Introduction to Model Checking and NuSMV

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Outline

- 1. How to write (temporal) properties:
 - (a) Linear Temporal Logic (LTL).
 - (b) Computation Tree Logic (CTL).
- 2. How to use the NuSMV model checker, part 1.

Linear Temporal Logic (LTL)

1. Propositions: p, $\neg p$, $p \land q$, $p \lor q$ (also for subformulas)

2. Temporal operators

X ne**x**t

U until

F finally ◊

G globally □

Other operators exists but they are not used quite as frequently, and can be derived from the ones above.

Semantics: defined on paths

1. Propositions: $p, \neg p, p \land q, p \lor q$ (also for subformulas) Formula p is true if p holds in first state: $w \models p$ if $p \in w(0)$ Negation: $w \models \neg p$ if $w \not\models p$; conjunct: $w \models p \land q$ if $w \models p$ and $w \models q$

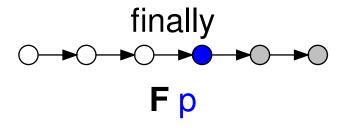
2. Temporal operators

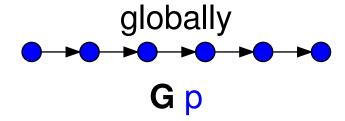
X p next $\bigcirc p$ $w \models \mathbf{X}p$ if $w_1 \models p$ p $\exists j \geq 0, w_j \models q \land \forall i, 0 \leq i < j, w_i \models p$ **F** p finally $\Diamond p$ true $\mathbf{U}p$, equivalent to $\exists j \geq 0, w_j \models p$ **G** p globally $\Box p$ $\neg \mathbf{F} \neg p$, equivalent to $\forall j \geq 0, w_j \models p$

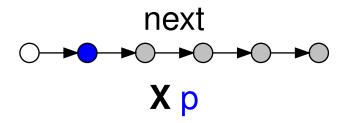
3. Temporal operators can be nested.

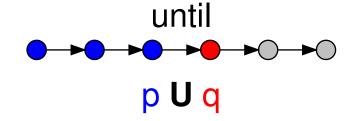
Furthermore, instead of just atomic propositions for p and q, we can also use other temporal formulas as subexpressions.

Examples

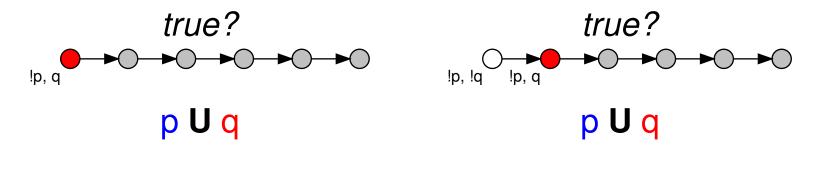


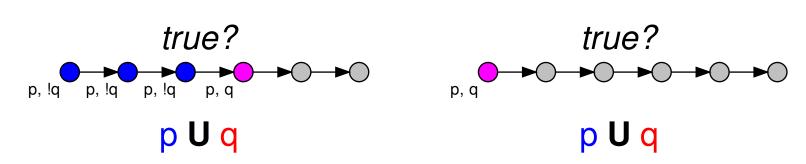




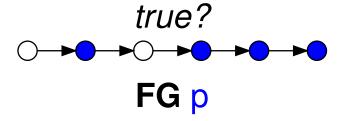


Until





Nesting

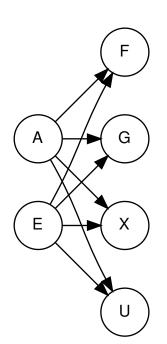


How about infinite traces?

Computation Tree Logic

1. Propositions

2. Path quantifiers + temporal operators



AF p: For all paths, p is eventually true.

AG p: For all paths, p is always true.

AX p: For all paths, p is true in the next state.

A[p U q]: For all paths, p holds until q holds.

E: There exists a path...

3. Temporal operators always follow path quantifier

Semantics: Defined on transition systems

- 1. Propositions: same as above
- 2. **Temporal operators** for model $M(S, \rightarrow, L)$

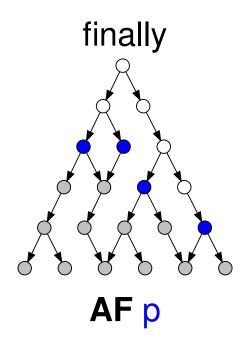
$$\begin{array}{lll} \textbf{AX p} & ((M,s) \models \textbf{AX}p) \Leftrightarrow (\forall \langle s \rightarrow s_1 \rangle \, ((M,s_1) \models p)) \\ \textbf{AG p} & ((M,s) \models \textbf{AG}p) \Leftrightarrow (\forall \langle s_1 \rightarrow s_2 \rightarrow \ldots \rangle (s=s_1) \forall i \, ((M,s_i) \models p)) \\ \textbf{AF p} & ((M,s) \models \textbf{AF}p) \Leftrightarrow (\forall \langle s_1 \rightarrow s_2 \rightarrow \ldots \rangle (s=s_1) \exists i \, ((M,s_i) \models p)) \\ \textbf{A [p U q]} & ((M,s) \models \textbf{A}[p \, \textbf{U} \, q]) \Leftrightarrow \forall \, (\langle s_1 \rightarrow s_2 \rightarrow \ldots \rangle (s=s_1) \exists j \\ & ((M,s_j) \models q) \land (\forall (i < j) \, (M,s_i) \models p))) \\ \end{array}$$

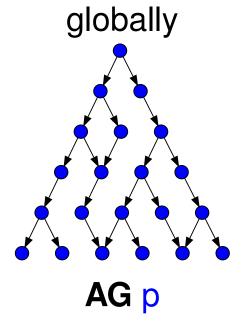
- **E**... defined analogously with existential path quantifier.
- 3. Temporal operators canNOT be directly nested.

However, instead of just atomic propositions for p and q, we can also use other temporal formulas as subexpressions.

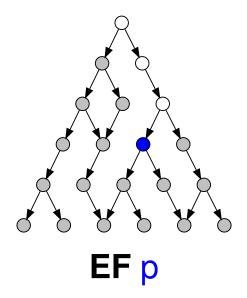
Computation Tree Logic (CTL): finally, globally

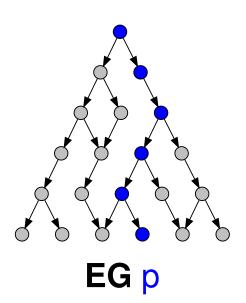
for **all** paths





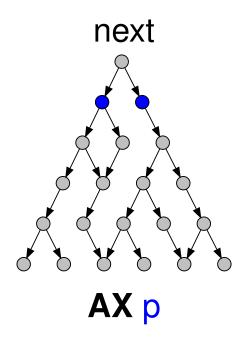
there exists a path

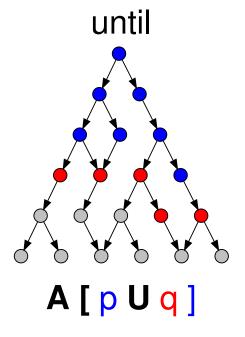




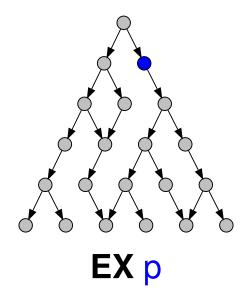
Computation Tree Logic (CTL): next, until

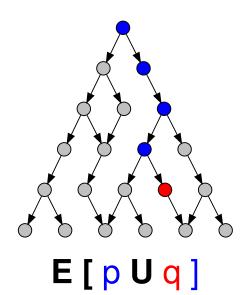
for **all** paths





there exists a path





$LTL \neq CTL$

- 1. **FG**(p)
- 2. **EX**(p)
 - Which logic can express the formulas above?
 - What is the semantics of each formula?
 - Where does the counterpart fail to express it?

CTL*: Combines LTL and CTL.

SMV and **NuSMV**

- Symbolic Model Verifier (SMV):
 First practical symbolic model checker by Ken McMillan/CMU.
- Re-implementation NuSMV (open source) at IRST Trento, Italy.
- NuSMV is still being maintained and developed.
- Current version is 2.6.0 (used in this course).

Usage of NuSMV in the real world

- As a back-end to other tools:
 - → NuSMV-PA: Safety analysis platform
 - → Back-end for Petri net model checking (another modeling approach).
 - \rightarrow Test case generation.
- Case studies:
 - → Kerberos protocol.
 - → Web service composition.
 - → Railway interlocking control tables.

A critique of NuSMV

Pro Con

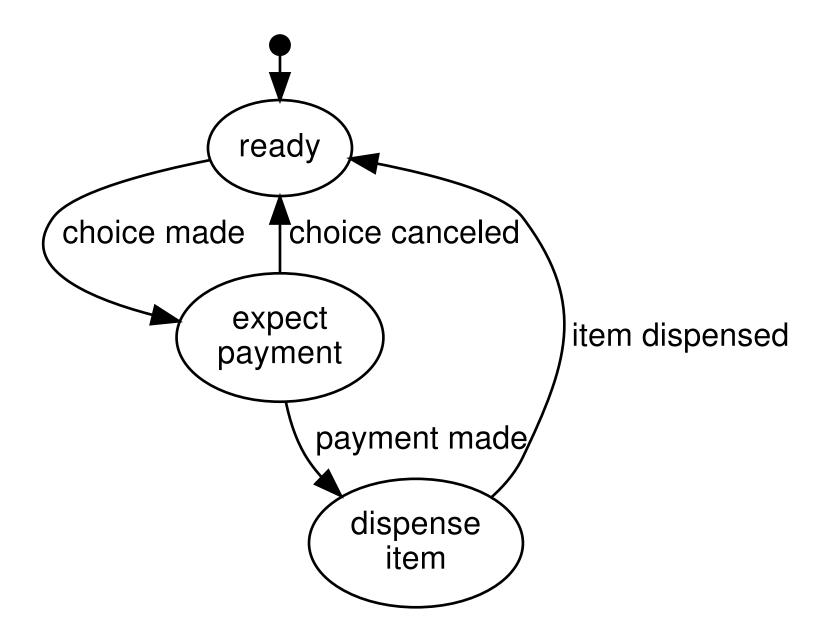
open source limited open tool set

mature limited syntax

fast no arrays of modules

well-defined semantics focus on synchronous systems

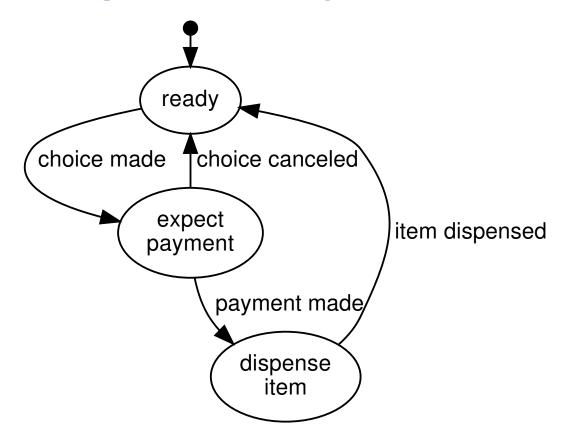
Example: Vending machine



Details not modeled

- How choice is made (how many choices) and canceled.
 - → Button, timeout, both?
- How payment is handled/accepted; price of goods.
- Item dispenser mechanism, time taken to dispense item.

Example: Vending machine—2



- Three states: ready, expect_payment, dispense_item.
- Two user inputs (non-deterministic):
 - 1. Choice (of item); can be cancelled.
 - 2. Payment (requires choice to be made first).

Vending machine in NuSMV

```
MODULE main
VAR
  choice, payment: boolean;
  state: { ready, expect_payment, dispense_item };
ASSIGN
  init (state) := ready;
  next (state) := case
    state = ready & choice: expect_payment;
    state = expect_payment & payment: dispense_item;
    state = expect_payment & !choice: ready;
    state = dispense_item: ready;
    esac;
```

NuSMV syntax

- Module, variables, assignments.
- case (follows order of declaration); can have multiple outcomes.

Error message

```
file vending.smv: line 3: at token ",": syntax error file vending.smv: line 3: Parser error NuSMV terminated by a signal
```

- Cannot declare more than one variable per line!
- Try again...

Another error message

```
file vending.smv: line 14: case conditions are not exhaustive
```

Recall the case block:

• State should remain the same by default: specify!

Complete case block

```
init (state) := ready;
next (state) := case

state = ready     & choice: expect_payment;
state = expect_payment & payment: dispense_item;
state = expect_payment & !choice: ready;
state = dispense_item: ready;
TRUE:
esac;
```

- Transitions from ready and expect_payment depend on user choice.
- Cancellation is modeled as choice reverting to false.
- Transition from dispense_item back to ready is automatic.

Run NuSMV

- Nothing happens!
- We need properties...

```
LTLSPEC
   G(choice -> F state = dispense_item);
```

"Every time I choose something, I eventually get it".

Nice try!

```
-- specification
  G (choice -> F state = dispense_item) is false
-- as demonstrated by the following execution sequence
Trace Description: LTL Counterexample
Trace Type: Counterexample
 -- Loop starts here
 -> State: 1.1 <-
    choice = TRUE
   payment = FALSE
    state = ready
 -> State: 1.2 <-
    choice = FALSE
    state = expect_payment
  -> State: 1.3 <-
    choice = TRUE
    state = ready
```

OK, I'll pay...

LTLSPEC

```
G(payment -> F state = dispense_item);
-- specification
   G (payment -> F state = dispense_item) is false
-- as demonstrated by the following execution sequence
Trace Description: LTL Counterexample
Trace Type: Counterexample
   -- Loop starts here
   -> State: 1.1 <-
      choice = FALSE
      payment = TRUE
      state = ready
   -> State: 1.2 <-</pre>
```

- State 1.2: no progress.
- Payment is accepted even when no choice has been made!

Accept payment only when choice is made

```
MODULE main
VAR
 choice: boolean;
 payment: boolean;
 acc_payment: boolean;
 state: { ready, expect_payment, dispense_item };
ASSIGN
 init (state) := ready;
 next (state) := case
   state = expect_payment & acc_payment: dispense_item;
   state = expect_payment & !choice: ready;
   state = dispense_item:
                                   ready;
   TRUE:
                                   state;
 esac;
 init (acc_payment) := FALSE;
 next (acc_payment) := (state = expect_payment & payment);
```

Another problem?!

```
G (acc_payment -> F state = dispense_item) is false
-> State: 1.1 <-
  choice = FALSE
  payment = FALSE
  acc_payment = FALSE
  state = ready
-> State: 1.2 <-
  choice = TRUE
-> State: 1.3 <-
  choice = FALSE
  payment = TRUE
  state = expect_payment
-> State: 1.4 <-
  payment = FALSE
  acc_payment = TRUE
  state = ready
-- Loop starts here
-> State: 1.5 <-
  acc_payment = FALSE
-> State: 1.6 <-
```

State 1.3: Choice is made, next state = accept payment State 1.4: accepting payment, but choice is canceled just now!

- Need a way to prevent this transition back to *ready*.
- Use stricter case condition!
- Lab exercise 1.

Extension of the vending machine

- Limited capacity of *n* items.
- Payment should not be accepted when no items available.
- Counting down items:

```
next(n_items) := case
    ...: n_items - 1;
    TRUE: n_items;
esac;
```

Fails!

```
file vending3.smv: line 16:
  cannot assign value -1 to variable n_items
```

Counting without over- or underflow

NuSMV recognized possible over- or underflow at compile time.

```
next(n_items) := case
    ... & n_items > 0: n_items - 1;
    TRUE: n_items;
esac;
```

• Underflow needs to be prevented in code.

Additional properties

- 1. Number of items should always be ≥ 0 .
- 2. Payment should only be accepted if number of items > 0.
- 3. If an item is dispensed, the counter of items is always reduced by 1.

First lab exercise (part of assignment 1): Summary

- 1. Use NuSMV on vending1.smv.
 - (a) Study error trace.
 - (b) Refine transition (case condition).
- 2. Counting remaining items.
 - (a) Add a counter **n_items** (see above).
 - (b) Write LTL or CTL properties for the three properties above.
 - (c) Ensure your model fulfills all properties.

Summary

Temporal logics

Linear temporal logic (LTL): Computational tree logic (CTL):

No branching.

Defined on paths.

Branching.

Defined on transition systems.

Model checking

Enumerate all reachable states.

- Check if "bad" state reachable.
- Active research, many optimizations (such as BDDs).