

Metoda nejmenších čtverců

1. Pomocí programu v Matlabu proložte zadanou sadu hodnot x, y, σ_y teoretickou lineární závislostí $y = ax + b$ a $y = mx$ pomocí lineární metody nejmenších čtverců.

data lindata.dat

Matlab linfit.m

$$y = ax + b$$

```
%% obecná přímka y=theta2*x+theta1
fprintf(1, '\n');
fprintf(1, 'obecná přímka y=a*x+b\n');
%vytvoreni matice A
A0=ones(n,1);
A=[A0,x];
%vytvoreni matice B
B=inv(A'*inv(V)*A)*A'*inv(V);
%odhad parametrů theta
theta=B*y;
%kovarianční matice parametrů
U=B*V*B';
%% standardní odchylky
e_1=sqrt(U(1,1));            %odchylka konst. parametru
e_2=sqrt(U(2,2));            %odchylka lin. parametru
cor=U(1,2)/(e_1*e_2);        %korelace parametrů
```

$$y = mx$$

```
%% přímka procházející počátkem y=m*x
fprintf(1, '\n');
fprintf(1, 'přímka procházející počátkem y=m*x\n');
s1=x'*(y./(vp.*vp));
s2=x'*(x./(vp.*vp));
m=s1/s2;
%% standardní odchylka
e_m=sqrt(1/s2);
```

Metoda nejmenších čtverců

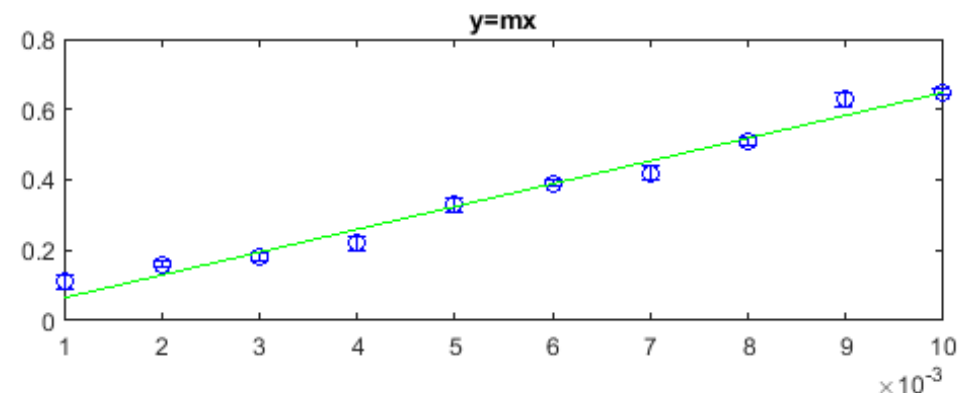
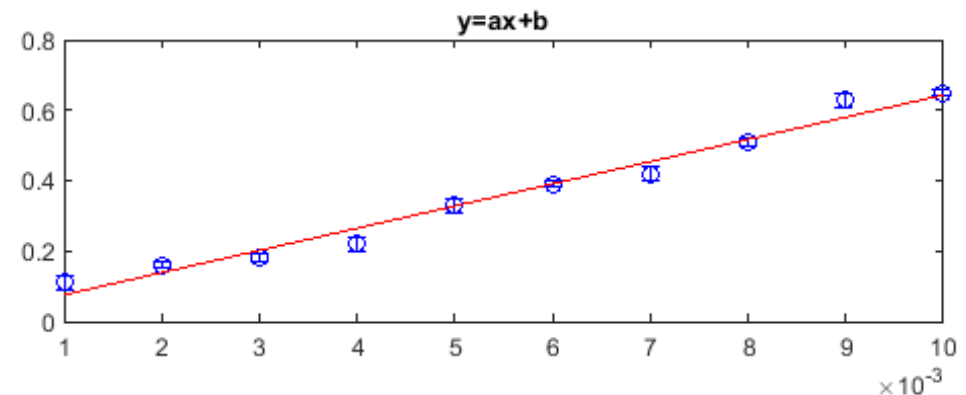
1. Pomocí programu v Matlabu proložte zadanou sadu hodnot x, y, σ_y teoretickou lineární závislostí $y = ax + b$ a $y = mx$ pomocí lineární metody nejmenších čtverců.

data lindata.dat

Matlab linfit.m

```
obecná přímka  $y = a \cdot x + b$   
 $b = 0.012498 \pm 0.008680$   
 $a = 63.081310 \pm 1.356314$   
korelace(a,b) = -0.887500
```

```
přímka procházející počátkem  $y = m \cdot x$   
 $m = 64.814453 \pm 0.625000$ 
```



Metoda nejmenších čtverců

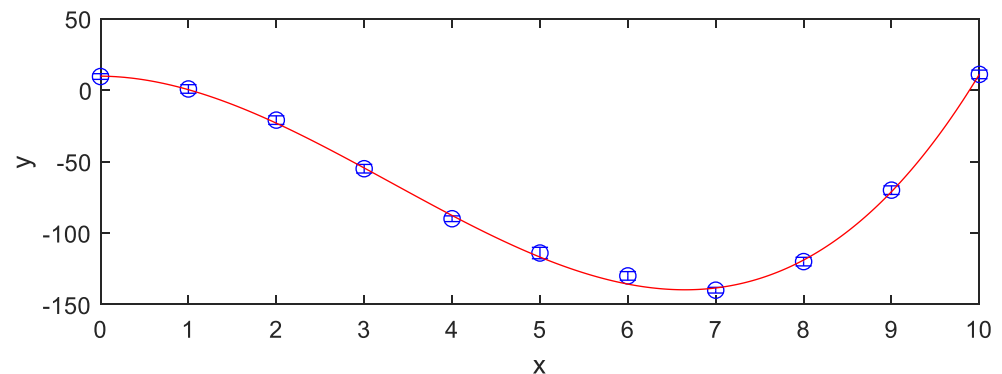
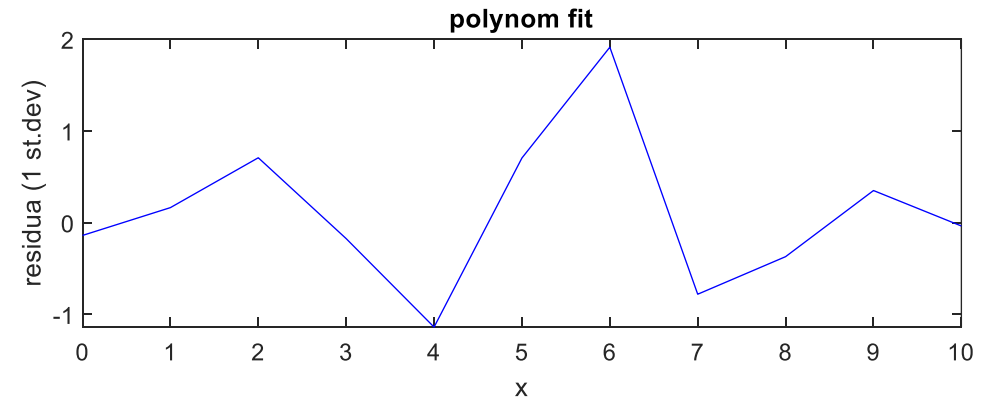
2. Pomocí programu v Matlabu proložte zadanou sadu hodnot x, y, σ_y teoretickým polynomem

m -tého stupně $y = \sum_{i=0}^m \theta_i x^i$ pomocí lineární metody nejmenších čtverců.

data polydata.dat

Matlab polyfit.m

```
%% fit polynomu stupne m
%vytvoreni matice A
for i=1:n
    for j=1:m+1
        A(i,j)=x(i)^(j-1);
    end
end
%vytvoreni matice B
B=inv(A'*inv(V)*A)*A'*inv(V);
%odhady parametru theta
theta=B*y;
%kovariancni matice parametru theta
U=B*V*B';
R=U;
%korelacni matice parametru theta
for i=1:m+1
    for j=1:m+1
        R(i,j)=U(i,j)/sqrt(U(i,i)*U(j,j));
    end
end
```



Metoda nejmenších čtverců

$m = 1$

```
stupen polynomu: 1  
theta0: -21.013396 +/- 1.401552  
theta1: -9.670547 +/- 0.248492
```

kovariancni matice:

U =

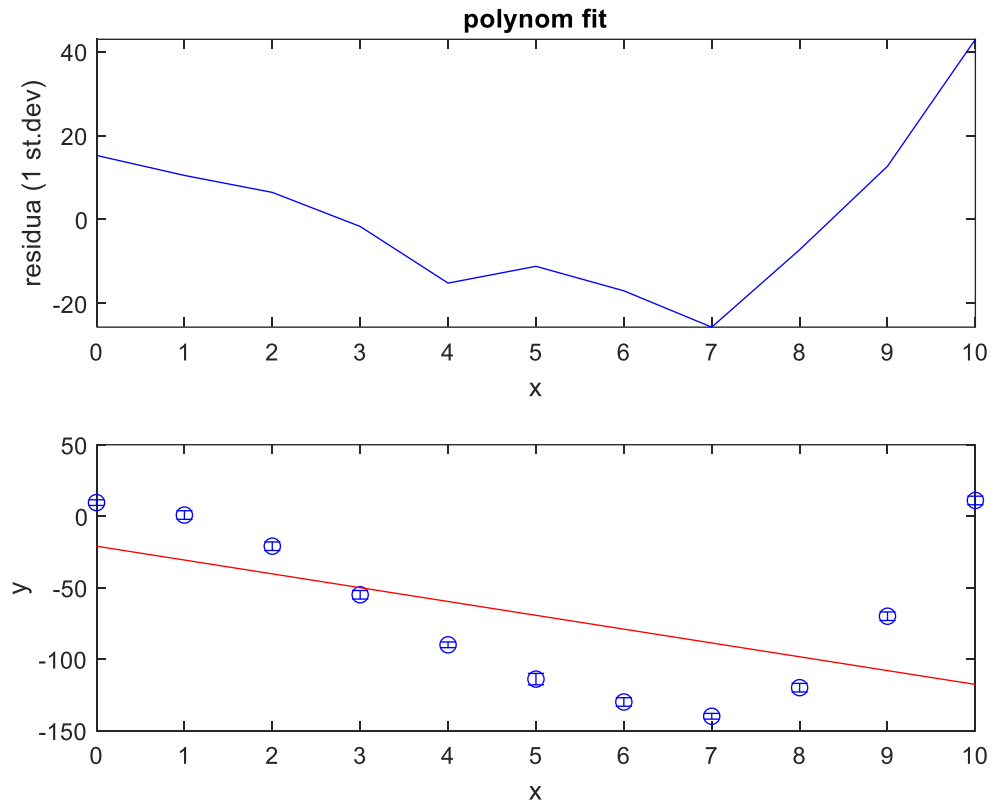
```
1.9643  -0.2872  
-0.2872  0.0617
```

korelacni matice:

R =

```
1.0000  -0.8246  
-0.8246  1.0000
```

```
pocet stupnu volnosti: 9  
chisq = 3741.447845 +/- 4.242641  
chisq/deg.freedom = 415.716427 +/- 1.414214
```



Metoda nejmenších čtverců

$m = 2$

```
stupen polynomu: 2  
theta0: 32.598569 +/- 1.731697  
theta1: -52.725477 +/- 0.853755  
theta2: 4.608972 +/- 0.087436
```

kovariancni matice:

U =

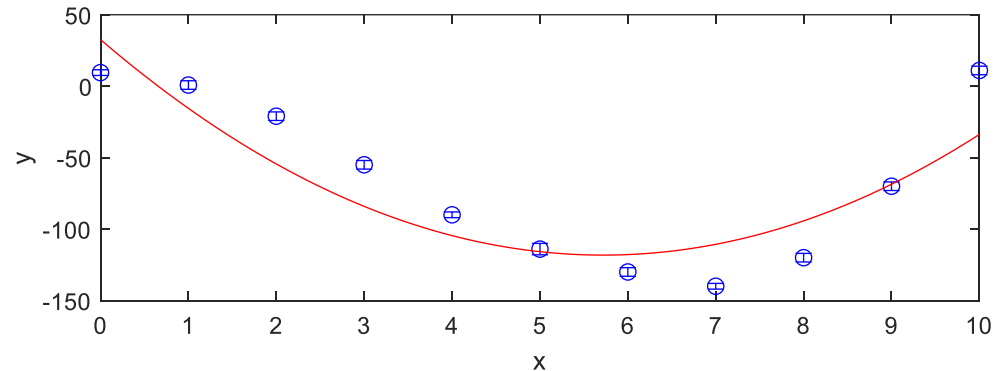
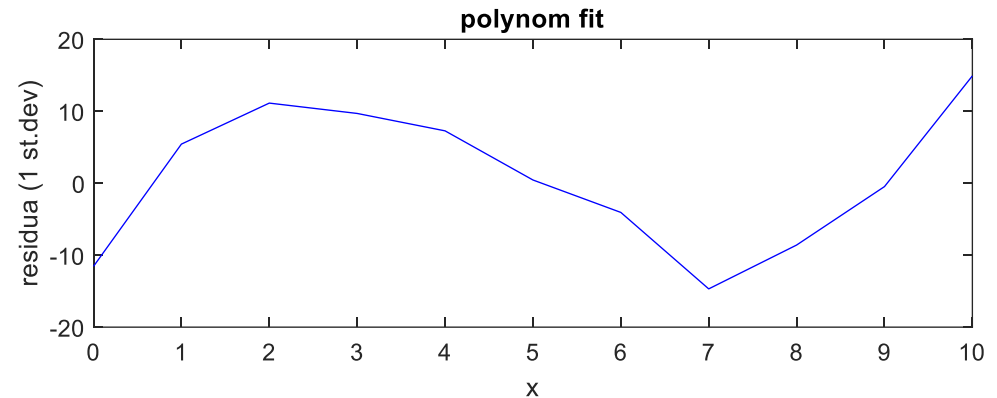
2.9988	-1.1179	0.0889
-1.1179	0.7289	-0.0714
0.0889	-0.0714	0.0076

korelacni matice:

R =

1.0000	-0.7561	0.5873
-0.7561	1.0000	-0.9567
0.5873	-0.9567	1.0000

```
pocet stupnu volnosti: 8  
chisq = 962.865871 +/- 4.000000  
chisq/deg.freedom = 120.358234 +/- 1.414214
```



Metoda nejmenších čtverců

$m = 3$

```
stupen polynomu: 3  
theta0: 9.777893 +/- 1.882431  
theta1: -0.479484 +/- 1.893218  
theta2: -9.997465 +/- 0.480438  
theta3: 1.005872 +/- 0.032533
```

kovariancni matice:

U =

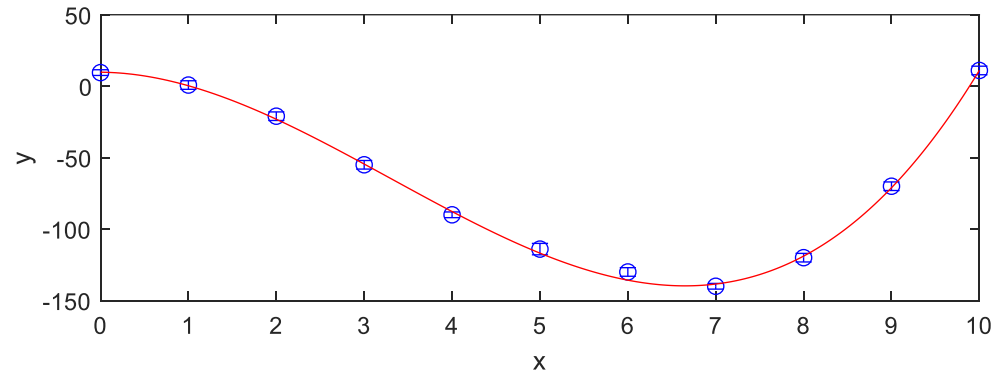
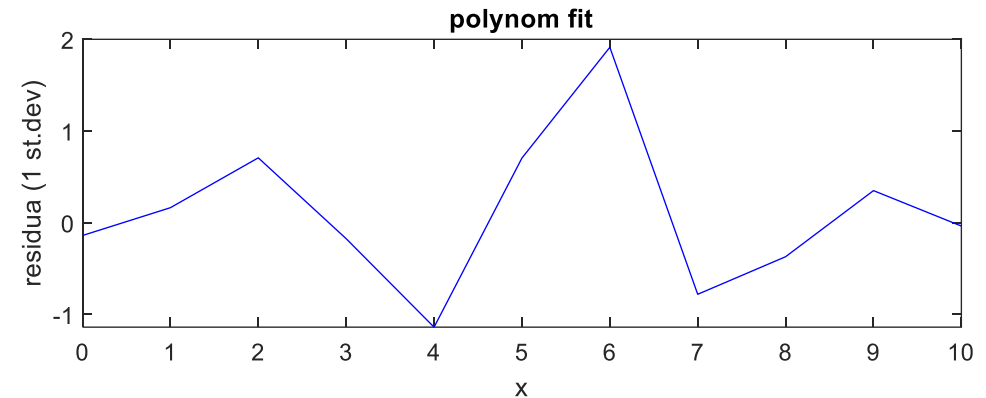
3.5435	-2.3651	0.4376	-0.0240
-2.3651	3.5843	-0.8697	0.0550
0.4376	-0.8697	0.2308	-0.0154
-0.0240	0.0550	-0.0154	0.0011

korelacni matice:

R =

1.0000	-0.6636	0.4839	-0.3921
-0.6636	1.0000	-0.9562	0.8925
0.4839	-0.9562	1.0000	-0.9833
-0.3921	0.8925	-0.9833	1.0000

```
pocet stupnu volnosti: 7  
chisq = 6.900470 +/- 3.741657  
chisq/deg.freedom = 0.985781 +/- 1.414214
```



Metoda nejmenších čtverců

$m = 4$

```
stupen polynomu: 4  
theta0: 9.739719 +/- 1.959859  
theta1: -0.246522 +/- 3.829354  
theta2: -10.119055 +/- 1.802518  
theta3: 1.025531 +/- 0.282775  
theta4: -0.000986 +/- 0.014094
```

kovariancni matice:

U =

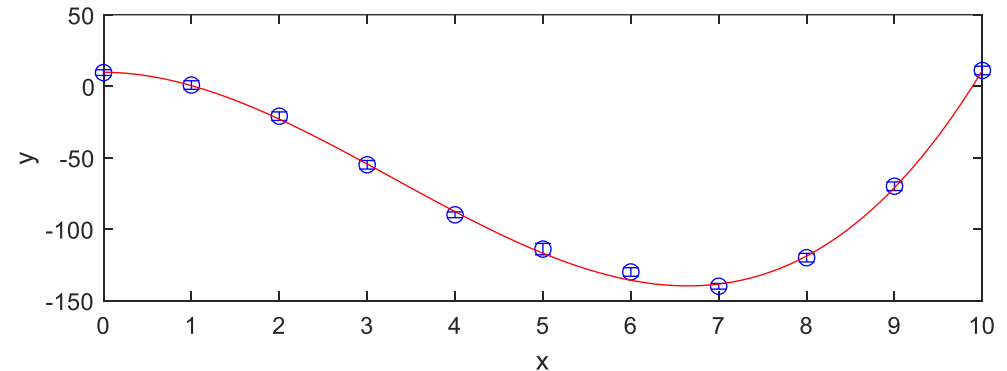
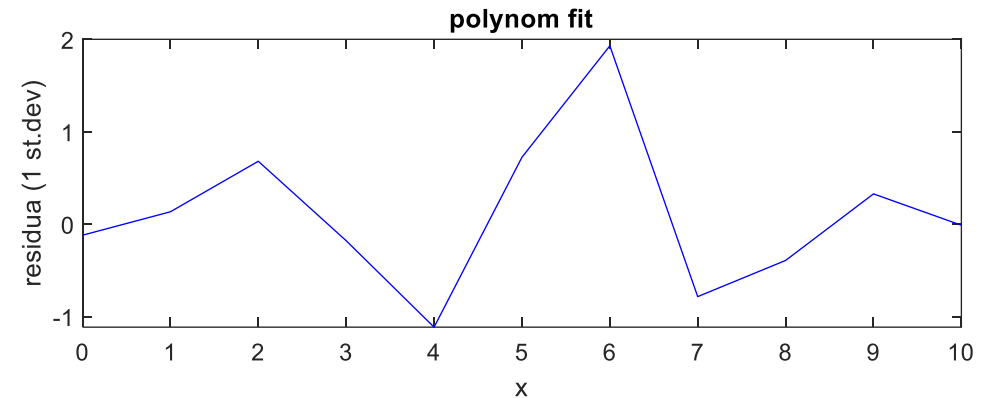
3.8410	-4.1807	1.3852	-0.1772	0.0077
-4.1807	14.6640	-6.6525	0.9900	-0.0469
1.3852	-6.6525	3.2491	-0.5034	0.0245
-0.1772	0.9900	-0.5034	0.0800	-0.0040
0.0077	-0.0469	0.0245	-0.0040	0.0002

korelacni matice:

R =

1.0000	-0.5570	0.3921	-0.3198	0.2783
-0.5570	1.0000	-0.9638	0.9142	-0.8692
0.3921	-0.9638	1.0000	-0.9876	0.9638
-0.3198	0.9142	-0.9876	1.0000	-0.9934
0.2783	-0.8692	0.9638	-0.9934	1.0000

```
pocet stupnu volnosti: 6  
chisq = 6.895572 +/- 3.464102  
chisq/deg.freedom = 1.149262 +/- 1.414214
```



Metoda nejmenších čtverců

$m = 5$

```
stupen polynomu: 5  
theta0: 9.483401 +/- 1.987158  
theta1: 3.426614 +/- 6.065604  
theta2: -13.230846 +/- 4.373807  
theta3: 1.918074 +/- 1.177492  
theta4: -0.104913 +/- 0.133838  
theta5: 0.004221 +/- 0.005405
```

kovariancni matice:

U =

3.9488	-5.7248	2.6933	-0.5524	0.0514	-0.0018
-5.7248	36.7916	-25.3985	6.3668	-0.6730	0.0254
2.6933	-25.3985	19.1302	-5.0585	0.5549	-0.0215
-0.5524	6.3668	-5.0585	1.3865	-0.1561	0.0062
0.0514	-0.6730	0.5549	-0.1561	0.0179	-0.0007
-0.0018	0.0254	-0.0215	0.0062	-0.0007	0.0000

korelacni matice:

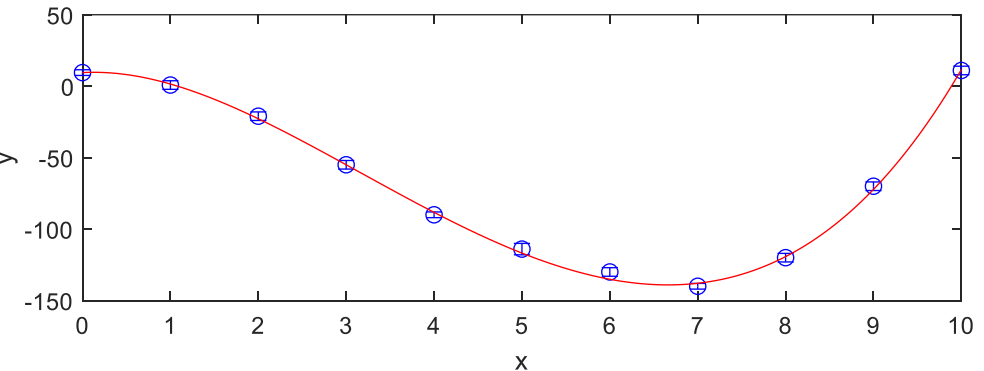
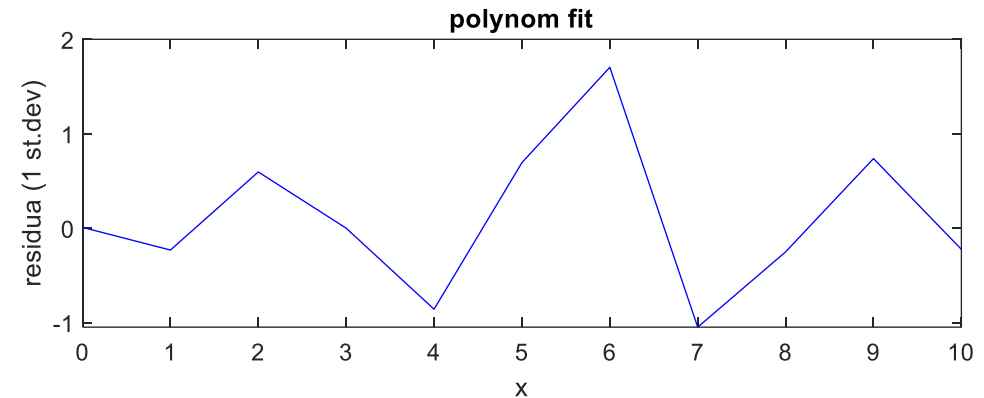
R =

1.0000	-0.4750	0.3099	-0.2361	0.1932	-0.1652
-0.4750	1.0000	-0.9574	0.8914	-0.8290	0.7755
0.3099	-0.9574	1.0000	-0.9822	0.9479	-0.9111
-0.2361	0.8914	-0.9822	1.0000	-0.9905	0.9707
0.1932	-0.8290	0.9479	-0.9905	1.0000	-0.9944
-0.1652	0.7755	-0.9111	0.9707	-0.9944	1.0000

pocet stupnu volnosti: 5

chisq = 6.285838 +/- 3.162278

chisq/deg.freedom = 1.257168 +/- 1.414214



Metoda nejmenších čtverců

$m = 9$

```
stupen polynomu: 9
theta0: 9.499356 +/- 1.999998
theta1: 39.613446 +/- 74.930638
theta2: -116.317282 +/- 173.815397
theta3: 112.494059 +/- 156.210567
theta4: -59.528511 +/- 72.899603
theta5: 17.901582 +/- 19.694182
theta6: -3.153088 +/- 3.197009
theta7: 0.322257 +/- 0.307574
theta8: -0.017684 +/- 0.016154
theta9: 0.000403 +/- 0.000357
```

korelacni matice:

R =

1.0000	-0.0726	0.0340	-0.0219	0.0162	-0.0130				
-0.0726	1.0000	-0.9946	0.9844	-0.9722	0.9587				
0.0340	-0.9946	1.0000	-0.9971	0.9900	-0.9806				
-0.0219	0.9844	-0.9971	1.0000	-0.9978	0.9923				
0.0162	-0.9722	0.9900	-0.9978	1.0000	-0.9983				
-0.0130	0.9587	-0.9806	0.9923	-0.9983	1.0000				
0.0110	-0.9446	0.9695	-0.9846	0.9938	-0.9986	1.0000	-0.9988	0.9958	-0.9915
-0.0096	0.9303	-0.9576	0.9754	-0.9874	0.9949	-0.9988	1.0000	-0.9991	0.9966
0.0086	-0.9161	0.9453	-0.9654	0.9797	-0.9896	0.9958	-0.9991	1.0000	-0.9992
-0.0078	0.9024	-0.9330	0.9550	-0.9714	0.9833	-0.9915	0.9966	-0.9992	1.0000

pocet stupnu volnosti: 1

chisq = 0.048254 +/- 1.414214

chisq/deg.freedom = 0.048254 +/- 1.414214

