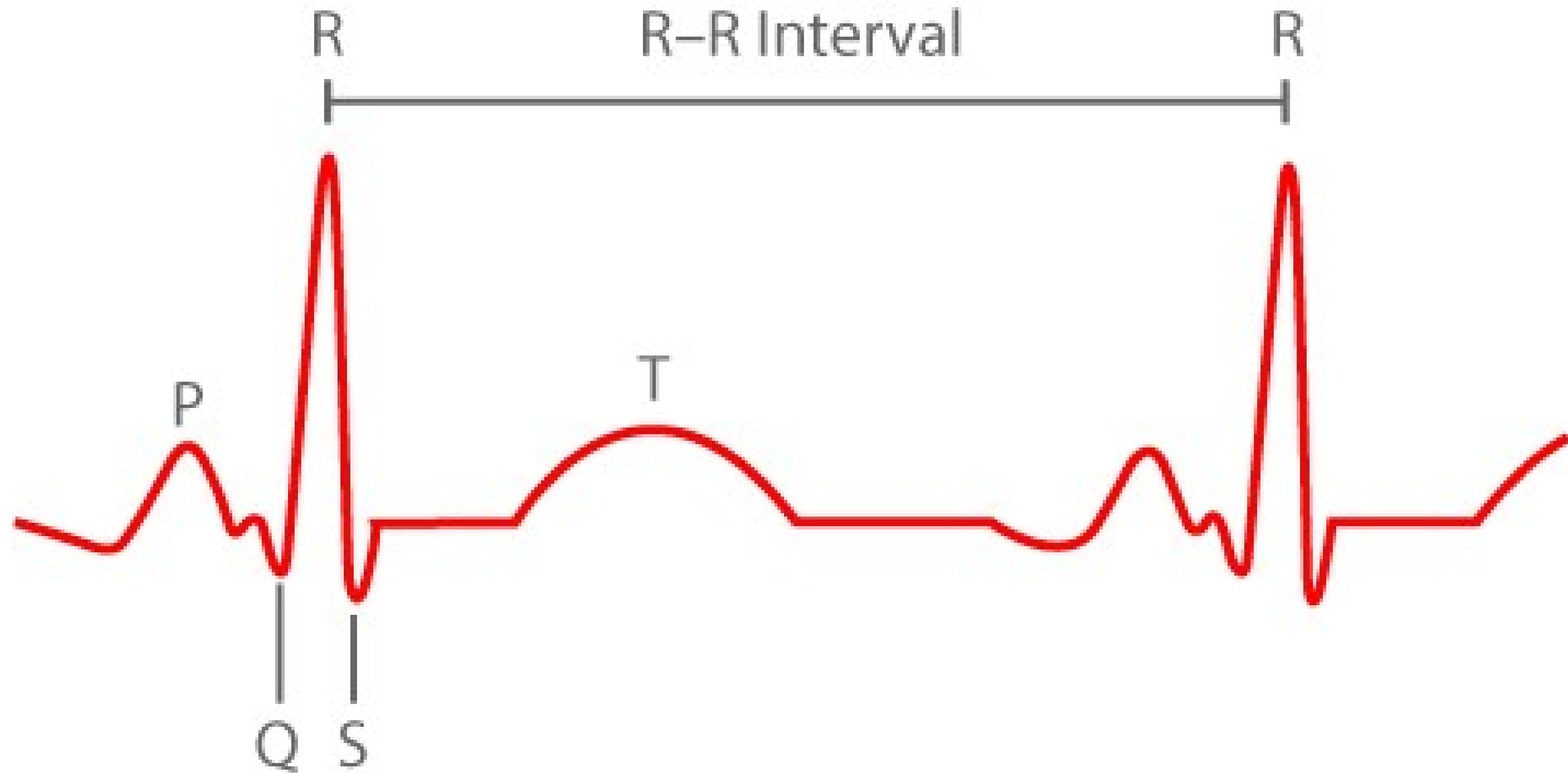
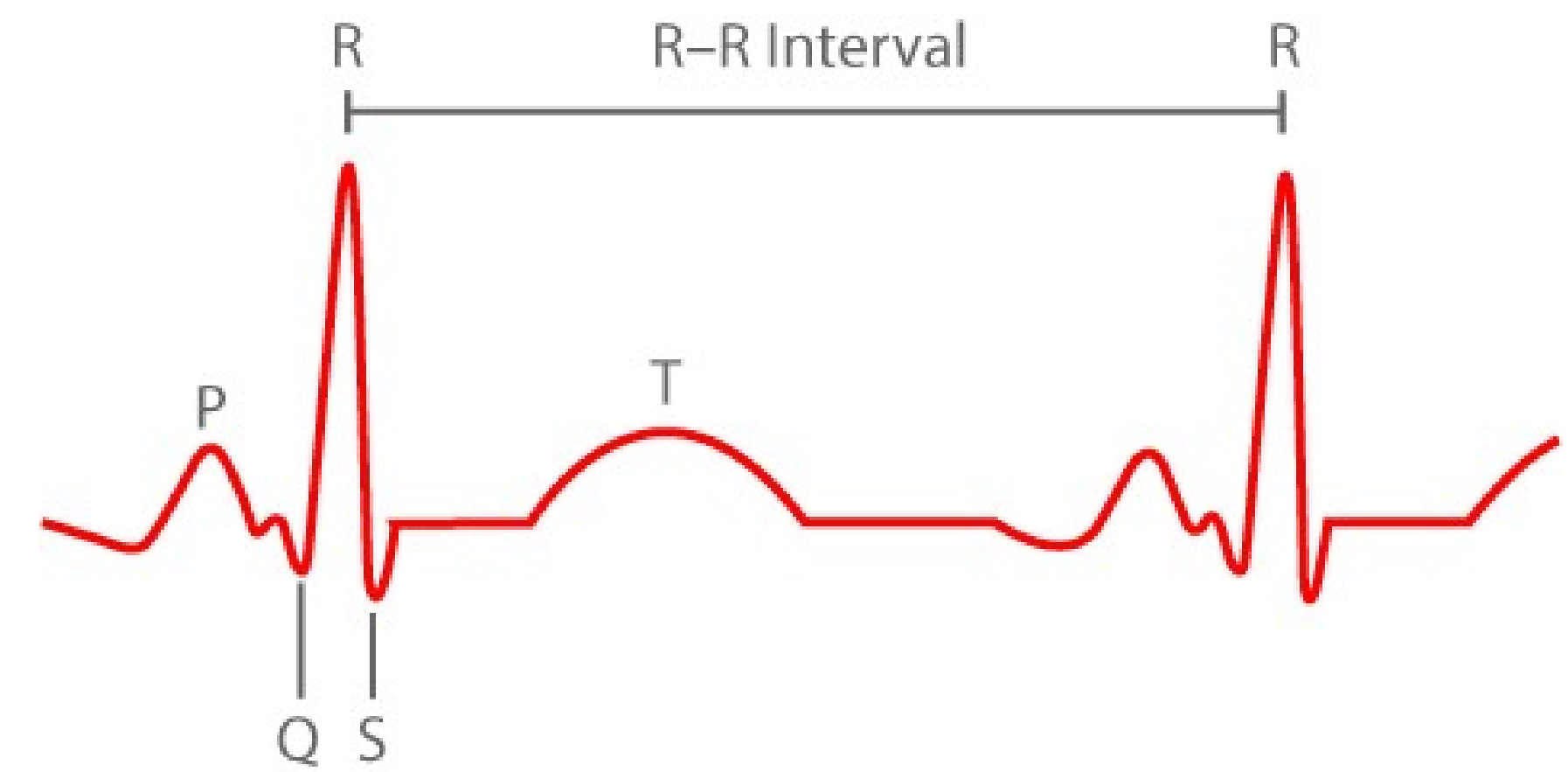


# Heart rate variability (HRV)



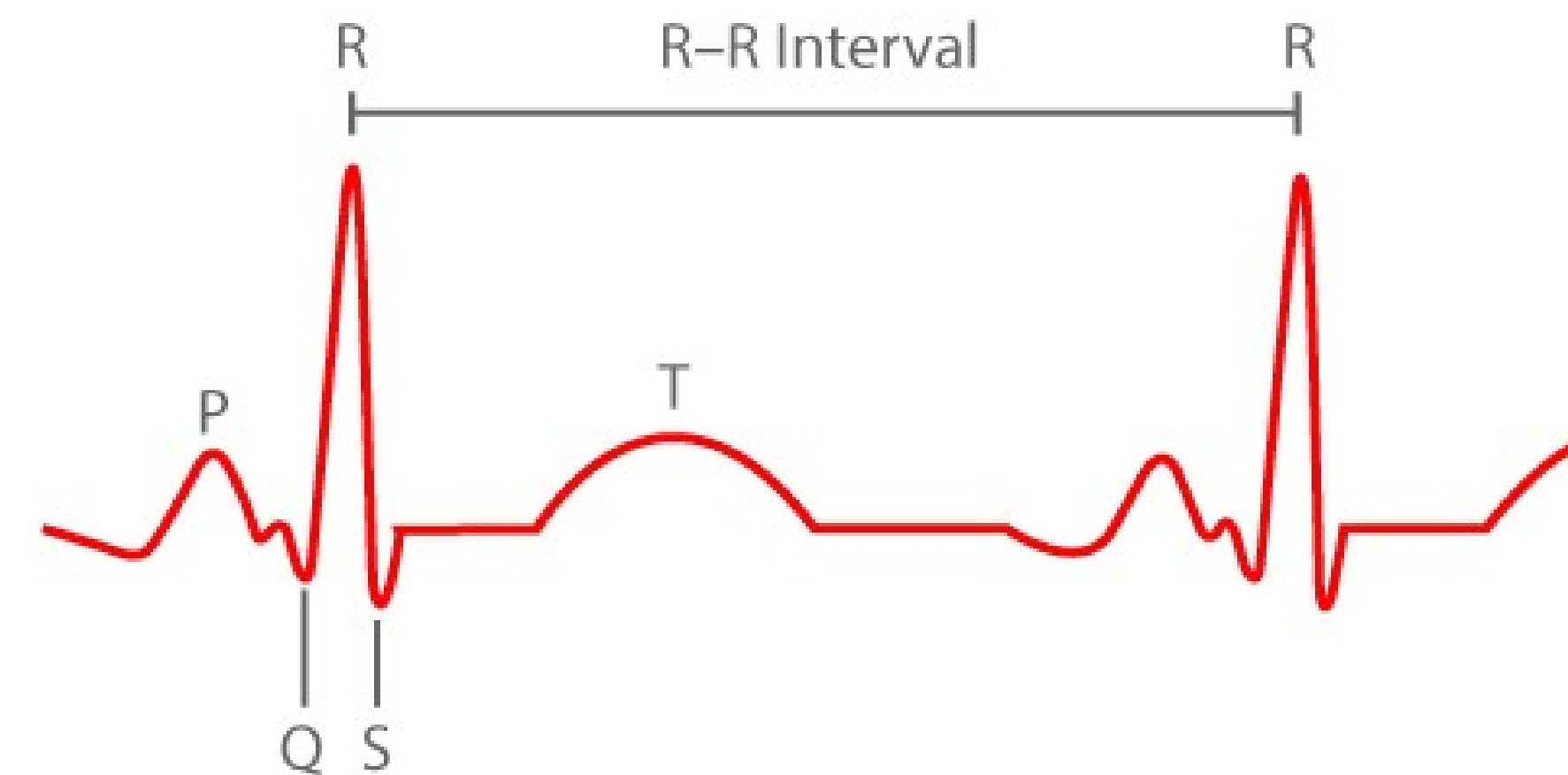
# Linear methods – time domain



Source: <https://www.myithlete.com/what-is-hrv>

- mean RR 
$$\overline{RR} = \frac{1}{N} \sum_{i=1}^N RR_i$$
- RR variation 
$$RR_{variation} = \frac{(RR_{max} - RR_{min}) \times 100}{RR_{mean}}$$
- std RR 
$$std\ RR = \sqrt{\frac{1}{N-1} \sum_{i=1}^N (\overline{RR} - RR_i)^2}$$

# Linear methods – time domain



Source: <https://www.myithlete.com/what-is-hrv>

- RMSSD (root mean square of successive differences)

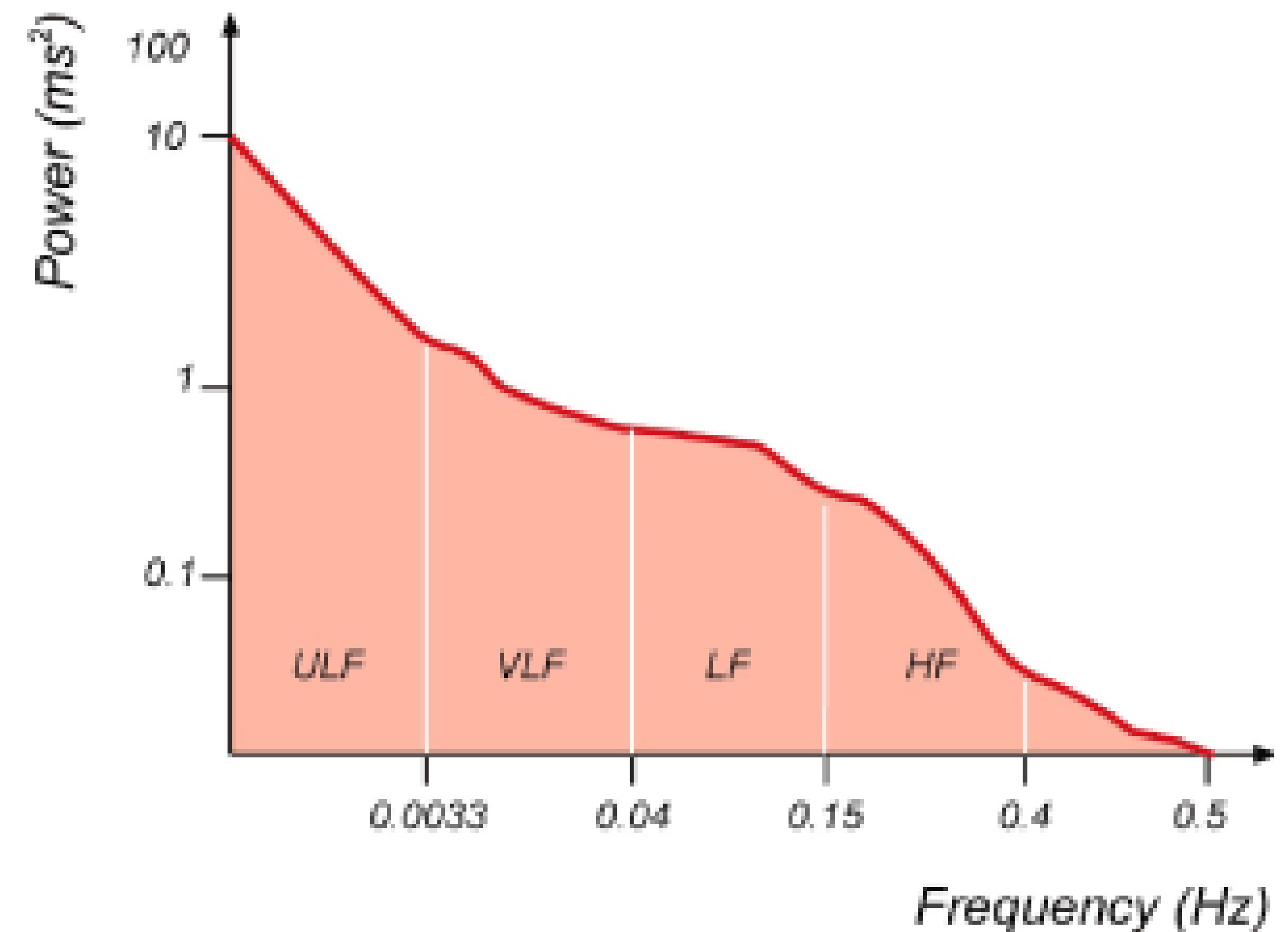
$$RMSSD = \sqrt{\frac{1}{N-1} \sum_{i=1}^N (RR_{i+1} - RR_i)^2}$$

- successive RR interval  $> 20$  or  $50$  ms

$$P(|RR_{i+1} - RR_i| > 50 \text{ ms})$$

# Linear methods – frequency domain

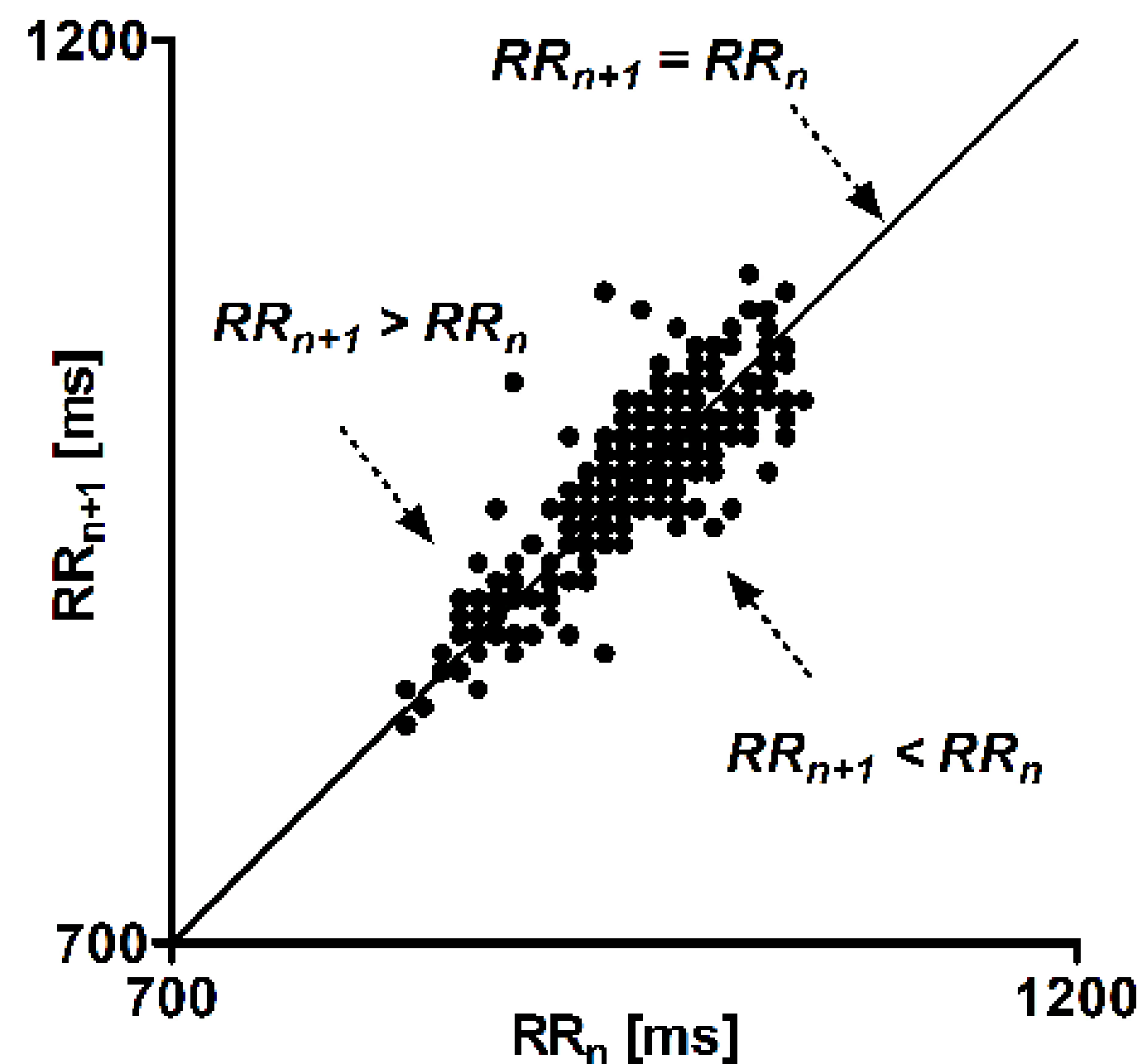
- total power (TP);
- ultra-low frequency (ULF) ( $<0,0033\text{Hz}$ );
- very low frequency (VLF) ( $0,0033\text{--}0,04\text{Hz}$ );
- low frequency (LF) ( $0,04\text{--}0,15\text{Hz}$ );
- high frequency (HF) ( $0,15\text{--}0,4\text{Hz}$ );



Source: Yilmaz M,  
Kayancicek H, Cekici Y,  
Heart rate variability:  
Highlights from hidden  
signals, Journal of  
Integrative Cardiology,  
January 2018, 5:265

# Nonlinear method - Poincare plot

- Visual pattern whereby the shape of the plot is categorized into functional classes that indicate the degree of heart failure;
- Can be evaluated quantitatively through the computation of the SD indexes of the plot.



Source: Guzik P., Piskorski J., Krauze T., Correlation between the Poincare Plot and conventional Heart Rate Variability Parameters Assessed during Paced Breathing, The Journal of Physiological Science, March 2007, 57(1):63-71

# Time irreversibility/asymmetry in HRV

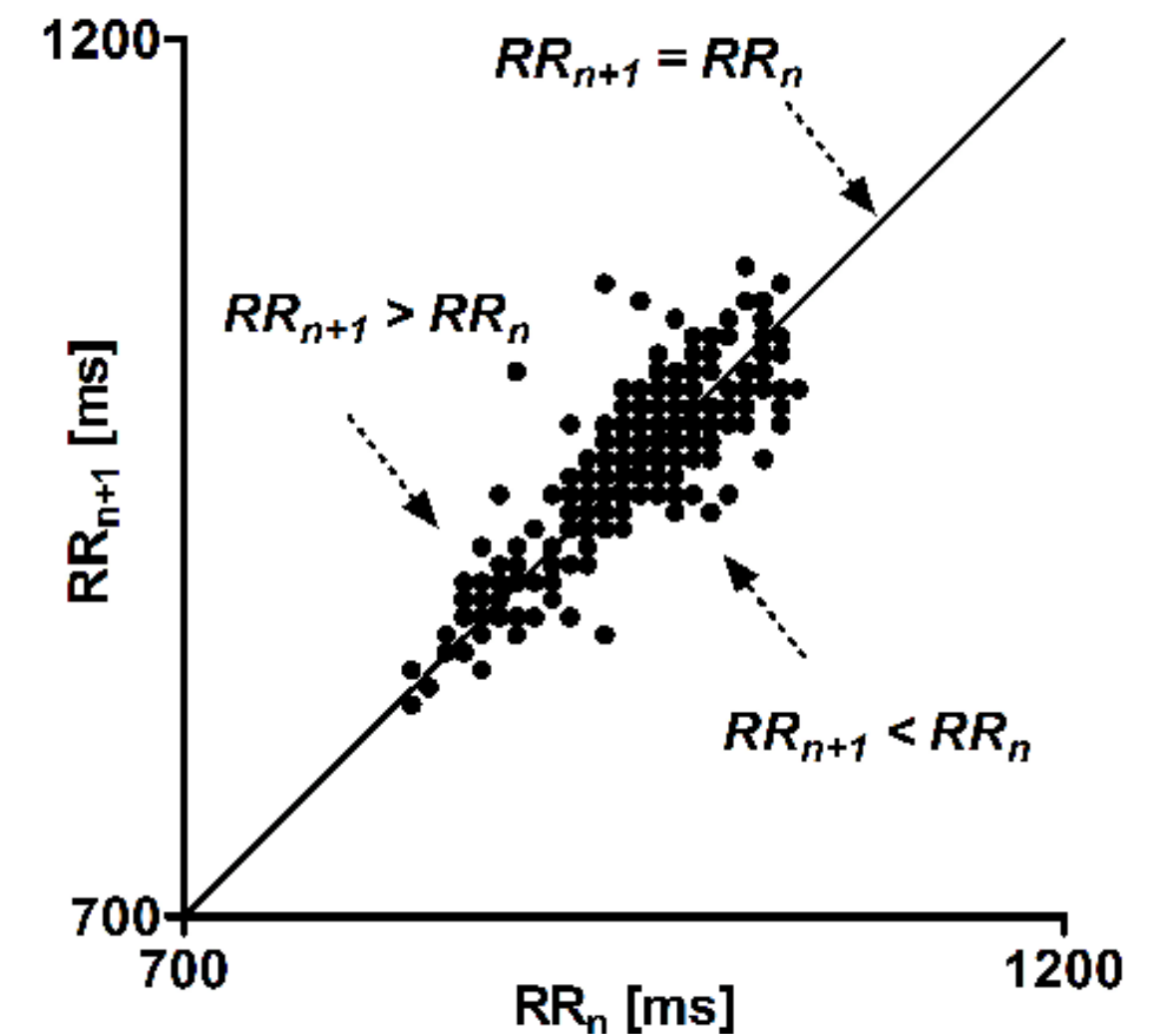
- Guzik index (GI)

$$D_i = \frac{|RR_i - RR_{i+1}|}{\sqrt{2}}$$

$$GI = \frac{\sum_{i=1}^{C(P_i^+)} (D_i^+)^2}{\sum_{i=1}^{N-1} (D_i)^2} \times 100\%$$

- Porta index (PI)

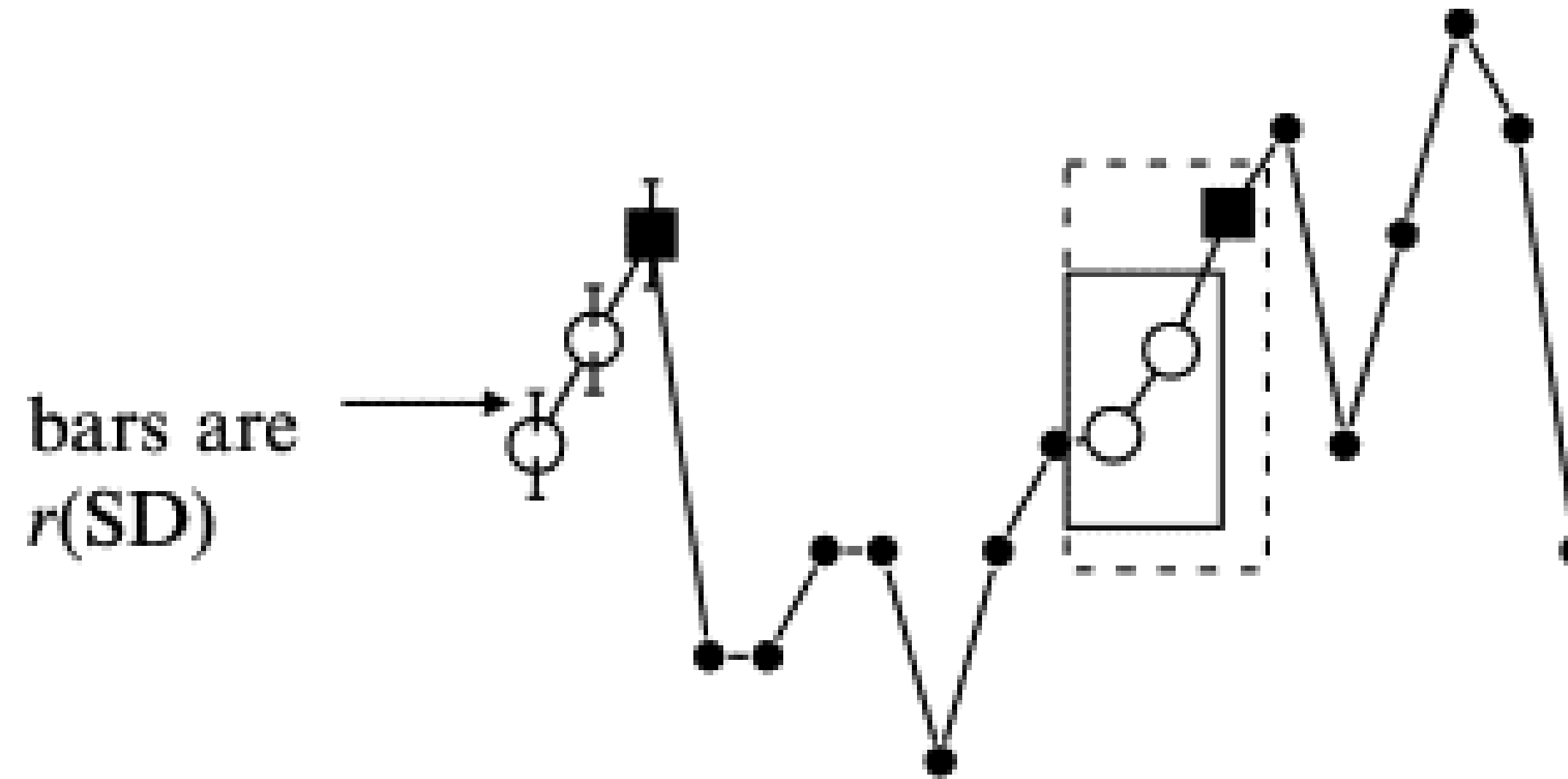
$$PI = \frac{C(P_i^-)}{C(P_i^+) + C(P_i^-)} \times 100\%$$



Source: Guzik P., Piskorski J., Krauze T., Correlation between the Poincare Plot and conventional Heart Rate Variability Parameters Assessed during Paced Breathing, The Journal of Physiological Science, March 2007, 57(1):63-71

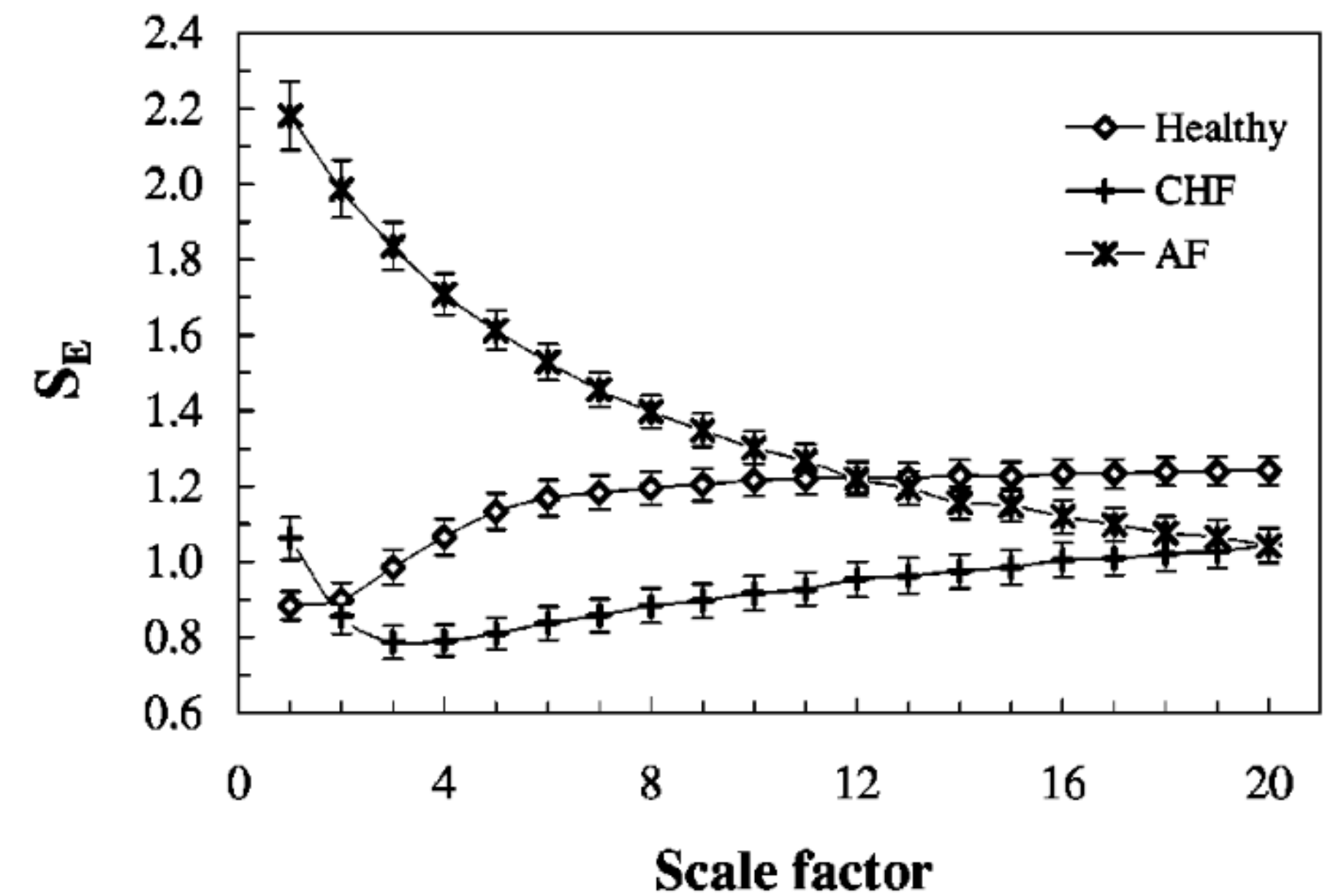
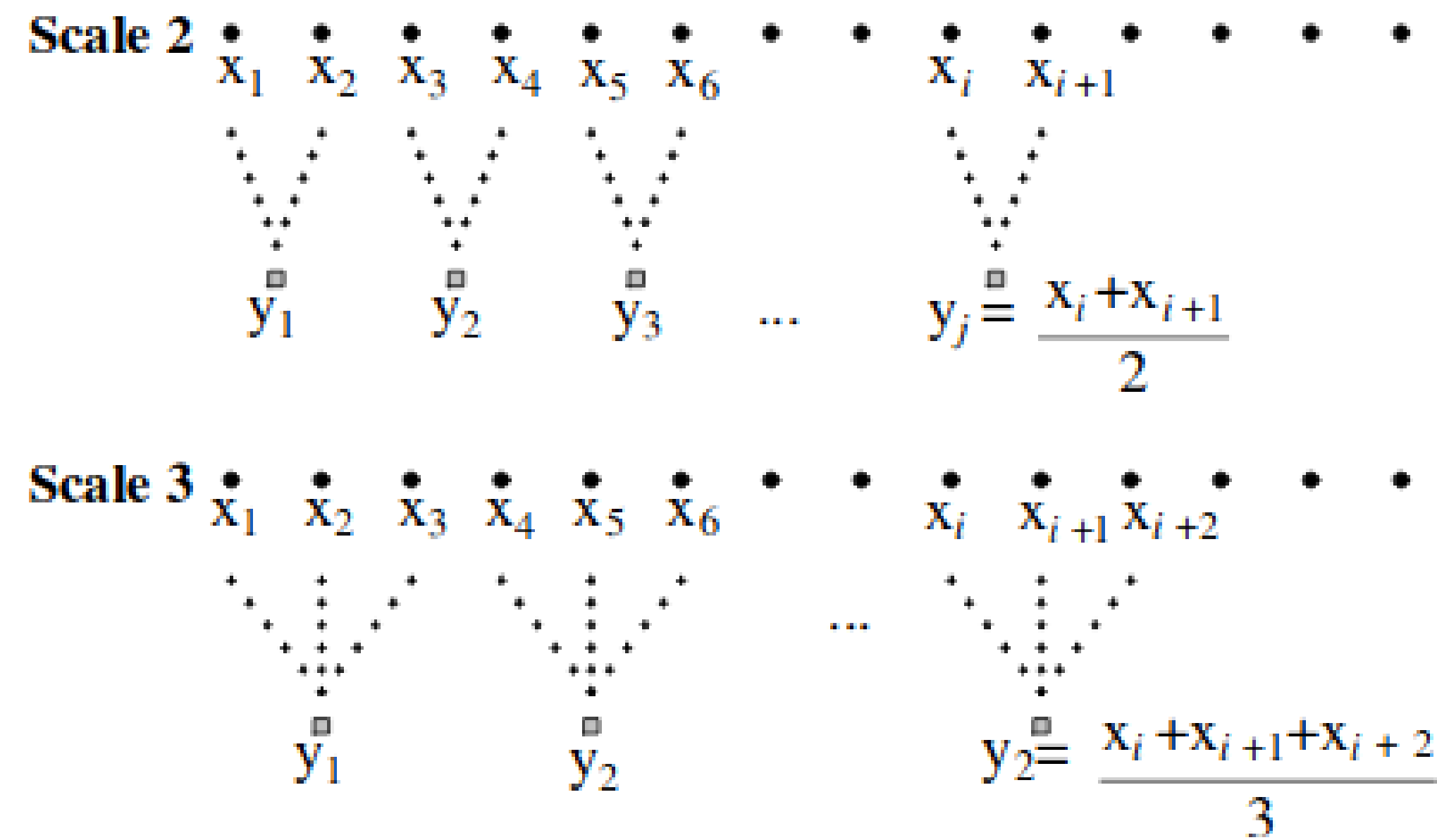
# Sample Entropy

$$\text{SampEn}(m, r, N) = -\ln \left[ \frac{A^m(r)}{B^m(r)} \right]$$



$$\text{SampEn} = -\log \left( \frac{\sum A_i}{\sum B_i} \right) = -\log A/B$$

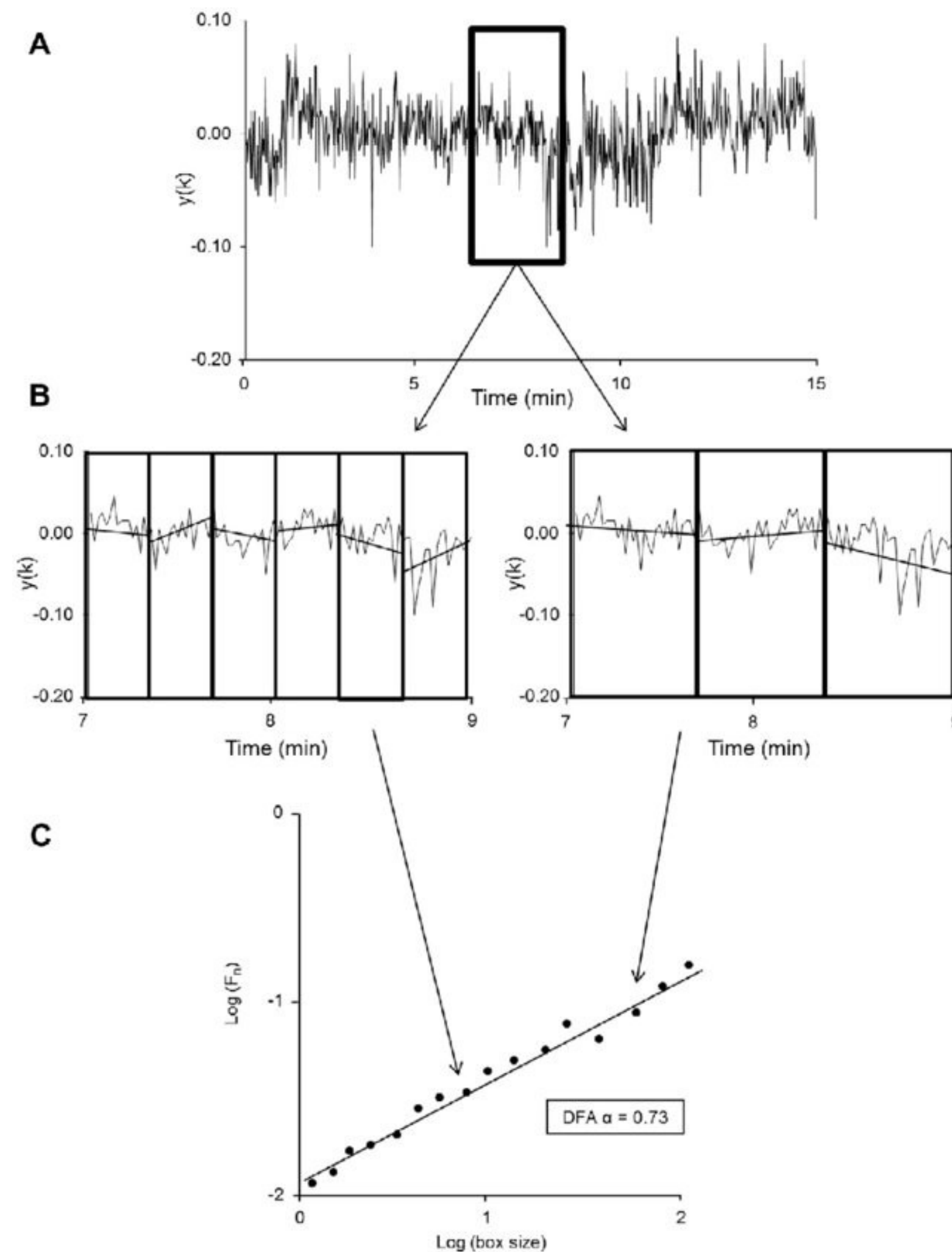
# Multiscale Entropy



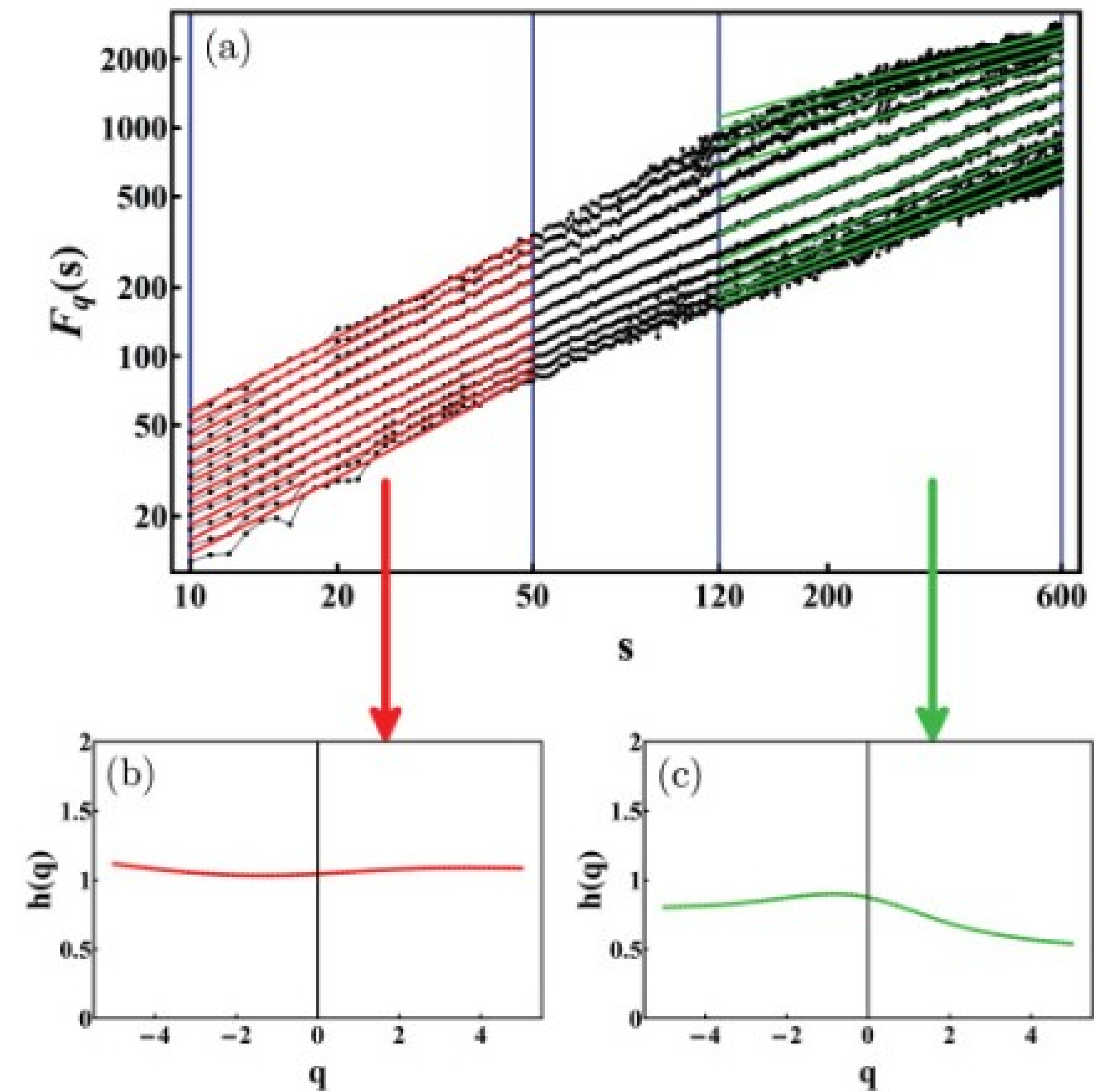
Source: Costa M.; Golderberg G.; Peng C.-K. Multiscale entropy analysis of complex physiologic time series. Physical Review Letters, 89, 2002



# Multiscale Multifractal Analysis (MMA)

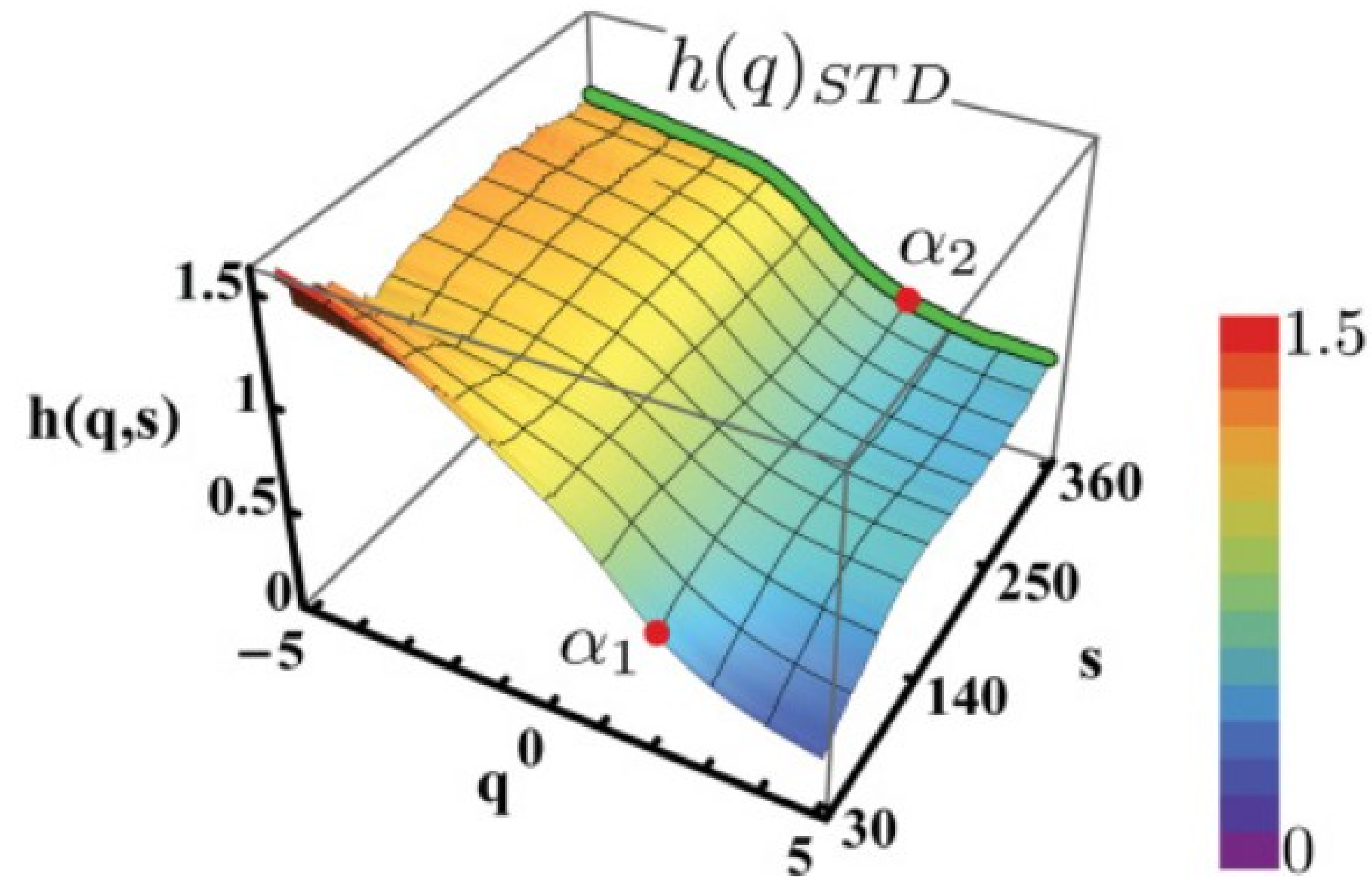


Source: Costa M.; Goldberger G.; Peng C.-K. Multiscale entropy analysis of complex physiologic time series. Physical Review Letters, 89, 2002



Source: Gieraltowski J.; Żebrowski J.J.; Baranowski R. Multiscale multifractal analysis of heart rate variability recordings with a large number of occurrences of arrhythmia. Physical Review E, 85, 2012

# Multiscale Multifractal Analysis (MMA)



Source: Gieraltowski J.; Żebrowski J.J.; Baranowski R.  
Multiscale multifractal analysis of heart rate  
variability recordings with a large number of  
occurrences of arrhythmia. Physical Review E, 85,  
2012