

## Module 3 :: Switching Algebra and Properties

### Practice Problems

1. Simplify the following switching expressions using algebraic method:

$$x' + y' + x \cdot y \cdot z'$$

$$(x' + x \cdot y \cdot z') + (x' + x \cdot y \cdot z') \cdot (x + x' \cdot y' \cdot z)$$

$$a + a' \cdot b + a' \cdot b' \cdot c + a' \cdot b' \cdot c' \cdot d + \dots$$

$$w' \cdot x' + x' \cdot y' + w' \cdot z' + y \cdot z$$

$$((x + y' \cdot z') \cdot (y + x' \cdot z') \cdot (z + x' \cdot y'))'$$

2. Determine the canonical sum-of-products expressions for the following functions:

a)  $f(x,y,z) = z + ((x' + y) \cdot (x + y'))$

b)  $f(x,y,z) = x + (x' \cdot y' + x' \cdot z)'$

3. Determine which of the following are functionally complete / universal? Justify your answer.

a) NAND

b) NOR

c) (EXOR, AND)

d) 2-input Multiplexer

e) The function  $f(A,B,C) = A' \cdot B \cdot C + A \cdot B' + B' \cdot C'$

4. You are presented with a set of requirements under which an insurance policy will be issued. The applicant must be:

A married female 25 years old or over, or

A female under 25, or

A married male under 25 who has not been involved in a car accident, or

A married male who has been involved in a car accident, or

A married male 25 years or over who has not been involved in a car accident.

Define appropriate variables to capture the requirements.

- Find an algebraic expression that assumes the value 1 whenever the policy should be issued.
- Simplify algebraically the above expression and suggest a simpler set of requirements.