## Quiz 1

MA3.101: Linear Algebra (Spring 2019)

Time: 20 Mins Total Marks: 15

January 23, 2019

## Questions

- 1. Let  $\mathbf{v}_1$ ,  $\mathbf{v}_2$  and  $\mathbf{v}_3$  be 3 vectors in  $\mathbb{R}^3$ .  $\mathbf{v}_3$  is not a linear combination of  $\mathbf{v}_1$  and  $\mathbf{v}_2$ . Is  $\{\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3\}$  linearly independent? Please support your answer with proper reasoning.
- 2. The **column space** of a matrix  $A \in \mathbb{R}^{m \times n}$  is the set of vectors in  $\mathbb{R}^m$  spanned by the columns of matrix A. Is column space of A a subspace? Please support your answer with proper reasoning.
- 3. Let S denote the set of all possible Fibonacci sequences, i.e.,  $S = \{(x_1, x_2, ...) : x_i \in \mathbb{R}, x_j = x_{j-1} + x_{j-2}, \forall j \geq 3\}$ . Is S a vector space? Please support your answer with proper reasoning.