CS61C Spring 2015 Discussion 9

Floating Point

The IEEE 754 standard defines a binary representation for floating point values using three fields:

- The *sign* determines the sign of the number (0 for positive, 1 for negative)
- The exponent is in biased notation with a bias of 127
- The significand is akin to unsigned, but used to store a fraction instead of an integer.

The below table shows the bit breakdown for the single precision (32-bit) representation:

Sign	Exponent	Significand
1 bit	8 bits	23 bits

There is also a double precision encoding format that uses 64 bits. This behaves the same as the single precision but uses 11 bits for the exponent (and thus a bias of 1023) and 52 bits for the significand.

How a float is interpreted depends on the values in the exponent and significand fields:

For normalized floats:

Value =
$$(-1)^{Sign} \times 2^{(Exponent - Bias)} \times 1.significand_2$$

For denormalized floats:

Value =
$$(-1)^{Sign} \times 2^{(Exponent - Bias + 1)} \times 0.significand_2$$

Exponent	Significand	Meaning
0	Anything	Denorm
1-254	Anything	Normal
255	0	Infinity
255	Nonzero	NaN

Exercises

- 1. How many zeroes can be represented using a float? 2
- 2. What is the largest finite positive value that can be stored using a single precision float? $0x7F7FFFFF = (2 - 2^{-23}) \times 2^{127}$
- 3. What is the smallest positive value that can be stored using a single precision float? $0x00000001 = 2^{-23} \times 2^{-126}$
- 4. What is the smallest positive normalized value that can be stored using a single precision float? $0x00800000 = 2^{-126}$
- 5. Convert the following numbers from binary to decimal or from decimal to binary: 0x00000000 8.25 0x00000F00 39.5625 0xFF94BEEF

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0x00000000 = 0

8.25 = 0x41040000

0x0000000F0 = (2^{-12} + 2^{-13} + 2^{-14} + 2^{-15}) \times 2^{-126}

39.5625 = 0x421E4000

0xFF94BEEF = NaN

-\infty = 0xFF800000
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AMAT

AMAT is the average (expected) time it takes for memory access. It can be calculated using this formula: $AMAT = \text{hit time} + \text{miss rate} \times \text{miss penalty}$

Miss rates can be given in terms of either local miss rates or global miss rates. The *local miss rate* of a cache is the percentage of accesses into the particular cache that miss at the cache, while the *global miss rate* is the percentage of all accesses that miss at the cache.

Exercises

Suppose your system consists of:

- A L1\$ that hits in 2 cycles and has a local miss rate of 20%
- A L2\$ that hits in 15 cycles and has a global miss rate of 5%
- Main memory hits in 100 cycles
- 1. What is the local miss rate of L2\$? Local miss rate = 5% / 20% = 0.25 = 25%
- 2. What is the AMAT of the system?

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AMAT = 2 + 20\% \times 15 + 5\% \times 100 = 10 (using global miss rates)
Alternatively, AMAT = 2 + 20\% \times (15 + 25\% \times 100) = 10
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3. Suppose we want to reduce the AMAT of the system to 8 or lower by adding in a L3\$. If the L3\$ has a local miss rate of 30%, what is the largest hit time that the L3\$ can have?

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Let H = hit time of the cache. Using the AMAT equation, we can write:
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2 + 20\% \times (15 + 25\% \times (H + 30\% \times 100)) \le 8
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Solving for H, we find that $H \le 30$. So the largest hit time is 30 cycles.

Flynn Taxonomy

1. Explain SISD and give an example if available.

Single Instruction Single Data; each instruction is executed in order, acting on a single stream of data. For example, traditional computer programs.

2. Explain SIMD and give an example if available.

Single Instruction Multiple Data; each instruction is executed in order, acting on multiple streams of data. For example, the SSE Intrinsics.

3. Explain MISD and give an example if available.

Multiple Instruction Single Data; multiple instructions are executed simultaneously, acting on a single stream of data. There are no good modern examples.

4. Explain MIMD and give an example if available.

Multiple Instruction Multiple Data; multiple instructions are executed simultaneously, acting on multiple streams of data. For example, map reduce or multithreaded programs.