



Task projection

1. Hip Task

Control in speed in X axis

$$\begin{aligned} x_{hip} &= l_1 \sin(q_1) \\ z_{hip} &= l_1 \cos(q_1) \\ J_{hip} &= \begin{bmatrix} l_1 \cos(q_1) & 0 & 0 \\ -l_1 \sin(q_1) & 0 & 0 \end{bmatrix} \\ f_{hip} &= \begin{bmatrix} kdx_{hip}(v_{hipRef} - dx_{hip}) \\ 0 \end{bmatrix} \\ u_{hip} &= B^+ J_{hip} f_{hip} \end{aligned}$$

2. Top Task

Control with damp between Hip and top:

$$\begin{aligned} x_{top} &= l_1 \sin(q_1) + l_3 \sin(q_3) \\ z_{top} &= l_1 \cos(q_1) + l_3 \cos(q_3) \\ J_{top} &= \begin{bmatrix} l_1 \cos(q_1) & 0 & l_3 \cos(q_3) \\ -l_1 \sin(q_1) & 0 & -l_3 \sin(q_3) \end{bmatrix} \\ f_{top} &= \begin{bmatrix} kpx_{top}(x_{hip} - x_{top}) \\ kpz_{top}((z_{hip} + l_3) - z_{top}) \end{bmatrix} \\ u_{top} &= B^+ J_{top} f_{top} \end{aligned}$$

Other possibility control in angle on u_1 directly:

$$u_{1angle} = kpa(\text{angle}_{ref} - q_3) + kda(0 - dq_3)$$

3. Swing foot Task

Trajectory to follow:

$$z_{target} = h \sin\left(\frac{\pi}{stepLength}(x_{swf} - x_{0_{swf}})\right)$$

Control position for z and speed for x:

$$\begin{aligned}
x_{swf} &= l_1 \sin(q_1) - l_2 \sin(q_2) \\
z_{swf} &= l_1 \cos(q_1) - l_2 \cos(q_2) \\
J_{swf} &= \begin{bmatrix} l_1 \cos(q_1) & -l_2 \cos(q_2) & 0 \\ -l_1 \sin(q_1) & l_2 \sin(q_2) & 0 \end{bmatrix} \\
f_{top} &= \begin{bmatrix} kdx_{swf}(v_{swfRef} - dx_{swf}) \\ kpz_{swf}(z_{target} - z_{swf}) \end{bmatrix} \\
u_{swf} &= B^+ J_{swf} f_{swf}
\end{aligned}$$

4. Control total:

Normal:

$$u = u_{hip} + u_{top} + u_{swf}$$

If angle:

$$u = u_{hip} + \begin{bmatrix} u_{angle} \\ 0 \end{bmatrix} + u_{swf}$$