PLACEHOLDER-TITLE: Functional Linear Regression in a Scalar-on-Function Setting with Applications to SOMETHING

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whenever

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1 Introduction

- Describe the idea of regressing a scalar on functional data
- Describing the difference to multiple linear regression intuitively
- Giving an intuitive example

2 Theory

2.1 Draft-Overview

- Introduce the concept of random functions
- Introduce the concept of square integrable deterministic & random functions
- Explain basis expansions (so basis of the vector space L^2 and b-spline basis as an example)
- Motivate Karhunen-Loeve-Expansion and Eigenbasis from PCA
- Explain Scalar-on-Function Regression
- Estimation through basis-expansion (incl. Eigenbasis) [and estimation with roughness penalty]
- Address approximation error due to basis-truncation

2.2 Literature

- Kokoszka and Reimherr 2017
- Hsing and Eubank 2015
- Ramsay and Silverman 2005
- Horváth and Kokoszka 2012
- Cai and Hall 2006
- Levitin et al. 2007

3 Simulation

3.1 Draft-Overview

- Motivate Simulation for some data generating process from application
- Describe Simulation Setting from technical standpoint (DGP, set-up for replication, ...)
- Prediction not Inference
- Present Results
- Explain relevance for application

3.2 Literature

- $\bullet\,$ Shonkwiler and Mendivil 2009
- R-packages: fda, refund, mgcv

4 Application

4.1 Draft-Overview

- Prediction not Inference
- IID data set (no dependence between the curves, don't want to do functional time series)
- Not necessarily data from economics (like biology, sports, whatever)
- Smooth curves or random walk (both fine)
- $\bullet \ \, https://functional data.wordpress.ncsu.edu/resources/$

4.2 Literature

• Carey et al. 2002

5 Outlook

5.1 Literature

• James, Wang, and Zhu 2009 (shape-restrictions)

6 Appendix

7 Bibliography

- Cai, T. Tony and Peter Hall (Oct. 2006). "Prediction in functional linear regression". In: *The Annals of Statistics* 34.5. Publisher: Institute of Mathematical Statistics, pp. 2159-2179. ISSN: 0090-5364, 2168-8966. DOI: 10.1214/009053606000000830. URL: https://projecteuclid.org/journals/annals-of-statistics/volume-34/issue-5/Prediction-in-functional-linear-regression/10.1214/009053606000000830.full (visited on 10/24/2021).
- Carey, James R. et al. (2002). "Life history response of Mediterranean fruit flies to dietary restriction". en. In: Aging Cell 1.2. _eprint: https://onlinelibrary.wiley.com/doi/pdf/10.1046/j.1474-9728.2002.00019.x, pp. 140-148. ISSN: 1474-9726. DOI: 10.1046/j.1474-9728.2002.00019.x. URL: https://onlinelibrary.wiley.com/doi/abs/10.1046/j.1474-9728.2002.00019.x (visited on 10/24/2021).
- Horváth, Lajos and Piotr Kokoszka (May 2012). *Inference for Functional Data with Applications*. en. Google-Books-ID: OVezLB_ZpYC. Springer Science & Business Media. ISBN: 978-1-4614-3655-3.
- Hsing, Tailen and Randall Eubank (Mar. 2015). Theoretical Foundations of Functional Data Analysis, with an Introduction to Linear Operators. en. Google-Books-ID: om9uBwAAQBAJ. John Wiley & Sons. ISBN: 978-1-118-76256-1.
- James, Gareth M., Jing Wang, and Ji Zhu (2009). "Functional linear regression that's interpretable". In: *The Annals of Statistics* 37.5A. ISSN: 0090-5364. DOI: 10.1214/08-A0S641.
- Kokoszka, Piotr and Matthew Reimherr (Aug. 2017). *Introduction to Functional Data Analysis*. Englisch. 1st ed. Boca Raton: Chapman and Hall/CRC. ISBN: 978-1-4987-4634-2.
- Levitin, Daniel et al. (Aug. 2007). "Introduction to Functional Data Analysis". In: Canadian Psychology/Psychologie canadienne 48, pp. 135–155. DOI: 10.1037/cp2007014.
- Ramsay, James and B. W. Silverman (2005). Functional Data Analysis. en. 2nd ed. Springer Series in Statistics. New York: Springer-Verlag. ISBN: 978-0-387-40080-8. DOI: 10.1007/b98888. URL: https://www.springer.com/de/book/9780387400808 (visited on 10/23/2021).
- Shonkwiler, Ronald W. and Franklin Mendivil (2009). Explorations in Monte Carlo Methods. en. Undergraduate Texts in Mathematics. New York: Springer-Verlag. ISBN: 978-0-387-87836-2. DOI: 10.1007/978-0-387-87837-9. URL: https://www.springer.com/gp/book/9780387878362 (visited on 10/23/2021).