

Automata Theory

Converting NFA to DFA

Objectives:

- Converting a Nondeterministic finite automaton to a deterministic finite automaton.
- Input as well as output taken as Json five tuples for a file input.json.
- Output as well as output taken as Json five tuples for a file Output.json

A Finite Automata consists of the following :

Q : Finite set of states.
 Σ : set of Input Symbols.
 q : Initial state.
 F : set of Final States.
 δ : Transition Function.

DFA (Deterministic Finite Automata):

DFA consists of 5 tuples $\{Q, \Sigma, q, F, \delta\}$.
 Q : set of all states.
 Σ : set of input symbols. (Symbols which machine takes as input)
 q : Initial state. (Starting state of a machine)
 F : set of final state.
 δ : Transition Function, defined as $\delta : Q \times \Sigma \rightarrow Q$.

NFA (Non Deterministic Automata):

δ : Transition Function
 $\delta : Q \times (\Sigma \cup \epsilon) \rightarrow 2^Q$.

INPUT:

- Input is taken from a file input.json as shown below:

```
{  
    "states": 8,  
    "letters": ["a", "b", "c"],  
    "t_func" : [1, 'a', [1,3,0]],  
    "start" : 0,  
    "final" : [4]  
}
```

Here:

states : Number of states. Assume the states are numbered 0,1,2....n-1 for n states. letters: Alphabet used by the NFA.

t func: The transition function for the NFA. Each transition is an array of 3 elements. original state, input and the new state.

start: The index of the starting state.

final: List of accepted states.

Executing the Script:

```
python3 script.py
```

Caution

- Both input.json and output.json should be the same directory as [script.py](#)

Code Expaination:

Function Description:

- Generating a POWER SET(Set of all subsets of a Set)

```
def PowerSet(set, set_size):
```

- Taking Union Of a Set

```
def UNION(StateA, t_func, input):
```

- Combining Two Sets

```
def Set_Combiner(set1, set2):
```

- Generates Transition Function for DFA:

```
def Generator(TF_NFA, TF_DFA, alphabet, cur, states_dfa):
```

1 . PowerSet:

This function is used to calculate all the Possible States for the DFA. 2^n States

$0, 1, 2, \dots, 2^n - 1$.

code

```
pow_set_size = (int)(pow(2+check, set_size))
power_set = list()
for counter in range(0+check, pow_set_size):
    each_element = list()
    for j in range(0+check, set_size):
        if((counter & (1+check << j)) > 0+check):
            each_element.append(set[j])
    power_set.append(each_element)
return power_set
```

pow calls function power.Pow_set_size of power set of a set with set_size 2^n .

Check if jth bit in the counter is set

If set then save jth element from set

2. Gererator:

This uses Transition state of NFA ,Alphabet and Initial state of NFA as Inputs.

```
def Generator(TF_NFA, TF_DFA, alphabet, cur, states_dfa):
    states_dfa.append(cur)
    for i in range(len(alphabet)) :
        inp=alphabet[i]
        Present= []
        Present.append(cur);Present.append(inp);Present.append(UNION(cur, nfa["t_func"],
inp))
        TF_DFA.append(Present)
        trace.append(Present)
        if(Present[2+check] not in states_dfa):
            TF_DFA = Generator(TF_NFA, TF_DFA,alphabet, Present[2+check], states_dfa)
    return TF_DFA
```

This uses Transition state of NFA ,Alphabet and Initial state of NFA as Inputs.

The function is used RECURSIVELY calls itself.

And later union is taken

3 Union :

This function is used to take union of two sets.Specifially for generation of new State.

OUTPUT:

Js Beautifier

```
opts = jsbeautifier.default_options()
dfa["final"] = Set_Combiner(Possible_States, nfa["final"])

opts.indent_size = 2
```

```
formatted_json = jsbeautifier.beautify(json.dumps(dfa), opts)

with open('./output.json', 'w') as json_file:
    json_file.write(formatted_json)
```

It is Useful to store files in an Organised Json format.

Output is Stored in output.json