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It reaches the post at a time: $t_h = \frac{d}{u}$

The vertical velocity obeys: $y(t_h) = h = -\frac{g}{2}t_h^2 + V_0 t_h$

$$\Rightarrow V_0 = \frac{hu}{d} + \frac{gd}{2u}$$

The time for it to reach $y(t_0) = 0$ again is

$$y(t_0) = 0 = -\frac{g}{2}t_0^2 + V_0 t_0 \Rightarrow t_0 = \frac{2V_0}{g} = \frac{2hu}{gd} + t_h$$

So in a time $t_0 - t_h$, it travelled a

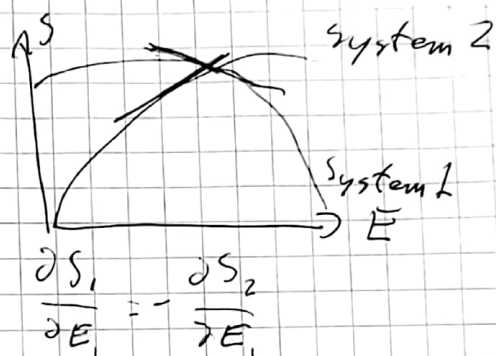
distance: $r = u(t_0 - t_h) = \frac{2hu^2}{gd}$ from the post

which is independent of the starting point on ℓ since it is only expressed in terms of the constants h, u, g, d . Thus it lands on a circle of radius $\frac{2hu^2}{gd}$ around the pole.

(10a)

$$E = \frac{1}{8\pi T}, \quad C_T = \frac{-1}{8\pi T^2}$$

Thermal equilibrium:
Negative C_T makes it
unstable.



(b)

$$\frac{\partial S_{total}}{\partial M} = 0; \quad \frac{\partial S_{total}}{\partial T} = \frac{\partial S_{BH}}{\partial M} \frac{\partial M}{\partial T} - \frac{\partial S_R}{\partial M} \frac{\partial M}{\partial T}$$

$$\frac{\partial M}{\partial T} = - \frac{\partial E_R}{\partial T} \Rightarrow -C_{BH} = C_R = \frac{1}{8\pi T^2}$$