

Hybrid beamforming using massive antenna arrays for fixed sensor networks

by:

Jamal BEIRANVAND

supervisors:

Vahid MEGHDADI, Cyrille MENUDIER

Faculté des Sciences et Techniques – Institut de Recherche XLIM

Université de Limoges

June 30, 2023

Outline

1 Introduction

- Motivation
- mmWave
- Massive MIMO
- Beamforming

2 Hybrid Beamforming Fundamentals

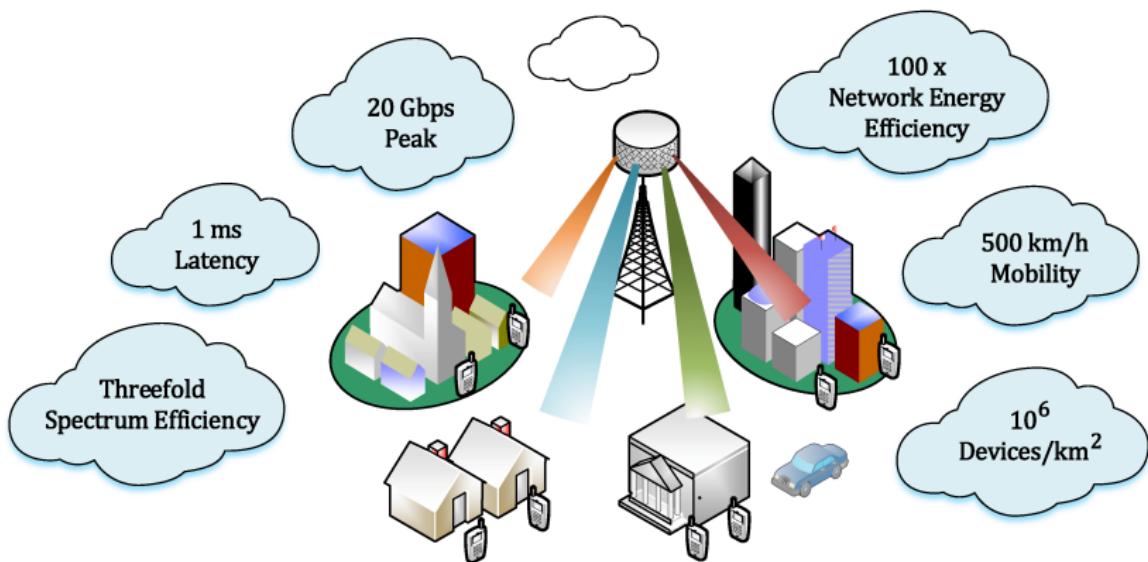
- Challenges
- Analog Network Complexity

3 Contributions

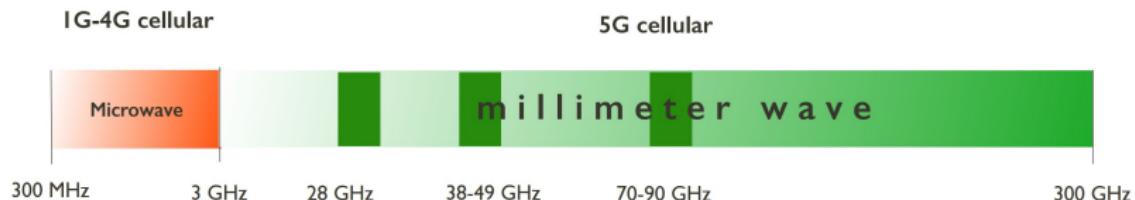
- HBF Matrices Calculation: A New Approach
- Hardware Implementation: Optimal Number of PSs
- Mapping Strategy: A Machine Learning-Based Approach
- Hybrid Beamforming for Wideband Channels

4 Conclusion and Perspectives

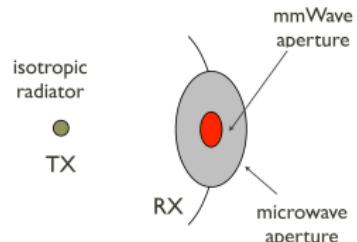
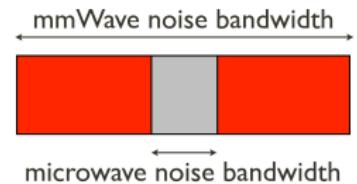
Motivation



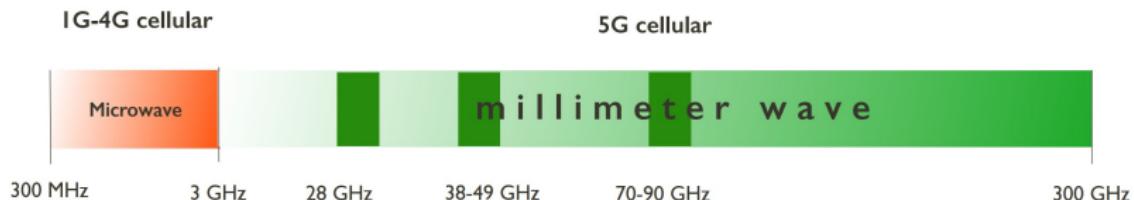
Why Millimeter Wave?



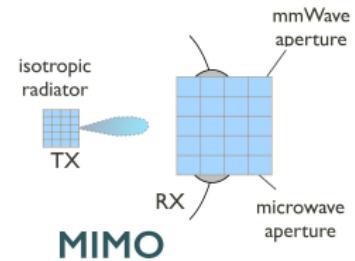
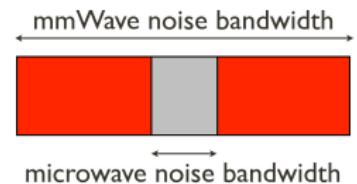
- Abundance of Spectrum
- Larger Bandwidth and Signal-to-Noise Ratio (SNR)
- Smaller Wavelength and Captured Energy
- Exploiting Antenna Array Gain



Why Millimeter Wave?

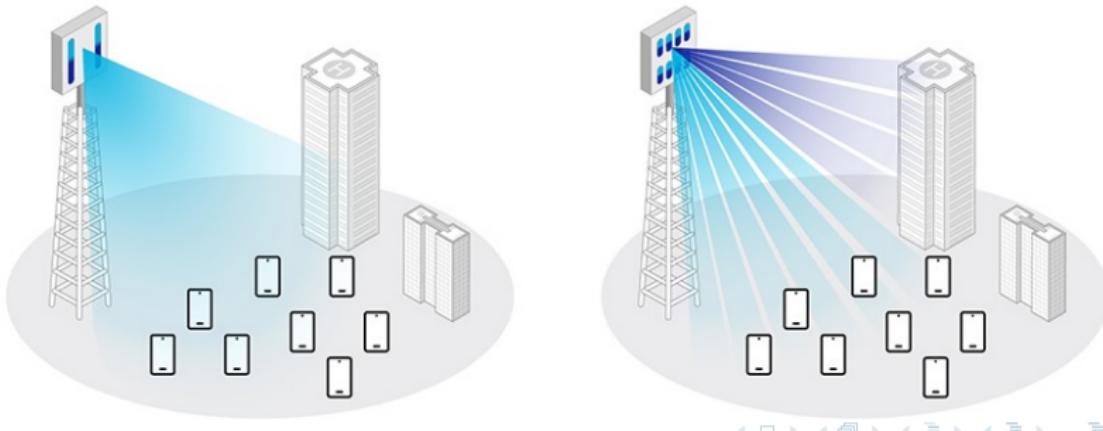


- Abundance of Spectrum
- Larger Bandwidth and Signal-to-Noise Ratio (SNR)
- Smaller Wavelength and Captured Energy
- Exploiting Antenna Array Gain

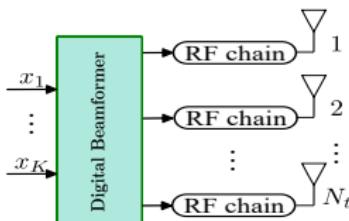


Massive MIMO

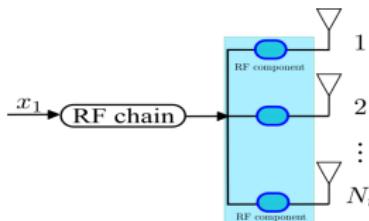
- **Increased Spectral Efficiency:**
Simultaneous transmission and reception of multiple data streams.
- **Enhanced Signal Strength and Coverage:**
Improved signal strength and coverage, even in challenging environments.
- **Expanded Connectivity:**
Support for a larger number of concurrent users and devices.
- **Improved Energy Efficiency:**
Efficient beamforming and reduced interference for optimized energy consumption.



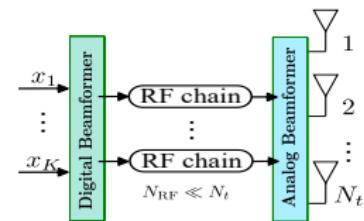
Beamforming for mmWave Massive MIMO Systems



(a) Digital beamforming



(b) Analog beamforming



(c) Hybrid beamforming

● Digital Beamforming (DBF)

- Precise control over beamforming weights.
- Requires a dedicated RF chain per antenna; high hardware complexity, high cost and power consumption.

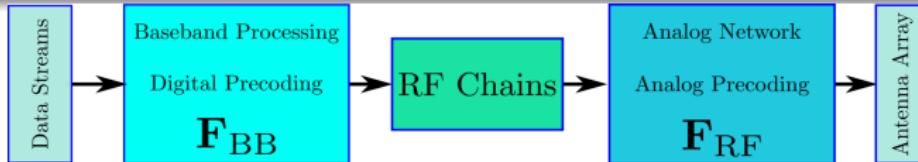
● Analog Beamforming (ABF)

- Requires a shared RF chain; supports single-stream transmission.
- Implemented using phase shifters; control signal's phase.

● Hybrid Beamforming (HBF)

- Combines DBF and ABF; balance between performance and complexity
- Requires $N_{RF} \ll N_t$ RF chains; supports multi-stream transmission.

Challenges



① Hardware complexity

- The number of RF chains
- The analog network's complexity
 - The hardware implementation
 - The mapping strategy

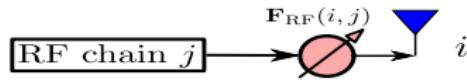
② Computational complexity

- The algorithm's complexity in obtaining both Beamforming matrices, i.e., F_{BB} , and F_{RF}

③ Spectral efficiency

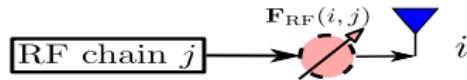
- Spectral efficiency is a key performance indicator for any communication system

The Hardware Implementation



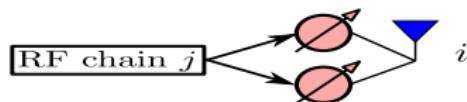
$$\mathbf{F}_{\text{RF}}(i, j) = e^{j\theta} \quad \theta \in [0, 2\pi)$$

(a) Single phase shifter



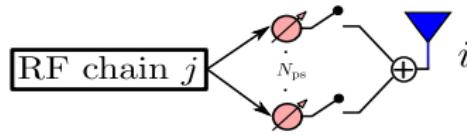
$$\mathbf{F}_{\text{RF}}(i, j) \in \left\{ 0, e^{j2\pi \frac{1}{N_{ps}}}, \dots, e^{j2\pi \frac{N_{ps}-1}{N_{ps}}} \right\}$$

(b) Quantized phase shifter



$$\mathbf{F}_{\text{RF}}(i, j) = e^{j\theta_1} + e^{j\theta_2} \quad \theta_1, \theta_2 \in [0, 2\pi)$$

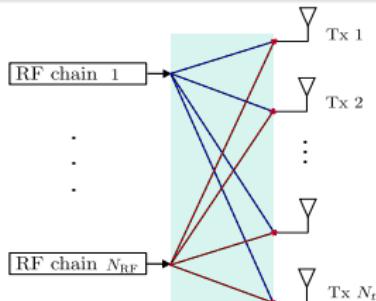
(c) Double phase shifter



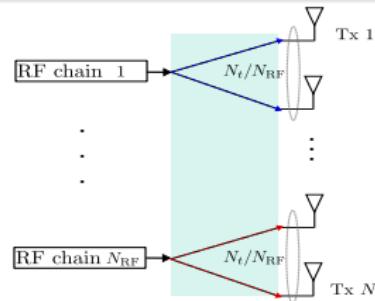
$$\mathbf{F}_{\text{RF}}(i, j) = \sum_{n=1}^{N_{\text{ps}}} s_n e^{j\theta_n} \quad \theta_n = e^{j2\pi n / N_{\text{ps}}}$$

(d) Fixed phase shifters

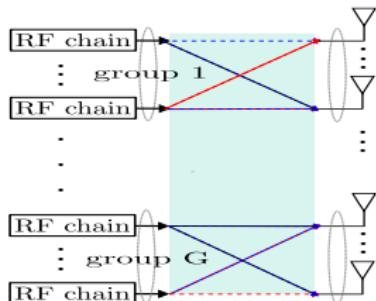
The Mapping Strategy



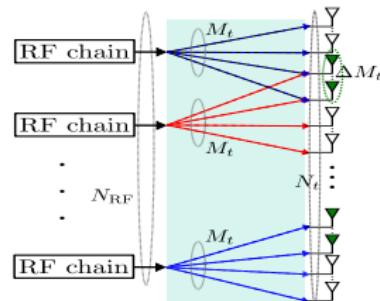
(a) Fully-Connected (FC)



(b) Partially-Connected (PC)



(c) Group Connected (GC)



(d) Overlapped Subarray (OSA)

1 Introduction

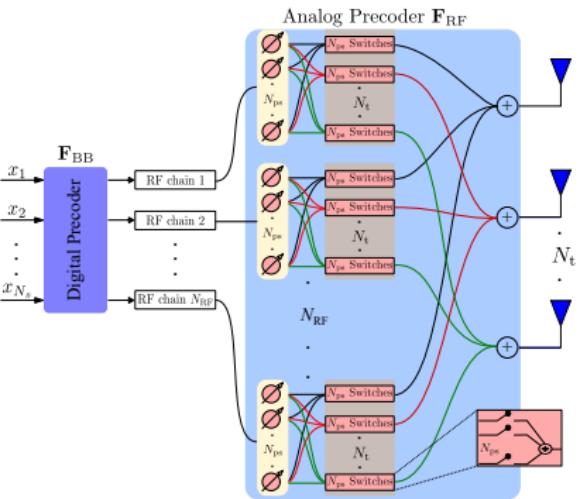
2 Hybrid Beamforming Fundamentals

3 Contributions

- HBF Matrices Calculation: A New Approach
- Hardware Implementation: Optimal Number of PSs
- Mapping Strategy:A Machine Learning-Based Approach
- Hybrid Beamforming for Wideband Channels

4 Conclusion and Perspectives

System Model

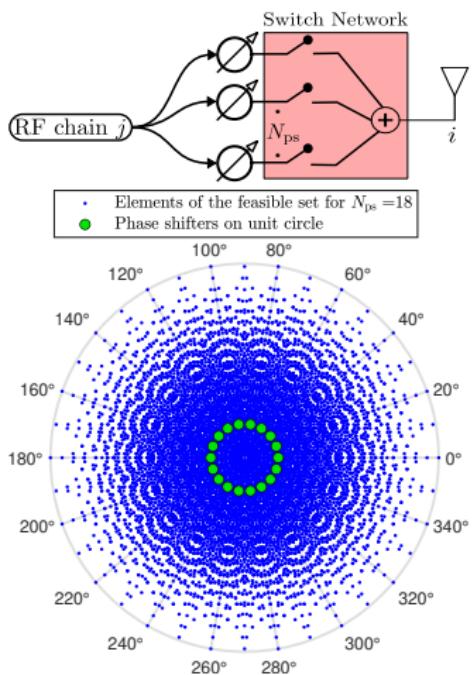


- Hardware implementation: fixed phase shifter
- Mapping strategy: fully-connected strategy
- The number of RF chains: minimum number
- The number of PSs is N_{ps} for each RF chain.
- PSs outputs are shared
- The received signal

$$\mathbf{y} = \sqrt{\rho} \mathbf{H} \mathbf{F}_{RF} \mathbf{F}_{BB} \mathbf{x} + \mathbf{n}$$

J. Beiranvand et al, "An Efficient Low-Complexity Method to Calculate Hybrid Beamforming Matrices for mmWave Massive MIMO Systems," in *IEEE Open Journal of the Communications Society*, vol. 2, pp. 1239-1248, 2021, doi: 10.1109/OJCOMS.2021.3084343.

Analog beamforming coefficients



- $\mathbf{F}_{\text{RF}}(i, j) = \mathbf{s}_{ij} \mathbf{c}$
- The vector $\mathbf{c} = \left[1, e^{j2\pi \frac{1}{N_{\text{ps}}}}, \dots, e^{j2\pi \frac{N_{\text{ps}}-1}{N_{\text{ps}}}} \right]^T$ represents the phase shift vector.
- The binary vector \mathbf{s}_{ij} represents switch states
- $2^{N_{\text{ps}}}$ switch combinations generate beamforming coefficients (see the scatter plot)
- The analog precoder $\mathbf{F}_{\text{RF}} = \mathbf{S}\mathbf{C}$

$$\mathbf{S} \triangleq \begin{bmatrix} \mathbf{s}_{11} & \mathbf{s}_{12} & \cdots & \mathbf{s}_{1N_s} \\ \vdots & \ddots & & \vdots \\ \mathbf{s}_{N_t 1} & \mathbf{s}_{N_t 2} & \cdots & \mathbf{s}_{N_t N_s} \end{bmatrix}_{N_t \times N_{\text{RF}} N_{\text{ps}}}$$

$$\mathbf{C} \triangleq \begin{bmatrix} \mathbf{c} & \mathbf{0} & \cdots & \mathbf{0} \\ \mathbf{0} & \mathbf{c} & & \mathbf{0} \\ \vdots & \vdots & \ddots & \vdots \\ \mathbf{0} & \mathbf{0} & \cdots & \mathbf{c} \end{bmatrix}_{N_{\text{RF}} N_{\text{ps}} \times N_{\text{RF}}},$$

Problem Formulation

- The precoder design problem can be written as:

$$\begin{aligned} \left(\mathbf{S}^{\text{opt}}, \mathbf{F}_{\text{BB}}^{\text{opt}} \right) &= \underset{\mathbf{S}, \mathbf{F}_{\text{BB}}}{\operatorname{argmin}} \quad \left\| \mathbf{F}_{\text{opt}} - \mathbf{S} \mathbf{C} \mathbf{F}_{\text{BB}} \right\|_{\text{F}}^2 \\ \text{s.t.} \quad &\left\| \mathbf{S} \mathbf{C} \mathbf{F}_{\text{BB}} \right\|_{\text{F}}^2 = 1 \\ &\mathbf{S}(i, \ell) \in \{0, 1\}, \quad \forall i, \ell. \end{aligned}$$

- The matrix \mathbf{F}_{opt} is the optimal fully-digital precoder
- The binary matrix $\mathbf{S} \in \mathbb{Z}_2^{N_t \times N_{\text{RF}} N_{\text{Ps}}}$, where $\mathbb{Z}_2 = \{0, 1\}$.
- The optimal solution is obtained through an exhaustive search
- The exhaustive search on the switch matrix \mathbf{S} is infeasible

For example with 256 antennas, 10 RF chains, and 16 phase shifters, the size of the search space is $2^{256 \times 10 \times 16} \approx \infty$

Decompose the optimization problem

- Assume $\mathbf{F}_{\text{BB}} = \mathbf{I}_{N_s}$ and $\mathbf{F}_{\text{optn}} = \gamma \mathbf{F}_{\text{opt}}$
- Under these assumptions:

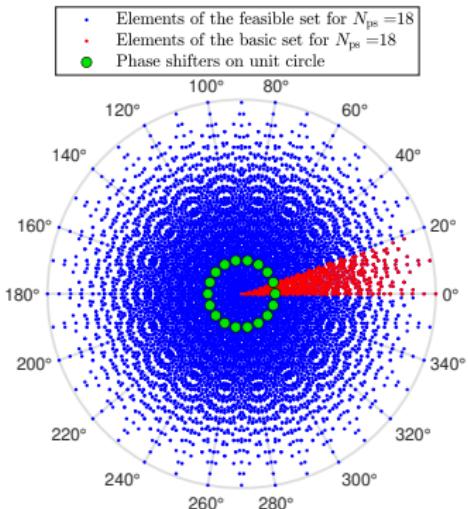
$$\begin{aligned} \mathbf{S}^* = \operatorname{argmin}_{\mathbf{S}} \quad & \| \mathbf{F}_{\text{optn}} - \mathbf{S} \mathbf{C} \|_{\text{F}}^2 \\ \text{s.t.} \quad & \mathbf{S}(i, \ell) \in \{0, 1\}, \quad \forall i, \ell, \end{aligned}$$

- As a result, the problem is decomposed into $N_t N_s$ independent sub-problems

$$\begin{aligned} \mathbf{s}_{ij} = \operatorname{argmin}_{\mathbf{s}_{ij}} \quad & | \mathbf{F}_{\text{optn}}(i, j) - \mathbf{s}_{ij} \mathbf{c} |^2 \\ \text{s.t.} \quad & \mathbf{s}_{ij}(\ell) \in \{0, 1\}, \quad \forall \ell. \end{aligned}$$

- $\mathbf{s}_{ij} \mathbf{c}$ generates a feasible set \mathcal{F} with maximum size of $2^{N_{\text{PS}}}$
- The size of the feasible set \mathcal{F} is independent of the number of antennas and RF chains
- The exhaustive search is tractable even in a massive MIMO system.

Periodic property



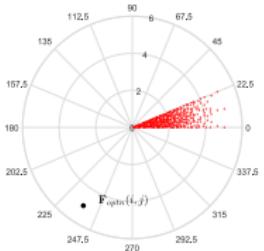
- The feasible set is created by N_{ps} periods of a basic sector
- The points in the basic sector form a basic set (red points) $\mathcal{F}_{N_{ps}}^b$
- The size of the search space is reduced N_{ps} times, i.e., $|\mathcal{F}_{N_{ps}}^b| = |\mathcal{F}_{N_{ps}}| / N_{ps}$
- Exploit the property to reduce computational complexity.

Using the basic set to find switch states

- Scaling the beamforming coefficient within the feasible circle
- Transferring the beamforming coefficient within the basic sector

$$M(i, j) = \left\lfloor \frac{\angle F_{optn}(i, j)}{2\pi/N_{ps}} \right\rfloor$$

- Finding the nearest point in the basic sector
- Extracting the corresponding switch states
 $\tilde{s}_{ij} = [0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1]$
- Shifting the corresponding switch states
 $s_{ij} = [1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1]$



(a)

(b)

(c)

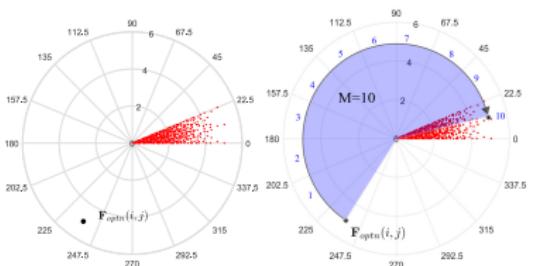
(d)

Using the basic set to find switch states

- Scaling the beamforming coefficient within the feasible circle
- Transferring the beamforming coefficient within the basic sector

$$\mathbf{M}(i, j) = \left\lfloor \frac{\angle \mathbf{F}_{\text{optn}}(i, j)}{2\pi/N_{\text{ps}}} \right\rfloor$$

- Finding the nearest point in the basic sector
- Extracting the corresponding switch states
 $\tilde{s}_{ij} = [0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1]$
- Shifting the corresponding switch states
 $s_{ij} = [1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1]$



(a)

(b)

(c)

(d)

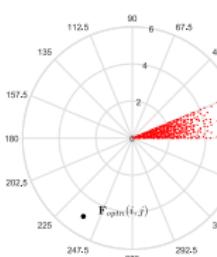
Using the basic set to find switch states

- Scaling the beamforming coefficient within the feasible circle
 - Transferring the beamforming coefficient within the basic sector

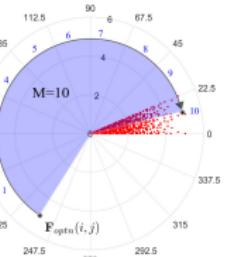
$$\mathbf{M}(i, j) = \left| \frac{\angle \mathbf{F}_{\text{optn}}(i, j)}{2\pi/N_{\text{ps}}} \right|$$

- Finding the nearest point in the basic sector
 - Extracting the corresponding switch states

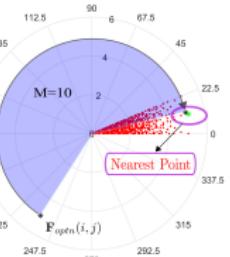
$$\tilde{\mathbf{s}}_{i,j} = [0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1]$$



(a)



(b)



(c)

(d)

Using the basic set to find switch states

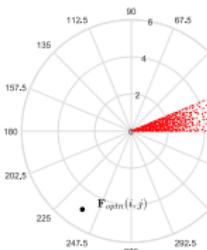
- Scaling the beamforming coefficient within the feasible circle
 - Transferring the beamforming coefficient within the basic sector

$$\mathbf{M}(i, j) = \left| \frac{\angle \mathbf{F}_{\text{optn}}(i, j)}{2\pi/N_{\text{ps}}} \right|$$

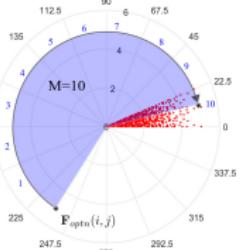
- Finding the nearest point in the basic sector
 - Extracting the corresponding switch states

$$\tilde{\mathbf{s}}_{ij} = [0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1]$$

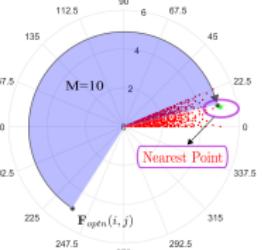
- Shifting the corresponding switch states



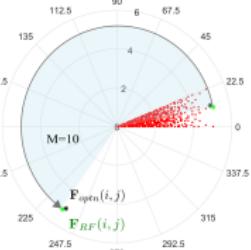
(a)



(b)



(c)



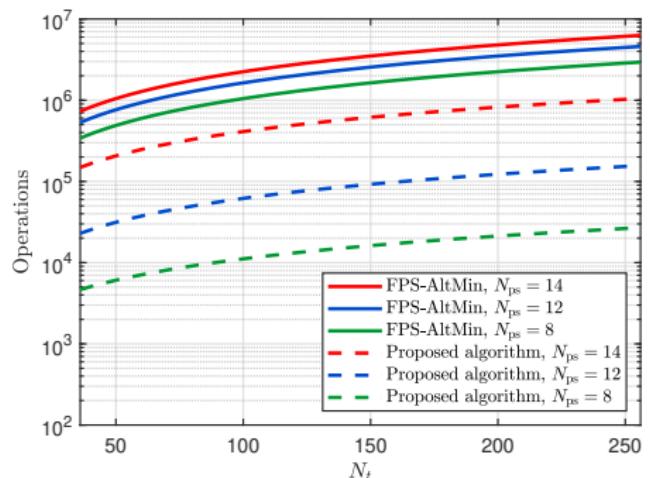
(d)

Algorithm 1 A Low-Complexity Algorithm for Hybrid Systems

Require: \mathbf{F}_{opt} ;

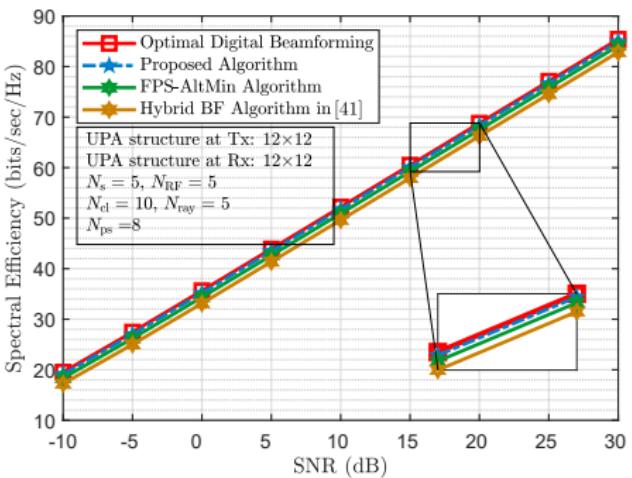
- 1: Compute $\mathbf{F}_{\text{optn}} = \gamma \mathbf{F}_{\text{opt}}$;
 - 2: Obtain the matrix \mathbf{M} ;
 - 3: Transfer \mathbf{F}_{optn} into the basic sector and obtain \mathbf{F}_s ;
 - 4: **For** $i = 1, \dots, N_t$ and $j = 1, \dots, N_s$;
 - 5: Find the nearest point of the basic set to $\mathbf{F}_s(i, j)$, $\mathbf{F}_s(i, j) \longmapsto \mathbf{F}_m(i, j)$;
 - 6: Extract $\tilde{\mathbf{s}}_{ij}$ corresponds $\mathbf{F}_m(i, j)$ from the code book of $\mathcal{F}_{N_{\text{ps}}}^b$;
 - 7: Compute \mathbf{s}_{ij} by $\mathbf{M}(i, j)$ circular right-shifts of $\tilde{\mathbf{s}}_{ij}$;
 - 8: Calculate $\mathbf{F}_{\text{RF}}(i, j) = \mathbf{s}_{ij} \mathbf{c}$;
 - 9: **End for**
 - 10: $\hat{\mathbf{F}}_{\text{BB}} = (\mathbf{F}_{\text{RF}}^H \mathbf{F}_{\text{RF}})^{-1} \mathbf{F}_{\text{RF}}^H \mathbf{F}_{\text{opt}}$;
 - 11: $\mathbf{F}_{\text{BB}} = \frac{\hat{\mathbf{F}}_{\text{BB}}}{\|\mathbf{F}_{\text{RF}} \hat{\mathbf{F}}_{\text{BB}}\|_F}$.
-

Numerical results



Computational complexity

FPS-AltMin algorithm [45]



Spectral efficiency

1 Introduction

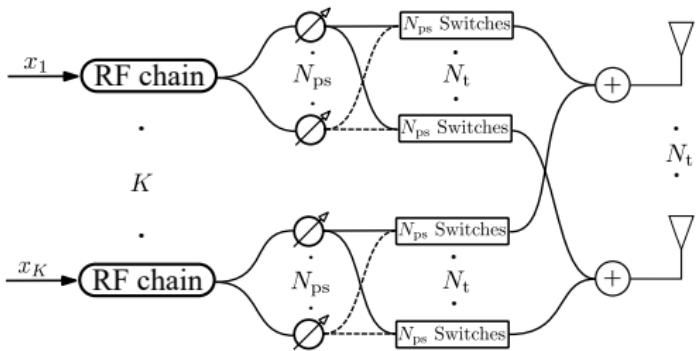
2 Hybrid Beamforming Fundamentals

3 Contributions

- HBF Matrices Calculation: A New Approach
- **Hardware Implementation: Optimal Number of PSs**
- Mapping Strategy:A Machine Learning-Based Approach
- Hybrid Beamforming for Wideband Channels

4 Conclusion and Perspectives

System Model

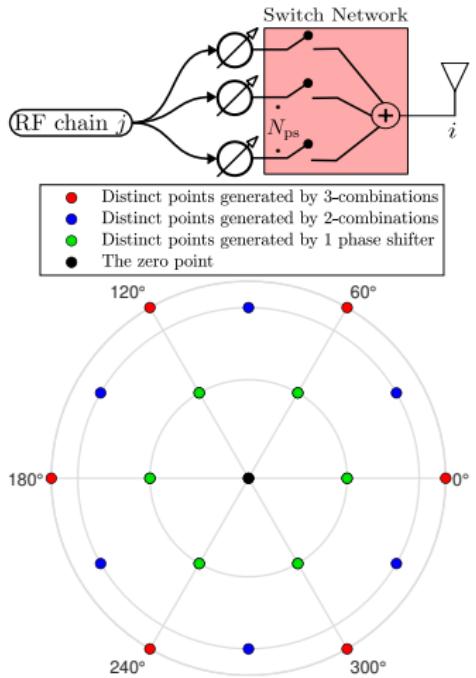


- Hardware implementation: fixed phase shifter
- Mapping strategy: fully-connected strategy
- With digital beamforming set as the identity matrix; focus on the impact of the number of phase shifters on the system's performance.
- The received signal

$$\mathbf{y} = \sqrt{\rho} \mathbf{H} \mathbf{F}_{RF} \mathbf{x} + \mathbf{n},$$

J. Beiranvand et al, "How Many Fixed Phase Shifters Are Needed in a Hybrid BF Structure?," *ICC 2022 - IEEE International Conference on Communications*, Seoul, Korea, Republic of, 2022, pp. 444-449, doi: 10.1109/ICC45855.2022.9838503.

superposed points in the complete set



- The complete set, denoted as $\mathcal{S}_{N_{ps}}$, consists of all the generated outputs of switch combinations.
- Some of these points are superposed.
- The distinct points form the feasible set $\mathcal{F}_{N_{ps}}$
- For example, with $N_{ps} = 6$
 $|\mathcal{F}_6| = 19$ and $|\mathcal{S}_6| = 64$
- The distinct points are the ones that truly impact beamforming performance.
- We analyze the number of distinct points

The complete set $\mathcal{S}_{N_{\text{ps}}}$ vs the feasible set $\mathcal{F}_{N_{\text{ps}}}$

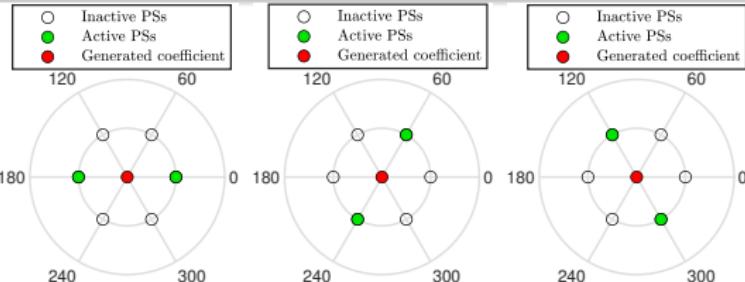
- The complete set $\mathcal{S}_{N_{\text{ps}}}$ can be express as:

$$\sum_{m \in \mathcal{A}_i} P_m \in \mathcal{S}_{N_{\text{ps}}} \quad \forall i = 1, \dots, 2^{N_{\text{ps}}},$$

- \mathcal{A}_i is a set representing the i th switch combination, and $P_m = e^{j \frac{2\pi}{N_{\text{ps}}} (m-1)}$
- There are two reasons for superposed points;
 - **Zero-summation set (ZSS):** which adds up to zero, $\mathcal{S}_{N_{\text{ps}}}$ i.e., $\sum_{m \in \mathcal{X}_{N_{\text{ps}}, p}} P_m = 0$
 - **Subset of ZSS (SZSS):** which adds up to non-zero, $\mathcal{S}_{N_{\text{ps}}}$ i.e., $\sum_{m \in \mathcal{R}_{N_{\text{ps}}, p}} P_m = \sum_{m \in \bar{\mathcal{B}}_{N_{\text{ps}}, p}} P_m \neq 0$
- We express the size of the feasible set as:

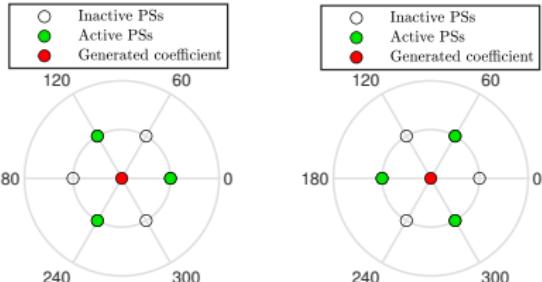
$$|\mathcal{F}_{N_{\text{ps}}}| = \sum_{n=0}^{\xi_{N_{\text{ps}}}-1} \binom{N_{\text{ps}}}{n} - \underbrace{\mathcal{Z}_{N_{\text{ps}}}(n)}_{ZSS} - \underbrace{\mathcal{Q}_{N_{\text{ps}}}(n)}_{SZSS}$$

Zero-Summation Sets



- Consider $\mathcal{X}_{N_{\text{ps}},p}$ composed of p elements
- p is a prime factor of N_{ps}
- For a given pair (N_{ps}, p) , there are N_{ps}/p different ZSSs

$$(a) X_{6,3}^1 = \{1, 4\} \quad (b) X_{6,3}^1 = \{2, 5\} \quad (c) X_{6,3}^1 = \{3, 6\}$$



$$(d) X_{6,2}^1 = \{1, 3, 5\} \quad (e) X_{6,2}^2 = \{2, 4, 6\}$$

Subset of Zero-Summation Set

- Consider $\mathcal{X}_{N_{\text{PS}}, p}$ and $\bar{\mathcal{X}}_{N_{\text{PS}}, p}$
- Two subsets $\mathcal{R}_{N_{\text{PS}}, p}$ and $\mathcal{B}_{N_{\text{PS}}, p}$ of $\mathcal{X}_{N_{\text{PS}}, p}$

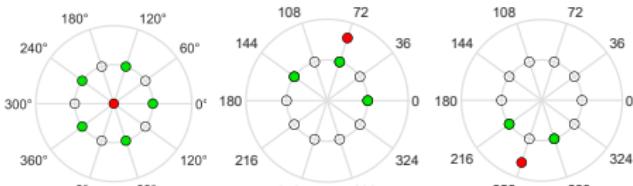
$$\sum_{m \in \mathcal{B}_{N_{\text{PS}}, p}} P_m + \sum_{m \in \mathcal{R}_{N_{\text{PS}}, p}} P_m = 0.$$

- Likewise, $\bar{\mathcal{B}}_{N_{\text{PS}}, p}$ and $\bar{\mathcal{R}}_{N_{\text{PS}}, p}$

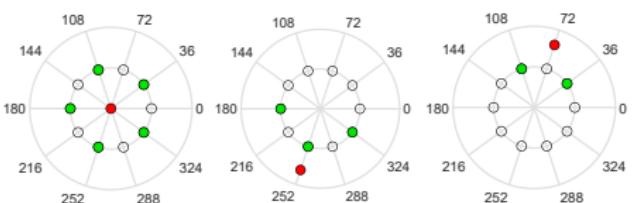
$$\sum_{m \in \bar{\mathcal{B}}_{N_{\text{PS}}, p}} P_m + \sum_{m \in \bar{\mathcal{R}}_{N_{\text{PS}}, p}} P_m = 0,$$

- We can see that

$$\sum_{m \in \mathcal{B}_{N_{\text{PS}}, p}} P_m + \sum_{m \in \bar{\mathcal{B}}_{N_{\text{PS}}, p}} P_m = 0$$



(a) $X_{10,5} = \{1, 3, 5, 7, 9\}$ (b) $\mathcal{R}_{10,5} = \{1, 3, 5\}$ (c) $\mathcal{B}_{10,5} = \{7, 9\}$

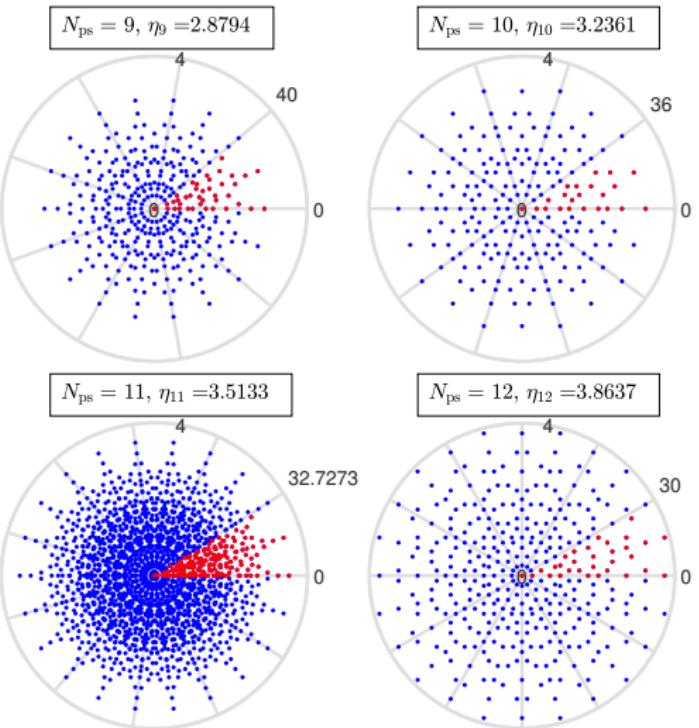


(d) $\bar{X}_{10,5} = \{2, 4, 6, 8, 10\}$ (e) $\bar{\mathcal{R}}_{10,5} = \{6, 8, 10\}$ (f) $\bar{\mathcal{B}}_{10,5} = \{2, 4\}$

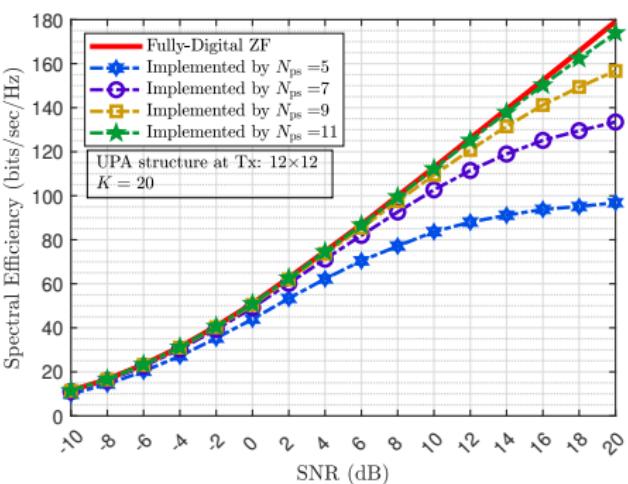
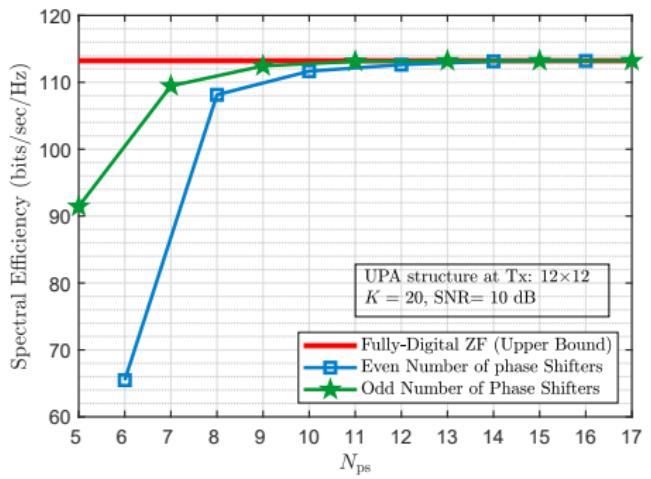
Characteristics of the system as a function of N_{ps}

N_{ps}	$\xi_{N_{\text{ps}}}$	$\eta_{N_{\text{ps}}}$	$ \mathcal{F}_{N_{\text{ps}}} $	$ \mathcal{F}_{N_{\text{ps}}}^b $	$\mathcal{E}_{N_{\text{ps}}} \times 10^2$	$\frac{ \mathcal{F}_{N_{\text{ps}}} }{ \mathcal{S}_{N_{\text{ps}}} }$
2	2	1	3	2	33.97	75.00%
3	3	1	7	3	13.48	87.50%
4	3	1.4142	9	3	10.87	56.25%
5	5	1.6180	31	7	4.34	96.88%
6	4	2	19	4	6.68	29.69%
7	7	2.2470	127	19	2.07	99.22%
8	5	2.6131	81	11	2.60	31.64%
9	7	2.8794	343	39	1.19	66.99 %
10	6	3.2361	211	22	1.46	20.61%
11	11	3.5133	2047	187	0.69	99.95%
12	7	3.8637	361	31	1.05	08.81%
13	13	4.1481	8191	631	0.46	99.99%
14	8	4.4940	2059	148	0.58	12.57%
15	11	4.7834	16081	1073	0.34	49.08%
16	9	5.1258	6561	411	0.41	10.01%
17	17	5.4190	131071	7711	0.26	100.00%

As examples, the feasible set for $N_{\text{ps}} = 9, 10, 11$, and 12



Numerical results



1 Introduction

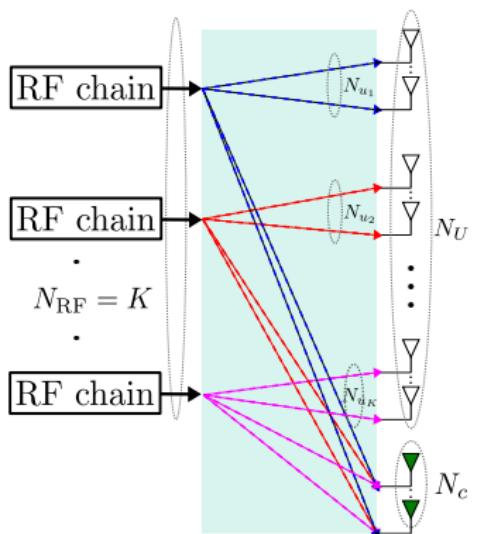
2 Hybrid Beamforming Fundamentals

3 Contributions

- HBF Matrices Calculation: A New Approach
- Hardware Implementation: Optimal Number of PSs
- **Mapping Strategy:A Machine Learning-Based Approach**
- Hybrid Beamforming for Wideband Channels

4 Conclusion and Perspectives

Partially/Fully-Connected Mapping Strategy



- N_{u_k} single-connected antennas (SCAs) are assigned for the k th user.
- N_c fully-connected antennas (FCAs) are common for all users
- Controlling user priority by assigning more or fewer SCAs to a specific user.
- $N_c = 0$ converges to partially-connected strategy
- $N_c = N_t$ converges to fully-connected strategy
- Allowing to adjust the number of RF paths in $N_t + 1$ different levels
- Shaping a simple precoder matrix suitable for analytical optimization.

J. Beiranvand et al, "An Efficient Beamforming Architecture to Handle the Trade-Off Between Performance and Hardware Complexity in Multiuser Massive MISO Systems," in *IEEE Access*, vol. 10, pp. 132853-132862, 2022, doi: 10.1109/ACCESS.2022.3230326.

Partially/Fully-Connected Mapping Strategy

- The analog precoder and channel matrix can be expressed as

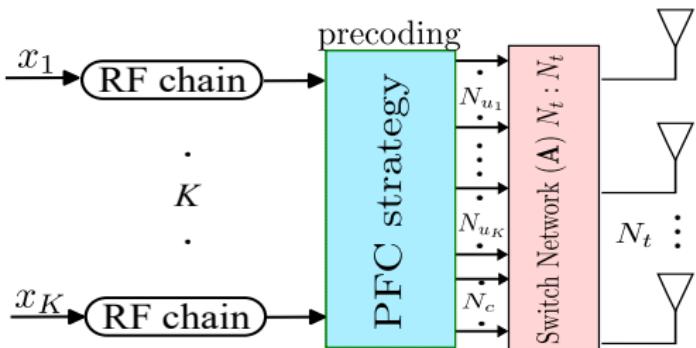
$$\mathbf{F} = \begin{bmatrix} \mathbf{f}_{\mathbf{u}_1} & \mathbf{0} & \dots & \mathbf{0} \\ \mathbf{0} & \mathbf{f}_{\mathbf{u}_2} & \dots & \mathbf{0} \\ \vdots & \vdots & \ddots & \vdots \\ \mathbf{0} & \mathbf{0} & \dots & \mathbf{f}_{\mathbf{u}_K} \\ \mathbf{f}_{\mathbf{c}_1} & \mathbf{f}_{\mathbf{c}_2} & \dots & \mathbf{f}_{\mathbf{c}_K} \end{bmatrix}, \quad \mathbf{H} = [\mathbf{H}_{\mathcal{U}_1}, \mathbf{H}_{\mathcal{U}_2}, \dots, \mathbf{H}_{\mathcal{U}_K}, \mathbf{H}_{\mathcal{C}}],$$

- Based on the ZF precoder, non-zero coefficients in the k th column can be obtained from:

$$\widehat{\mathbf{f}}_k = \mathbf{H}_k^H \left(\mathbf{H}_k \mathbf{H}_k^H \right)^{-1} \mathbf{i}_k,$$

- $\widehat{\mathbf{f}}_k = [\mathbf{f}_{\mathbf{u}_k}^T, \mathbf{f}_{\mathbf{c}_k}^T]^T$, $\mathbf{H}_k = [\mathbf{H}_{\mathcal{U}_k} | \mathbf{H}_{\mathcal{C}}]$,
- \mathbf{i}_k is the k th column of the matrix \mathbf{I}_K

Dynamic Partially/Fully-Connected Strategy



- Dynamic PFC strategy allows us to select FCAs and assign SCAs to users
- Dynamic PFC strategy adapts the RF paths through the switch network **A**
- It can be mathematically represented by

$$\mathbf{y} = \sqrt{\rho} \mathbf{H} \mathbf{A} \mathbf{F} \mathbf{x} + \mathbf{n}.$$

- **A** is a permutation matrix of size $N_t \times N_t$

Dynamic Partially/Fully-Connected Strategy

Example; 8 antennas, 2 users

- $\mathcal{U}_1 = \{1, 4, 8\}$
- $\mathcal{U}_2 = \{2, 5, 7\}$
- $\mathcal{C} = \{3, 6\}$

$$\mathbf{A} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \end{bmatrix}_{8 \times 8}$$

- The objective function can be written as:

$$(\mathcal{C}^{opt}, \mathcal{U}_1^{opt}, \dots, \mathcal{U}_K^{opt}) = \underset{\mathcal{C}, \mathcal{U}_1, \dots, \mathcal{U}_K}{\operatorname{argmin}} \sum_{k=1}^K \left[\left(\mathbf{H}_k \mathbf{H}_k^H \right)^{-1} \right]_{k,k}.$$

- Exploring all possible combinations of antenna allocation is impractical.
- We propose two algorithms to select FCAs and assign SCAs to users.

Dynamic Partially/Fully-Connected Strategy

Example; 8 antennas, 2 users

- $\mathcal{U}_1 = \{1, 4, 8\}$
- $\mathcal{U}_2 = \{2, 5, 7\}$
- $\mathcal{C} = \{3, 6\}$

$$\mathbf{A} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \end{bmatrix}_{8 \times 8}$$

- The objective function can be written as:

$$(\mathcal{C}^{opt}, \mathcal{U}_1^{opt}, \dots, \mathcal{U}_K^{opt}) = \underset{\mathcal{C}, \mathcal{U}_1, \dots, \mathcal{U}_K}{\operatorname{argmin}} \sum_{k=1}^K \left[\left(\mathbf{H}_k \mathbf{H}_k^H \right)^{-1} \right]_{k,k}.$$

- Exploring all possible combinations of antenna allocation is impractical.
- We propose two algorithms to select FCAs and assign SCAs to users.

Algorithm 2 Selecting FCAs

- As FCAs perform the majority of beamforming, selecting the FCAs is prioritize
- The problem of selecting FCAs can be formulated as a combinatorial column selection problem as:

$$\mathcal{C} = \operatorname{argmin}_{\mathcal{C}} \text{Tr} \left\{ \left(\mathbf{H}_{\mathcal{C}} \mathbf{H}_{\mathcal{C}}^H \right)^{-1} \right\}$$

- To solve this problem, we adopt a greedy removal method [70].

Require: \mathbf{H}, N_c ;

1: $\mathcal{C}^{(0)} = \{\ell \in \mathbb{N} : \ell \leq N_t\}$;

2: **For** $t = 1, \dots, N_t - N_c$

3: $\ell = \operatorname{argmin}_{\ell} \text{Tr} \left\{ \left(\mathbf{H}_{\mathcal{C}^{(t)}} \mathbf{H}_{\mathcal{C}^{(t)}}^H - \mathbf{h}_{\ell} \mathbf{h}_{\ell}^H \right)^{-1} \right\}$;

 s.t. $\ell \in \mathcal{C}^{(t)}$;

4: $\mathcal{C}^{(t+1)} = \mathcal{C}^{(t)} - \{\ell\}$;

5: **end**

6: **Output:** \mathcal{C} and $\mathbf{H}_{\mathcal{C}}$.

Algorithm 3 Allocating to the users SCAs

```

Require:  $\mathbf{H}, \mathcal{C}$ ;
1: Initialization
2:  $\mathcal{N} = [N_t] - \mathcal{C}$ ;
3:  $\mathcal{U}_k = \{\}, \quad \forall k = 1, \dots, K$ ;
4:  $\mathbf{H}_k = \mathbf{H}_{\mathcal{C}}, \quad \forall k = 1, \dots, K$ ;
5: For  $k = 1 : K$ 
6:    $\hat{\mathbf{H}}_{ki} = [\mathbf{h}_i, \mathbf{H}_k] \quad \forall i \in \mathcal{N}$ ;
7:    $p_k = \left[ (\mathbf{H}_k \mathbf{H}_k^H)^{-1} \right]_{k,k};$ 
8:    $p_{ki} = \left[ (\hat{\mathbf{H}}_{ki} \hat{\mathbf{H}}_{ki}^H)^{-1} \right]_{k,k};$ 
9:    $\Delta(k, i) = p_k - p_{ki};$ 
10:  end
11:  Repeat
12:     $(k, \ell) = \operatorname{argmax}_{k, \ell \in \mathcal{N}} \Delta(k, \ell)$ 
          s.t.  $|\mathcal{U}_k| < N_{\mathbf{u}_k};$ 
13:    Allocate  $\ell$ th ant. to the  $k$ th user:  $\mathcal{U}_k = \mathcal{U}_k \cup \{\ell\}$ ;
14:    Remove  $\ell$ th ant. and set:  $\mathcal{N} = \mathcal{N} - \{\ell\}$ ;
15:    Update  $\mathbf{H}_k = [\mathbf{H}_{\mathcal{U}_k}, \mathbf{H}_{\mathcal{C}}]$ ;
16:    Update  $k$ th row of  $\Delta$  from steps 5 to 10;
17: Until  $|\mathcal{N}| = 0$ 
18: Output:  $\mathcal{U}_k, \quad \forall k = 1, \dots, K$ ;

```

Proposed DNN for the Dynamic PFC Architecture

- Using DNN to enable real-time antenna allocation
- DNN is used to predict the results of algorithms 2 and 3 directly
- The dataset:** Generated with different channel realizations, and for each of these matrices, 99 noisy channel matrices
- Input:** the matrix $\mathbf{X} \in \mathbb{R}^{K \times N_t \times 3}$ containing the absolute value, real part, and imaginary part of the channel matrix.
- The training label:** the binary matrix \mathbf{Y} of the size $K \times N_t$

For example: $\mathcal{U}_1 = \{1, 4, 8\}$ $\mathcal{U}_2 = \{2, 5, 7\}$ $\mathcal{C} = \{3, 6\}$

$$\mathbf{Y} = \begin{bmatrix} 1 & 0 & 1 & 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 & 1 & 1 & 1 & 0 \end{bmatrix}$$

Algorithm 4 Post-processing for the proposed DNN

- The trained DNN predicts the matrix $\hat{\mathbf{Y}}$
- E.g. $\mathcal{U}_1 = \{1, 4, 8\}$ $\mathcal{U}_2 = \{2, 5, 7\}$
 $\mathcal{C} = \{3, 6\}$

$$\hat{\mathbf{Y}} = \begin{bmatrix} .9 & .2 & .8 & .7 & 0 & .9 & .7 & .9 \\ .1 & .9 & .9 & .2 & .9 & .9 & .8 & .2 \end{bmatrix}$$

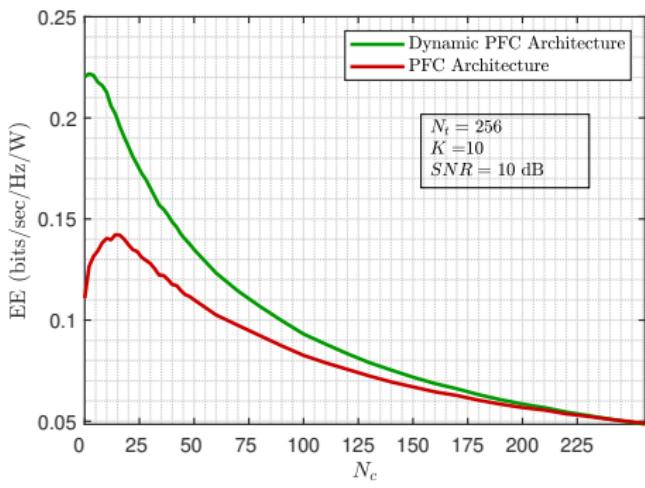
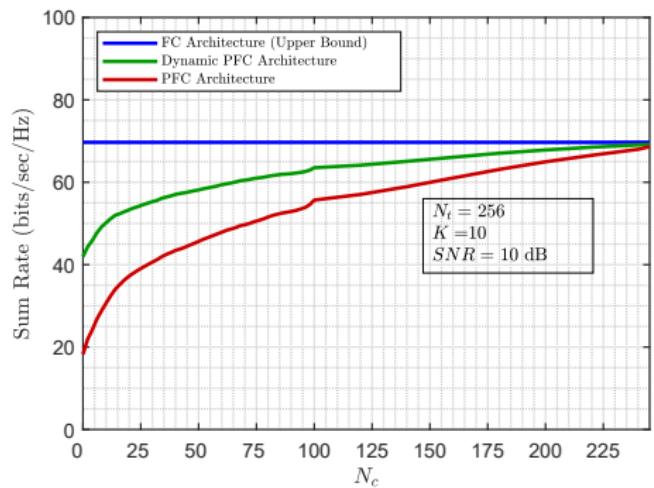
- Selecting the N_c columns of $\hat{\mathbf{Y}}$ with the largest sum-value to set \mathcal{C}
- Assign the antennas to the users, a min-max approach
- Computation times (in milliseconds)

No. FACs, N_c	10	25	50	100	113
Alg. 2 & 3	1317	1219	1183	822	792
Proposed DNN	8.5	8.3	8.1	7.4	7.3

Require: $\hat{\mathbf{Y}}$;

- 1: $\mathcal{N} = [N_t]$;
- 2: $\mathcal{U}_k = \{\}$, $\forall k = 1, \dots, K$;
- 3: $\mathcal{C} = \{\}$;
- 4: **Repeat**
- 5: $\ell = \text{argmax}_{\ell \in \mathcal{N}} \sum_{k=1}^K \hat{\mathbf{Y}}(k, \ell)$
- 6: $\mathcal{C} = \mathcal{C} \cup \{\ell\}$;
- 7: $\mathcal{N} = \mathcal{N} - \{\ell\}$;
- 8: **Until** $|\mathcal{C}| = N_c$
- 9: **Repeat**
- 10: $\ell = \text{argmin}_{\ell \in \mathcal{N}} \sum_{k=1}^K \hat{\mathbf{Y}}(k, \ell)$
- 11: $k = \text{argmax}_k \hat{\mathbf{Y}}(k, \ell)$
 s.t. $|\mathcal{U}_k| < N_{u_k}$;
- 12: $\mathcal{U}_k = \mathcal{U}_k \cup \{\ell\}$;
 $\mathcal{N} = \mathcal{N} - \{\ell\}$;
- 13: **Until** $|\mathcal{N}| = 0$
- 14: **Outputs:** \mathcal{C} , and \mathcal{U}_k , $\forall k = 1, \dots, K$.

Numerical results



Fully-Connected (FC)
Partially/Fully-Connected (PFC)

1 Introduction

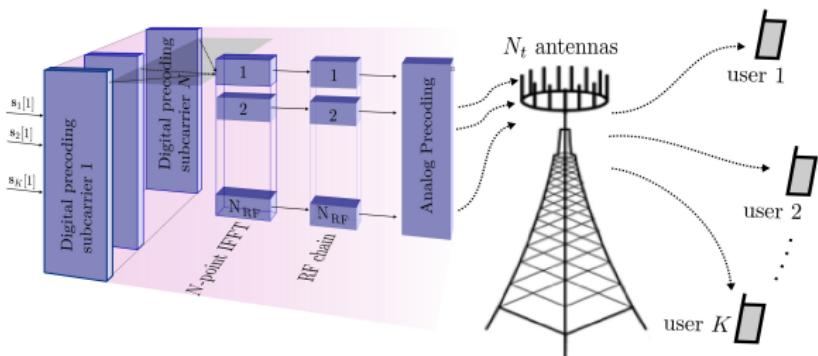
2 Hybrid Beamforming Fundamentals

3 Contributions

- HBF Matrices Calculation: A New Approach
- Hardware Implementation: Optimal Number of PSs
- Mapping Strategy:A Machine Learning-Based Approach
- Hybrid Beamforming for Wideband Channels

4 Conclusion and Perspectives

System Model



- A multiuser MISO-OFDM system that use FC strategy at analog network
- A shared analog beamformer needs to be designed to work for all subcarriers
- A digital beamformer is required for each subcarrier
- The received signal at the user's side

$$\mathbf{r}[n] = \mathbf{h}_k[n] \mathbf{F}_{\text{RF}} \mathbf{F}_{\text{BB}}[n] \mathbf{s}[n] + z[n],$$

- \mathbf{F}_{RF} is identical for all subcarriers

J. Beiranvand et al, "Hybrid beamforming with fixed phase shifters in ofdm-based multiuser miso systems," submitted to *IEEE Global Communications Conference (GLOBECOM)*, 2023

Problem Formulation

- The problem has a combinatorial nature due to the limited points in the feasible set.

$$\begin{aligned}
 & \underset{\mathbf{F}_{\text{RF}}, \{\mathbf{F}_{\text{BB}}[n]\}_{n=1}^N}{\text{maximize}} && \frac{1}{N} \sum_{n=1}^N \sum_{k=1}^K \log(1 + \text{SINR}_{k,n}) \\
 & \text{s.t.} && \text{Tr} \left\{ \mathbf{F}_{\text{RF}} \mathbf{F}_{\text{BB}}[n] \mathbf{F}_{\text{BB}}^H[n] \mathbf{F}_{\text{RF}}^H \right\} \leq P, \forall n, \\
 & && \mathbf{F}_{\text{RF}}(i, j) \in \mathcal{F}_{N_{\text{PS}}},
 \end{aligned}$$

- Assume that the feasible set encompasses all points inside a circle with a radius of r_0 .

$$\begin{aligned}
 & \underset{\mathbf{F}, \{\mathbf{F}_{\text{BB}}[n]\}_{n=1}^N}{\text{maximize}} && \frac{1}{N} \sum_{n=1}^N \sum_{k=1}^K \log(1 + \text{SINR}_{k,n}) \\
 & \text{s.t.} && \text{Tr} \left\{ \mathbf{F} \mathbf{F}_{\text{BB}}[n] \mathbf{F}_{\text{BB}}^H[n] \mathbf{F}^H \right\} \leq P, \forall n, \\
 & && |\mathbf{F}(i, j)| \leq r_0.
 \end{aligned}$$

- The new constraint on \mathbf{F} can be temporarily removed, because the digital beamforming part can satisfy the transmit power constraint.
- We employ the Lagrangian dual transformation technique using FP method.

Step 1 - Lagrangian Dual Transformation

- Moving the SINR term outside the logarithm by applying *Lagrangian Dual Transformation* [71]
- The objective function can be expressed as:

$$\begin{aligned} \mathcal{G}_r(\mathbf{F}, \mathbf{F}_{\text{BB}}[n], \boldsymbol{\gamma}[n]) = & \sum_{k=1}^K \log_2 (1 + \gamma_k[n]) - \sum_{k=1}^K \gamma_k[n] \\ & + \sum_{k=1}^K (1 + \gamma_k[n]) \left(\mathbf{h}_k[n] \mathbf{F} \mathbf{f}_{\text{BB}_k}[n] \right)^H \\ & \times \left(\sigma_z^2 + \sum_{j=1}^K \mathbf{h}_k[n] \mathbf{F} \mathbf{f}_{\text{BB}_j}[n] \mathbf{f}_{\text{BB}_j}^H[n] \mathbf{F}^H \mathbf{h}_k[n]^H \right)^{-1} \mathbf{h}_k[n] \mathbf{F} \mathbf{f}_{\text{BB}_k}[n], \end{aligned}$$

- Red term is the ratio term
- The optimal $\gamma_k[n]$ can be obtained by setting $\frac{\partial \mathcal{G}_r}{\partial \gamma_k[n]} = 0$:

$$\gamma_k^*[n] = \mathbf{f}_{\text{BB}_k}^H[n] \mathbf{F}^H \mathbf{h}_k^H[n] \left(\sigma_z^2 + \sum_{j \neq k}^K \mathbf{h}_k[n] \mathbf{F} \mathbf{f}_{\text{BB}_j}[n] \mathbf{f}_{\text{BB}_j}^H[n] \mathbf{F}^H \mathbf{h}_k^H[n] \right)^{-1} \mathbf{h}_k[n] \mathbf{F} \mathbf{f}_{\text{BB}_k}[n].$$

Step 2 - Quadratic Transformation

- Decoupling the numerator and denominator of each ratio term by applying Quadratic Transformation [71]
- Expressing the objective function \mathcal{G}_r into a new form \mathcal{G}_q as follows:

$$\begin{aligned}\mathcal{G}_q(\mathbf{F}, \mathbf{F}_{\text{BB}}[n], \mathbf{Y}[n], \boldsymbol{\gamma}[n]) = & \sum_{k=1}^K \log_2 (1 + \gamma_k[n]) \\ & - \sum_{k=1}^K \gamma_k[n] + \sum_{k=1}^K 2\sqrt{1 + \gamma_k[n]} \Re \left(y_k[n]^H \mathbf{h}_k[n] \mathbf{F} \mathbf{f}_{\text{BB}_k}[n] \right) \\ & - y_k[n]^H \left(\sigma_z^2 + \sum_{j=1}^K \mathbf{h}_k[n] \mathbf{F} \mathbf{f}_{\text{BB}_j}[n] \mathbf{f}_{\text{BB}_j}^H[n] \mathbf{F}^H \mathbf{h}_k^H[n] \right) y_k[n],\end{aligned}$$

- With the other variables fixed, the optimal $y_k[n]$ can be obtained by solving $\frac{\partial \mathcal{G}_q}{\partial y_k[n]} = 0$:

$$y_k^*[n] = \left(\sigma_z^2 + \sum_{j=1}^K \mathbf{h}_k[n] \mathbf{F} \mathbf{f}_{\text{BB}_j}[n] \mathbf{f}_{\text{BB}_j}^H[n] \mathbf{F}^H \mathbf{h}_k^H[n] \right)^{-1} \sqrt{1 + \gamma_k[n]} \mathbf{h}_k[n] \mathbf{F} \mathbf{f}_{\text{BB}_k}[n].$$

- Likewise, the optimal $\mathbf{f}_{\text{BB}_k}[n]$ is

$$\mathbf{f}_{\text{BB}_k}^*[n] = \left(\eta \mathbf{F}^H \mathbf{F} + \sum_{j=1}^K \mathbf{F}^H \mathbf{h}_k^H[n] y_j[n] y_j^H[n] \mathbf{h}_k[n] \right)^{-1} \sqrt{1 + \gamma_k[n]} \mathbf{F}^H \mathbf{h}_k^H[n] y_k,$$

Step 3 - Solving Optimization Problem

- With the other variables fixed, the optimization problem of \mathbf{F} can be formulated as follows:

$$\begin{aligned} & \underset{\mathbf{F}}{\text{maximize}} && \delta(\mathbf{F}) \\ & \text{s.t.} && \text{Tr} \left\{ |\mathbf{F}\mathbf{F}_{\text{BB}}[n]|^2 \right\} \leq P, \forall n, \end{aligned}$$

where

$$\delta(\mathbf{F}) = \sum_{n=1}^N \sum_{k=1}^K \sqrt{1 + \gamma_k[n]} 2\Re \left(y_k[n]^H \mathbf{h}_k[n] \mathbf{F} \mathbf{f}_{\text{BB},k}[n] \right) - |y_k[n]|^2 \sum_{j=1}^K \left| \mathbf{h}_k[n] \mathbf{F} \mathbf{f}_{\text{BB},j}[n] \right|^2.$$

- The problem is a convex problem, which can be solved by a convex optimization solver such as CVX-MoseK.

Algorithm 5 Hybrid beamforming for wideband channels

- The three steps can be iteratively executed as summarized in Algorithm 5

Require: K users, N subcarriers, N_t , N_{RF} RF chains;

1: **Initialization:** \mathbf{F} , $\mathbf{F}_{BB}[n]$ for all n ;

Ensure: Max sum rate;

2: **repeat**

3: Update $\gamma[n]$ for all n ;

4: Update $\mathbf{y}[n]$ for all n ;

5: Update \mathbf{F} ;

6: Update $\mathbf{F}_{BB}[n]$ for all n ;

7: **until** Convergence

8: Obtain \mathbf{F}_{RF} via mapping \mathbf{F} into $\mathcal{F}_{N_{ps}}$.

- Algorithm 5 can handle the constraints directly, but the number of constraints can become very large
- High computational complexity makes practical implementation difficult

Algorithm 6 Low-complex precoder design for wideband channels

- Designing \mathbf{F}_{RF} to include the principal components of the fully digital precoder matrices

$$\tilde{\mathbf{F}}_{\text{opt}} = [\mathbf{F}_{\text{opt}_1}, \mathbf{F}_{\text{opt}_2}, \dots, \mathbf{F}_{\text{opt}_N}],$$

- Computing SVD of $\tilde{\mathbf{F}}_{\text{opt}}$ as $\tilde{\mathbf{F}}_{\text{opt}} = \mathbf{U}\mathbf{S}\mathbf{V}^H$,
- Selecting the first N_{RF} columns of \mathbf{U} , denoted as $\mathbf{U}_{N_{\text{RF}}}$
- Obtaining \mathbf{F}_{RF} via mapping $\mathbf{U}_{N_{\text{RF}}}$ into $\mathcal{F}_{N_{\text{ps}}}$

Require: K users, N subcarriers, N_t , N_{RF} RF chains;

1: Initialization:

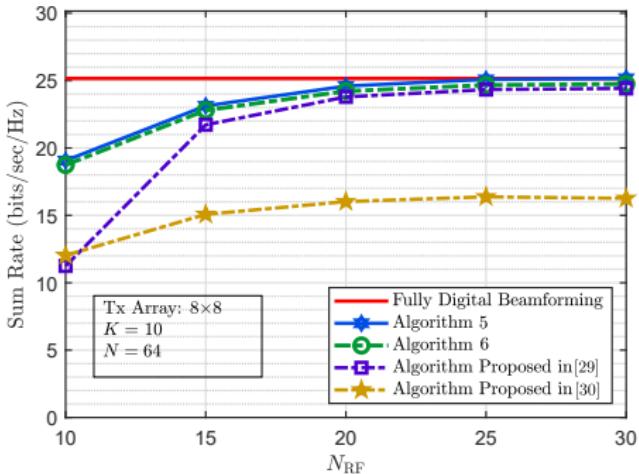
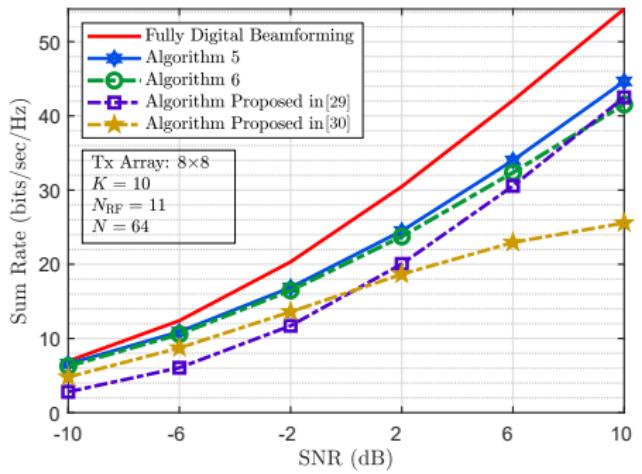
- 2: Obtain $\mathbf{U}_{N_{\text{RF}}}$ via calculating SVD of $\tilde{\mathbf{F}}_{\text{opt}}$;
- 3: Obtain \mathbf{F}_{RF} via mapping $\mathbf{U}_{N_{\text{RF}}}$ into $\mathcal{F}_{N_{\text{ps}}}$;

Ensure: Max sum rate;

4: repeat

- 5: Update $\gamma[n]$ for all n ;
 - 6: Update $\mathbf{y}[n]$ for all n ;
 - 7: Update $\mathbf{F}_{\text{BB}}[n]$ for all n ;
- 8: until** Convergence

Numerical results



Conclusion

- Addressing the computational complexity issue by proposing an algorithm to obtain beamforming matrices
- Addressing the hardware complexity issue associated with the analog network
 - Hardware implementation: analyze the number of PSs
 - Mapping strategy: proposing PFC mapping strategy
- Proposing a novel approach for designing hybrid precoding for wideband channels

Perspectives

- Devolve an approach to estimate the channel for the proposed systems.
- Explore the application of the PFC mapping strategy to the SPS and QPS hardware implementations.
- Investigate the extension of the PFC mapping strategy to multicarrier scenarios
- User scheduling and user clustering

Publications

- **J. Beiranvand** et al, "An Efficient Low-Complexity Method to Calculate Hybrid Beamforming Matrices for mmWave Massive MIMO Systems," in *IEEE Open Journal of the Communications Society*, vol. 2, pp. 1239-1248, 2021, doi: 10.1109/OJCOMS.2021.3084343.
- **J. Beiranvand** et al, "How Many Fixed Phase Shifters Are Needed in a Hybrid BF Structure?," *ICC 2022 - IEEE International Conference on Communications*, Seoul, Korea, Republic of, 2022, pp. 444-449, doi: 10.1109/ICC45855.2022.9838503.
- **J. Beiranvand** et al, "An Efficient Beamforming Architecture to Handle the Trade-Off Between Performance and Hardware Complexity in Multiuser Massive MISO Systems," in *IEEE Access*, vol. 10, pp. 132853-132862, 2022, doi: 10.1109/ACCESS.2022.3230326.
- **J. Beiranvand** et al, "Hybrid beamforming with fixed phase shifters in ofdm-based multiuser miso systems," submitted to *IEEE Global Communications Conference (GLOBECOM)*, 2023

References

- [29] F. Sohrabi and W. Yu, Hybrid analog and digital beamforming for mmwave ofdm large-scale antenna arrays, *IEEE Journal on Selected Areas in Communications*, vol. 35, no. 7, pp. 1432–1443, 2017.
- [30] X. Yu, J. Zhang, and K. B. Letaief, “Doubling phase shifters for efficient hybrid precoder design in millimeter-wave communication systems,” *Journal of Communications and Information Networks*, vol. 4, no. 2, pp. 51–67, 2019
- [41] F. Sohrabi and W. Yu, “Hybrid digital and analog beamforming design for largescale antenna arrays,” *IEEE Journal of Selected Topics in Signal Processing*, vol. 10, no. 3, pp. 501–513, 2016
- [45] X. Yu, J. Zhang, and K. B. Letaief, “A hardware-efficient analog network structure for hybrid precoding in millimeter wave systems,” *IEEE Journal of Selected Topics in Signal Processing*, vol. 12, no. 2, pp. 282–297, 2018.
- [70] F. De Hoog and R. Mattheij, “Subset selection for matrices,” *Linear Algebra and its Applications*, vol. 422, no. 2-3, pp. 349–359, 2007
- [71] K. Shen and W. Yu, “Fractional programming for communication systems—part i: power control and beamforming,” *IEEE Transactions on Signal Processing*, vol. 66, no. 10, pp. 2616–2630, 2018.

THANKS FOR YOUR ATTENTION