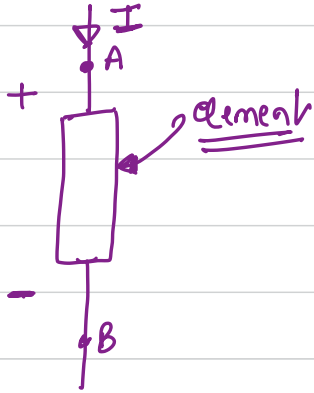


## Lecture 4

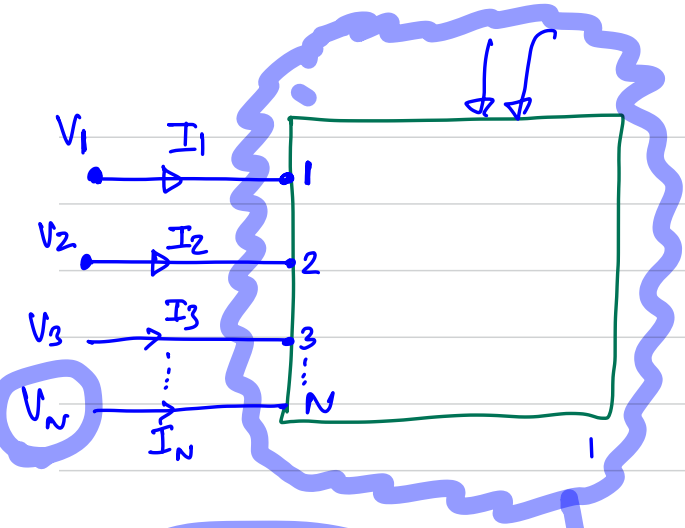


$$P = VI = \overset{\longleftrightarrow} V(t) \overset{\longleftrightarrow} I(t) \rightarrow P(t)$$

$P > 0$  "absorbing"

$P < 0$  "delivering power" Watts.

$$E = \int_{t_1}^{t_2} p(t) dt \quad \text{Joules}$$



$$P = \sum_{k=1}^N V_k I_k \quad \text{"p"}$$

$$P = V_1 I_1 + V_2 I_2 + \dots + V_N I_N$$

$$I_1 + I_2 + \dots + I_N = 0$$

$$I_N = -(I_1 + I_2 + \dots + I_{N-1})$$

$$V_{AB} = (V_A - V_B) \rightarrow$$

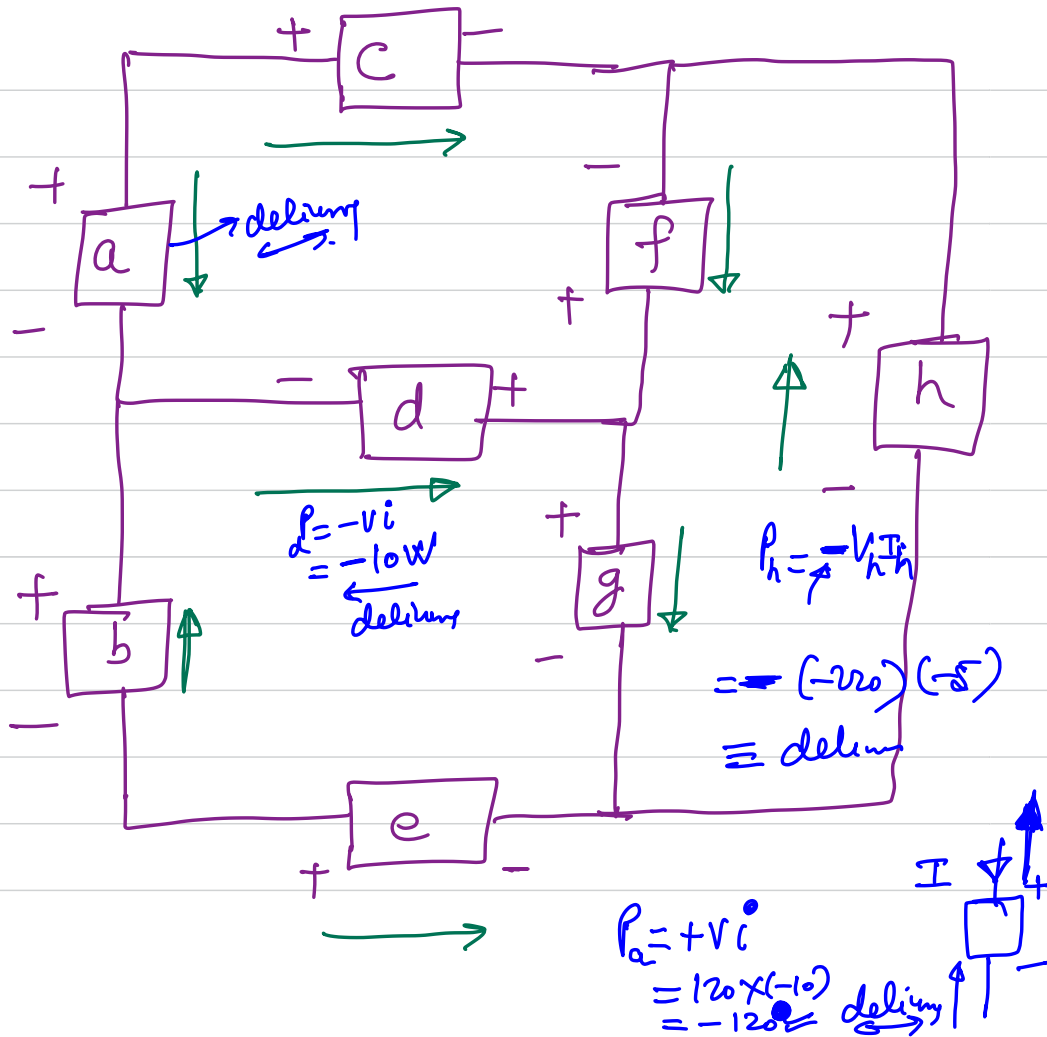
$$V_{BA} = -V_{AB}$$

surface

$$P = V_1 I_1 + V_2 I_2 + \dots + V_N (-I_1 - I_2 - \dots - I_{N-1})$$

$$P = \underbrace{(V_1 - V_N)} I_1 + \underbrace{(V_2 - V_N)} I_2 + \dots + \underbrace{(V_{N-1} - V_N)} I_{N-1}$$

$$P = V_{1N} I_1 + V_{2N} I_2 + \dots + V_{N-1N} I_{N-1}$$



	V	I
a	120	-10
b	120	9
c	10	10
d	10	1
e	-10	-9
f	-100	-5
g	120	4
h	-220	-5

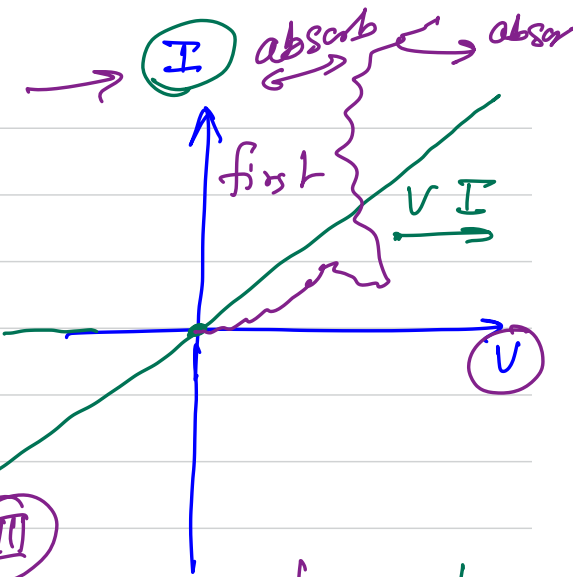
$v = iR$

$P = VI$

$= I^2 R$   
 $= \frac{V^2}{R}$

Resistor

$p(t) = V(t) I(t)$   
 $= I^2(t) R, \frac{V^2(t)}{R}$

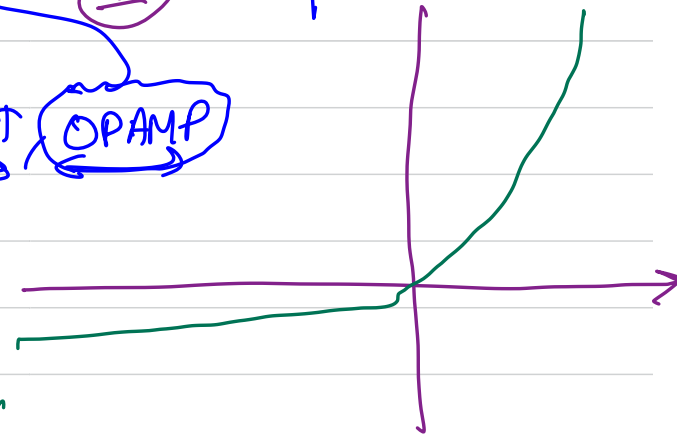


BJT, MOSFET

$R, L, C$   
 $E = \int P(t) dt = \int_{t_1}^{t_2} \frac{V_C^2}{R} dt$



$= \frac{V^2}{R} \int_{t_1}^{t_2} dt$



# Capacitors

$$P_{dc} = VI$$

$$P_{ac}(t) = V(t) I(t)$$

$$I(t) = C \frac{dV(t)}{dt}$$

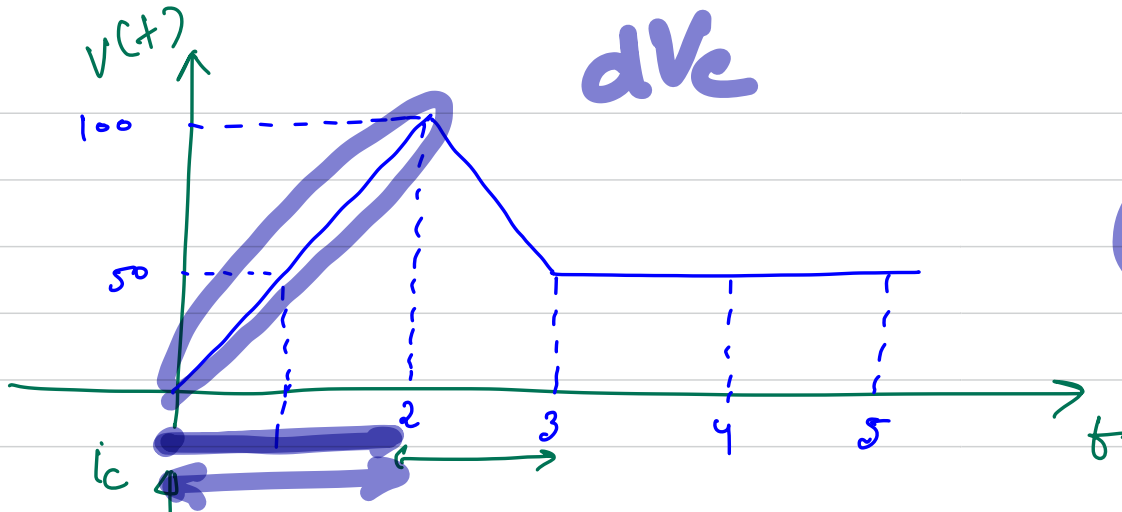
$$P_{ac}(t) = C V(t) \frac{dV(t)}{dt}$$



$dV_c$

$$C = 5 \text{ mF}$$

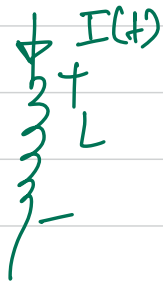
$$i_c = C \frac{dV_c}{dt} = \frac{100 \times 5 \text{ mF}}{2}$$



$$E_{\text{cap}} = \int_{t_0}^{t_1} p(t) dt = \int_{t_0}^{t_1} V_c(t) \overset{\uparrow}{I_c(t)} dt$$

$$= C \int_{t_0}^{t_1} V_c(t) \frac{dV_c(t)}{dt} dt \equiv C \int_{t_0}^{t_1} V_c(t) dV_c(t)$$

$$E_{\text{cap}} \equiv \frac{C}{2} V_c^2(t) \Big|_{t_0}^{t_1} \equiv \frac{C}{2} \left[ \underbrace{V_c^2(\overset{\downarrow}{t_1}) - V_c^2(\overset{\downarrow}{t_0})}_{\longleftarrow \hspace{10em} \longrightarrow}$$



$\overleftrightarrow{I_{\text{ductor.}}}$

$$W(t) = \int_0^t L I(t) \frac{dI(t)}{dt} dt$$

$$V_L = L \frac{dI}{dt}$$

$$P = v I$$

$$I(t) > 0, \frac{dI(t)}{dt} > 0$$

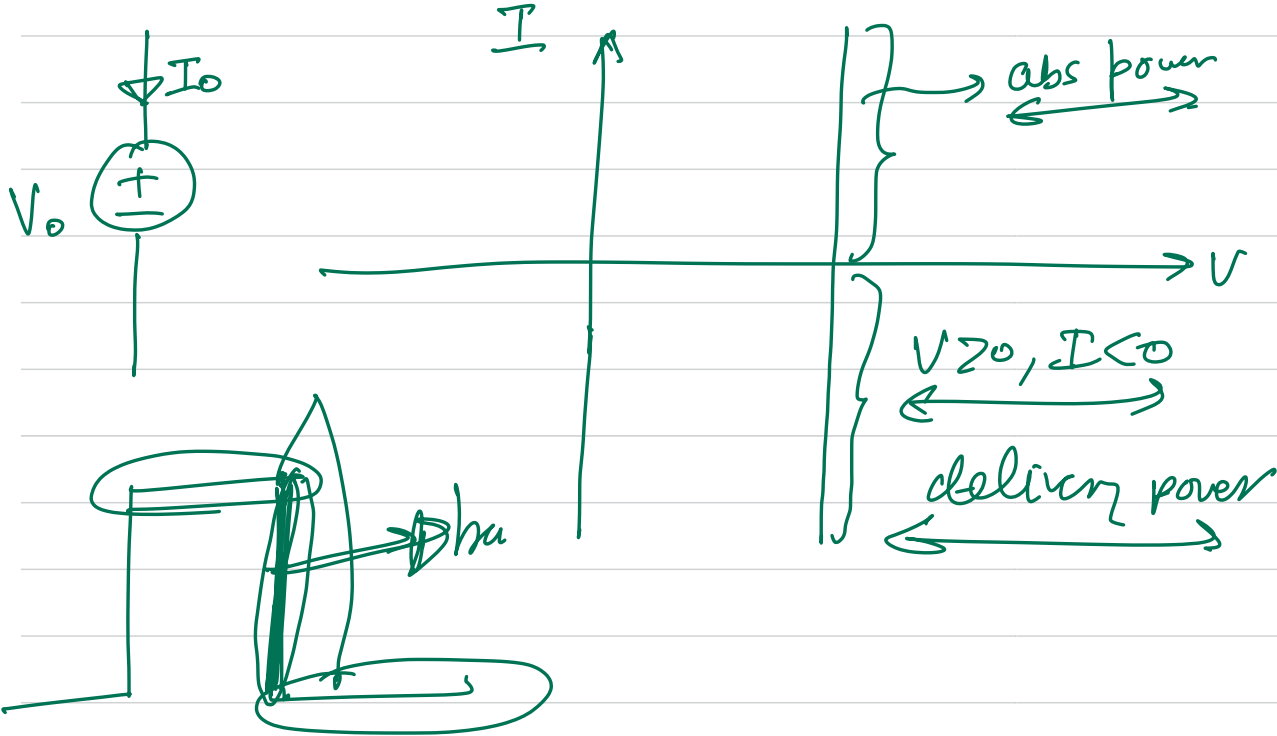
$$\overleftrightarrow{\quad \quad \quad}$$

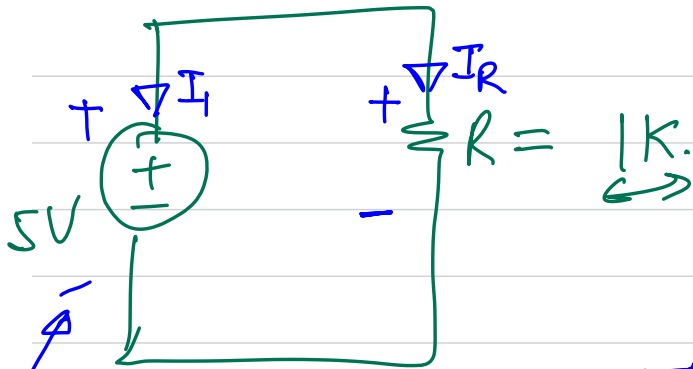
$> 0 \qquad \qquad < 0$

$\overleftrightarrow{\text{abs power}}$



# Energy / Power for voltage source





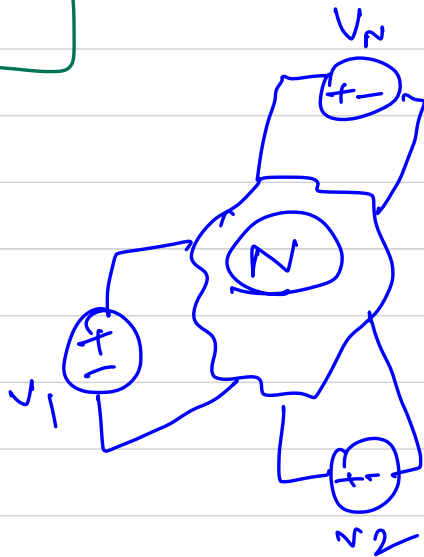
$$(I_1 = -I_R)$$

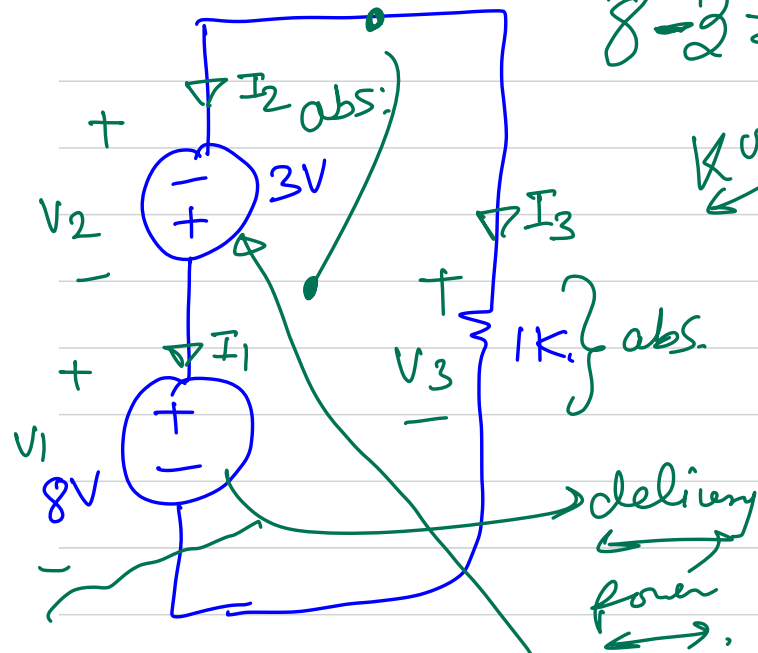
$$I_R = \frac{5}{1K} = 5mA$$

$$V_R = 5V$$

$$P_R = 5 \times 5 = 25mW$$

$$P_{sv} = -5mA \times 5V = 25mW$$





$$8 - 3 = 5V \quad I_1 = \boxed{I_2} = -I_3$$

$$KVL$$

$$V_3 = 5V$$

$$P_{Resr} = \frac{5 \cdot 5}{1k} \approx 25mW$$

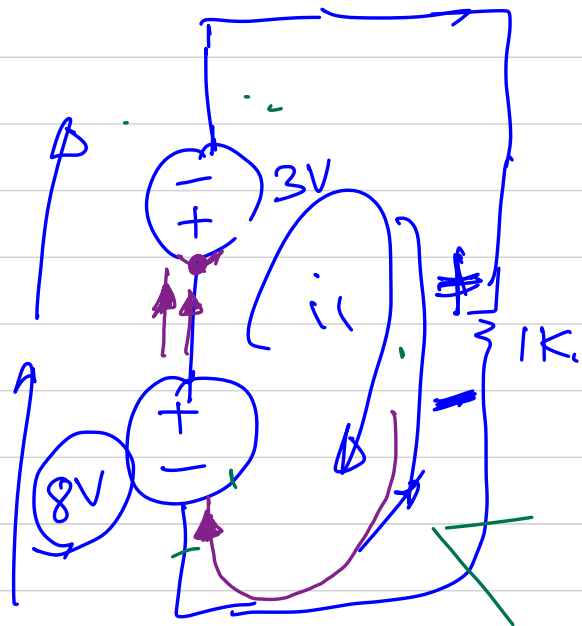
$$P_{8V} = V_1 I_1$$

$$P_{8V} = -8 \times 5mA \approx -40mW$$

→ delivery

$$(V_2 = -3V)$$

$$\boxed{P_{3V} = V_2 I_2 = (-3)(-5mA) \approx 15mW}$$



$$8 - 3 - 1k \times i = 0$$

$$i = 5 \text{ mA}$$

$$P = -vi = \ominus$$

$$+vi = 3 \times 5$$

abs: