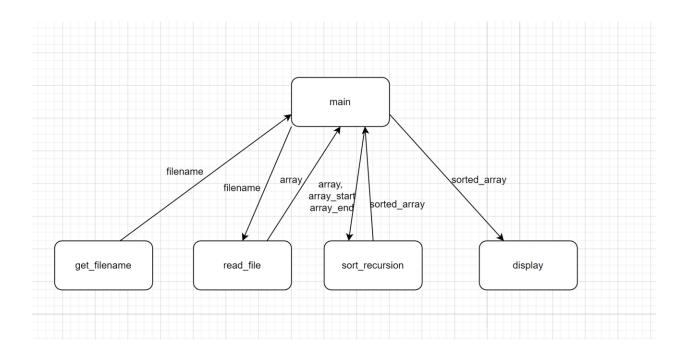
```
Sort_recursive(i_start, i_end)
        Global array
        i_up = i_start
        i_down = i_end
        i_pivot = (i_start + i_end) / 2
        WHILE i_up < i_down
                IF array[i_up] < array[i_pivot] and array[i_down] > array[i_pivot]:
                        i_up++
                        i_down- -
                ELSE IF array[i_up] >= array[i_pivot] and array[i_down] > array[i_pivot]
                        i_down- -
                ELSE IF array[i_up] < array[i_pivot] and array[i_down] < array[i_pivot]</pre>
                        i_up++
                ELSE IF array[i_up] >= array[i_pivot] and array[i_down] < array[i_pivot]</pre>
                        array[i_up], array[i_down] = array[i_down], array[i_up]
                        IF i_up == i_pivot
                                 i_pivot = i_down
                                i_up ++
                        ELSE IF i_down == i_pivot
                                 i_pivot = i_up
                                 i_down++
                        ELSE
                                 i_up++
                                 i_down++
                IF i_start < i_end
                        Sort_recursive(i_start, i_pivot - 1)
                        Sort_recursive(i_pivot + 1, i_end)
                ELSE
```

RETURN

Algorithm Metrics:

O(3n), So the while loop is iterative in nature which causes it to be O(n), the recursive function is called twice at the end of the loop so that's 2 O(n) 's, thereby meaning that there are 3 O(n) or in other words O(3n).



Modularization Metrics:

get_filename:

Strong Cohesion, only gets the filename and returns it

Trivial Coupling, doesn't receive any data

read_file:

Strong Cohesion, only reads the file and returns it

Simple Coupling, receives one parameter and passes a variable based off of that parameter

sort_recursion:

Strong Cohesion, only sorts the list by means of recursion

Interactive Coupling, Due to the function calling itself several times and passing the parameters it received into itself on the recursion it should technically be Interactive

display:

Strong Cohesion, only displays the results of the sort

Simple Coupling, Receives one parameter from main

Test Cases:

- 1. [1,5,2,3,4,8,6,45,3,3,15,33,10,500,300,34,23,12,45,67]
- 2. [12, 20, 40, 19, 10]
- [0, 0, 0, 0]
- 4. [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]
- 5. [1]

Trace:

Context: I put a trace into the program I wrote and this is how it popped out, Called is everytime that the function is called and Iteration should keep track of how many times the while loop goes through, there's 30 something pages of results so good luck with that:

```
i_end: 10
i_pivot: 9

Iteration: 1
i_up: 8
i_down: 10
i_pivot: 9

[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]

Block 1

Called -------
```

i_start: 8
i_end: 8
i_pivot: 8
Called
i_start: 10
i_end: 10
i_pivot: 10
Called
i_start: 12
i_end: 19
i_pivot: 15
Iteration: 1
i_up: 12
i_down: 19
i_pivot: 15
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 12
i_end: 14
i_pivot: 13
Iteration: 1
i_up: 12
i_down: 14

i_pivot: 13
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 12
i_end: 12
i_pivot: 12
Called
i_start: 14
i_end: 14
i_pivot: 14
Called
i_start: 16
i_end: 19
i_pivot: 17
Iteration: 1
i_up: 16
i_down: 19
i_pivot: 17
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 16
i_end: 16

```
i_pivot: 16
Called -----
i_start: 18
i_end: 19
i_pivot: 18
Iteration: 1
i_up: 18
i_down: 19
i_pivot: 18
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called -----
i_start: 18
i_end: 17
i_pivot: 17
Called -----
i_start: 19
i_end: 19
i_pivot: 19
Iteration: 2
i_up: 17
i_down: 18
i_pivot: 17
```

[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]

Block 2
Called
i_start: 16
i_end: 16
i_pivot: 16
Callad
Called
i_start: 18
i_end: 19
i_pivot: 18
Iteration: 1
i_up: 18
i_down: 19
i_pivot: 18
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called
i_start: 18
i_end: 17
i_pivot: 17
Called

i_end: 19

i_pivot: 19

Iteration: 2
i_up: 13
i_down: 18
i_pivot: 15
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 12
i_end: 14
i_pivot: 13
Iteration: 1
i_up: 12
i_down: 14
i_pivot: 13
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 12
i_end: 12
i_pivot: 12
Called
i_start: 14
i_end: 14
i_pivot: 14

Called
i_start: 16
i_end: 19
i_pivot: 17
Iteration: 1
i_up: 16
i_down: 19
i_pivot: 17
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 16
i_end: 16
i_pivot: 16
Called
i_start: 18
i_end: 19
i_pivot: 18
Iteration: 1
i_up: 18
i_down: 19
i_pivot: 18
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2

Called
i_start: 18
i_end: 17
i_pivot: 17
Called
i_start: 19
i_end: 19
i_pivot: 19
Iteration: 2
i_up: 17
i_down: 18
i_pivot: 17
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called
i_start: 16
i_end: 16
i_pivot: 16
Called
i_start: 18
i_end: 19
i_pivot: 18
Iteration: 1
i_up: 18

```
i_down: 19
i_pivot: 18
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called -----
i_start: 18
i_end: 17
i_pivot: 17
Called -----
i_start: 19
i_end: 19
i_pivot: 19
Iteration: 3
i_up: 14
i_down: 17
i_pivot: 15
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called -----
i_start: 12
i_end: 14
i_pivot: 13
Iteration: 1
```

i_up: 12

i_down: 14
i_pivot: 13
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 12
i_end: 12
i_pivot: 12
Called
i_start: 14
i_end: 14
i_pivot: 14
Called
i_start: 16
i_end: 19
i_pivot: 17
Iteration: 1
i_up: 16
i_down: 19
i_pivot: 17
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called

i_end: 16
i_pivot: 16
Called
i_start: 18
i_end: 19
i_pivot: 18
Iteration: 1
i_up: 18
i_down: 19
i_pivot: 18
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called
i_start: 18
i_end: 17
i_pivot: 17
Called
i_start: 19
i_end: 19
i_pivot: 19
Iteration: 2
i_up: 17
i_down: 18
i_pivot: 17

[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500] Block 2
Called
i_start: 16
i_end: 16
i_pivot: 16
Called
i_start: 18
i_end: 19
i_pivot: 18
Iteration: 1
i_up: 18
i_down: 19
i_pivot: 18
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called
i_start: 18
i_end: 17
i_pivot: 17
Called
i_start: 19
i_end: 19
i_pivot: 19

```
Iteration: 4
i_up: 15
i_down: 16
i_pivot: 15
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 4
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Called -----
i_start: 12
i_end: 15
i_pivot: 13
Iteration: 1
i_up: 12
i_down: 15
i_pivot: 13
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called -----
i_start: 12
i_end: 12
i_pivot: 12
Called -----
i_start: 14
i_end: 15
```

```
i_pivot: 14
Iteration: 1
i_up: 14
i_down: 15
i_pivot: 14
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called -----
i_start: 14
i_end: 13
i_pivot: 13
Called -----
i_start: 15
i_end: 15
i_pivot: 15
Iteration: 2
i_up: 13
i_down: 14
i_pivot: 13
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called -----
i_start: 12
i_end: 12
```

i_pivot: 12
Called
i_start: 14
i_end: 15
i_pivot: 14
Iteration: 1
i_up: 14
i_down: 15
i_pivot: 14
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called
i_start: 14
i_end: 13
i_pivot: 13
Called
i_start: 15
i_end: 15
i_pivot: 15
Called
i_start: 17
i_end: 19
i_pivot: 18

Iteration: 1
i_up: 17
i_down: 19
i_pivot: 18
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 17
i_end: 17
i_pivot: 17
Called
i_start: 19
i_end: 19
i_pivot: 19
Iteration: 8
i_up: 11
i_down: 12
i_pivot: 11
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called
i_start: 4
i_end: 10
i_pivot: 7

Iteration: 1
i_up: 4
i_down: 10
i_pivot: 7
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 4
i_end: 6
i_pivot: 5
Iteration: 1
i_up: 4
i_down: 6
i_pivot: 5
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 4
i_end: 4
i_pivot: 4
Called
i_start: 6
i_end: 6
i_pivot: 6

Called
i_start: 8
i_end: 10
i_pivot: 9
Iteration: 1
i_up: 8
i_down: 10
i_pivot: 9
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 8
i_end: 8
i_pivot: 8
Called
i_start: 10
i_end: 10
i_pivot: 10
Iteration: 2
i_up: 5
i_down: 9
i_pivot: 7
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1

Called
i_start: 4
i_end: 6
i_pivot: 5
Iteration: 1
i_up: 4
i_down: 6
i_pivot: 5
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 4
i_end: 4
i_pivot: 4
Called
i_start: 6
i_end: 6
i_pivot: 6
Called
i_start: 8
i_end: 10
i_pivot: 9
Iteration: 1
i_up: 8

i_down: 10
i_pivot: 9
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 8
i_end: 8
i_pivot: 8
Called
i_start: 10
i_end: 10
i_pivot: 10
Iteration: 3
i_up: 6
i_down: 8
i_pivot: 7
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 4
i_end: 6
i_pivot: 5
Iteration: 1

i_up: 4

i_down: 6
i_pivot: 5
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 4
i_end: 4
i_pivot: 4
Called
i_start: 6
i_end: 6
i_pivot: 6
Called
i_start: 8
i_end: 10
i_pivot: 9
Iteration: 1
i_up: 8
i_down: 10
i_pivot: 9
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called

i_end: 8
i_pivot: 8
Called
i_start: 10
i_end: 10
i_pivot: 10
Called
i_start: 12
i_end: 19
i_pivot: 15
Iteration: 1
i_up: 12
i_down: 19
i_pivot: 15
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 12
i_end: 14
i_pivot: 13
Iteration: 1
i_up: 12
i_down: 14
i_pivot: 13

[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500] Block 1
Called
i_start: 12
i_end: 12
i_pivot: 12
Called
i_start: 14
i_end: 14
i_pivot: 14
Called
i_start: 16
i_end: 19
i_pivot: 17
Iteration: 1
i_up: 16
i_down: 19
i_pivot: 17
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 16
i_end: 16
i_pivot: 16

```
Called -----
i_start: 18
i_end: 19
i_pivot: 18
Iteration: 1
i_up: 18
i_down: 19
i_pivot: 18
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called -----
i_start: 18
i_end: 17
i_pivot: 17
Called -----
i_start: 19
i_end: 19
i_pivot: 19
Iteration: 2
i_up: 17
i_down: 18
i_pivot: 17
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
```

Called
i_start: 16
i_end: 16
i_pivot: 16
Called
i_start: 18
i_end: 19
i_pivot: 18
Iteration: 1
i_up: 18
i_down: 19
i_pivot: 18
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called
i_start: 18
i_end: 17
i_pivot: 17
Called
i_start: 19
i_end: 19
i_pivot: 19

Iteration: 2

i_up: 13
i_down: 18
i_pivot: 15
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 12
i_end: 14
i_pivot: 13
Iteration: 1
i_up: 12
i_down: 14
i_pivot: 13
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 12
i_end: 12
i_pivot: 12
Called
i_start: 14
i_end: 14
i_pivot: 14

Called -----

```
i_start: 16
i_end: 19
i_pivot: 17
Iteration: 1
i_up: 16
i_down: 19
i_pivot: 17
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called -----
i_start: 16
i_end: 16
i_pivot: 16
Called -----
i_start: 18
i_end: 19
i_pivot: 18
Iteration: 1
i_up: 18
i_down: 19
i_pivot: 18
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
```

Called -----

i_start: 18
i_end: 17
i_pivot: 17
Called
i_start: 19
i_end: 19
i_pivot: 19
Iteration: 2
i_up: 17
i_down: 18
i_pivot: 17
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called
i_start: 16
i_end: 16
i_pivot: 16
Called
i_start: 18
i_end: 19
i_pivot: 18
Iteration: 1
i_up: 18
i_down: 19

```
i_pivot: 18
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called -----
i_start: 18
i_end: 17
i_pivot: 17
Called -----
i_start: 19
i_end: 19
i_pivot: 19
Iteration: 3
i_up: 14
i_down: 17
i_pivot: 15
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called -----
i_start: 12
i_end: 14
i_pivot: 13
Iteration: 1
i_up: 12
i_down: 14
```

i_pivot: 13
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 12
i_end: 12
i_pivot: 12
Called
i_start: 14
i_end: 14
i_pivot: 14
Called
i_start: 16
i_end: 19
i_pivot: 17
Iteration: 1
i_up: 16
i_down: 19
i_pivot: 17
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called
i_start: 16
i_end: 16

```
i_pivot: 16
Called -----
i_start: 18
i_end: 19
i_pivot: 18
Iteration: 1
i_up: 18
i_down: 19
i_pivot: 18
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called -----
i_start: 18
i_end: 17
i_pivot: 17
Called -----
i_start: 19
i_end: 19
i_pivot: 19
Iteration: 2
i_up: 17
i_down: 18
i_pivot: 17
```

[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]

Block 2
Called
i_start: 16
i_end: 16
i_pivot: 16
Callad
Called
i_start: 18
i_end: 19
i_pivot: 18
Iteration: 1
i_up: 18
i_down: 19
i_pivot: 18
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called
i_start: 18
i_end: 17
i_pivot: 17
Called

i_end: 19

i_pivot: 19

```
Iteration: 4
i_up: 15
i_down: 16
i_pivot: 15
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 4
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Called -----
i_start: 12
i_end: 15
i_pivot: 13
Iteration: 1
i_up: 12
i_down: 15
i_pivot: 13
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 1
Called -----
i_start: 12
i_end: 12
i_pivot: 12
Called -----
i_start: 14
i_end: 15
i_pivot: 14
```

```
Iteration: 1
i_up: 14
i_down: 15
i_pivot: 14
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called -----
i_start: 14
i_end: 13
i_pivot: 13
Called -----
i_start: 15
i_end: 15
i_pivot: 15
Iteration: 2
i_up: 13
i_down: 14
i_pivot: 13
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called -----
i_start: 12
i_end: 12
i_pivot: 12
```

Called
i_start: 14
i_end: 15
i_pivot: 14
Iteration: 1
i_up: 14
i_down: 15
i_pivot: 14
[1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]
Block 2
Called
i_start: 14
i_end: 13
i_pivot: 13
Called
i_start: 15
i_end: 15
i_pivot: 15
Called
i_start: 17
i_end: 19
i_pivot: 18

Iteration: 1

i_up: 17 i_down: 19 i_pivot: 18 [1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]Block 1 Called ----i_start: 17 i_end: 17 i_pivot: 17 Called -----

i_start: 19

i_end: 19

i_pivot: 19

Sorted: [1, 2, 3, 3, 3, 4, 5, 6, 8, 10, 12, 15, 23, 33, 34, 45, 45, 67, 300, 500]