

Infix to Prefix Conversion

$$A + B * C$$

$$= A + (B * C) \quad (\text{scan 1})$$

$$= A + * B C \quad (\text{scan 2})$$

$$= + A * B C \quad (\text{scan 3})$$

Input Exp.

Stack

Prefix

Reverse the infix Exp

$$\rightarrow C * B + A$$

C

*

B

+

A

$$\boxed{+ A * B C}$$

*

*

+

+

Reverse

C

C

CB

CB*

CB* A

CB* A +

Eg: $K + L - M * N + (O \wedge P) * W / U / V * T + Q$

Reverse: $Q + T * V / U / W *) P \wedge O (+ N * M - L + K$

<u>InputExp</u>	<u>Stack</u>	<u>Prefin</u>
Q		Q
+	+	Q
T	+	QT
*	+	QT
V	+	QTV
/	+	QTV (L-R Asso, just push)
U	+	QTVU
/	+	QTVU
W	+	QTVUW
*	+	QTVUW
)	+	QTVUW
P	+	QTVUWP
^	+	QTVUWP
O	+	QTVUWPO
(+	QTVUWPO^
+	+	QTVUWPO^*
N	+	QTVUWPO^*/
*	+	QTVUWPO^**
M	+	QTVUWPO^**N

Reverse: $Q + T * V / U / W *) P ^ \wedge O (+ N * M - L + K \rightarrow$

M	++*	$QTVUWP O ^ \wedge * // * NM$
-	++-	$QTVUWP O ^ \wedge * // * NM *$
L	++-	$QTVUWP O ^ \wedge * // * NM * L$
+	++-+	$QTVUWP O ^ \wedge * // * NM * L$
K	++-+	$QTVUWP O ^ \wedge * // * NM * L K$

$QTVUWP O ^ \wedge * // * NM * L K + - ++$

↓ Reverse

$++-+KL * MN * // * ^ \wedge OPWUV T Q$

Without Stack

$$K + L - M * N + (O \wedge P) * W / U / V * T + Q$$

$$= K + L - M * N + \wedge O P * W / U / V * T + Q$$

$$= K + L - * M N + \wedge O P * W / U / V * T + Q$$

$$= K + L - * M N + * \wedge O P W / U / V * T + Q$$

$$= K + L - * M N + / * \wedge O P W U / V * T + Q$$

$$= K + L - * M N + / / * \wedge O P W U V * T + Q$$

$$= K + L - * M N + * / / * \wedge O P W U V T + Q$$

$$= + K L - * M N + * / / * \wedge O P W U V T + Q$$

$$= - + K L * M N + * / / * \wedge O P W U V T + Q$$

$$= + - + K L * M N * / / * \wedge O P W U V T + Q$$

$$= ++ - + K L * M N * / / * \wedge O P W U V T Q$$

Things to Remember

* Infix \rightarrow Prefix

- \rightarrow Operators of same precedence, then check Asso.,
 - if L-R simply push in stack
 - if R-L pop & check with the top of the stack
- \rightarrow Reverse \rightarrow get Exp. \rightarrow Reverse

* Infix \rightarrow Postfix

- \rightarrow Operators of same precedence, then check Asso.
 - if L-R pop & check with top of the stack
 - if R-L simply push in stack
- Prefix/Postfix - Do NOT need precedence & asso., hence becomes highly efficient for parsing.

Eg: $a - b + c$, $a = 3, b = 4, c = 5$

$$\begin{array}{ccc}
 (a-b)+c & & a-(b+c) \\
 = 4 & \swarrow \searrow & = -6 \\
 & 4 & -6
 \end{array}$$

which is correct ??

Pre-fix:

$$\begin{array}{l|l}
 (a-b)+c & a-(b+c) \\
 = -ab+c & = a-+bc \\
 = +-abc & = -a+bc \\
 = 4 & = -6
 \end{array}$$

Post-fix:

$$\begin{array}{l|l}
 (a-b)+c & a-(b+c) \\
 = ab-+c & = a-bc+ \\
 = ab-c+ & = abc+- \\
 = 4 & = -6
 \end{array}$$