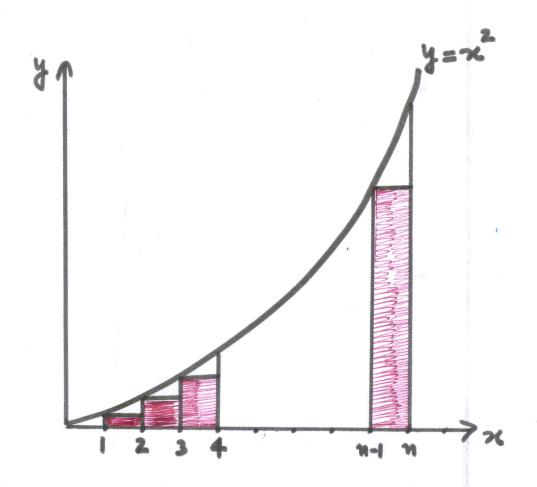
$$F(n) = \sum_{j=0}^{n} j^{2}$$

$$= 1^{2} + 2^{2} + 3^{2} + \dots + n^{2}$$

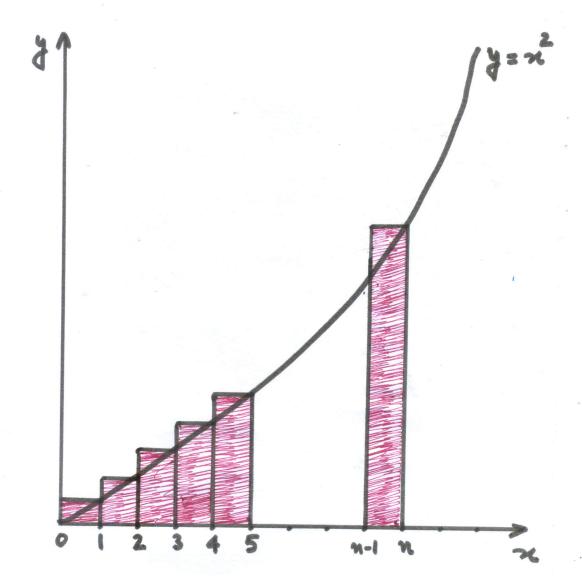
$$F(w) = O(w^3)$$



$$\sum_{j=1}^{m-1} j^2 \leqslant \int_{-\infty}^{\infty} x^2 dx = \frac{(n^2-1)}{3}$$

$$\sum_{j=1}^{m} j^{2} \leqslant \frac{(m+1)^{3}-1}{3}$$

- . We have got the upper bound.
- . Now let's try to get the lower bound.



$$\sum_{j=1}^{m} j^2 \geqslant \int_0^{n} x^2 \cdot dx = \frac{n^3}{3}$$

This is the lower bound.