

1 About p-values

Unsignificant values don't permit us to draw the conclusion that there is no real effect. Looking at papers in detail is like looking at the backyard of a slaughterhouse. Only the p-value is almost never sufficient to draw meaningful conclusions on significance of a coefficient. At least we should take the effect size into account.

1.1 Panel data

Repeated observations of some individual unit over time. standard case: The same individual over the same unit of time. -> balanced panel

But "attrition" often leads to unbalanced panels. Notation: Notation for subscript

i : index for individual observations

t : index for time periods

$$X_i, t, \dots$$

if N individuals for T time periods => sample size NT: balanced panel

everything else: unbalanced people

Further examples:

Rotating panels (Socio-Economic panel SOEP)

Pseudo panels (mean cohort values over time): often used for poverty research in developing countries. Advantage: can combine data, once the cohort is identified. Deaton (1985)

Why panel data?

- more observations => more information
- dynamic analysis:
- shocks over time average out
- **unobserved heterogeneity**

2 Notation:

Linear Regression

cross section

$$Y_i = \beta_0 + \beta_1 * X_{1i} + u_i \dots$$

panel structure

$$Y_{it} = \beta_0 + \beta_1 * X_{1it} + u_{it} \dots$$

$$Y_{it} = \beta_{0t} + \beta_1 * X_{1it} + u_{it} \dots$$

t = 1

$$Y_{i1} = \beta_{01} + \beta_1 * X_{1,1} + u_{i1} \dots$$

t = T

$$Y_{iT} = \beta_{0T} + \beta_{1T} * X_{1iT} + u_{iT} \dots$$

$$D_i = 1 \text{ if } i = j, D_i = 0 \text{ if } i \neq j \text{ for } j = 1, \dots, N$$

least-squares dummy variable estimator LSDV
with individual means over time.

$$(Y_{it} - \bar{Y}_{i0}) = \beta_1(X_{it} - x_{1i.}) + (u_{it} - \bar{u}_i)$$

how to get

$$\hat{\beta}_{0i}$$

?

$$\hat{\beta}_{0i} = \bar{Y}_{i0} - \beta$$

```

#==
library(plm)
setwd("C:/Users/jakob/OneDrive/University/Data_analysis/Oct19/Panel_data") dataNL <-
readRDS("dataNL.rds") names(dataNL) <- c("index", "year", "milk", "other", "x1", "x2", "x3", "x4", "x5")
summary(dataNL)
dataNLmilk <- -log(-dataNLmilk) dataNLlx1 <- -log(dataNLlx1)
dataNLlx2 <- -log(dataNLlx2) dataNLlx3 <- -log(dataNLlx3) dataNLlx4 <-
-log(dataNLlx4) dataNLlx5 <- -log(dataNLlx5)
@ The trend variable remains unlogged.
#== plot(dataNLmilk dataNLlx1) plot(dataNLmilk dataNLlx2) plot(dataNLmilk dataNLlx3)
plot(dataNLmilk dataNLlx4) plot(dataNLmilk dataNLlx5)
formula.NL <- lm(milk ~ lx1 + lx2 + lx3 + lx4 + lx5 + trend)
lm.NL <- lm(formula.NL, data=dataNL)
summary(lm.NL)
Pool.NL <- plm(formula.NL, data = dataNL, model = "pooling")
summary(Pool.NL)
formula.LSDV <- lm(milk ~ lx1 + lx2 + lx3 + lx4 + lx5 + trend + as.factor(index))
if we run that, index has 140 dummy variables we run into the problem of
perfect multicollinearity. So R automatically drops one of the dummies.
lm.LSDV <- lm(formula.LSDV, data = dataNL)
summary(lm.LSDV)
@ In order to extract a coefficient, we use the coef() function #==
coef(Pool.NL)[2:6] sum(coef(Pool.NL)[2:6])
@ output at 1.06 which is too high. Maybe we get different results with the
LSDV estimator. #==
coef(lm.LSDV)[2:6] sum(coef(lm.LSDV)[2:6])
@ now lower coefficient taking the index dummies into account.
#==

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require(car)
linearHypothesis(Pool.NL, "lx1+lx2+lx3+lx4+lx5=1")
summary(Pool.NL) summary(lm(formula.NL, data = dataNL)) sum(coef(Pool.NL)[2:6])
WI.NL <- plm(formula.NL, data = dataNL, model = "within") cbind(coef(lm.LSDV[2:7],
coef(WI.NL)))
@ About manually applying F-Tests : - unrestricted (ignoring H0) -  $RSS^U R[residualsumofsquares]restrict$ 
 $RSS^R$ 

```

$$F = \frac{RSS^R - RSS^U R / + 1}{RSS^U R / (NT - (k - 1))}$$

Subtract means from every variable.. Using loops (?)

Dummy variables you cannot meaningfully de-mean over time. So we use the LM, but should get out the same results as with the LSDV model. ■= wi2.NL
 <- plm(formula.NL, data = dataNL, effect = "twoways", model = "within")
 plot(density(fixef(WI.NL)))

@ Problem: time-invariant variables and how to deal with them.. ■=
 dataNLTimeInvar <- runif(141) formula.TimeInvar <- -lmilk + lx1 + lx2 +
 lx3 + lx4 + lx5 + trend + TimeInvar

head(dataNLTimeInvar) WI.NL <- plm(formula.NL, data = dataNL, model =
 "within")

@ Next steps: random effects model

3 scenario

No interest in the unobserved heterogeneity, no need to interpret the individual effects;

$$\alpha_i$$

- parameters are a mere nuisance (guidance?) -> error

$$Y_{i,t} = \alpha_i + \beta_1 * X_{1,i,t} + u_{i,t}$$

alpha is error

$$= \beta_0 + \beta_1 * X_{1,i,t} + \alpha_i + u_{i,t}$$

two error components α_i, u_{it}

Ignore error structure: OLS $\rightarrow unbiased \rightarrow inefficient$

$$\alpha_i \sim N(0, \sigma_\alpha^2) \text{ with } u_{it} \sim N(0, \sigma_u^2)$$

Estimating: Feasible Generalised Least Squares FGLS

$$E(Cov[X, u]) = 0$$

$$E(Cov[X, \alpha]) = 0$$

← in many contexts this is a critical assumption. It is often questionable that individual effects and regressors are uncorrelated in the effects model.

⇒ Wald test :

$$(\beta_{FE} - \beta_{RE})(\hat{VCov}_{FE} - \hat{VCov}_{RE})'(\beta_{FE} - \beta_{RE})$$

⇒ Hausmann Test: Alternative: Variable addition

FE by within

2) plus all X_i ⇒ should be not having any explanatory power if $E(cov(x, \alpha)) = 0$

Test by F-test whether all $\bar{X}_{i,s}$ have zero parameters or not.

"Mundlak correction"

■ =

```
RE.NL <- plm(formula.NL, data=dataNL, model = "random") cbind(coef(WI.NL),
coef(Pool.NL)[2:7])
```

```
cbind(coef(WI.NL), coef(Pool.NL)[2:7], coef(RE.NL)[2:7])
```

@

We got a lower R^2