

# Foundations of Data Science

DS 3001

Data Science Program

Department of Computer Science

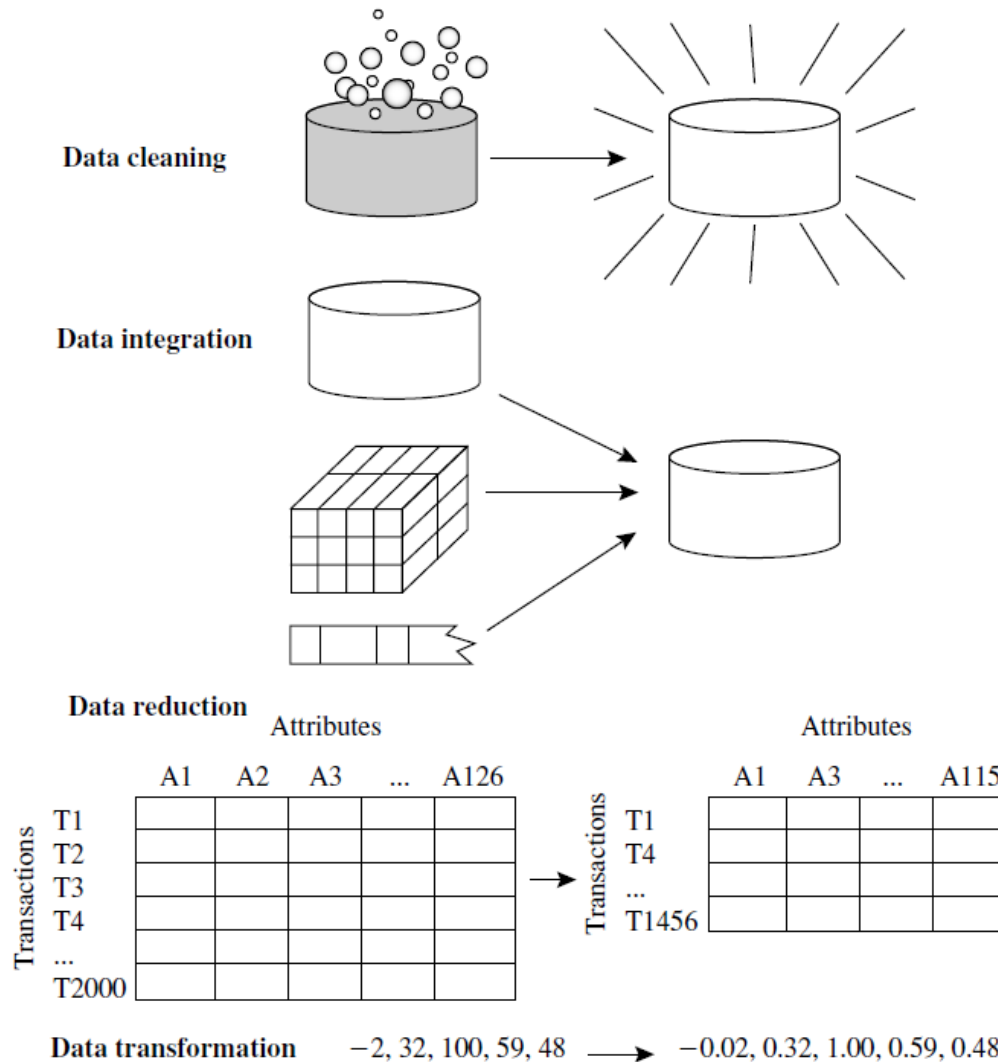
Worcester Polytechnic Institute

Instructor: Prof. Kyumin Lee

# Project Teams

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  6. Noah Puchovsky, Katherine Handy, Alex Tavares, Angelica Puchovsky
  7. Armando Zubillaga, Gabriel Rodrigues, Humberto Leon, Joao Omena de Lucena
  8. Edward Carlson, Samuel Goldman, Nick Krichevsky, Christopher Myers
  9. Jessie White, Lindsay MacInnis, Bao Huynh, Ziqian Zeng
  10. Suverino Frith, Nicholas Odell, Fay Whittall, Johvanni Perez
  11. Alp Piskin, Robert Scalfani, Jake Barefoot, Mark Bernardo
  12. Amanda Chan, Nugzar Chkhaidze, Luke Gebler
  13. Daniel Pelaez, Nathan Savard, Kate Sincaglia
- So far, 49 students expressed their preferences

# Forms of Data Preprocessing



# Data Integration

# Data Integration

- **Data integration:**
  - Combines data from multiple sources into a coherent store
- **Handling Redundancy in Data Integration**
  - Redundant data occur often when integration of multiple databases
    - *Object identification:* The same attribute or object may have different names in different databases
    - *Derivable data:* One attribute may be a “derived” attribute in another table, e.g., annual revenue
  - Redundant attributes may be able to be detected by correlation analysis and covariance analysis
- How to find redundant attributes or almost duplicate attributes?

# Correlation Analysis (Nominal Data)

- $\chi^2$  (chi-square) test

$$\chi^2 = \sum \frac{(\textit{Observed} - \textit{Expected})^2}{\textit{Expected}}$$

- The larger the  $\chi^2$  value, the more likely the variables are related
- The cells that contribute the most to the  $\chi^2$  value are those whose actual count is very different from the expected count
- Expected frequency of  $(A_i, B_j)$ , which can be calculated as

$$e_{ij} = \frac{\textit{count}(A = a_i) \times \textit{count}(B = b_j)}{n},$$

- Correlation does not imply causality
  - # of hospitals and # of car-theft in a city are correlated
  - Both are causally linked to the third variable: population

# Chi-Square Calculation: An Example

	Play chess	Not play chess	Sum (row)
Like science fiction	250(90)	200(360)	450
Not like science fiction	50(210)	1000(840)	1050
Sum(col.)	300	1200	1500

- $\chi^2$  (chi-square) calculation (numbers in parenthesis are expected counts calculated based on the data distribution in the two categories)

$$\chi^2 = \frac{(250 - 90)^2}{90} + \frac{(50 - 210)^2}{210} + \frac{(200 - 360)^2}{360} + \frac{(1000 - 840)^2}{840} = 507.93$$

- It shows that two attributes are correlated in the group

# Correlation Analysis (Numeric Data)

- Correlation coefficient (also called Pearson's product moment coefficient)

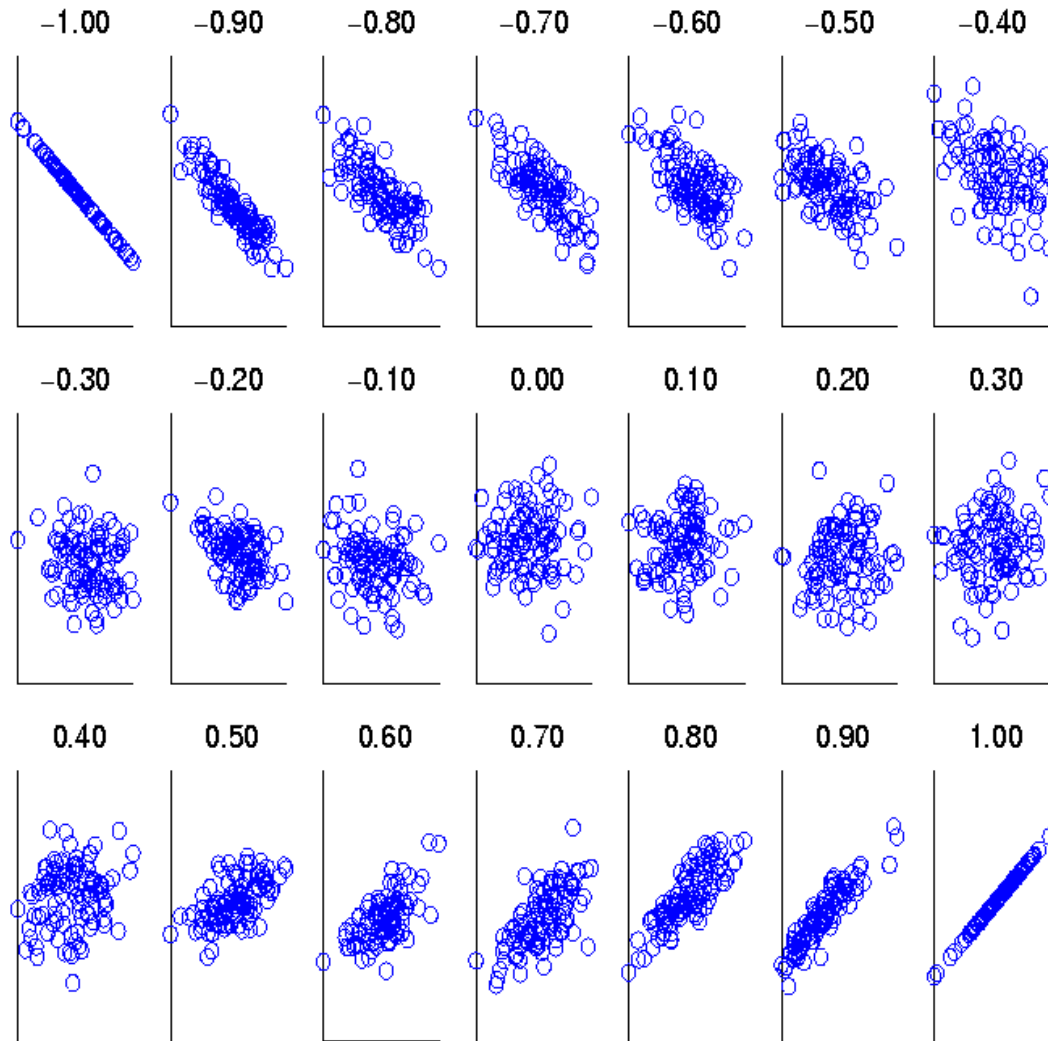
$$r_{A,B} = \frac{\sum_{i=1}^n (a_i - \bar{A})(b_i - \bar{B})}{(n-1)\sigma_A\sigma_B} = \frac{\sum_{i=1}^n (a_i b_i) - n\bar{A}\bar{B}}{(n-1)\sigma_A\sigma_B}$$

where  $n$  is the number of tuples,  $\bar{A}$  and  $\bar{B}$  are the respective means of  $A$  and  $B$ ,  $\sigma_A$  and  $\sigma_B$  are the respective standard deviation of  $A$  and  $B$ , and  $\sum(a_i b_i)$  is the sum of the  $AB$  cross-product.

- If  $r_{A,B} > 0$ ,  $A$  and  $B$  are positively correlated ( $A$ 's values increase as  $B$ 's). The higher the value, the stronger the correlation.
- $r_{A,B} = 0$ : independent;  $r_{AB} < 0$ : negatively correlated



# Visually Evaluating Correlation



**Scatter plots  
showing the  
similarity from  
-1 to 1.**

# Data Reduction

# Data Reduction

- **Data reduction:** Obtain a reduced representation of the data set that is much smaller in volume but yet produces the same (or almost the same) analytical results
- Why data reduction? — A database/data warehouse may store petabytes of data. Complex data analysis may take a very long time to run on the complete data set.

# Dimensionality Reduction

- **Curse of dimensionality**
  - When dimensionality increases, data becomes increasingly sparse
  - Density and distance between points, which is critical to clustering, outlier analysis, becomes less meaningful
  - The possible combinations of subspaces will grow exponentially
- **Dimensionality reduction**
  - Avoid the curse of dimensionality
  - Help eliminate irrelevant features and reduce noise
  - Reduce time and space required in data mining
  - Allow easier visualization

# Data Reduction

- Dimensionality reduction, e.g., remove unimportant attributes
  - Principal Components Analysis (PCA)
  - Feature selection (i.e., Attribute subset selection), attribute creation
- Numerosity reduction
  - data is replaced or estimated by alternative, smaller data representations
  - Parametric
    - Regression and Log-Linear Models
  - Non-parametric
    - Histograms, clustering, sampling

# Data Transformation and Data Discretization

# Data Transformation

- A function that maps the entire set of values of a given attribute to a new set of replacement values so that each old value can be identified with one of the new values
- Why conduct data transformation?
  - The resulting mining process may be more efficient, the patterns found may be easier to understand
- Data Transformation Methods
  - Smoothing: Remove noise from data
  - Attribute/feature construction
    - New attributes constructed from the given ones
  - Aggregation: Summarization, data cube construction
  - Normalization: Scaled to fall within a smaller, specified range
    - min-max normalization
    - z-score normalization
    - normalization by decimal scaling
  - Discretization: raw values of numeric attributes (e.g., age) replaced by interval labels (e.g., 0-10, 11-20, etc.) or conceptual labels (e.g., youth, adult, senior)

# Normalization

- **Min-max normalization:** to  $[new\_min_A, new\_max_A]$

$$v' = \frac{v - min_A}{max_A - min_A} (new\_max_A - new\_min_A) + new\_min_A$$

- Ex. Let income range \$12,000 to \$98,000 normalized to [0.0, 1.0]. Then \$73,600 is mapped to  $\frac{73,600 - 12,000}{98,000 - 12,000} (1.0 - 0) + 0 = 0.716$

- **Z-score normalization** ( $\mu$ : mean,  $\sigma$ : standard deviation):

$$v' = \frac{v - \mu_A}{\sigma_A}$$

- Ex. Let  $\mu = 54,000$ ,  $\sigma = 16,000$ . Then  $\frac{73,600 - 54,000}{16,000} = 1.225$

- **Normalization by decimal scaling**

$$v' = \frac{v}{10^j} \quad \text{Where } j \text{ is the smallest integer such that } \text{Max}(|v'|) < 1$$



# Summary

- **Data quality:** accuracy, completeness, consistency, timeliness, believability, interpretability
- **Data cleaning:** e.g. missing/noisy values, outliers
- **Data integration** from multiple sources:
  - Entity identification problem
  - Remove redundancies
  - Detect inconsistencies
- **Data reduction**
  - Dimensionality reduction
  - Numerosity reduction
  - Data compression
- **Data transformation and data discretization**
  - Normalization
  - Concept hierarchy generation
- Read section 3 in Data Mining Concepts and Techniques

# Data Science: The Context

Ask question: What data needs to be recorded? or collected?



Real World



Humans behaving  
Biology  
Finance  
Internet  
Medicine  
Sociology  
Olympics



Raw Data is  
Collected / Recorded

email  
logs  
medical records  
surveys  
blood drawn  
(microarray)  
olympic records  
NYT web pages



Data is  
Processed

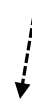
pipelines  
web scraping  
cleaning  
munging  
joining  
wrangling



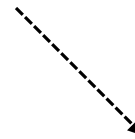
Data Set

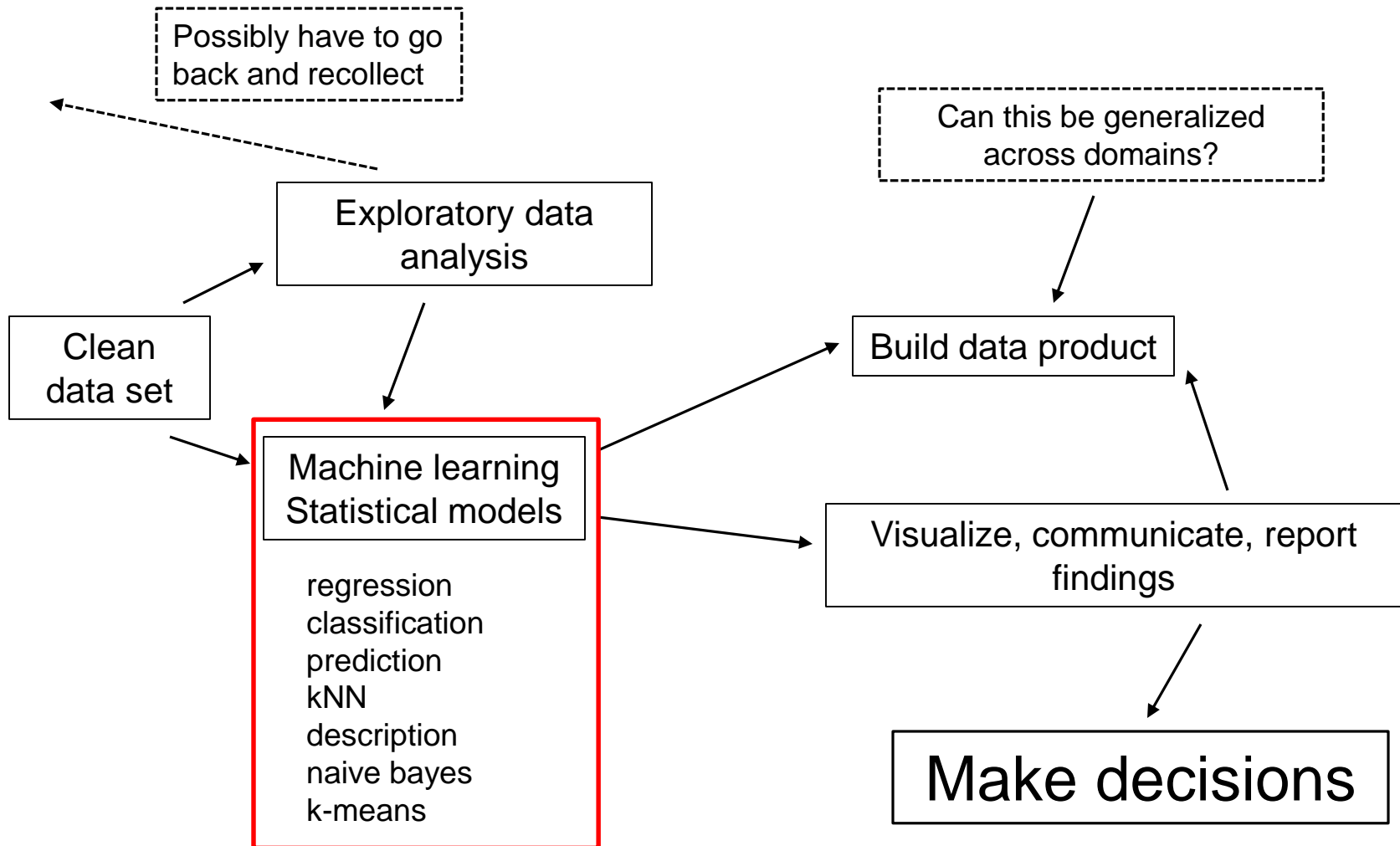
“clean” table

Why? What research question  
am I going to answer?



What do I want it to look like?

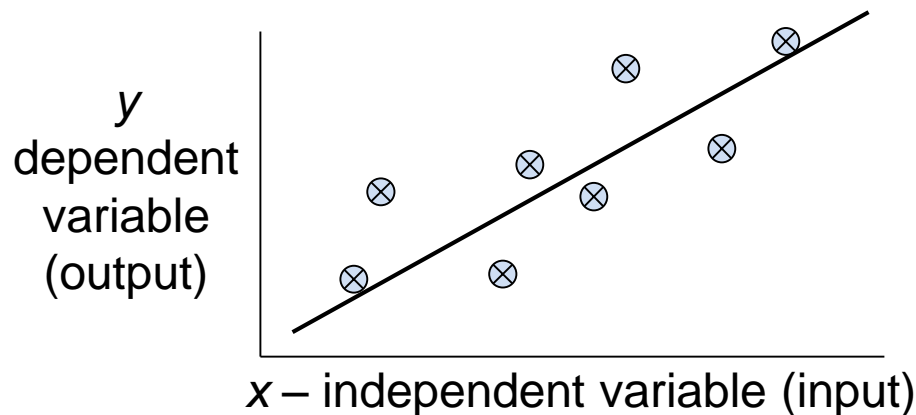




# Mining and Analytics: Linear Regression

# Regression

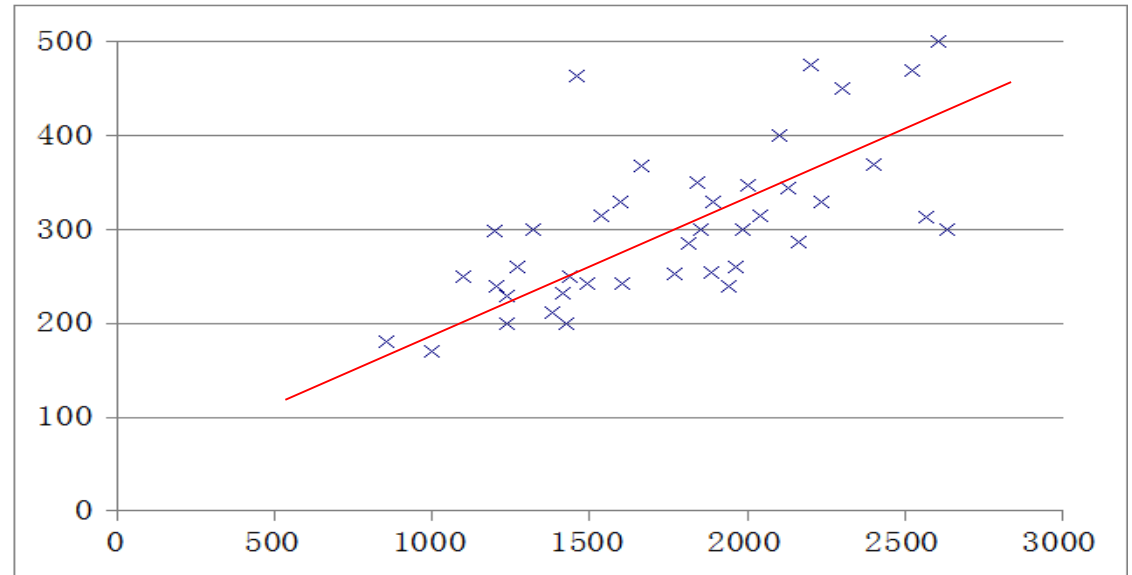
- In regression the output is continuous
  - Function Approximation
  - Also a supervised learning
    - Given the “right answer” for each example in the data.
- Many models could be used – Simplest is linear regression
  - Fit data with the best hyper-plane which "goes through" the points



# Linear Regression with one Variable

## Housing Prices (Portland, OR)

Price  
(in 1000s  
of dollars)



Size (feet<sup>2</sup>)

Regression Problem

Predict real-valued output

# Any applications?

- advertising and sales
- consumption and income
- etc



## Training set of housing prices

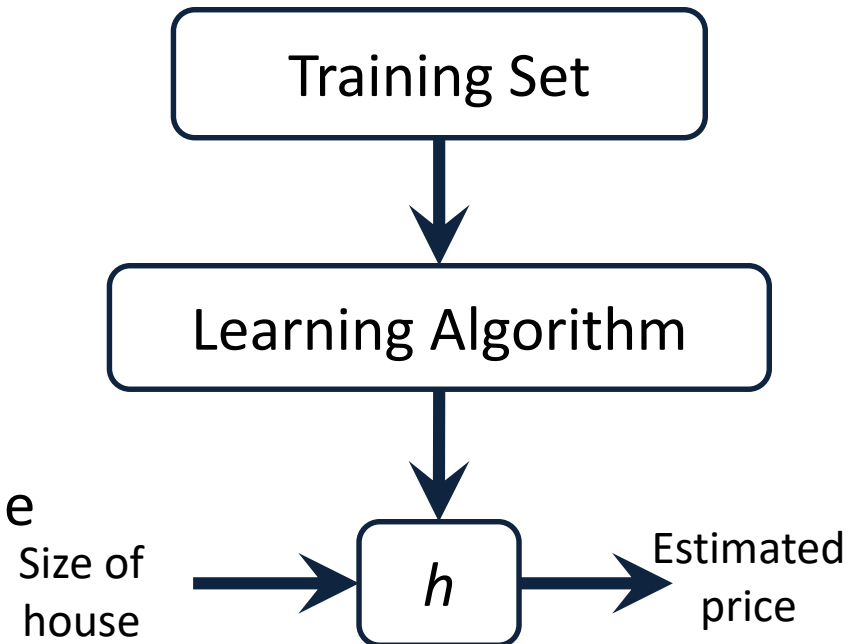
Size in feet <sup>2</sup> ( $x$ )	Price (\$) in 1000's ( $y$ )
2104	460
1416	232
1534	315
852	178
...	...

Notation:

$n$  = Number of training examples

$x$ 's = "input" variables / features

$y$ 's = "output" variable / "target" variable



Question : How to describe  $h$ ?

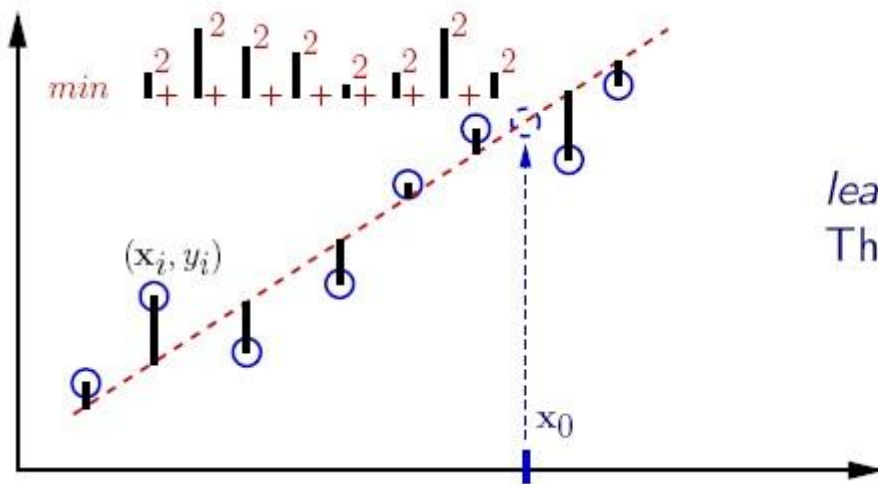
# Linear Regression

- Hypothesis:

$$h_{\theta}(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \dots + \theta_d x_d = \sum_{j=0}^d \theta_j x_j$$

Assume  $x_0 = 1$

- Fit model by minimizing sum of squared errors



*least squares (LSQ)*

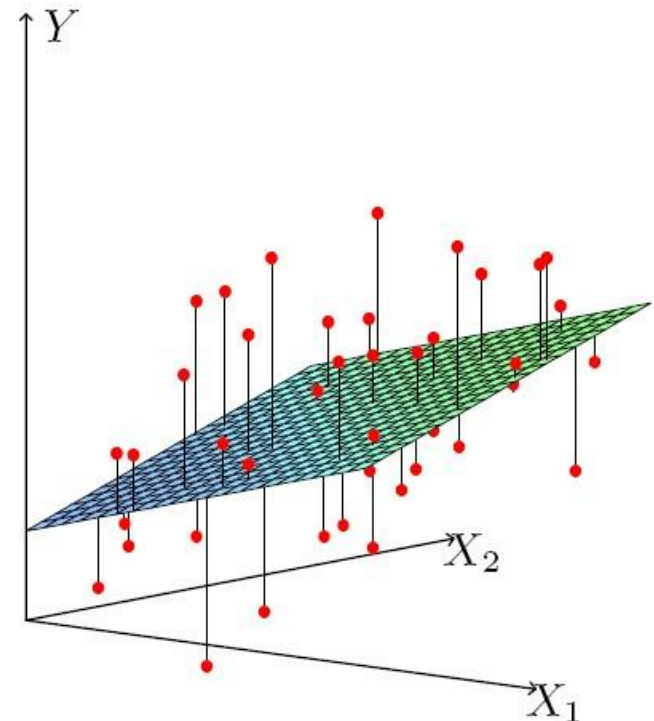
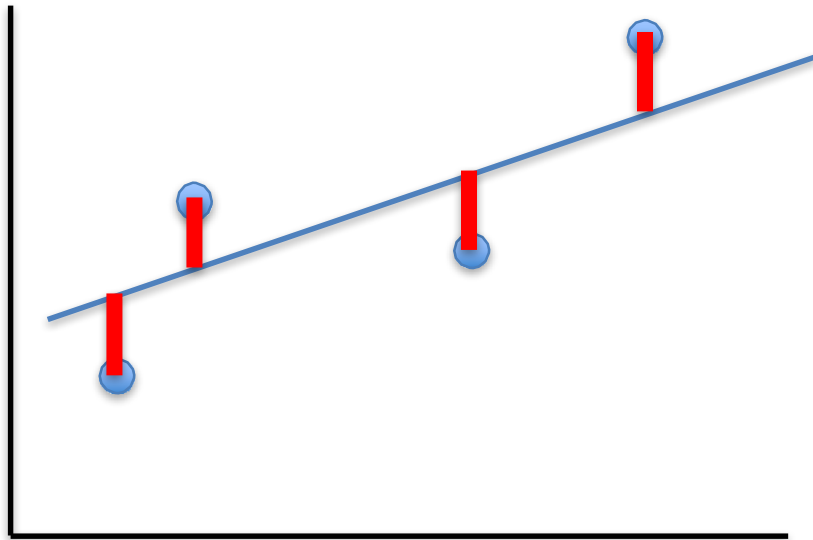
The fitted line is used as a predictor

# Least Squares Linear Regression

- Cost Function

$$J(\theta) = \frac{1}{2n} \sum_{i=1}^n (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

- Fit by solving  $\min_{\theta} J(\theta)$



# Intuition Behind Cost Function

$$J(\theta) = \frac{1}{2n} \sum_{i=1}^n (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

For insight on  $J()$ , let's assume  $x \in \mathbb{R}$  so  $\theta = [\theta_0, \theta_1]$

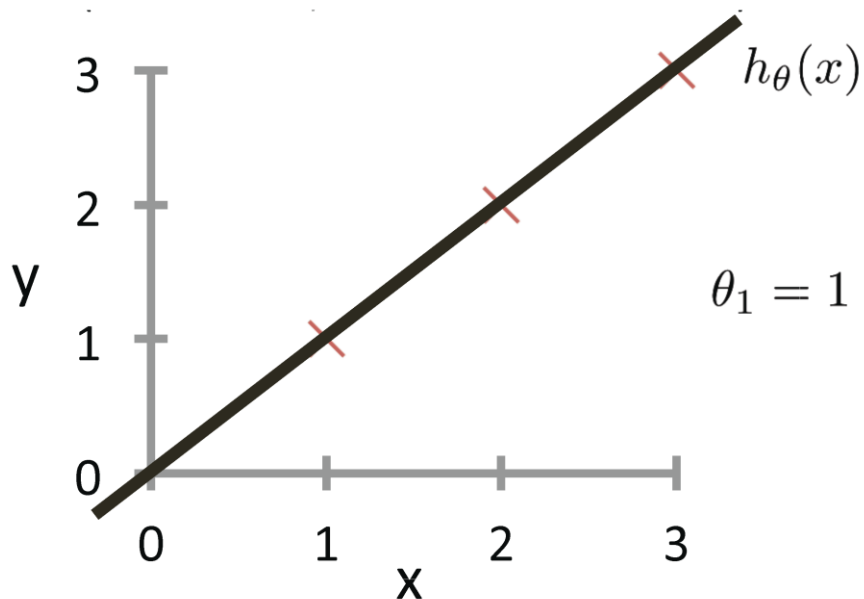
# Intuition Behind Cost Function

$$J(\theta) = \frac{1}{2n} \sum_{i=1}^n (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

For insight on  $J()$ , let's assume  $x \in \mathbb{R}$  so  $\theta = [\theta_0, \theta_1] \rightarrow \theta_0 = 0$

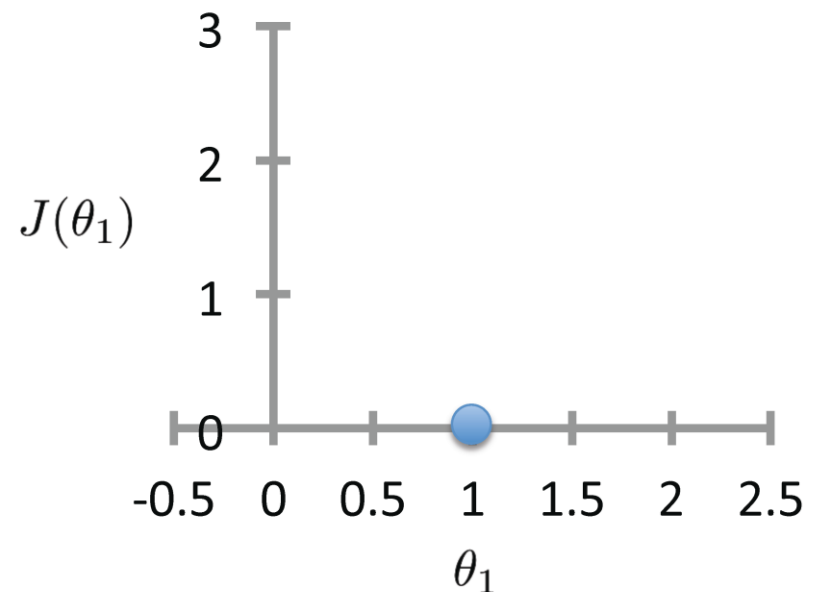
$h_{\theta}(x)$

(for fixed  $\theta_1$ , this is a function of  $x$ )



$J(\theta)$

(function of the parameter  $\theta_1$ )



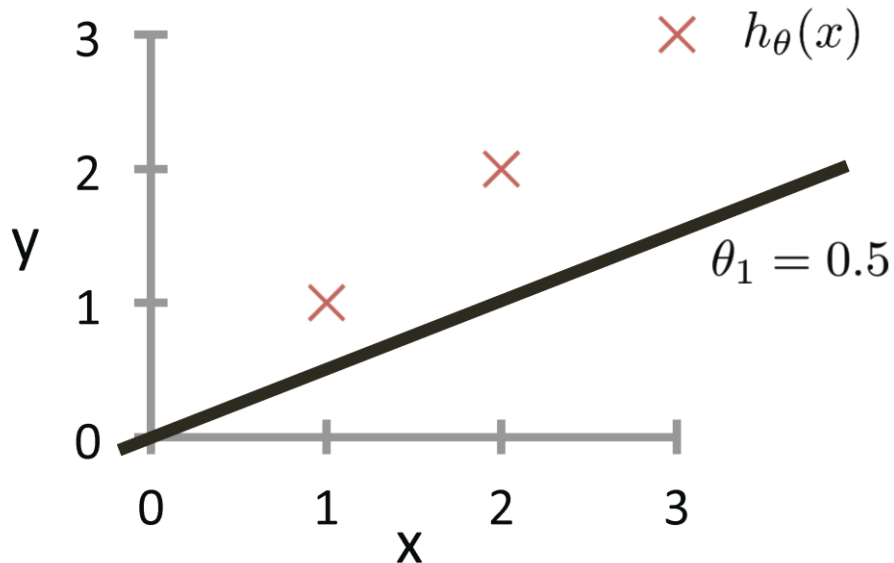
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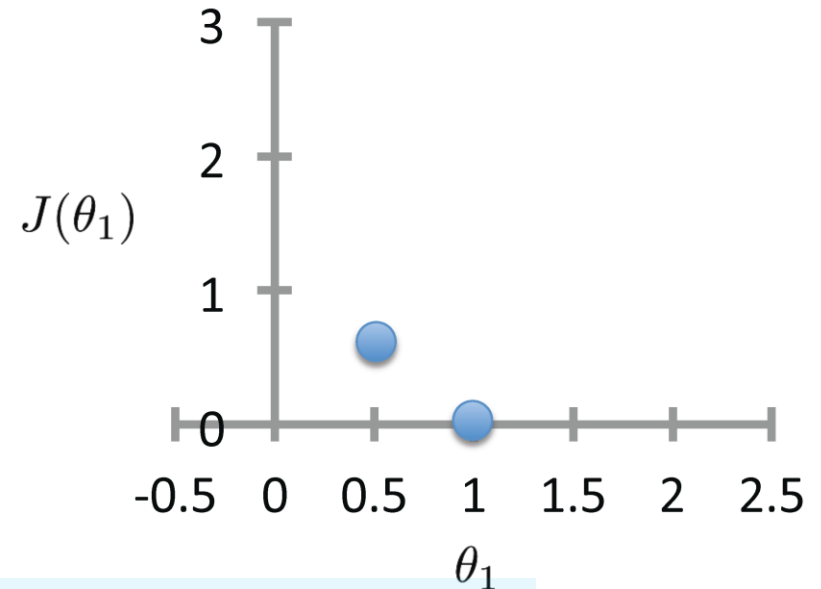
$h_{\theta}(x)$

(for fixed  $\theta_1$ , this is a function of  $x$ )



$J(\theta)$

(function of the parameter  $\theta_1$ )



$$J([0,0.5]) = \frac{1}{2 \times 3} [(0.5 - 1)^2 + (1 - 2)^2 + (1.5 - 3)^2] \approx 0.58$$

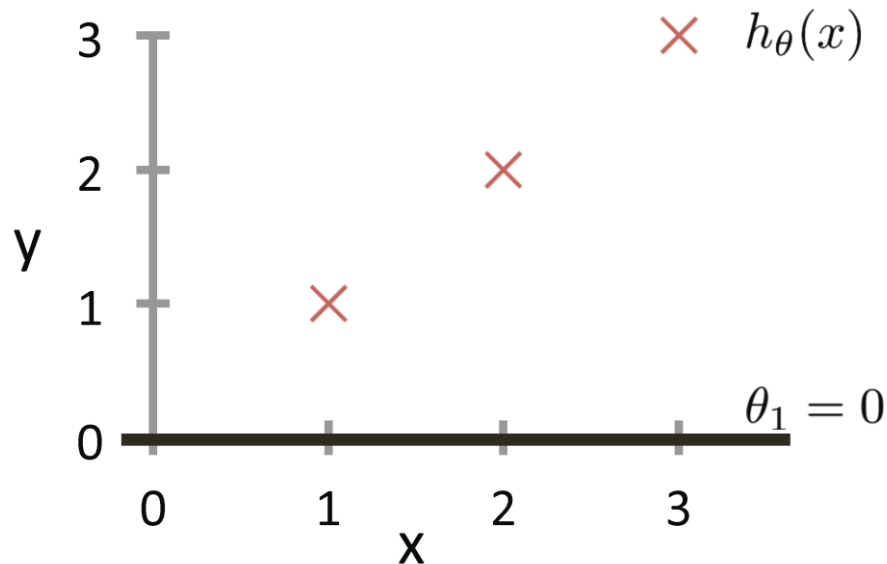
# Intuition Behind Cost Function

$$J(\theta) = \frac{1}{2n} \sum_{i=1}^n (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

For insight on  $J()$ , let's assume  $x \in \mathbb{R}$  so  $\theta = [\theta_0, \theta_1]$

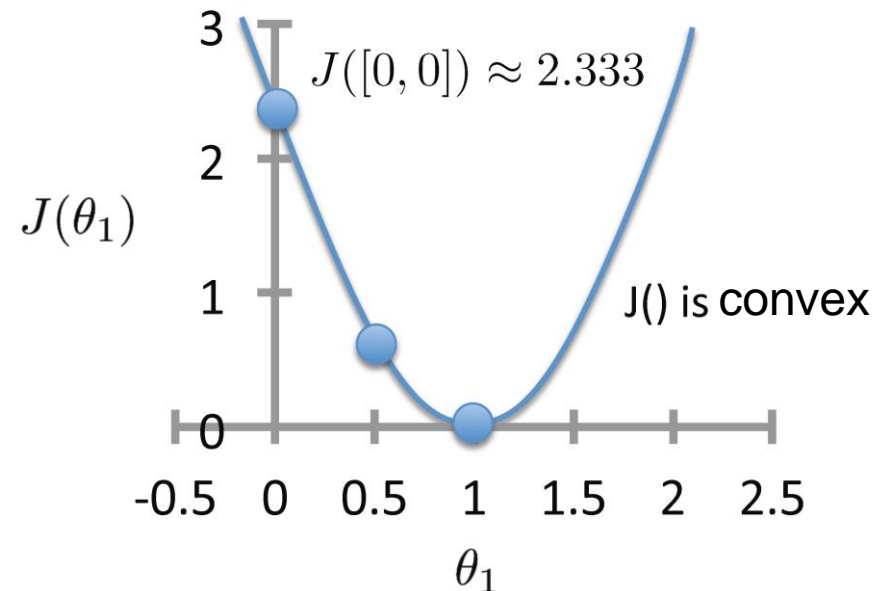
$h_{\theta}(x)$

(for fixed  $\theta_1$ , this is a function of  $x$ )



$J(\theta)$

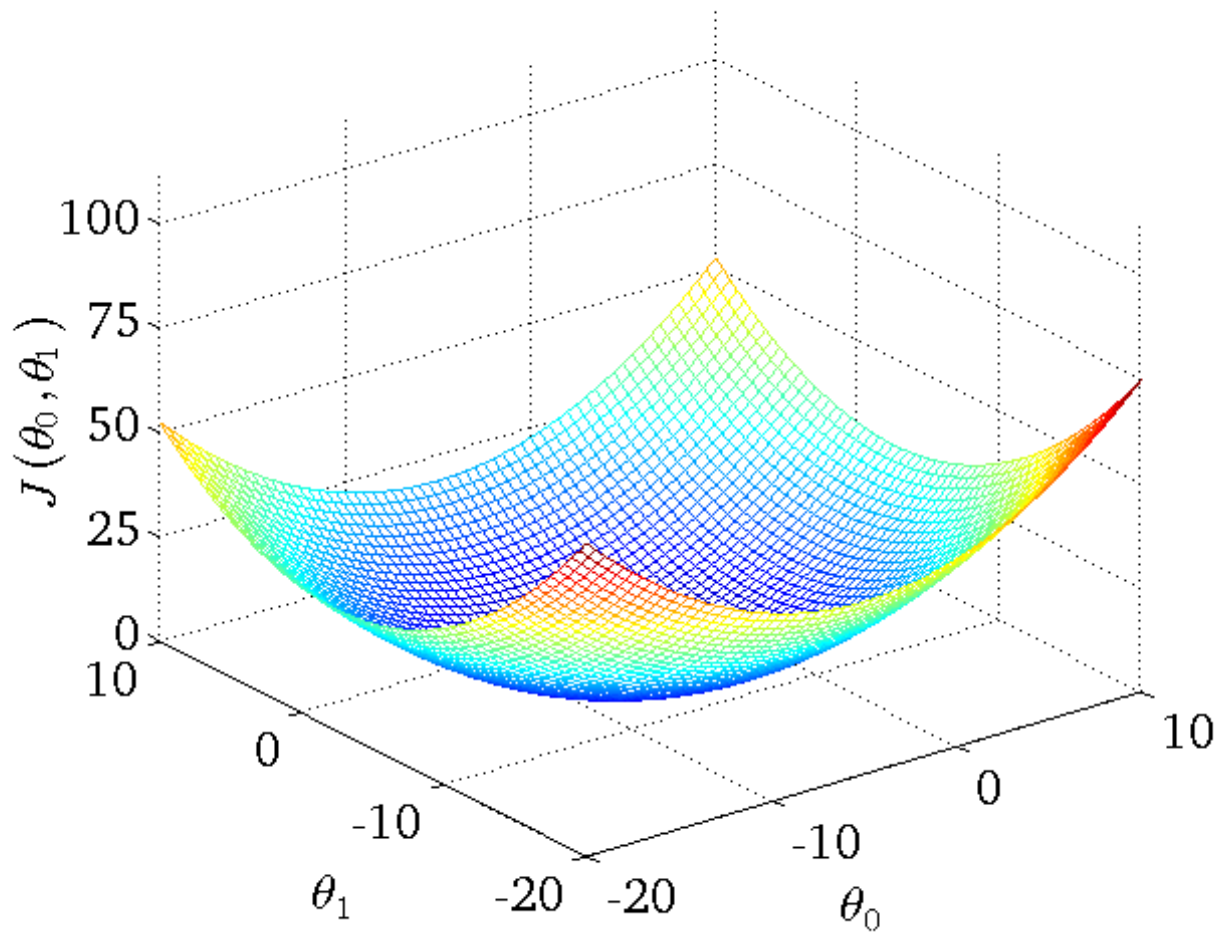
(function of the parameter  $\theta_1$ )



<http://mathworld.wolfram.com/ConvexFunction.html>

<https://www.desmos.com/calculator/kreo2ssqj8>

# Intuition Behind Cost Function (3-D surface plot)

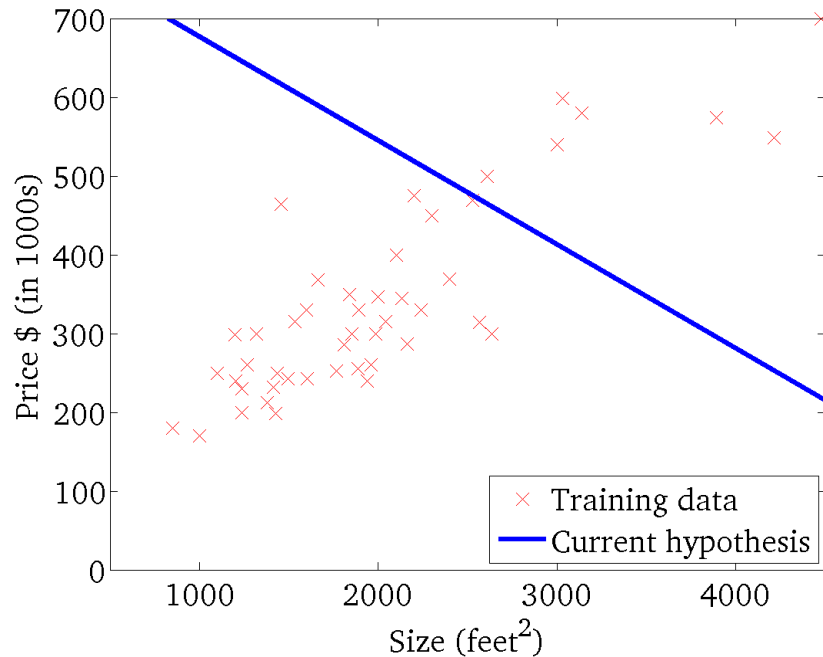




# Intuition Behind Cost Function

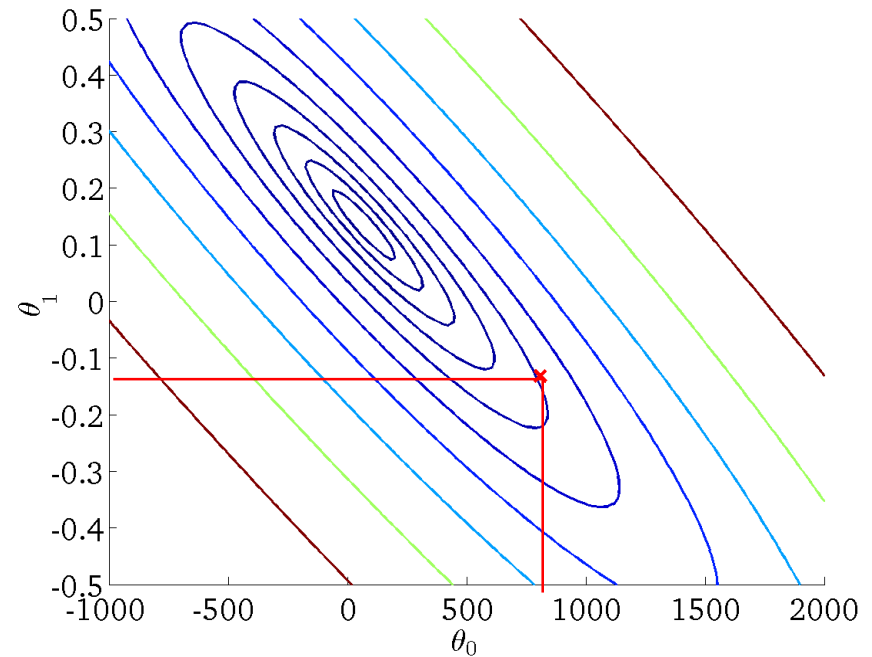
$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )



$$J(\theta_0, \theta_1)$$

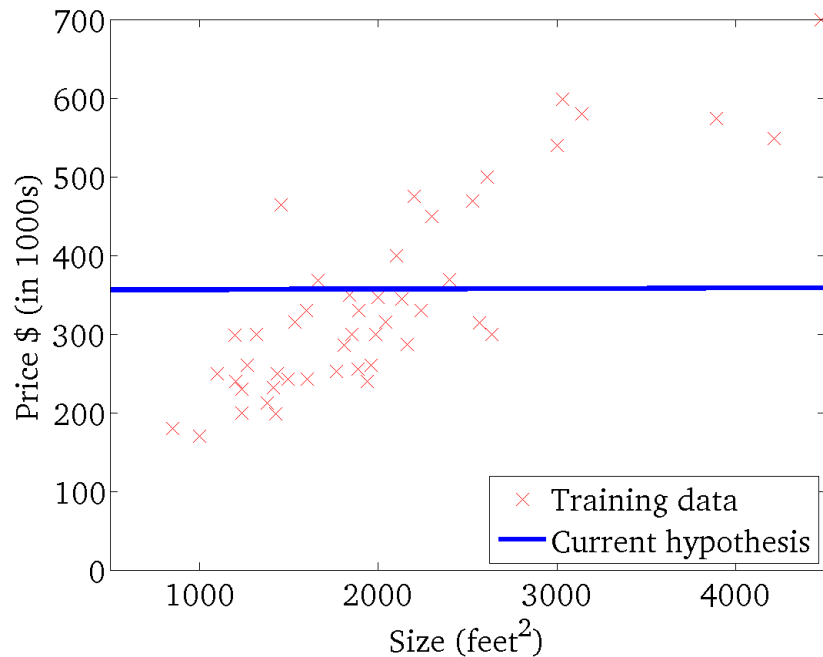
(function of the parameter  $\theta_0, \theta_1$ )



# Intuition Behind Cost Function

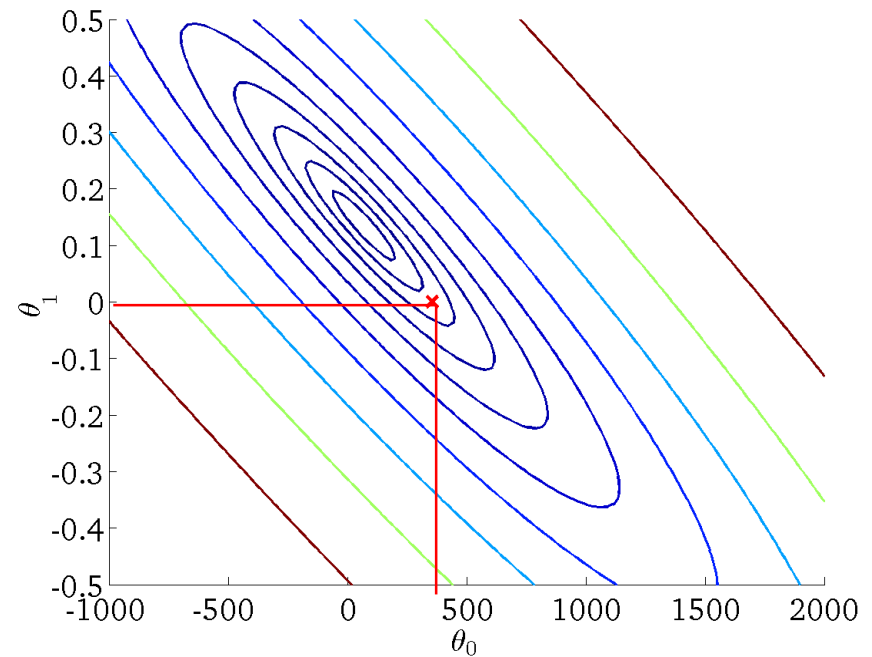
$$h_{\theta}(x)$$

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$$J(\theta_0, \theta_1)$$

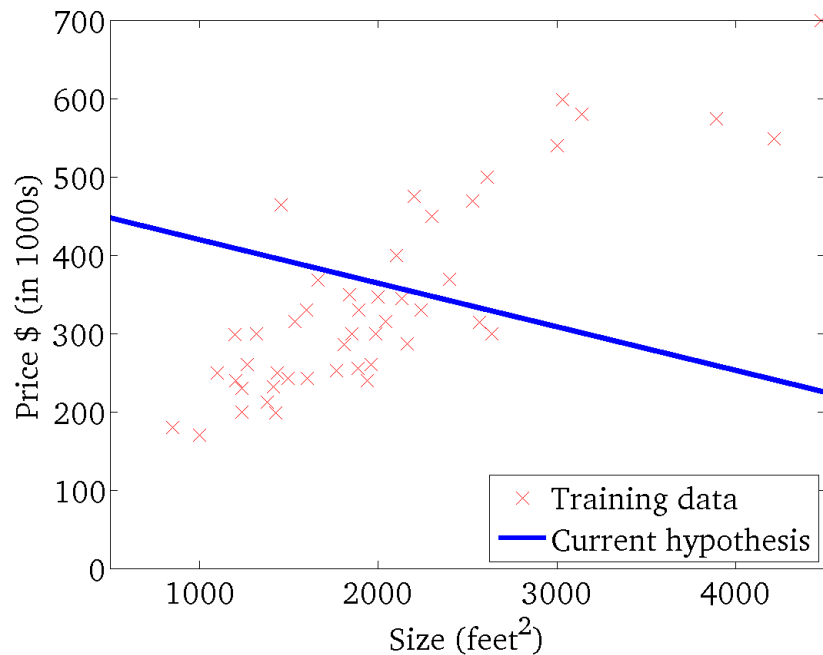
(function of the parameter  $\theta_0, \theta_1$ )



# Intuition Behind Cost Function

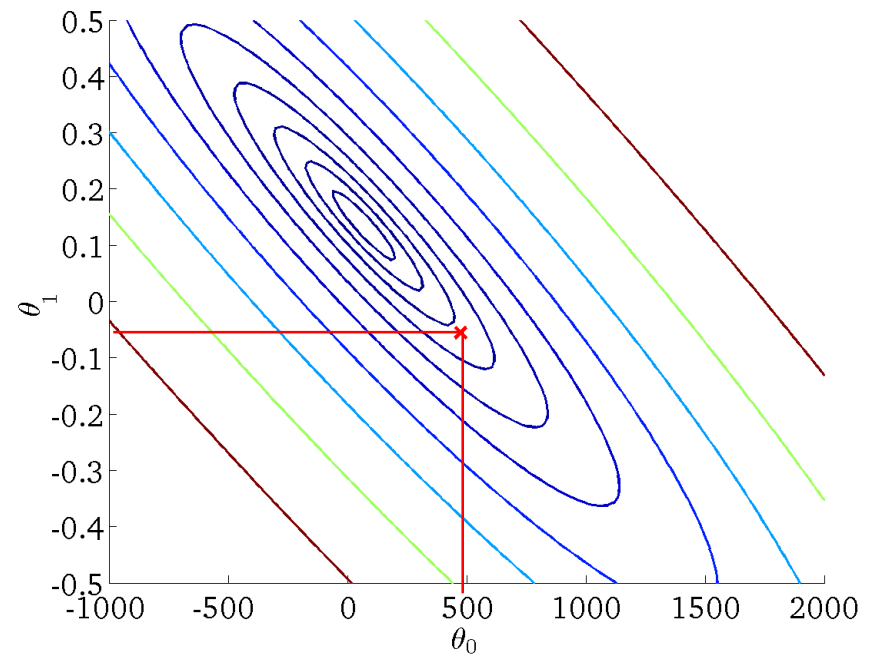
$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )



$$J(\theta_0, \theta_1)$$

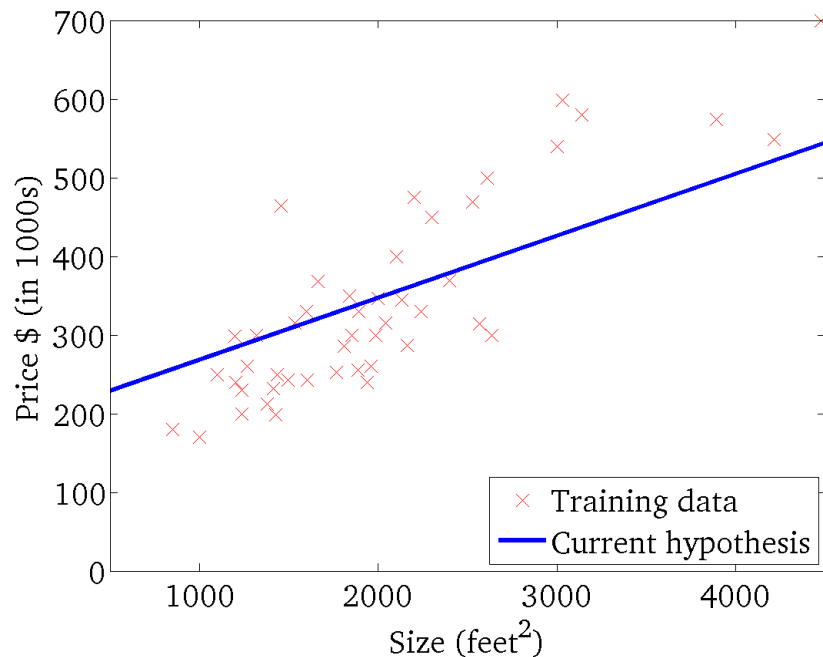
(function of the parameter  $\theta_0, \theta_1$ )



# Intuition Behind Cost Function

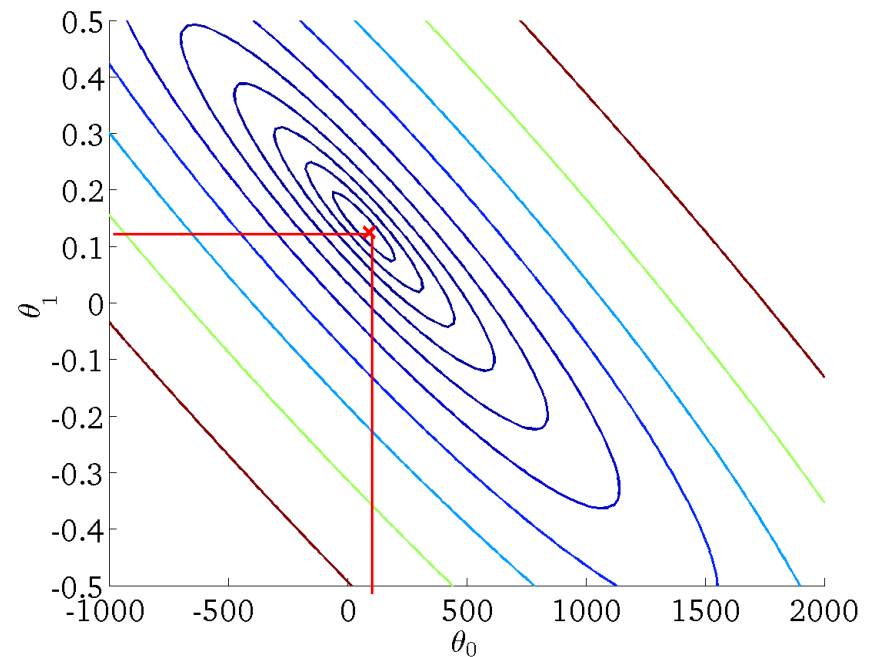
$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )



$$J(\theta_0, \theta_1)$$

(function of the parameter  $\theta_0, \theta_1$ )



# Basic Search Procedure

- Choose initial value for  $\theta$
- Until we reach a minimum:
  - Choose a new value for  $\theta$  to reduce  $J(\theta)$

