

# Descongelen a Victor Moreno

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## 1 Estructuras de Datos

### 1.1 Unordered Map

```

1 #include <ext/pb_ds/assoc_container.hpp>
2 using namespace __gnu_pbds;
3
4 struct custom_hash {
5     static uint64_t splitmix64(uint64_t x) {
6         // http://xorshift.di.unimi.it/splitmix64.c
7         x += 0x9e3779b97f4a7c15;
8         x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
9         x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
10        return x ^ (x >> 31);
11    }
12
13    size_t operator()(uint64_t x) const {
14        static const uint64_t FIXED_RANDOM = chrono::steady_clock::now().
15            time_since_epoch().count();
16        return splitmix64(x + FIXED_RANDOM);
17    }
18 };
19 gp_hash_table<int, int, custom_hash> m1;
20
21 //Funcion count
22 m1.find(x) != m1.end()

```

### 1.2 Segment tree Recursivo

```

1 %%
2 %% This is file `tex',
3 %% generated with the docstrip utility.
4 %%
5 %% The original source files were:
6 %%
7 %% fileerr.dtx (with options: `return')
8 %%
9 %% This is a generated file.
10 %%
11 %% The source is maintained by the LaTeX Project team and bug
12 %% reports for it can be opened at https://latex-project.org/bugs/
13 %% (but please observe conditions on bug reports sent to that address!)

```

```

14 %%
15 %%
16 %% Copyright (C) 1993-2021
17 %% The LaTeX Project and any individual authors listed elsewhere
18 %% in this file.
19 %%
20 %% This file was generated from file(s) of the Standard LaTeX `Tools Bundle
21 %%
22 %%
23 %% -----
24 %%
25 %% It may be distributed and/or modified under the
26 %% conditions of the LaTeX Project Public License, either version 1.3c
27 %% of this license or (at your option) any later version.
28 %% The latest version of this license is in
29 %% https://www.latex-project.org/lppl.txt
30 %% and version 1.3c or later is part of all distributions of LaTeX
31 %% version 2005/12/01 or later.
32 %%
33 %% This file may only be distributed together with a copy of the LaTeX
34 %% `Tools Bundle'. You may however distribute the LaTeX `Tools Bundle'
35 %% without such generated files.
36 %%
37 %% The list of all files belonging to the LaTeX `Tools Bundle' is
38 %% given in the file `manifest.txt'.
39 %%
40 \message{File ignored}
41 \endinput
42 %%
43 %% End of file `.tex'.

```

### 1.3 Segment Tree Iterativo

```

1 //Para procesar queries de tipo k-esimo es necesario crear un arbol binario
2 //perfecto (llenar con 0's)
3 template<typename T>
4 struct SegmentTree{
5     int N;
6     vector<T> ST;
7
8     //Creacion a partir de un arreglo 0(n)
9     SegmentTree(int N, vector<T> & arr): N(N){

```

```

9     ST.resize(N << 1);
10     for(int i = 0; i < N; ++i)
11         ST[N + i] = arr[i]; //Dato normal
12     ST[N + i] = creaNodo(); //Dato compuesto
13     for(int i = N - 1; i > 0; --i)
14         ST[i] = ST[i << 1] + ST[i << 1 | 1]; //Dato normal
15         ST[i] = merge(ST[i << 1], ST[i << 1 | 1]); //Dato compuesto
16 }
17
18 //Actualizacion de un elemento en la posicion i
19 void update(int i, T value){
20     ST[i += N] = value; //Dato normal
21     ST[i += N] = creaNodo(); //Dato compuesto
22     while(i >= 1)
23         ST[i] = ST[i << 1] + ST[i << 1 | 1]; //Dato normal
24         ST[i] = merge(ST[i << 1], ST[i << 1 | 1]); //Dato compuesto
25 }
26
27 //query en [l, r]
28 T query(int l, int r){
29     T res = 0; //Dato normal
30     nodo resl = creaNodo(), resr = creaNodo(); //Dato compuesto
31     for(l += N, r += N; l <= r; l >= 1, r >= 1){
32         if(l & 1) res += ST[l++]; //Dato normal
33         if(!(r & 1)) res += ST[r--]; //Dato normal
34
35         if(l & 1) resl = merge(resl, ST[l++]); //Dato compuesto
36         if(!(r & 1)) resr = merge(ST[r--], resr); //Dato compuesto
37     }
38     return res; //Dato normal
39     return merge(resl, resr); //Dato compuesto
40 }
41
42 //Para estas queries es necesario que el st tenga el tam de la siguiente
43 //potencia de 2
44 //ll nT = 1;
45 // while(nT<n) nT<=1;
46 //vector<int> a(nT,0);
47
48 //Encontrar k-esimo 1 en un st de 1's
49 int Kth_One(int k) {
50     int i = 0, s = N >> 1;
51     for(int p = 2; p < 2 * N; p <= 1, s >= 1) {

```

```

51     if(k < ST[p]) continue;
52     k -= ST[p++]; i += s;
53 }
54 return i;
55 }
56
57 //i del primer elemento >= k en todo el arr
58 int atLeastX(int k){
59     int i = 0, s = N >> 1;
60     for(int p = 2; p < 2 * N; p <= 1, s >= 1) {
61         if(ST[p] < k) p++, i += s;
62     }
63     if(ST[N + i] < k) i = -1;
64     return i;
65 }
66
67 //i del primer elemento >= k en [l,fin]
68 //Uso atLeastX(k,l,1,nT)
69 int atLeastX(int x, int l, int p, int s) {
70     if(ST[p] < x or s <= 1) return -1;
71     if((p << 1) >= 2 * N)
72         return (ST[p] >= x) - 1;
73     int i = atLeastX(x, l, p << 1, s >> 1);
74     if(i != -1) return i;
75     i = atLeastX(x, l - (s >> 1), p << 1 | 1, s >> 1);
76     if(i == -1) return -1;
77     return (s >> 1) + i;
78 }
79 };

```

## 1.4 Segment Tree Lazy Recursivo

```

1 %%
2 %% This is file `tex',
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4 %%
5 %% The original source files were:
6 %%
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```

```

12 %% reports for it can be opened at https://latex-project.org/bugs/
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14 %%
15 %%
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34 %% without such generated files.
35 %%
36 %% The list of all files belonging to the LaTeX `Tools Bundle' is
37 %% given in the file `manifest.txt'.
38 %%
39 \message{File ignored}
40 \endinput
41 %% End of file `tex'.

```

## 1.5 Segment Tree Lazy Iterativo

```

1 //Lazy propagation con incremento de u en rango y minimo
2 //Hay varias modificaciones necesarias para suma en ambos
3 template<typename T>
4 struct SegmentTreeLazy{
5     int N,h;
6     vector<T> ST, d;
7

```

```

8 //Creacion a partir de un arreglo
9 SegmentTreeLazy(int n, vector<T> &a): N(n){
10     //En caso de inicializar en cero o algo similar, revisar que la
        construccion tenga su respectivo neutro mult y 1
11     ST.resize(N << 1);
12     d.resize(N);
13     h = 64 - __builtin_clzll(n);
14
15     for(int i = 0; i < N; ++i)
16         ST[N + i] = a[i];
17     //Construir el st sobre la query que se necesita
18     for(int i = N - 1; i > 0; --i)
19         ST[i] = min(ST[i << 1] , ST[i << 1 | 1]);
20 }
21
22 //Modificar de acuerdo al tipo modificacion requerida, +,*,|,^,etc
23 void apply(int p, T value) {
24     ST[p] += value;
25     if(p<N) d[p] += value;
26 }
27
28 // Modifica valores de los padres de p
29 //Modificar de acuerdo al tipo modificacion requerida, +,*,|,^,etc y a la
        respectiva query
30 void build(int p){
31     while(p>1){
32         p >>= 1;
33         ST[p] = min(ST[p << 1], ST[p << 1 | 1]) + d[p];
34         //ST[p] = (ST[p << 1] & ST[p << 1 | 1]) | d[p]; Ejemplos con bitwise
35     }
36 }
37
38 // Propagacion desde la raiz a p
39 void push(int p){
40     for (int s = h; s > 0; --s) {
41         int i = p >> s;
42         if (d[i] != 0) {
43             apply(i << 1, d[i]);
44             apply(i << 1 | 1, d[i]);
45             d[i] = 0; //Tener cuidado si estoy haciendo multiplicaciones
46         }
47     }
48 }

```

```

49
50 // Sumar v a cada elemento en el intervalo [l, r)
51 void increment(int l, int r, T value) {
52     l += N, r += N;
53     int l0 = l, r0 = r;
54     for (; l < r; l >>= 1, r >>= 1) {
55         if(l & 1) apply(l++, value);
56         if(r & 1) apply(--r, value);
57     }
58     build(l0);
59     build(r0 - 1);
60 }
61
62 // min en el intervalo [l, r)
63 T range_min(int l, int r) {
64     l += N, r += N;
65     push(l);
66     push(r - 1);
67     T res = LLONG_MAX;
68     //T res = (1 << 30) - 1;    Requerir operacion and
69     for (; l < r; l >>= 1, r >>= 1) {
70         if(l & 1) res = min(res, ST[l++]);
71         //if(res >= mod) res -= mod;
72         if(r & 1) res = min(res, ST[--r]);
73         //if(res >= mod) res -= mod;
74     }
75     return res;
76 }
77
78 };

```

## 1.6 Rope

```

1 #include <ext/rope>
2 using namespace __gnu_cxx;
3 rope<int> s;
4 // Sequence with O(log(n)) random access, insert, erase at any position
5 // s.push_back(x);
6 // s.insert(i,r) // insert rope r at position i
7 // s.erase(i,k) // erase subsequence [i,i+k)
8 // s.substr(i,k) // return new rope corresponding to subsequence [i,i+k)
9 // s[i] // access ith element (cannot modify)
10 // s.mutable_reference_at(i) // acces ith element (allows modification)

```

```
11 // s.begin() and s.end() are const iterators (use mutable_begin(),
    mutable_end() to allow modification)
```

## 1.7 Ordered Set

```
1 #include<ext/pb_ds/assoc_container.hpp>
2 #include<ext/pb_ds/tree_policy.hpp>
3 using namespace __gnu_pbds;
4 typedef tree<int,null_type,less<int>,rb_tree_tag,
    tree_order_statistics_node_update> ordered_set;
5 // find_by_order(i) -> iterator to ith element
6 // order_of_key(k) -> position (int) of lower_bound of k
```

## 1.8 Union Find

```
1 vector<pair<int,int>>ds(MAX,{-1,0});
2 // Solo siu requieres los elementos del union find, utiliza
3 // dsext en caso contrario borrarlo
4 list<int>dsext[MAX];
5 void init(int n){
6     for(int i=0;i<n;i++)dsext[i].push_back(i);
7 }
8 int find(int x){
9     if(-1==ds[x].first) return x;
10    return ds[x].first=find(ds[x].first);
11 }
12 bool unionDs(int x, int y){
13     int px=find(x),py=find(y);
14     int &rx=ds[px].second,&ry=ds[py].second;
15     if(px==py) return false;
16     else{
17         if(rx>ry){
18             ds[py].first=px;
19         }
20         else{
21             ds[px].first=py;
22             if(rx==ry) ry+=1;
23         }
24     }
25     return true;
26 }
```

## 1.9 Segment Tree Persistente

```
1 #define inf INT_MAX
2 const int MAX=5e5+2;
3 typedef pair<ll, ll> item;
4 struct node{
5     item val;
6     node *l, *r;
7     node(): l(nullptr),r(nullptr),val({inf,inf}){};
8     node(node *l,node *r):l(_l),r(_r){
9         val=min(l->val,r->val);
10    }
11    node(ll value,ll pos):r(nullptr),l(nullptr){
12        val=make_pair(value,pos);
13    }
14 };
15 pair<ll,ll>all;
16 vector<node*>versions(MAX,nullptr);
17 node* build(int l,int r){
18     if(l==r)return new node(inf,l);
19     int m=(l+r)/2;
20     return new node(build(l,m),build(m+1,r));
21 }
22
23 node* update(node *root,int l,int r,int pos,int val){
24     if(l==r){
25         return new node(val,pos);}
26     int m=(l+r)/2;
27     if(pos<=m) return new node(update(root->l,l,m,pos,val),root->r);
28     return new node(root->l,update(root->r,m+1,r,pos,val));
29 }
30 item query(node *root,int l,int r,int a,int b){
31     if(a>r || b<l) return all;
32     if(a<=l && r<=b) return root->val;
33     int m=(l+r)/2;
34     return min(query(root->l,l,m,a,b),query(root->r,m+1,r,a,b));
35 }
```

## 1.10 Sparce Table

```
1 //Se usa para RMQ porque se puede hacer en O(1), no acepta updates
2 vector<int>lg;
3 vector<vector<int>>>st;
4 int *nums;
5 void init(int n){
```

```

6   int logn=(int) log2(n)+1;
7   lg.assign(n+1,0);
8   st.assign(logn,vector<int>(n+1));
9   for(int i=0;i<n;i++) st[0][i]=nums[i];
10  lg[1]=0;
11  for(int i=2;i<=n;i++) lg[i]=lg[i/2]+1;
12  for(int i=1;i<logn;i++)
13      for(int j=0;j+(1<<i)<n;j++)st[i][j]=min(st[i-1][j],st[i-1][j+(1<<(i-1))]);
14 }
15 int query(int a,int b){
16     int logn=lg[(b-a+1)];
17     cout<<st[logn][a]<<endl;
18     return min(st[logn][a],st[logn][b-(1<<logn)+1]);
19 }

```

### 1.11 Walvet Tree

```

1 // indexed in 1
2 // from pointer to first element and to to end
3 // x and y The minimum element and y the max element
4 // If you need only one function or more erase the others
5 // If you need tu construct other function you only required to undertand
6 // the limit, this
7 // are the same
8 struct wavelet_tree{
9     int lo, hi;
10    wavelet_tree *l, *r;
11    vector<int> b;
12    wavelet_tree(int *from, int *to, int x, int y){
13        lo = x, hi = y;
14        if(lo == hi or from >= to) return;
15        int mid = (lo+hi)/2;
16        auto f = [mid](int x){ return x <= mid;};
17        b.reserve(to-from+1);
18        b.pb(0);
19        for(auto it = from; it != to; it++)
20            b.push_back(b.back() + f(*it));
21        auto pivot = stable_partition(from, to, f);
22        l = new wavelet_tree(from, pivot, lo, mid);
23        r = new wavelet_tree(pivot, to, mid+1, hi);
24    }
25 //kth smallest element in [l, r]

```

```

25 int kth(int l, int r, int k){
26     if(l > r) return 0;
27     if(lo == hi) return lo;
28     int inLeft = b[r] - b[l-1];
29     int lb = b[l-1];
30     int rb = b[r];
31     if(k <= inLeft) return this->l->kth(lb+1, rb, k);
32     return this->r->kth(l-lb, r-rb, k-inLeft);
33 }
34 //count of nos in [l, r] Less than or equal to k
35 int LTE(int l, int r, int k) {
36     if(l > r or k < lo) return 0;
37     if(hi <= k) return r - l + 1;
38     int lb = b[l-1], rb = b[r];
39     return this->l->LTE(lb+1, rb, k) + this->r->LTE(l-lb, r-rb, k);
40 }
41 //count of nos in [l, r] equal to k
42 int count(int l, int r, int k) {
43     if(l > r or k < lo or k > hi) return 0;
44     if(lo == hi) return r - l + 1;
45     int lb = b[l-1], rb = b[r], mid = (lo+hi)/2;
46     if(k <= mid) return this->l->count(lb+1, rb, k);
47     return this->r->count(l-lb, r-rb, k);
48 }
49 };

```

## 2 Strings

### 2.1 Aho Corasick

```

1 int K, I = 1;
2 struct node {
3     int fail, ch[26] = {};
4     vector<int> lens;
5 } T[500005];
6
7 void add(string s) {
8     int x = 1;
9     for (int i = 0; i < s.size(); i++) {
10         if (T[x].ch[s[i] - 'a'] == 0)
11             T[x].ch[s[i] - 'a'] = ++I;
12         x = T[x].ch[s[i] - 'a'];
13     }

```

```

14     T[x].lens.PB(s.size());
15 }
16
17 void build() {
18     queue<int> Q;
19     int x = 1;
20     T[1].fail = 1;
21     for (int i = 0; i < 26; i++) {
22         if (T[x].ch[i])
23             T[T[x].ch[i]].fail = x, Q.push(T[x].ch[i]);
24         else
25             T[x].ch[i] = 1;
26     }
27     while (!Q.empty()) {
28         x = Q.front(); Q.pop();
29         for (int i = 0; i < 26; i++) {
30             if (T[x].ch[i])
31                 T[T[x].ch[i]].fail = T[T[x].fail].ch[i], Q.push(T[x].ch[i]);
32             else
33                 T[x].ch[i] = T[T[x].fail].ch[i];
34         }
35     }
36 }

```

## 2.2 Hashing

```

1 struct Hash{
2     const int mod=1e9+123;
3     const int p=257;
4     vector<int> prefix;
5     static vector<int> pow;
6     Hash(string str){
7         int n=str.size();
8         while(pow.size()<=n){
9             pow.push_back(1LL*pow.back()*p%mod);
10        }
11        vector<int> aux(n+1);
12        prefix=aux;
13        for(int i=0;i<n;i++){
14            prefix[i+1]=(prefix[i]+1LL*str[i]*pow[i])%mod;
15        }
16    }

```

```

17 inline int getHashInInterval(int i,int len,int MxPow){
18     int hashing=prefix[i+len]-prefix[i];
19     if(hashing<0) hashing+=mod;
20     hashing=1LL*hashing*pow[MxPow-(len+i-1)]%mod;
21     return hashing;
22 }
23 };
24 vector<int> Hash::pow{1};

```

## 2.3 KMP

```

1 vector<int> kmp(string s){
2     int n=s.size();
3     vector<int> pi(n);
4     for(int i=1;i<n;i++){
5         int j=pi[i-1];
6         while(j>0 && s[i]!=s[j])j=pi[j-1];
7         if(s[i]==s[j]) j++;
8         pi[i]=j;
9     }
10    return pi;
11 }

```

## 2.4 Manacher

```

1 vector<int> manacher_odd(string s) {
2     int n = s.size();
3     s = "$" + s + "~";
4     vector<int> p(n + 2);
5     int l = 1, r = 1;
6     for(int i = 1; i <= n; i++) {
7         p[i] = max(0, min(r - i, p[l + (r - i)]));
8         while(s[i - p[i]] == s[i + p[i]]) {
9             p[i]++;
10        }
11        if(i + p[i] > r) {
12            l = i - p[i], r = i + p[i];
13        }
14    }
15    return vector<int>(begin(p) + 1, end(p) - 1);
16 }
17 vector<int> manacher_even(string s){
18     string even;
19     for(auto c:s){

```

```

20     even+='#'+c;
21 }
22     even+='#';
23     return manacher_odd(even);
24 }

```

## 2.5 Suffix Automata

```

1 struct node{
2     map<char,int>edges;
3     int link,length,terminal=0;
4     node(int link,int length): link(link),length(length){};
5 };vector<node>sa;
6 // init in main with sa.push_back(node(-1,0));
7 int last=0;
8 // add one by one chars in order
9 void addChar(char s, int pos){
10     sa.push_back(node(0,pos+1));
11     int r=sa.size()-1;
12     int p=last;
13     while(p >= 0 && sa[p].edges.find(s) == sa[p].edges.end()) {
14         sa[p].edges[s] = r;
15         p = sa[p].link;
16     }
17     if(p != -1) {
18         int q = sa[p].edges[s];
19         if(sa[p].length + 1 == sa[q].length) {
20             sa[r].link = q;
21         } else {
22             sa.push_back(node(sa[q].link,sa[p].length+1));
23             sa[sa.size()-1].edges=sa[q].edges;
24             int qq = sa.size()-1;
25             sa[q].link = qq;
26             sa[r].link= qq;
27             while(p >= 0 && sa[p].edges[s] == q) {
28                 sa[p].edges[s] = qq;
29                 p = sa[p].link;
30             }
31         }
32     }
33     last = r;
34 }
35 // Not necessary functions

```

```

36 void findTerminals(){
37     int p = last;
38     while(p > 0) {
39         sa[p].terminal=1;
40         p = sa[p].link;
41     }
42 }

```

## 2.6 Trie

```

1 struct trie{
2     int len,id;
3     int children[26];
4     trie(int _id){
5         len=0,id=_id;
6         for(int i=0;i<26;i++)children[i]=-1;
7     }
8 };vector<trie>Trie;Trie.push_back(trie());
9 void insertString(string str,int root){
10     int aux=root;
11     for(int i=0;i<str.size();i++){
12         int index=str[i]-'a';
13         if(Trie[aux].children[index]==-1){
14             Trie.push_back(trie(Trie.size()));
15             Trie[aux].children[index]=Trie.size()-1;
16         }
17         aux=Trie[aux].children[index];
18     }
19     Trie[aux].len=str.size();
20 }
21 bool existInTrie(string str,int root){
22     int aux=root;
23     for(int i=0;i<str.size();i++){
24         int index=str[i]-'a';
25         if(Trie[aux].children[index]==-1) return false;
26         aux=Trie[aux].children[index];
27     }
28     return Trie[aux].len;
29 }

```

## 3 Geometria

### 3.1 Puntos y lineas



```

1 using ld = long double;
2 const ld eps = 1e-9, inf = numeric_limits<ld>::max(), pi = acos(-1);
3 // For use with integers, just set eps=0 and everything remains the same
4 bool geq(ld a, ld b){return a-b >= -eps;} //a >= b
5 bool leq(ld a, ld b){return b-a >= -eps;} //a <= b
6 bool ge(ld a, ld b){return a-b > eps;} //a > b
7 bool le(ld a, ld b){return b-a > eps;} //a < b
8 bool eq(ld a, ld b){return abs(a-b) <= eps;} //a == b
9 bool neq(ld a, ld b){return abs(a-b) > eps;} //a != b
10
11 struct point{
12     ld x, y;
13     point(): x(0), y(0){}
14     point(ld x, ld y): x(x), y(y){}
15
16     point operator+(const point & p) const{return point(x + p.x, y + p.y);}
17     point operator-(const point & p) const{return point(x - p.x, y - p.y);}
18     point operator*(const ld & k) const{return point(x * k, y * k);}
19     point operator/(const ld & k) const{return point(x / k, y / k);}
20
21     point operator+=(const point & p){*this = *this + p; return *this;}
22     point operator-=(const point & p){*this = *this - p; return *this;}
23     point operator*=(const ld & p){*this = *this * p; return *this;}
24     point operator/=(const ld & p){*this = *this / p; return *this;}
25
26     point rotate(const ld & a) const{return point(x*cos(a) - y*sin(a), x*sin(
27         a) + y*cos(a));}
28     point perp() const{return point(-y, x);}
29     ld ang() const{
30         ld a = atan2l(y, x); a += le(a, 0) ? 2*pi : 0; return a;
31     }
32     ld dot(const point & p) const{return x * p.x + y * p.y;}
33     ld cross(const point & p) const{return x * p.y - y * p.x;}
34     ld norm() const{return x * x + y * y;}
35     ld length() const{return sqrtl(x * x + y * y);}
36     point unit() const{return (*this) / length();}
37
38     bool operator==(const point & p) const{return eq(x, p.x) && eq(y, p.y);}
39     bool operator!=(const point & p) const{return !(*this == p);}
40     bool operator<(const point & p) const{return le(x, p.x) || (eq(x, p.x) &&
41         le(y, p.y));}
42     bool operator>(const point & p) const{return ge(x, p.x) || (eq(x, p.x) &&
43         ge(y, p.y));}

```

```

41     bool half(const point & p) const{return le(p.cross(*this), 0) || (eq(p.
42         cross(*this), 0) && le(p.dot(*this), 0));}
43 };
44 istream &operator>>(istream &is, point & p){return is >> p.x >> p.y;}
45 ostream &operator<<(ostream &os, const point & p){return os << "(" << p.x
46     << ", " << p.y << ")};
47
48 int sgn(ld x){
49     if(ge(x, 0)) return 1;
50     if(le(x, 0)) return -1;
51     return 0;
52 }
53
54 void polarSort(vector<point> & P, const point & o, const point & v){
55     //sort points in P around o, taking the direction of v as first angle
56     sort(P.begin(), P.end(), [&](const point & a, const point & b){
57         return point((a - o).half(v), 0) < point((b - o).half(v), (a - o).cross
58             (b - o));
59     });
60 }
61
62 bool pointInLine(const point & a, const point & v, const point & p){
63     //line a+tv, point p
64     return eq((p - a).cross(v), 0);
65 }
66
67 bool pointInSegment(const point & a, const point & b, const point & p){
68     //segment ab, point p
69     return pointInLine(a, b - a, p) && leq((a - p).dot(b - p), 0);
70 }
71
72 int intersectLinesInfo(const point & a1, const point & v1, const point & a2
73     , const point & v2){
74     //lines a1+tv1 and a2+tv2
75     ld det = v1.cross(v2);
76     if(eq(det, 0)){
77         if(eq((a2 - a1).cross(v1), 0)){
78             return -1; //infinity points
79         }else{
80             return 0; //no points
81         }
82     }else{
83

```

```

80     return 1; //single point
81 }
82 }
83
84 point intersectLines(const point & a1, const point & v1, const point & a2,
85     const point & v2){
86     //lines a1+tv1, a2+tv2
87     //assuming that they intersect
88     ld det = v1.cross(v2);
89     return a1 + v1 * ((a2 - a1).cross(v2) / det);
90 }
91
92 int intersectLineSegmentInfo(const point & a, const point & v, const point
93     & c, const point & d){
94     //line a+tv, segment cd
95     point v2 = d - c;
96     ld det = v.cross(v2);
97     if(eq(det, 0)){
98         if(eq((c - a).cross(v), 0)){
99             return -1; //infinity points
100         }else{
101             return 0; //no point
102         }
103     }else{
104         return sgn(v.cross(c - a)) != sgn(v.cross(d - a)); //1: single point,
105         0: no point
106     }
107 }
108
109 int intersectSegmentsInfo(const point & a, const point & b, const point & c
110     , const point & d){
111     //segment ab, segment cd
112     point v1 = b - a, v2 = d - c;
113     int t = sgn(v1.cross(c - a)), u = sgn(v1.cross(d - a));
114     if(t == u){
115         if(t == 0){
116             if(pointInSegment(a, b, c) || pointInSegment(a, b, d) ||
117                 pointInSegment(c, d, a) || pointInSegment(c, d, b)){
118                 return -1; //infinity points
119             }else{
120                 return 0; //no point
121             }
122         }else{
123             return 0; //no point
124         }
125     }
126 }

```

```

118     return 0; //no point
119 }
120 }else{
121     return sgn(v2.cross(a - c)) != sgn(v2.cross(b - c)); //1: single point,
122     0: no point
123 }
124 }
125
126 ld distancePointLine(const point & a, const point & v, const point & p){
127     //line: a + tv, point p
128     return abs(v.cross(p - a)) / v.length();
129 }

```

### 3.2 Circulos

```

1 ld distancePointCircle(const point & c, ld r, const point & p){
2     //point p, circle with center c and radius r
3     return max((ld)0, (p - c).length() - r);
4 }
5
6 point projectionPointCircle(const point & c, ld r, const point & p){
7     //point p (outside the circle), circle with center c and radius r
8     return c + (p - c).unit() * r;
9 }
10
11 pair<point, point> pointsOfTangency(const point & c, ld r, const point & p)
12 {
13     //point p (outside the circle), circle with center c and radius r
14     point v = (p - c).unit() * r;
15     ld d2 = (p - c).norm(), d = sqrt(d2);
16     point v1 = v * (r / d), v2 = v.perp() * (sqrt(d2 - r*r) / d);
17     return {c + v1 - v2, c + v1 + v2};
18 }
19
20 vector<point> intersectLineCircle(const point & a, const point & v, const
21     point & c, ld r){
22     //line a+tv, circle with center c and radius r
23     ld h2 = r*r - v.cross(c - a) * v.cross(c - a) / v.norm();
24     point p = a + v * v.dot(c - a) / v.norm();
25     if(eq(h2, 0)) return {p}; //line tangent to circle
26     else if(1e(h2, 0)) return {}; //no intersection
27     else{
28         point u = v.unit() * sqrt(h2);

```

```

27     return {p - u, p + u}; //two points of intersection (chord)
28 }
29 }
30
31 vector<point> intersectSegmentCircle(const point & a, const point & b,
    const point & c, ld r){
32     //segment ab, circle with center c and radius r
33     vector<point> P = intersectLineCircle(a, b - a, c, r), ans;
34     for(const point & p : P){
35         if(pointInSegment(a, b, p)) ans.push_back(p);
36     }
37     return ans;
38 }
39
40 pair<point, ld> getCircle(const point & m, const point & n, const point & p
    ){
41     //find circle that passes through points p, q, r
42     point c = intersectLines((n + m) / 2, (n - m).perp(), (p + n) / 2, (p - n
        ).perp());
43     ld r = (c - m).length();
44     return {c, r};
45 }
46
47 vector<point> intersectionCircles(const point & c1, ld r1, const point & c2
    , ld r2){
48     //circle 1 with center c1 and radius r1
49     //circle 2 with center c2 and radius r2
50     point d = c2 - c1;
51     ld d2 = d.norm();
52     if(eq(d2, 0)) return {}; //concentric circles
53     ld pd = (d2 + r1*r1 - r2*r2) / 2;
54     ld h2 = r1*r1 - pd*pd/d2;
55     point p = c1 + d*pd/d2;
56     if(eq(h2, 0)) return {p}; //circles touch at one point
57     else if(le(h2, 0)) return {}; //circles don't intersect
58     else{
59         point u = d.perp() * sqrt(h2/d2);
60         return {p - u, p + u};
61     }
62 }
63
64 int circleInsideCircle(const point & c1, ld r1, const point & c2, ld r2){
65     //test if circle 2 is inside circle 1

```

```

66     //returns "-1" if 2 touches internally 1, "1" if 2 is inside 1, "0" if
        they overlap
67     ld l = r1 - r2 - (c1 - c2).length();
68     return (ge(l, 0) ? 1 : (eq(l, 0) ? -1 : 0));
69 }
70
71 int circleOutsideCircle(const point & c1, ld r1, const point & c2, ld r2){
72     //test if circle 2 is outside circle 1
73     //returns "-1" if they touch externally, "1" if 2 is outside 1, "0" if
        they overlap
74     ld l = (c1 - c2).length() - (r1 + r2);
75     return (ge(l, 0) ? 1 : (eq(l, 0) ? -1 : 0));
76 }
77
78 int pointInCircle(const point & c, ld r, const point & p){
79     //test if point p is inside the circle with center c and radius r
80     //returns "0" if it's outside, "-1" if it's in the perimeter, "1" if it's
        inside
81     ld l = (p - c).length() - r;
82     return (le(l, 0) ? 1 : (eq(l, 0) ? -1 : 0));
83 }
84
85 vector<vector<point>> tangents(const point & c1, ld r1, const point & c2,
    ld r2, bool inner){
86     //returns a vector of segments or a single point
87     if(inner) r2 = -r2;
88     point d = c2 - c1;
89     ld dr = r1 - r2, d2 = d.norm(), h2 = d2 - dr*dr;
90     if(eq(d2, 0) || le(h2, 0)) return {};
91     point v = d*dr/d2;
92     if(eq(h2, 0)) return {{c1 + v*r1}};
93     else{
94         point u = d.perp()*sqrt(h2)/d2;
95         return {{c1 + (v - u)*r1, c2 + (v - u)*r2}, {c1 + (v + u)*r1, c2 + (v +
            u)*r2}};
96     }
97 }
98
99 ld signed_angle(const point & a, const point & b){
100     return sgn(a.cross(b)) * acosl(a.dot(b) / (a.length() * b.length()));
101 }
102
103 ld intersectPolygonCircle(const vector<point> & P, const point & c, ld r){

```

```

104 //Gets the area of the intersection of the polygon with the circle
105 int n = P.size();
106 ld ans = 0;
107 for(int i = 0; i < n; ++i){
108     point p = P[i], q = P[(i+1)%n];
109     bool p_inside = (pointInCircle(c, r, p) != 0);
110     bool q_inside = (pointInCircle(c, r, q) != 0);
111     if(p_inside && q_inside){
112         ans += (p - c).cross(q - c);
113     }else if(p_inside && !q_inside){
114         point s1 = intersectSegmentCircle(p, q, c, r)[0];
115         point s2 = intersectSegmentCircle(c, q, c, r)[0];
116         ans += (p - c).cross(s1 - c) + r*r * signed_angle(s1 - c, s2 - c);
117     }else if(!p_inside && q_inside){
118         point s1 = intersectSegmentCircle(c, p, c, r)[0];
119         point s2 = intersectSegmentCircle(p, q, c, r)[0];
120         ans += (s2 - c).cross(q - c) + r*r * signed_angle(s1 - c, s2 - c);
121     }else{
122         auto info = intersectSegmentCircle(p, q, c, r);
123         if(info.size() <= 1){
124             ans += r*r * signed_angle(p - c, q - c);
125         }else{
126             point s2 = info[0], s3 = info[1];
127             point s1 = intersectSegmentCircle(c, p, c, r)[0];
128             point s4 = intersectSegmentCircle(c, q, c, r)[0];
129             ans += (s2 - c).cross(s3 - c) + r*r * (signed_angle(s1 - c, s2 - c)
130                 + signed_angle(s3 - c, s4 - c));
131         }
132     }
133     return abs(ans)/2;
134 }

```

### 3.3 Poligonos

```

1 ld perimeter(vector<point> & P){
2     int n = P.size();
3     ld ans = 0;
4     for(int i = 0; i < n; i++){
5         ans += (P[i] - P[(i + 1) % n]).length();
6     }
7     return ans;
8 }

```

```

9
10 ld area(vector<point> & P){
11     int n = P.size();
12     ld ans = 0;
13     for(int i = 0; i < n; i++){
14         ans += P[i].cross(P[(i + 1) % n]);
15     }
16     return abs(ans / 2);
17 }
18
19 vector<point> convexHull(vector<point> P){
20     sort(P.begin(), P.end());
21     vector<point> L, U;
22     for(int i = 0; i < P.size(); i++){
23         while(L.size() >= 2 && leq((L[L.size() - 2] - P[i]).cross(L[L.size() -
24             1] - P[i]), 0)){
25             L.pop_back();
26         }
27         L.push_back(P[i]);
28     }
29     for(int i = P.size() - 1; i >= 0; i--){
30         while(U.size() >= 2 && leq((U[U.size() - 2] - P[i]).cross(U[U.size() -
31             1] - P[i]), 0)){
32             U.pop_back();
33         }
34         U.push_back(P[i]);
35     }
36     L.pop_back();
37     U.pop_back();
38     L.insert(L.end(), U.begin(), U.end());
39     return L;
40 }
41
42 bool pointInPerimeter(const vector<point> & P, const point & p){
43     int n = P.size();
44     for(int i = 0; i < n; i++){
45         if(pointInSegment(P[i], P[(i + 1) % n], p)){
46             return true;
47         }
48     }
49     return false;
50 }

```

```

50 bool crossesRay(const point & a, const point & b, const point & p){
51     return (geq(b.y, p.y) - geq(a.y, p.y)) * sgn((a - p).cross(b - p)) > 0;
52 }
53
54 int pointInPolygon(const vector<point> & P, const point & p){
55     if(pointInPerimeter(P, p)){
56         return -1; //point in the perimeter
57     }
58     int n = P.size();
59     int rays = 0;
60     for(int i = 0; i < n; i++){
61         rays += crossesRay(P[i], P[(i + 1) % n], p);
62     }
63     return rays & 1; //0: point outside, 1: point inside
64 }
65
66 //point in convex polygon in O(log n)
67 //make sure that P is convex and in ccw
68 //before the queries, do the preprocess on P:
69 // rotate(P.begin(), min_element(P.begin(), P.end()), P.end());
70 // int right = max_element(P.begin(), P.end()) - P.begin();
71 //returns 0 if p is outside, 1 if p is inside, -1 if p is in the perimeter
72 int pointInConvexPolygon(const vector<point> & P, const point & p, int
    right){
73     if(p < P[0] || P[right] < p) return 0;
74     int orientation = sgn((P[right] - P[0]).cross(p - P[0]));
75     if(orientation == 0){
76         if(p == P[0] || p == P[right]) return -1;
77         return (right == 1 || right + 1 == P.size()) ? -1 : 1;
78     }else if(orientation < 0){
79         auto r = lower_bound(P.begin() + 1, P.begin() + right, p);
80         int det = sgn((p - r[-1]).cross(r[0] - r[-1])) - 1;
81         if(det == -2) det = 1;
82         return det;
83     }else{
84         auto l = upper_bound(P.rbegin(), P.rend() - right - 1, p);
85         int det = sgn((p - l[0]).cross((l == P.rbegin() ? P[0] : l[-1]) - l[0])
            ) - 1;
86         if(det == -2) det = 1;
87         return det;
88     }
89 }
90

```

```

91 vector<point> cutPolygon(const vector<point> & P, const point & a, const
    point & v){
92     //returns the part of the convex polygon P on the left side of line a+tv
93     int n = P.size();
94     vector<point> lhs;
95     for(int i = 0; i < n; ++i){
96         if(geq(v.cross(P[i] - a), 0)){
97             lhs.push_back(P[i]);
98         }
99         if(intersectLineSegmentInfo(a, v, P[i], P[(i+1)%n]) == 1){
100             point p = intersectLines(a, v, P[i], P[(i+1)%n] - P[i]);
101             if(p != P[i] && p != P[(i+1)%n]){
102                 lhs.push_back(p);
103             }
104         }
105     }
106     return lhs;
107 }

```

## 4 Varios

### 4.1 Template

```

1  #include<bits/stdc++.h>
2  using namespace std;
3
4  #define forn(i,n)      for(int i=0; i<n; i++)
5  #define forr(i,a,n)    for(int i=a; i<n; i++)
6  #define fore(i,a,n)    for(int i=a; i<=n; i++)
7  #define each(a,b)      for(auto a: b)
8  #define all(v)          v.begin(),v.end()
9  #define sz(a)           (int)a.size()
10 #define debln(a)         cout << a << "\n"
11 #define deb(a)           cout << a << " "
12 #define pb               push_back
13
14 typedef long long ll;
15 typedef vector<int> vi;
16 typedef pair<int,int> ii;
17
18 void sol(){
19
20 }

```

```
21
22 int main(){
23     ios::sync_with_stdio(false);cin.tie(0);
24
25     int t=1;
26     cin>>t;
27     while(t--){
28         sol();
29     }
30
31     return 0;
32 }
```

## 4.2 String a vector<int>

```
1 //Convertir una cadena de numeros separados por " " en vector de enteros
2 //Leer varias de esas querys
3 cin.ignore();
4 while(q--){
5     string s;
6     getline(cin, s);
7     vector<int> qr;
8     stringstream ss(s);
9     int num;
10    while (ss >> num)    qr.push_back(num);
11 }
```

## 4.3 Generar permutaciones

```
1 //Generar todas las permutaciones de un arreglo
2 sort(all(a));
3 do{
4     //hacer lo que quieras con la perm generada
5 }while(next_permutation(all(a)));
```