

Appendix C: Demonstration of selected features

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```
library(phylosem)
```

`phylosem` is an R package for fitting phylogenetic structural equation models (PSEMs). We here highlight a few features in particular.

Estimability for multiple covariance transformations

By default, `phylosem` takes as input a phylogenetic tree and constructs a covariance under a Brownian motion evolutionary model. However, it also allows any combination of the following transformations:

- Ornstein-Uhlenbeck (OU);
- Pagel's lambda;
- Pagel's kappa;

This then results in eight possible covariance models formed from including or excluding each transformation. We first show that these transformations are all simultaneously estimable for a reference data set.

```
# Compare using Pagel's kappa
library(phylopath)

# Run phylosem
model = "
  DD -> RS, p1
  BM -> LS, p2
  BM -> NL, p3
  NL -> DD, p4
"

psem = phylosem( sem = model,
  data = rhino[,c("BM", "NL", "DD", "RS", "LS")],
  estimate_ou = TRUE,
  estimate_lambda = TRUE,
  estimate_kappa = TRUE,
  tree = rhino_tree,
  getJointPrecision = TRUE,
  quiet = TRUE )

#
V = psem$opt$SD$cov.fixed
Rsub = cov2cor(V)[c('lnalpha', 'logitlambda', 'lnkappa'), c('lnalpha', 'logitlambda', 'lnkappa')]

knitr::kable(c("minimum_eigenvalue"=min(eigen(psem$opt$SD$jointPrecision)$values),
  "maximum_eigenvalue"=max(eigen(psem$opt$SD$jointPrecision)$values)), digits=3)
```

	x
minimum_eigenvalue	0.035
maximum_eigenvalue	43439.097

```
knitr::kable(Rsub, digits=3)
```

	lnalpha	logitlambda	lnkappa
lnalpha	1.000	0.741	0.422
logitlambda	0.741	1.000	0.183
lnkappa	0.422	0.183	1.000

We see that the minimum eigenvalue for the precision matrix (which corresponds to the maximum eigenvalue of the covariance matrix) is greater than zero, such that the precision is invertible and the Hessian matrix is full rank. From this we can see that all parameters are estimable when applying all three transformations. We also see that transformation parameters are not perfectly correlated, although the logit-lambda and ln-alpha parameters have a correlation of approximately 0.75.

Scaling of runtime with increased tree size

The package `phylolm` is expected to have a “linear runtime”, i.e., a proportional increase in runtime with increasing tree size. We therefore compare runtime for `phylosem` and `phylolm` using a simulated tree across three orders of magnitude (10, 100, 1000, or 10000 tips).

```
# Settings
Ntree_config = c( 1e1, 1e2, 1e3, 1e4 )
Nreplicates = 5
sd_x = 0.3
sd_y = 0.3
b0_x = 1
b0_y = 0
b_xy = 1

# Simulate tree
set.seed(1)
Time_rcz = array(NA, dim=c(Nreplicates,length(Ntree_config),2), dimnames=list(NULL,"tree_size"=Ntree_config))

for( rI in seq_len(Nreplicates) ){
  for( cI in seq_along(Ntree_config) ){

    # Simulate data
    tree = ape::rtree(n=Ntree_config[cI])
    x = b0_x + sd_x * phylolm::rTrait(n = 1, phy=tree)
    ybar = b0_y + b_xy*x
    y_normal = ybar + sd_y * phylolm::rTrait(n = 1, phy=tree)
    Data = data.frame(x=x, y=y_normal)[]

    # Run phylolm
    start_time = Sys.time()
    plm_bm = phylolm::phylolm(y ~ 1 + x, data=Data, phy=tree, model="BM" )
```

```

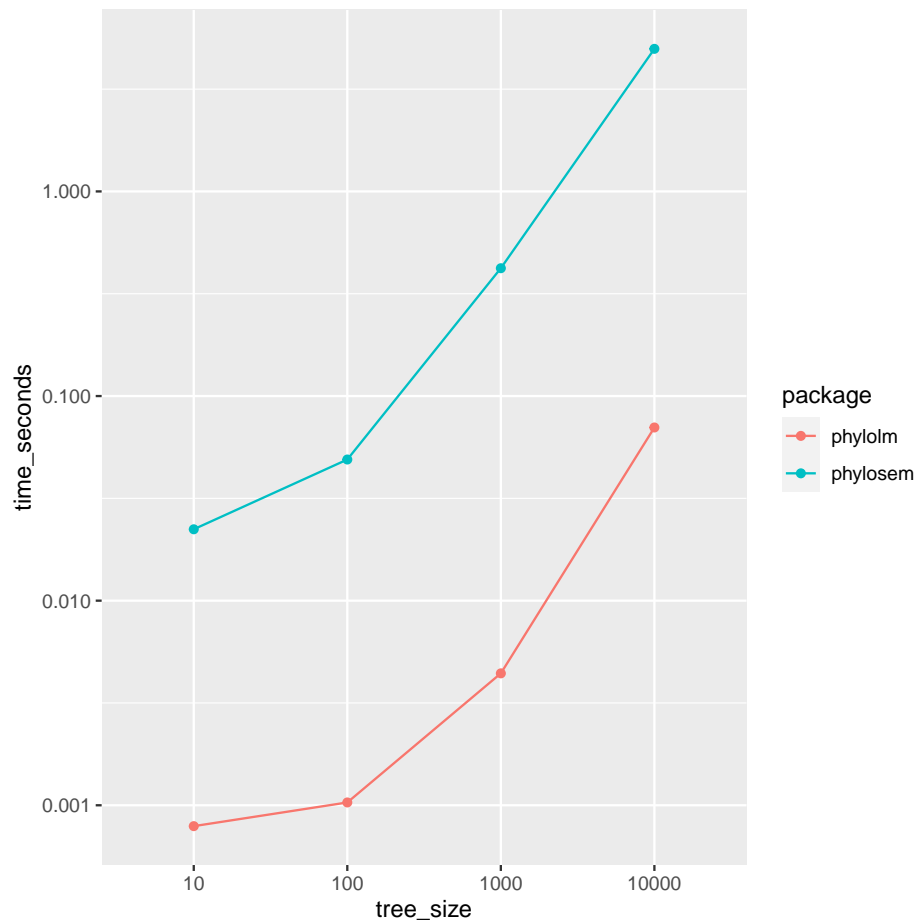
Time_rcz[rI,cI,"phylolm"] = Sys.time() - start_time

# Run phylosem
start_time = Sys.time()
psem_bm = phylosem( sem = "x -> y, p",
  data = Data,
  tree = tree,
  quiet = TRUE,
  newtonsteps = 0,
  getsd = FALSE )
Time_rcz[rI,cI,"phylosem"] = Sys.time() - start_time
}}

# Format
df = apply( Time_rcz, MARGIN=2:3, FUN=mean )
df = cbind( expand.grid(dimnames(df)), "time_seconds"=as.vector(df) )

# Plot
library(ggplot2)
ggplot(data=df, aes(x=tree_size, y=time_seconds, group=package, color=package)) +
  geom_line() +
  geom_point() + scale_y_log10()

```



Results show that both packages have approximately linear runtime, but that `phylolm` is approximately 10-100 times faster for any given tree size.