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In [ ]: import numpy as np
import matplotlib.pyplot as plt
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In [ ]: ## Question 1 (a) ##

alpha = 0.01 # decay constant
t = 1 # this is delta t
p = alpha*t # probability of decay when
q = 1-p # total probability is 1, so this is the survival probability
n1 = 100
T = 300

def Decay1(N):
    pop = []
    for t in range(T):
        r = np.random.random(N)
        survive = np.sum(r < q) # surviving atoms
        pop.append(survive)
        N = survive
    return pop

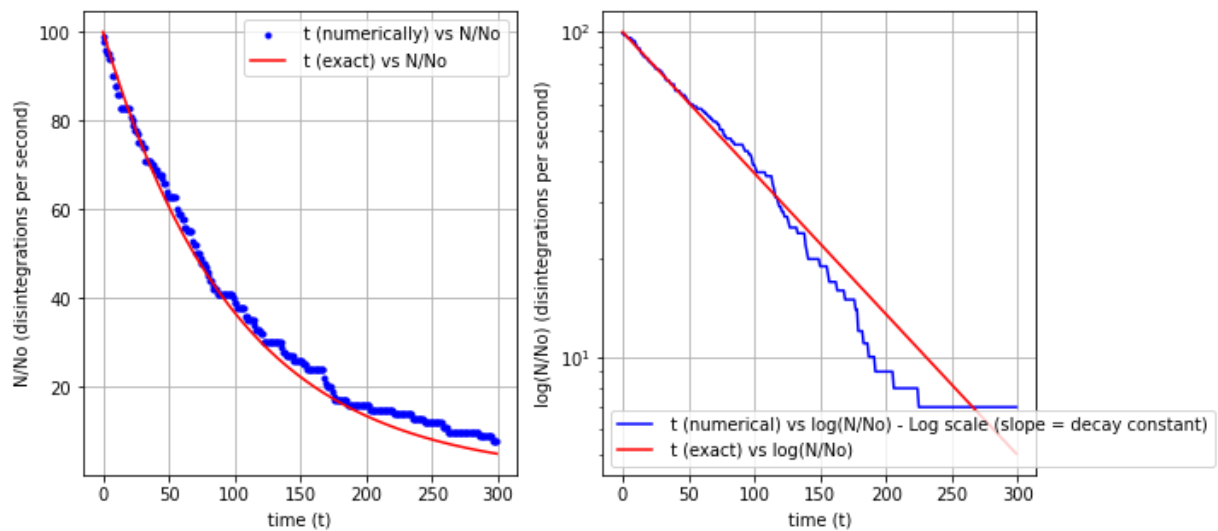
plt.figure(figsize =(10,5))

plt.subplot(1,2,1)
plt.plot(range(T),Decay1(n1),'b.', label = ' t (numerically) vs N/No')

analyticals = []
for i in range(T):
    analyticals.append(n1*np.exp(-alpha*i))
plt.plot(range(T),analyticals,'-r',label = ' t (exact) vs N/No' )
plt.xlabel('time (t)')
plt.ylabel('N/No (disintegrations per second)')
plt.legend()
plt.grid()

plt.subplot(1,2,2)

plt.semilogy()
plt.plot(range(T),Decay1(n1),'b',label = ' t (numerical) vs log(N/No) - Log scale (s
plt.semilogy()
plt.plot(range(T),analyticals,'-r', label = ' t (exact) vs log(N/No)' )
plt.xlabel('time (t)')
plt.ylabel('log(N/No) (disintegrations per second)')
plt.legend()
plt.grid()
```



In []:

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## Question 1 (b) ##

alpha2 = 0.03
p2 = alpha2
q2 = 1-p2
n2 = 5000
T=300

def Decay2(N):
    population = []
    for t in range(T):
        r = np.random.random(N)
        survive = np.sum(r<q2)
        population.append(survive)
        N = survive
    return population

plt.figure(figsize =(10,5))

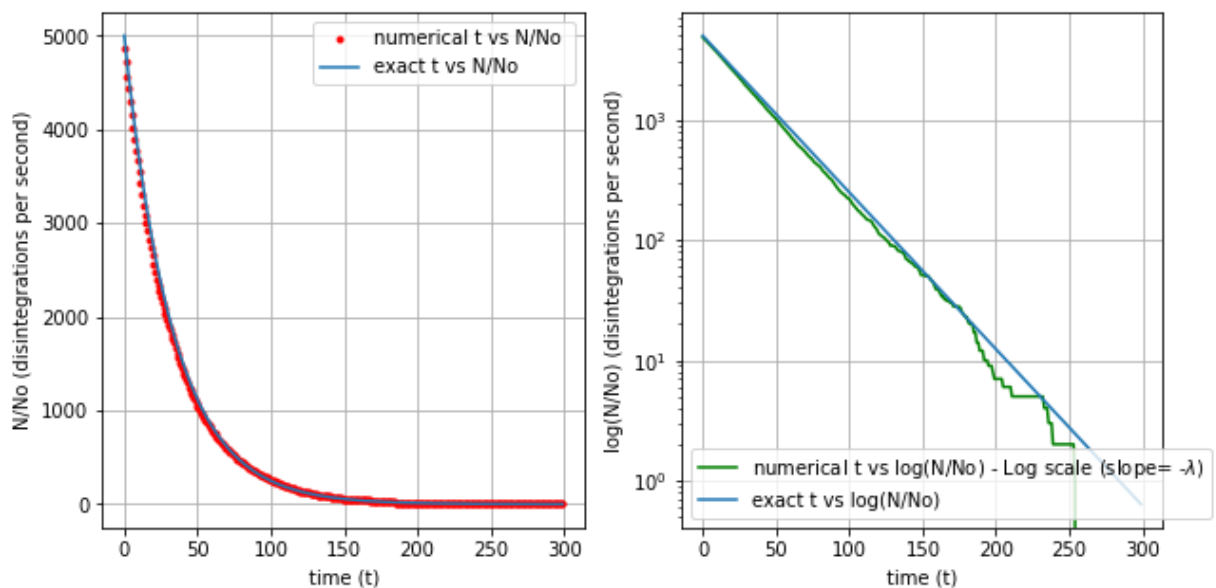
plt.subplot(1,2,1)
plt.plot(range(T),Decay2(n2),'r.',label = 'numerical t vs N/No ')

analyticals = []
for i in range(T):
    analyticals.append(n2*np.exp(-alpha2*i))
plt.plot(range(T),analyticals,label = 'exact t vs N/No' )

plt.xlabel('time (t)')
plt.ylabel('N/No (disintegrations per second)')
plt.legend()
plt.grid()

plt.subplot(1,2,2)
plt.semilogy()
plt.plot(range(T),Decay2(n2),'g-',label = 'numerical t vs log(N/No) - Log scale (slo
plt.semilogy()
plt.plot(range(T),analyticals,label = 'exact t vs log(N/No)' )
plt.grid()
plt.xlabel('time (t)')
plt.ylabel('log(N/No) (disintegrations per second)')
plt.legend()
```

Out[]: <matplotlib.legend.Legend at 0xf9acd0>



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In [ ]: ## Question 2 (a) ##

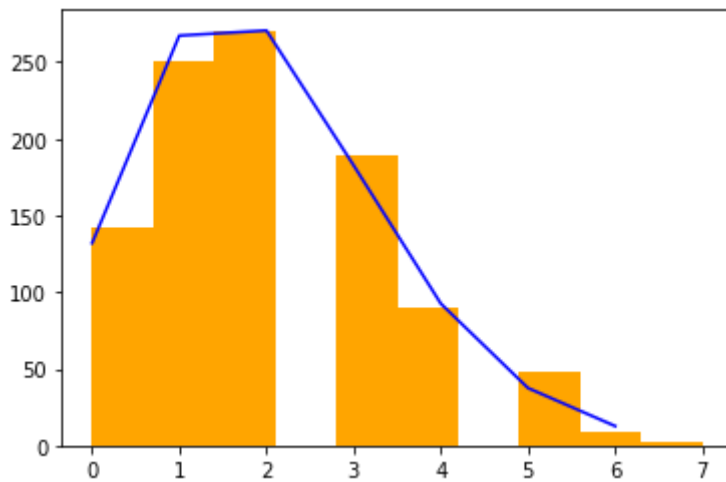
distribution = []
N = 500
def decays(N):
    alphas = 4*10**(-5) # decay constant
    delta_t = 10
    p = delta_t*alphas # decay probability for delta t =1
    q = 1-p # survival probability

    T=100
    jump = int(T/delta_t)
    populations = []
    for t in range(jump):
        r = np.random.random(N)
        survive = np.sum(r<q) # surviving atoms
        populations.append(survive)
        N = survive
    return populations

for i in range(1000):
    p = decays(N)
    distribution.append(N-p[-1])

plt.hist(distribution,color='orange')
average_distribution = np.mean(distribution)
from scipy.stats import poisson # we have used the poisson function from SciPy
x = np.arange(0,7,1)
y = 1000*poisson.pmf(x, mu =average_distribution)
plt.plot(x,y, 'blue')
```

Out[]: <matplotlib.lines.Line2D at 0xb792b0>



In []:

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## Question 2 (b) ##

distribution = []

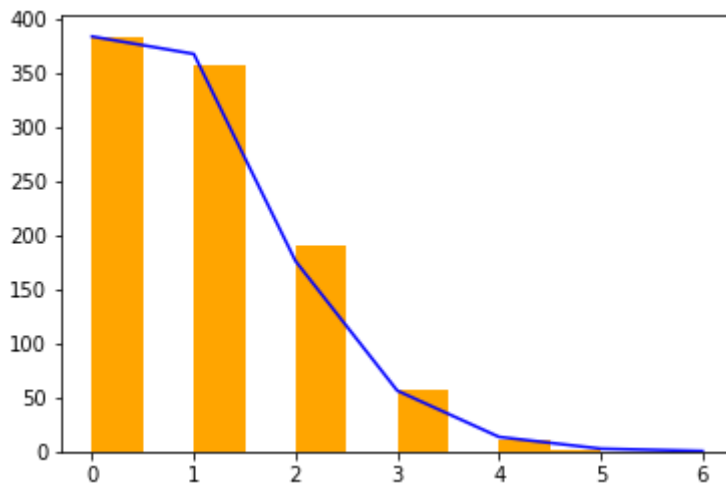
def decays(N):
    alphas = 2*10**(-5) # it is the decay constant
    delta_t = 10
    p = delta_t*alphas # decay probability for delta t =1
    q = 1-p # survival probability

    T=100
    jump = int(T/delta_t)
    populations = []
    for t in range(jump):
        r = np.random.random(N)
        survive = np.sum(r<q) # number of atoms survived
        populations.append(survive)
        N = survive
    return populations

for i in range(1000):
    p = decays(N)
    distribution.append(N-p[-1])

plt.hist(distribution,color='orange')
average_distribution = np.mean(distribution)
from scipy.stats import poisson
x = np.arange(0,7,1)
y = 1000*poisson.pmf(x, mu =average_distribution)
plt.plot(x,y, 'blue')
```

Out[]: [<matplotlib.lines.Line2D at 0x15f14450>]



In []:

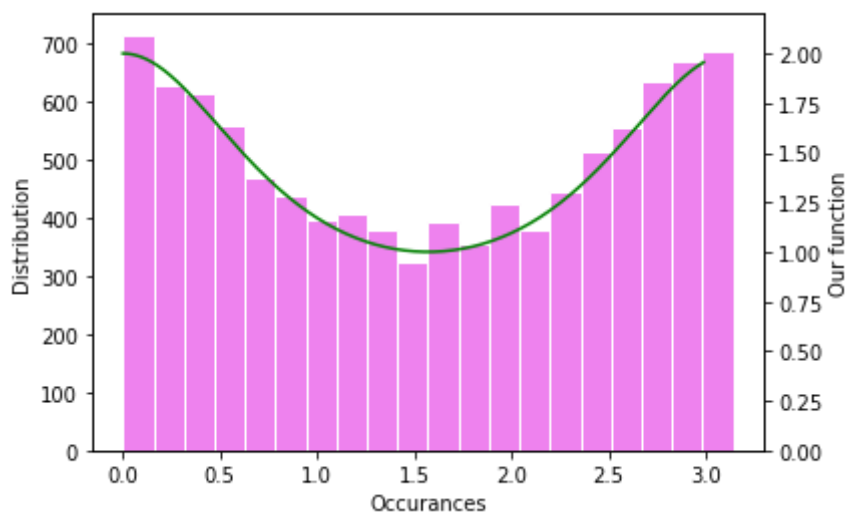
```
## Question 3 (a) ##

def DistF(u): # distribution function
    return(np.arctan(np.sqrt(0.5)*np.tan((u-1)*np.pi)))

DistF(0)
#DistFunction(1)
N=np.random.rand(10000)
def Func1(th):
    return(1/(np.sin(th)**2+0.5*np.cos(th)**2))

fig,ax1=plt.subplots()
Y=DistF(np.random.rand(10000))
for i in range(10000):
    if Y[i]<0:
        Y[i]=Y[i]+np.pi
X=np.arange(0,3,0.01)
Curve=Func1(X)
ax1.hist(Y,color='violet',edgecolor='white',bins=20)

ax1.set_xlabel('Occurances')
ax1.set_ylabel('Distribution')
ax2=ax1.twinx()
ax2.plot(X,Curve,linestyle='-',color='green')
ax2.set_ylim(0,2.2)
ax2.set_ylabel('Our function')
plt.show()
```



In []:

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## Question 3 (b) ##
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U1= np.random.rand(10000)
U2= np.random.rand(10000)
Y=[]
for i in range(10000):
    if Func1(np.pi*U1[i])>=U2[i]*2.25:
        Y.append(np.pi*U1[i])
fig,ax1=plt.subplots()
ax1.hist(Y,color='red',edgecolor='black',bins=20)
ax1.set_xlabel('Occurances')
ax1.set_ylabel('Distribution')
ax2=ax1.twinx()
X=np.arange(0,3.05,0.01)
Curve=Func1(X)
ax2.plot(X,Curve,linestyle='-',color='blue')
ax2.set_ylim(0,2.2)
ax2.set_ylabel('Our function')
plt.show()

```

