input.

1.3 Operators and Functions

Rev is an interpreted language for statistical computing and phylogenetic analysis. Therefore, the basics are simple mathematical operations. Entering each of the following lines will automatically execute these operations.

```
RevBayes is free software released under the GPL license, version 3. Type 'license()' for details.

To quit RevBayes type 'quit()' or 'q()'.

> 1 + 1
2
> 10 - 5
5
> 5 * 5
25
> 10 / 2
5
> 2 * 3
8
> 5 % 2
1
```

From now on, we will omit images of the terminal.

Each set of operations constitutes a *statement*. As you work through these tutorials, it is helpful to write the statements you enter into a blank text file, then copy-and-paste the statements into Rev to execute them. This way, you have a complete history of everything you've done, and can easily start over without having to rewrite everything. We refer to the text file containing the list of commands as a *script*, because it describes line-by-line instructions for the program to follow.

You can write multiple statements in the same line if you separate them by a semicolon (;). The statements will execute as if you wrote each on a single line.

```
1 + 1; 2 + 2 # Multiple statements in one line
```

Here you can see that comments always start with the hash symbol (#). Everything after the '#'-symbol will be ignored. In addition to these simple mathematical operations, Rev provides some standard math functions which can be called by:

```
# Math functions
exp(1)  # exponential function
ln(1)  # logarithmic function with natural base
sqrt(16)  # square root function
power(2,2)  # power function: power(a,b) = a b
```

Notice that Rev is case-sensitive. That means, Rev distinguishes upper and lower case letter for both variable names and function names. For example, only the first of these two calls will work:

```
exp(1) # correct lower case name
Exp(1) # wrong upper case name
```

1.4 Variable Declaration and Assignment

One of the most important features of RevBayes (or any programming language, really) is the ability to declare and assign variables. Variables store information to be referenced later, and can change throughout the execution of the program. There are three kinds of variables in RevBayes, called *constant*, *deterministic*, and *stochastic* variables. Constant variables contain values that are not random in your model. Deterministic variables are functions of other variables. Stochastic variables are random variables in your model, and will change during your analysis; importantly, stochastic variables (being random variables) are always associated with a particular statistical distribution.

Different types of variables differ in how you create them and assign values to them. We will begin by creating a constant variable with name a that starts with the value 1. The left arrow assignment (<-) always creates a constant variable, and automatically assigns the following value to it.

```
# Variable assignment: constant
a <- 1  # assignment of constant node 'a'
```

You see the value of 'a' by just typing in the variable name and pressing enter.

```
a # printing the value of 'a'
```

Next, we create a deterministic variable b using the := assignment computed by exp(a) and another deterministic variable c computed by ln(b). Deterministic variables are always created using the colon-equal assignment (:=).

```
# Variable assignment: deterministic

# assignment of deterministic node 'b' with
# the exponential function with parameter 'a'
b := exp(a)
b

# assignment of deterministic node 'c' with
# logarithmic function with parameter 'b'
c := ln(b)
c
```

Finally, we will create the third type of variables in Rev: stochastic variables. We will create a random

variable x from an exponential distribution with parameter lambda. Stochastic assignments use the \sim operation.

```
# Variable assignment: stochastic

# assign constant node 'lambda' with value '1'
lambda <- 1.0

# create stochastic node with exponential
# distribution and parameter 'lambda'
x ~ dnExponential(lambda)</pre>
```

The value of x is a random draw from the distribution. You can see the value and the probability (or log-probability) of the current value under the current parameter values by

```
x  # print value of stochastic node 'x'
x.probability()  # print the probability if 'x'
x.lnProbability()  # print the log-probability if 'x'
```

1.5 Distributions and Random Numbers

Rev provides functions for common statistical distributions. We'll demonstrate by generating random exponential numbers as we did in lecture. Recall that we can transform a random variable u sampled from a Uniform (0,1) distribution into an exponential distribution with rate parameter λ :

$$u \sim \text{Uniform}(0,1)$$

 $x = -\frac{1}{\lambda \ln u}$

In Rev, we might describe u as a stochastic variable, and x as a deterministic variable (since it is a function of u):

```
# create the random variable u
u ~ dnUniform(0,1)
u

# determine the rate parameter
lambda <- 1.0

# create x as a deterministic function of u
x := - 1 / lambda * ln(u)
x</pre>
```

Alternatively, we can create x directly as an exponential random variable:

```
# create the random variable x
x ~ dnExponential(lambda)
x
```

1.6 Vectors

Individual variables can have more than one value. Variables that have more than one value are called *vectors*. The simplest way to create a vector is like this:

```
v <- v(1.0,2.0,3.0) # create a vector
```

You can refer to a specific value in the vector using brackets, [i], where i is the index of the variable of interest.

```
v[1] # print the first entry
v[1] <- 10 # change the value of the first entry
v
```

1.7 for loops

for loops are important programming structures that allow you to repeat the same statement a number of times on different variables. The basic structure of a for loop is:

The for statement is followed by a set of parenthesis containing <variable>, which contains the name of the variable being iterated, and <set of values>, which are the values that the variable iterates over. The for loop variable is a special variable that is created by the for loop: you do not have to create it before executing the loop. This simple for loop creates the variable i, and for each value of i from 1 to 100, prints the value of i to the screen.

```
for (i in 1:100) {
   i
}
```

for loops are very powerful programming tools. We can use a for loop to create an entire *vector* of uniform random numbers, and transform them into a *second* vector of exponential random numbers.

```
for (i in 1:100) {
   u[i] ~ dnUniform(0,1)
   x[i] := - 1.0 / lambda * ln(u[i])
}
```

Close Rev using the statement q().

```
q()
```

1.8 References

References

Höhna, S., T. A. Heath, B. Boussau, M. J. Landis, F. Ronquist, and J. P. Huelsenbeck. 2014. Probabilistic graphical model representation in phylogenetics. Systematic Biology 63:753–771.

2 Exercises to the RevBayes introduction

- 1. Create a variable called z with the value 10 (z <- 10). What kind of variable is this (constant, stochastic or deterministic)?
- 2. Create a second variable y which is $y := f(z) := z^2$. What kind of variable is y? What is its value?

- 3. Change the value of z to 100. Before printing y, can you guess its value?
- 4. Write a for loop that creates 1000 random uniform numbers u and 1000 exponential random numbers x with $\lambda = 1$, as we did in the tutorial. Then, use the same random uniform numbers u to create 1000 exponential numbers y with $\lambda = 10$. Using the mean() function, compare the means of x and y. Which has a greater mean? Write your code and answer!

REVBAYES TUTORIAL — REV BASICS & REGRESSION MO	REVBAYES '	Tutorial -	— Rev	BASICS	& R1	EGRESSION	Mode
--	------------	------------	-------	--------	------	-----------	------

5. Experiment with different values of λ . How does the mean of x depend on λ ?

Version dated: January 30, 2018