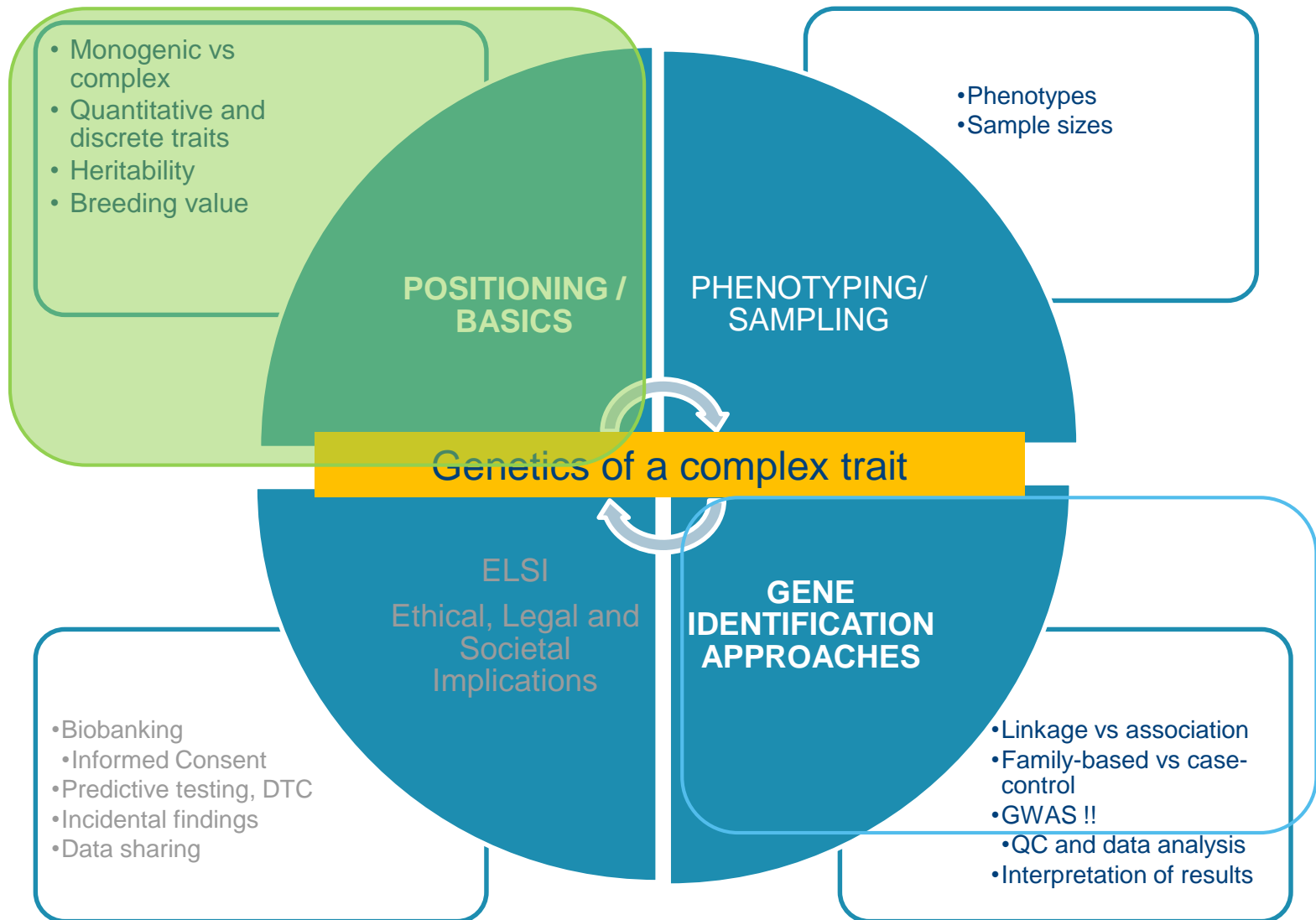
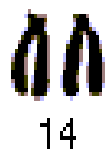
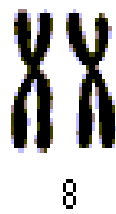
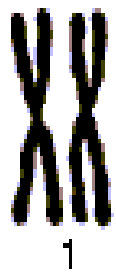




# Quantitative genetics

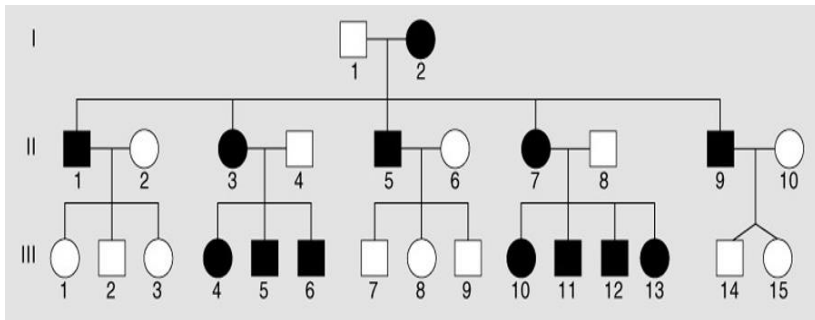
## 2. Gene identification approaches





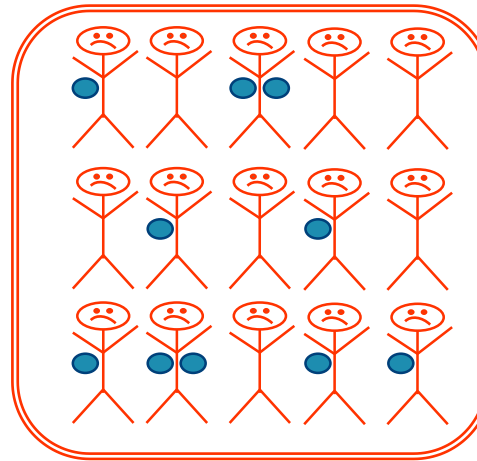
# Linkage versus association

- Linkage studies

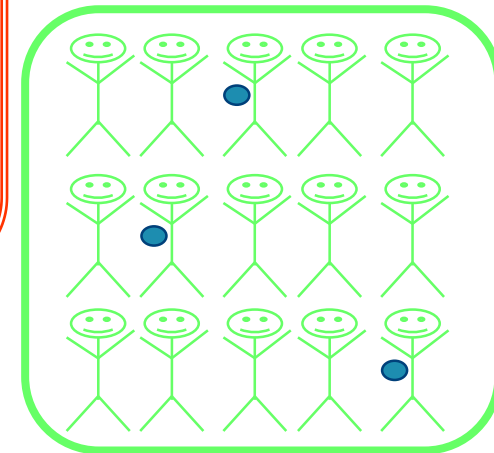


- Association studies

cases

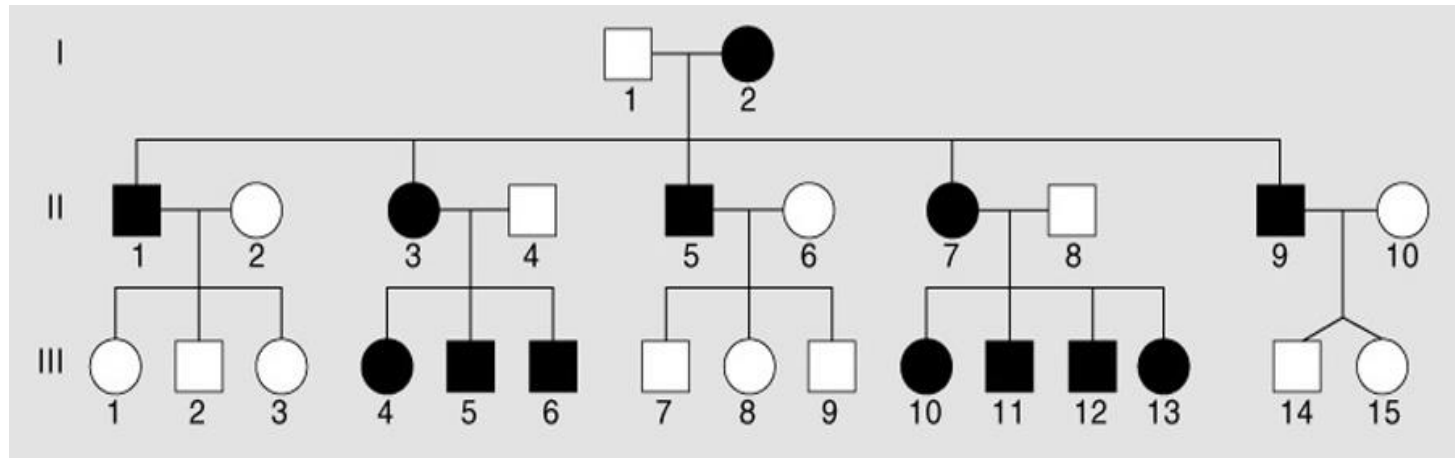


controls



# Linkage analysis

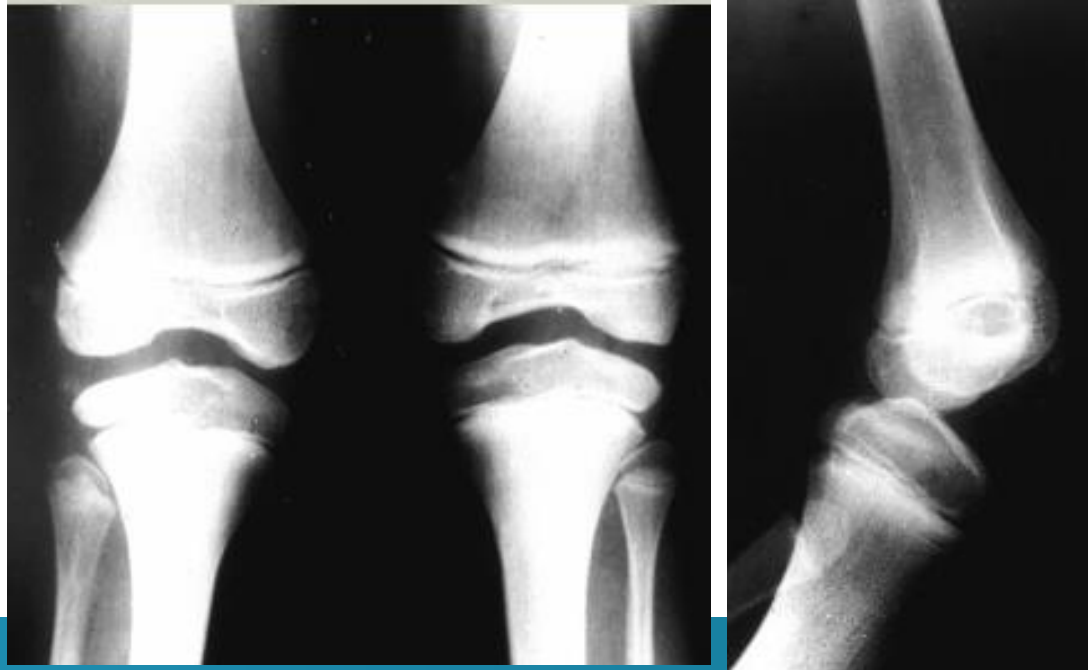
- co-segregation of genetic marker(s) and disease in a family



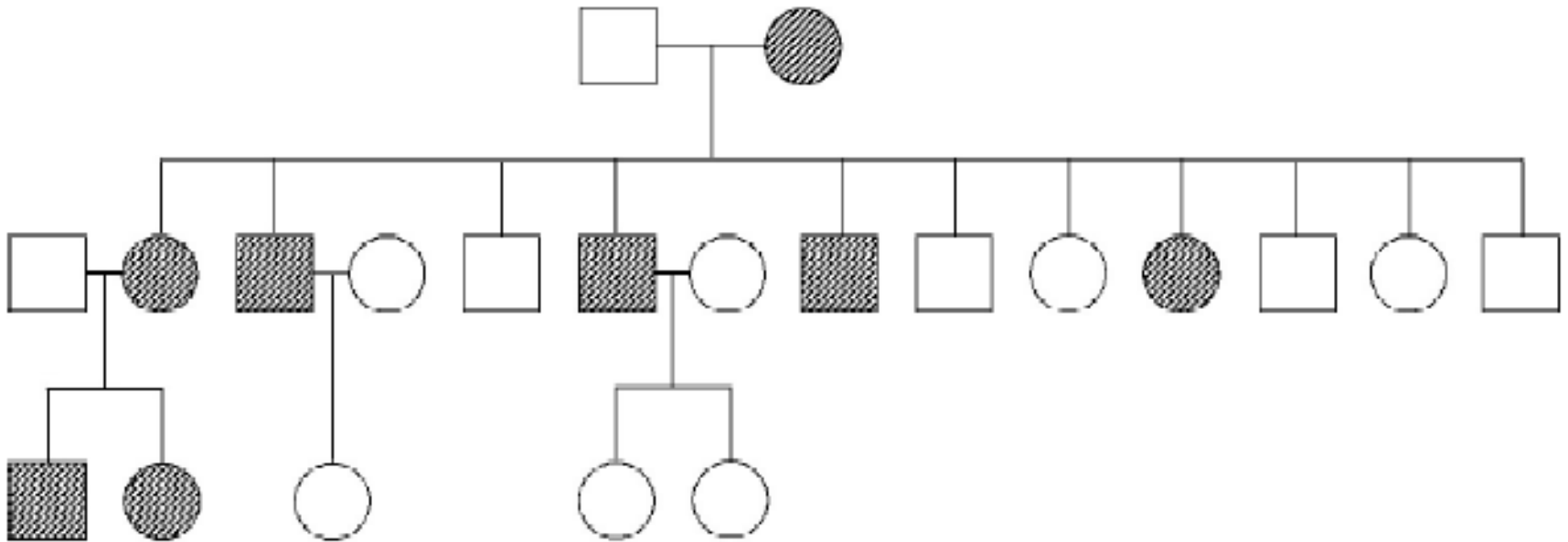
- Goal:
  - identify chromosomal region with risk gene
  - map traits of interest to particular chromosomal region

- What is linkage?
- How to quantify?
- How to use it to identify chromosomal region(s) with disease gene(s)?

Example – nail patella syndrome (NPS)



# Example – Nail patella syndrome

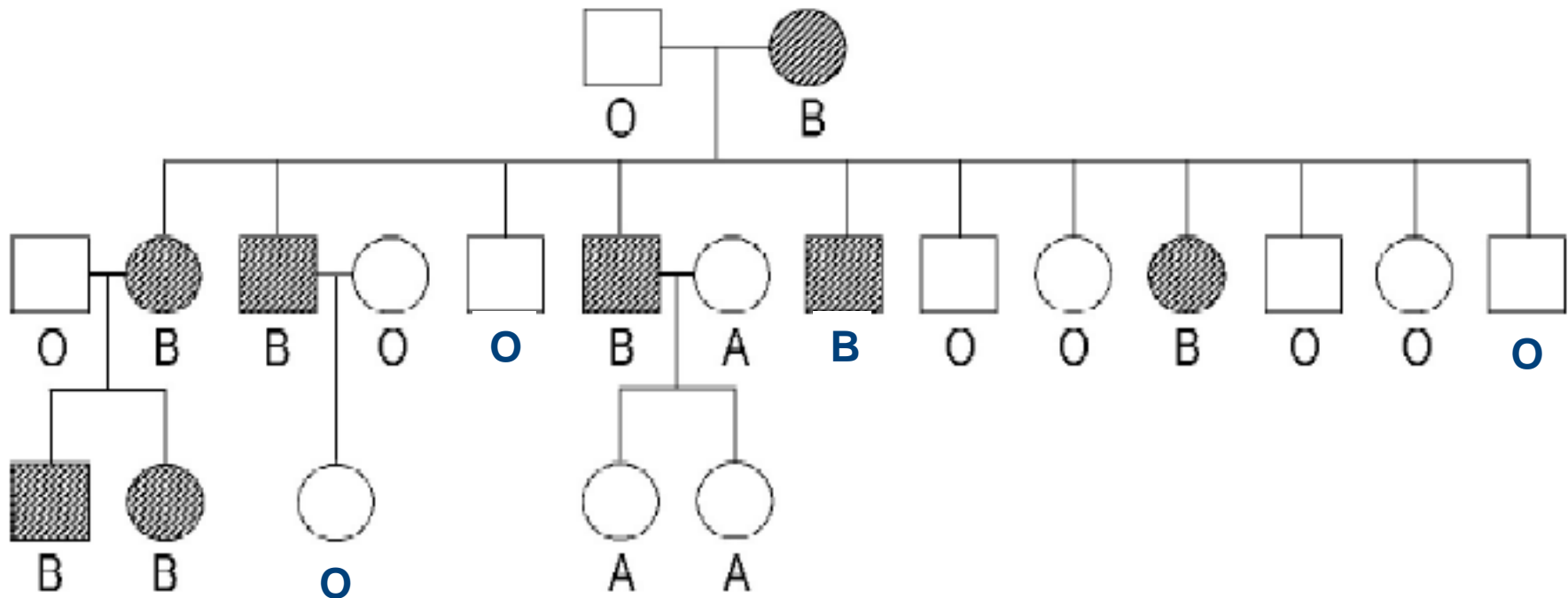


Autosomal dominant



# Example – Nail patella syndrome

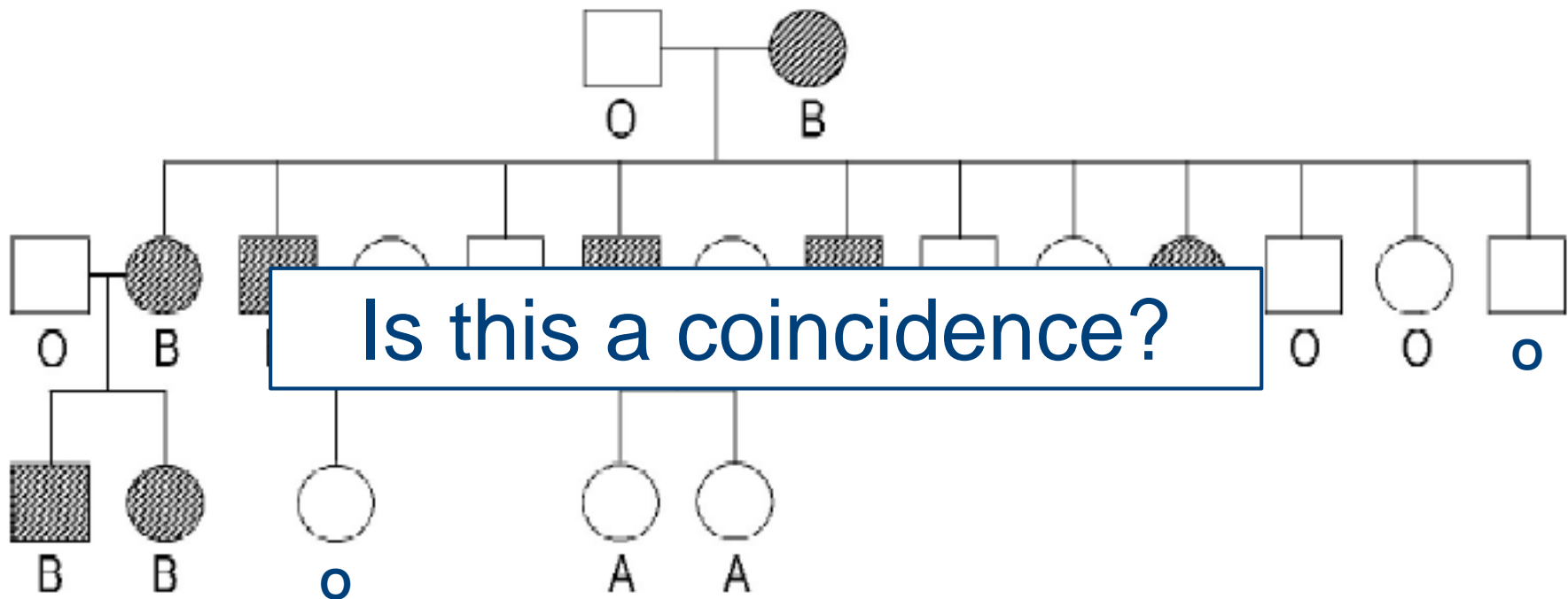
ABO-blood type



All individuals with NPS in this family have the same blood type

# Example – Nail patella syndrome

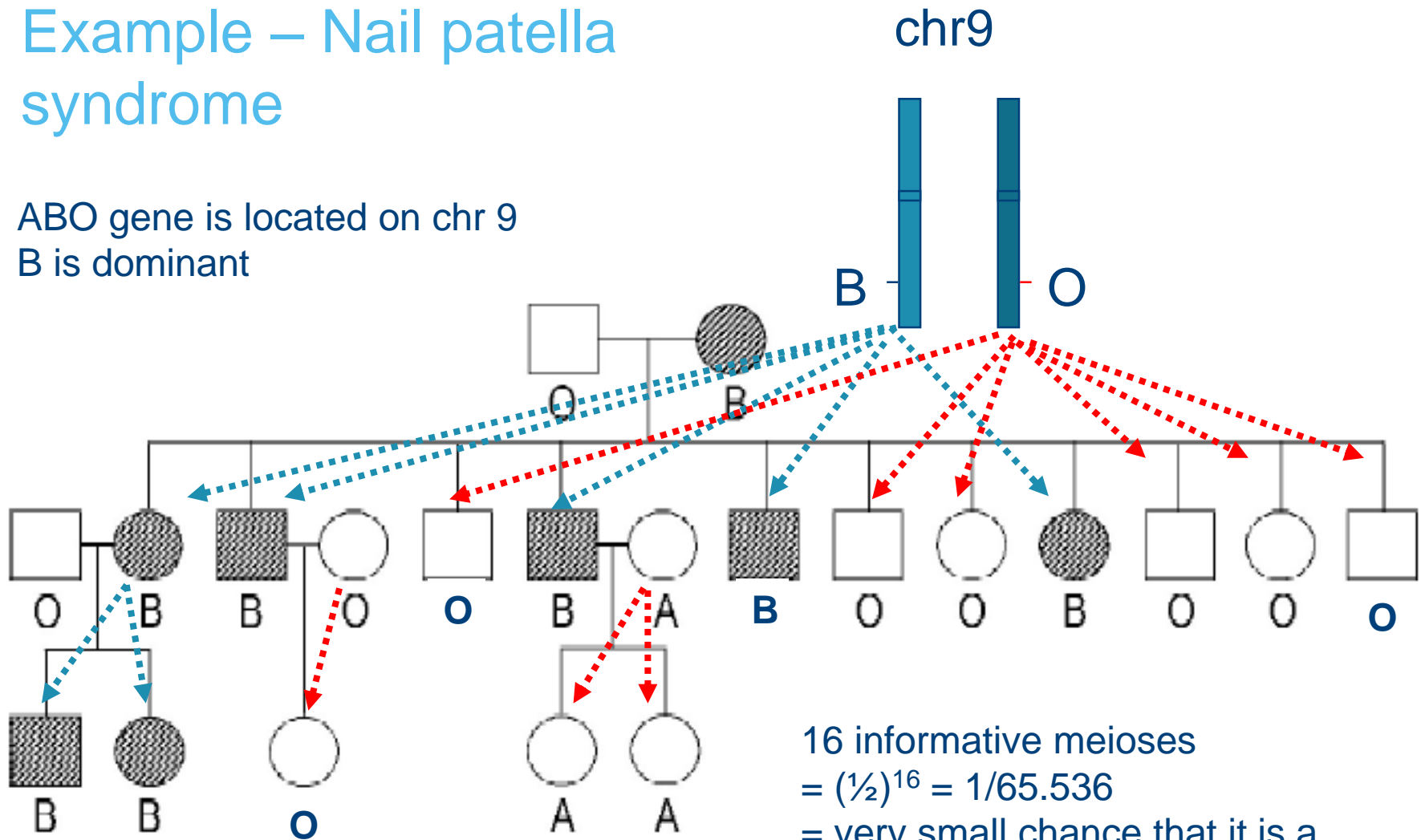
ABO-blood type



All individuals with NPS in this family have the same blood type

# Example – Nail patella syndrome

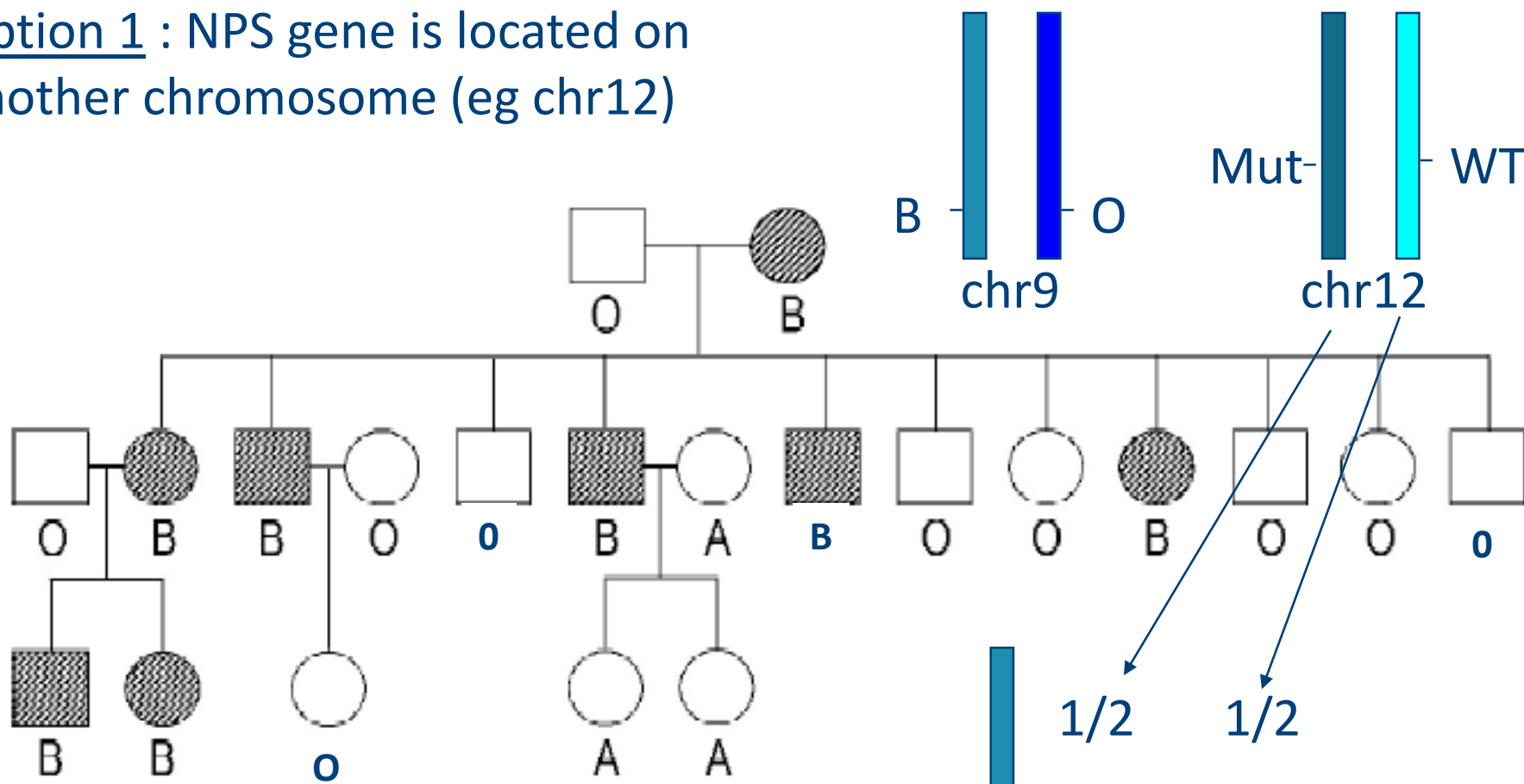
- ABO gene is located on chr 9
- B is dominant



16 informative meioses  
 $= (\frac{1}{2})^{16} = 1/65.536$   
 = very small chance that it is a coincidence that NPS is always co-inherited with blood type

# Where is the NPS gene located?

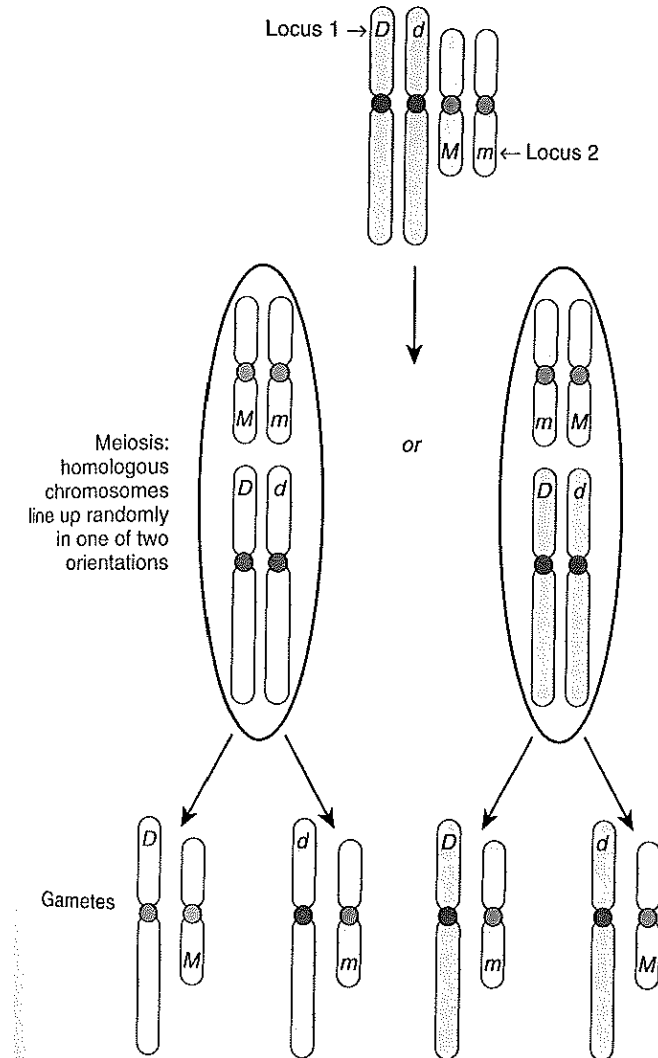
Option 1 : NPS gene is located on another chromosome (eg chr12)



Chance that someone has bloodtype B and the mutation?

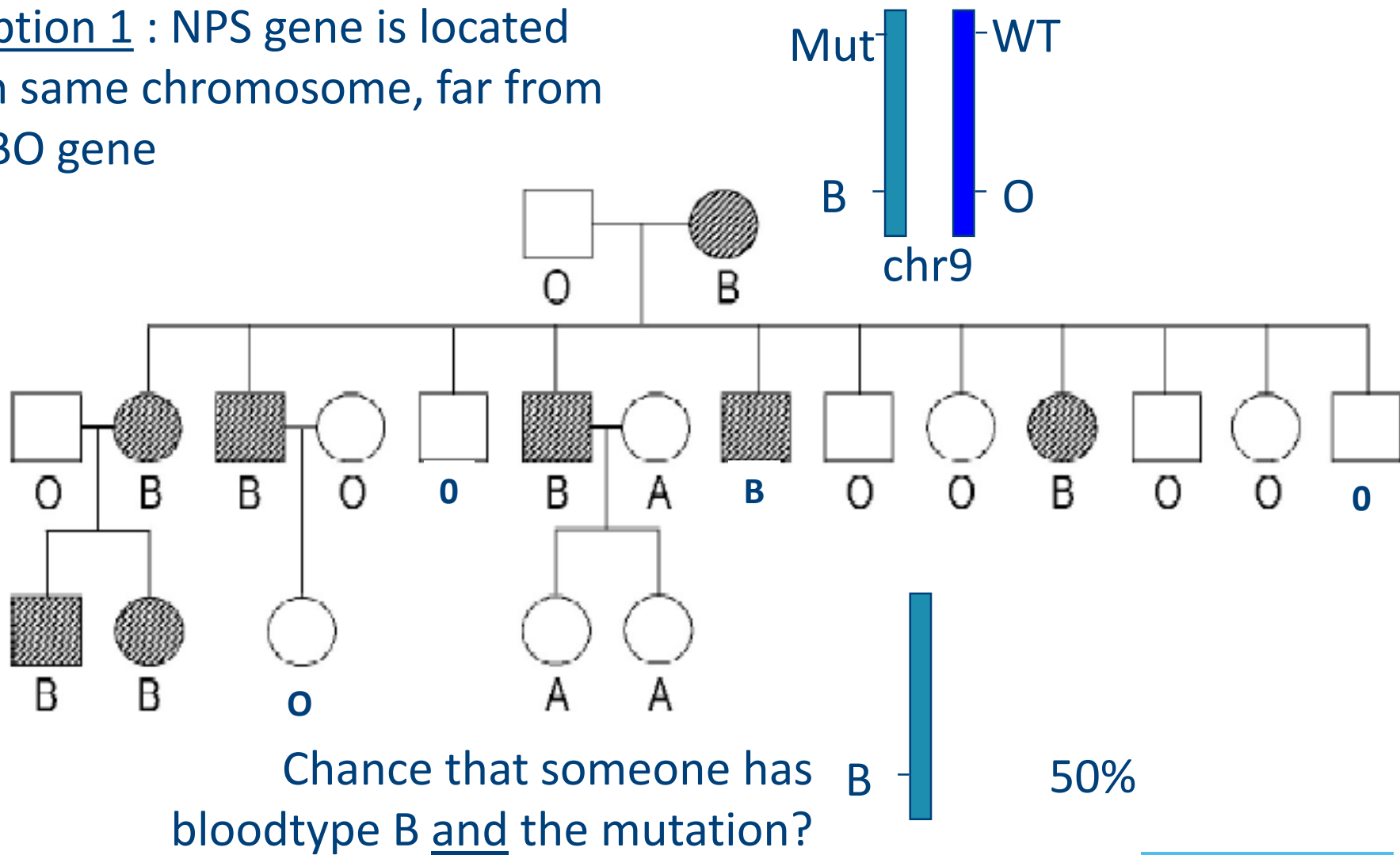
# Law of independent assortment (Mendel)

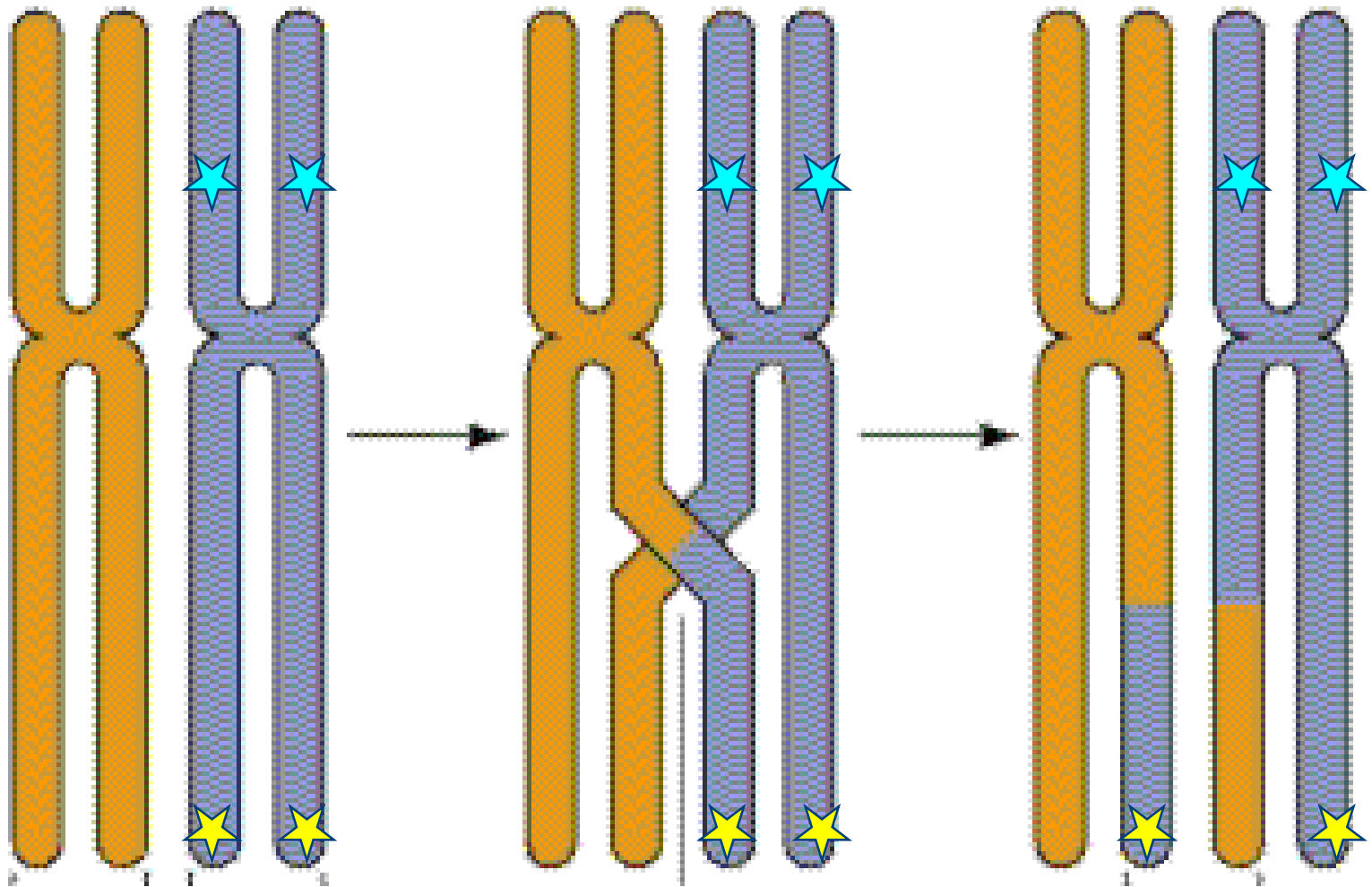
Alleles at loci on different chromosomes assort independently



# Where is the NPS gene located?

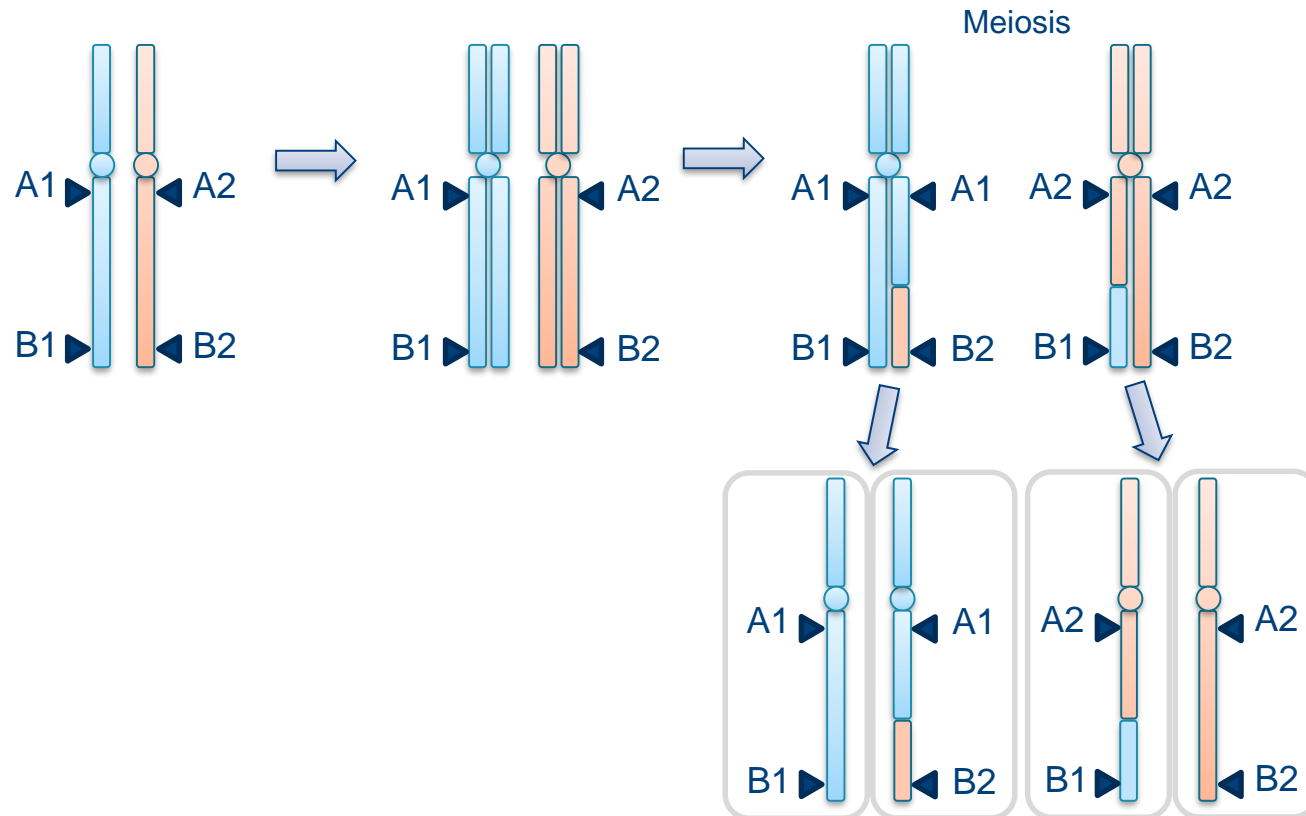
Option 1 : NPS gene is located on same chromosome, far from ABO gene





CROSSING-OVER  
=> are not co-inherited

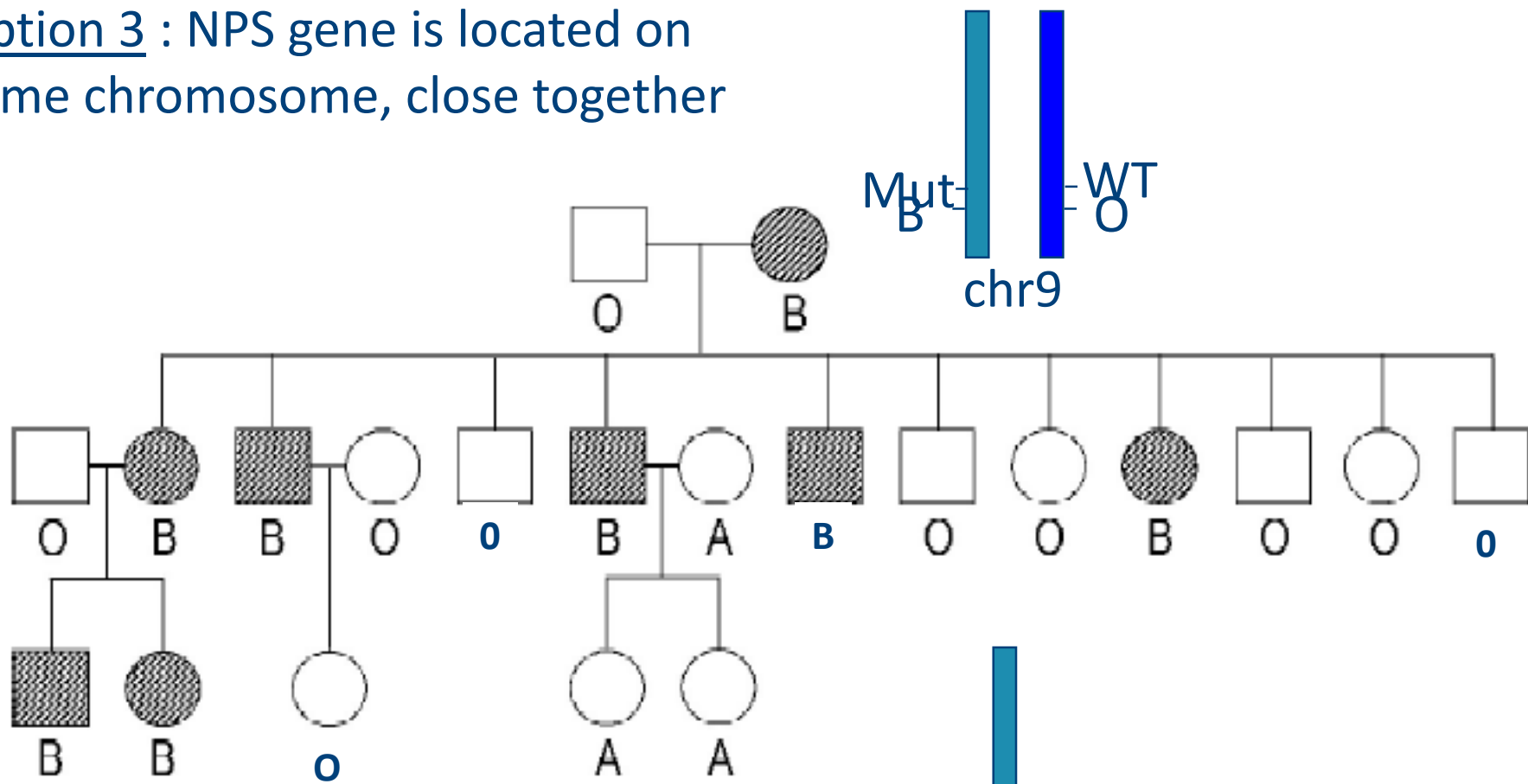
## Recombination during meiosis





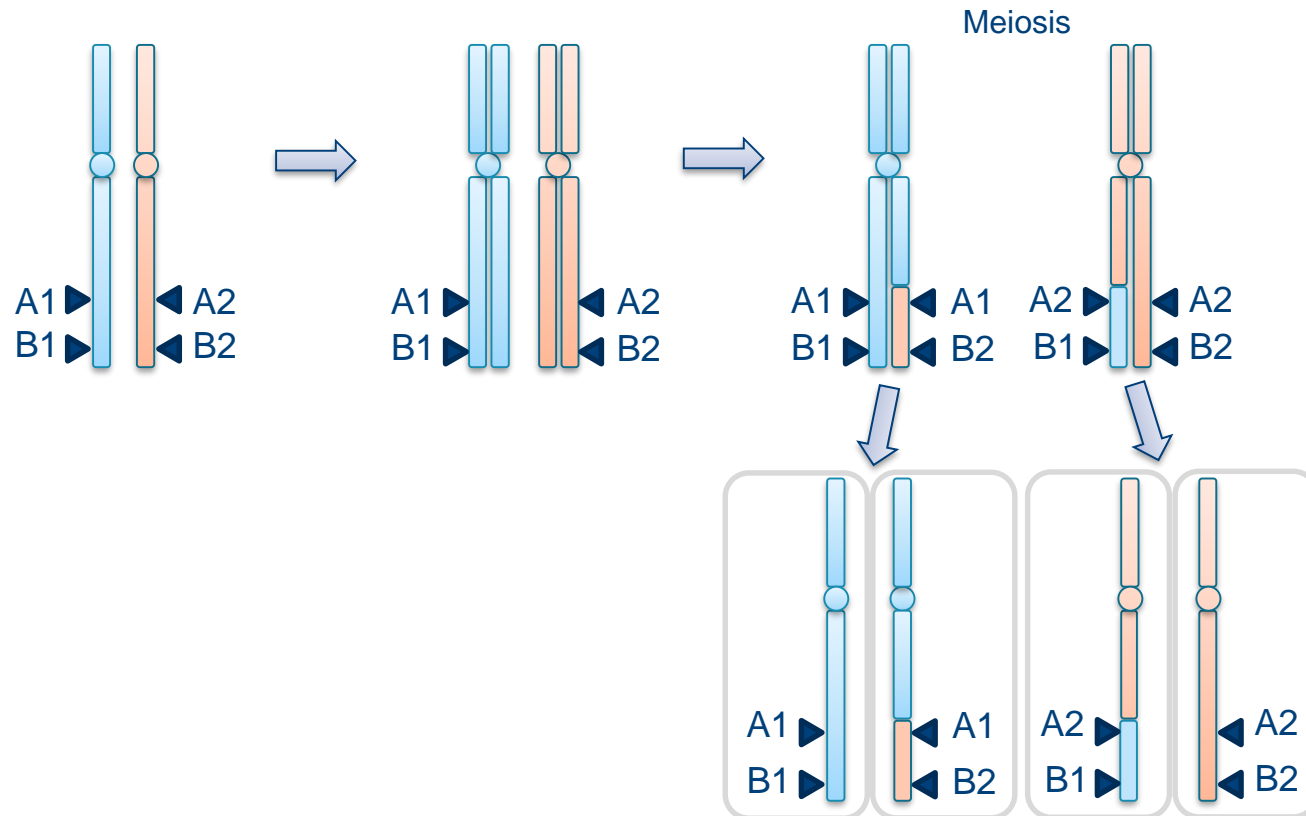
# Where is the NPS gene located?

Option 3 : NPS gene is located on same chromosome, close together



Chance that someone has bloodtype B and the mutation? B > 50%

## Recombination during meiosis

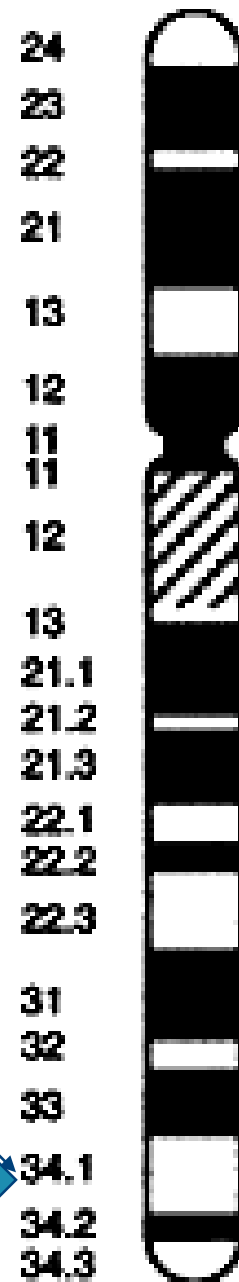


# Where is the NPS gene located?

Chromosome 9

ABO blood type gene

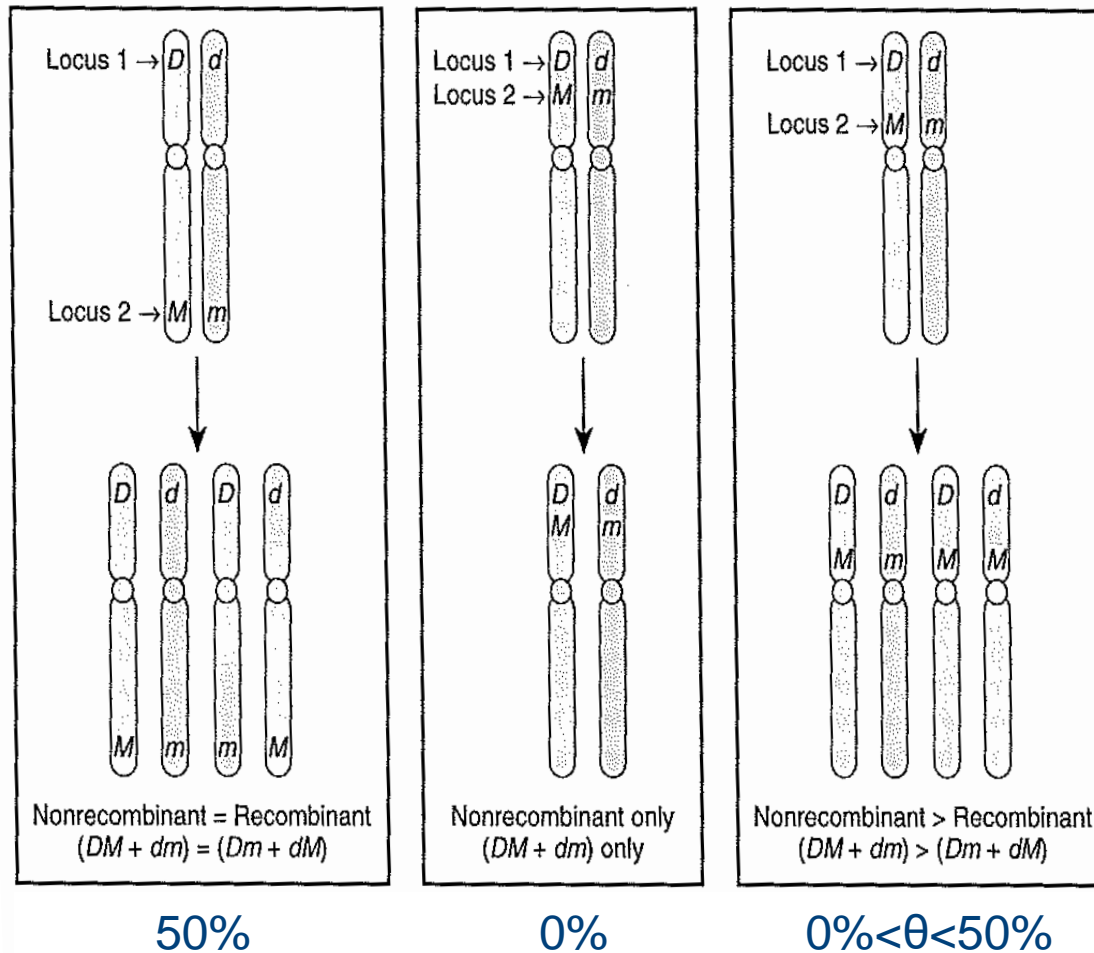
Nail Patella Syndrome gene



# Linkage

- When genes are found on different chromosomes or far apart on the same chromosome, they assort independently = **unlinked**
- When genes are close together on the same chromosome, the alleles, or gene versions, will be inherited as a unit more frequently than not = **linked**
- How can we measure this?

# Recombination during meiosis



The recombination fraction ( $\theta$ ) between two loci is a measure for the distance between these two loci

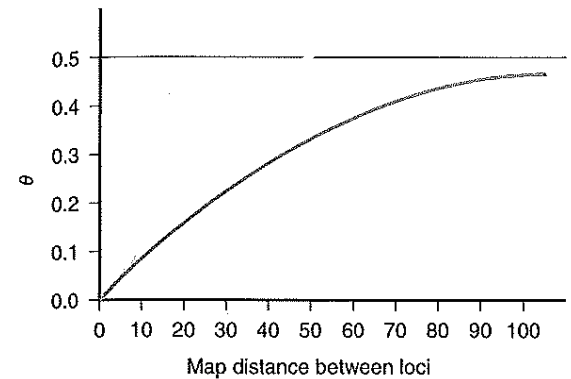
# Linkage

- When genes are found on different chromosomes or far apart on the same chromosome, they assort independently = **unlinked**
- When genes are close together on the same chromosome, the alleles, or gene versions, will be inherited as a unit more frequently than not = **linked**
- How can we measure this?
  - use data from genetic crosses ('meiotic mapping') to calculate the **recombination fraction ( $\theta$ )**
  - If you do this for many gene/marker pairs, we can make **linkage maps** that show the relative distances of the genes on the chromosome

# Recombination fraction $\theta$

$$\theta = \frac{\text{number of recombined gametes (r)}}{\text{number of gametes transmitted (n)}}$$

Parent	Gametes	$\theta$
<div><div>A</div><div>B</div><div><div></div><div></div></div><div>a</div><div>b</div></div>	50% non-rec and 50% rec	0.5
	90% non-rec and 10% rec	0.1
	99% non-rec and 1% rec	0.01
	100% non-rec	0



# Genetic distance

- Chromosomal position: physical vs. genetic
  - physical: base pair position (bp)
  - genetic: recombination fraction (Morgan)

- Mapping function

$$\text{Kosambi (1943): } W = \frac{1}{4} \ln \left( \frac{1 + 2\theta}{1 - 2\theta} \right)$$

- Globally: 1cM = 1Mb = 1% recombination
  - recombination deserts: 0.3 cM/Mb
  - recombination jungles: 3 cM/Mb



# Recombination fraction $\theta$

$$\theta = \frac{\text{number of recombined gametes } (r)}{\text{number of gametes transmitted } (n)}$$

- Recombination fraction ( $\theta$ ) as a measure for linkage

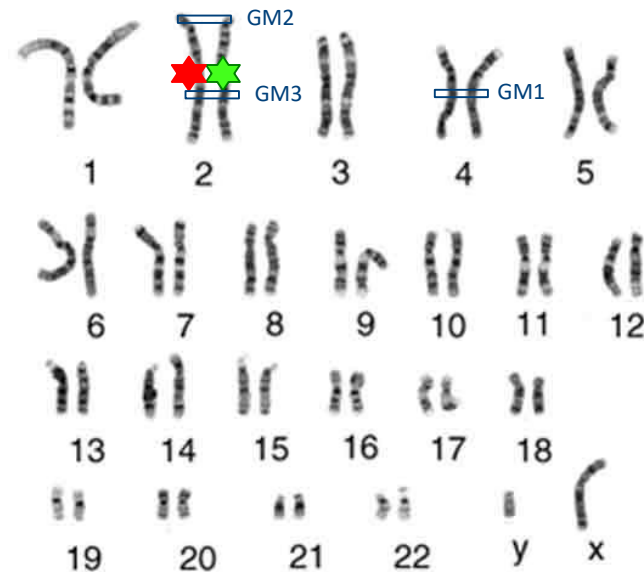
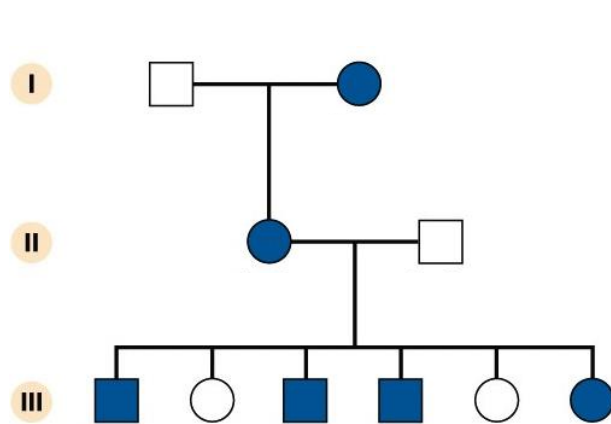
- $0 \leq \theta < \frac{1}{2}$  ?

50% chance of recombination when completely unlinked

- What is linkage?
- How to quantify?
- **How to use it to identify chromosomal region(s) with disease gene(s)?**

# Linkage analysis

- Linkage analysis is a method that is used to decide if two loci, or a genetic marker (GM) and a disease gene, are linked :
  - Ascertain whether the recombination fraction  $\theta$  between the two loci deviates significantly from 0.5



# Linkage analysis – how?

1. Collect familie(s)
2. Choose a genetic marker (eg microsatellite, SNP) for linkage analysis
3. Genotype this marker in all individuals of the familie(s)
4. Identify informative meioses (R vs NR → between heterozygous GM and heterozygous disease locus)
  - Based on the phenotype you know the disease locus genotype (affected vs unaffected)
  - Is phase known?
5. Determine whether there is linkage between the GM locus and the disease locus
  - Determine recombination fraction  $\theta$

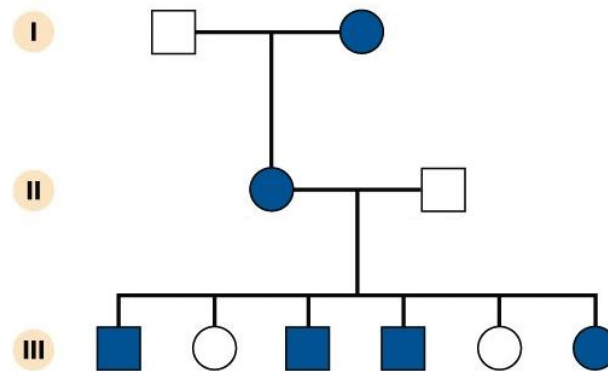
$$\log_{10} \left[ \frac{\text{Likelihood of linkage } (\theta)}{\text{Likelihood that loci are unlinked } \left(\theta = \frac{1}{2}\right)} \right] = \log_{10} \left[ \frac{L(\theta)}{L\left(\theta = \frac{1}{2}\right)} \right] = \log_{10} \left[ \frac{(1-\theta)^{NR} * \theta^R}{0.5^{(R+NR)}} \right] = \max$$

- Is this recombination significantly different from 0.5?  
(= null hypothesis; no linkage between GM and disease locus)

$$\log_{10} \left[ \frac{\text{Likelihood of linkage } (\theta)}{\text{Likelihood that loci are unlinked } \left(\theta = \frac{1}{2}\right)} \right] = \log_{10} \left[ \frac{L(\theta)}{L\left(\theta = \frac{1}{2}\right)} \right] = \log_{10} \left[ \frac{(1-\theta)^{NR} * \theta^R}{0.5^{(R+NR)}} \right] \geq 3 ?$$

6. Do we need more informative meioses / families?

# Collect families



# Linkage analysis – how?

1. Collect familie(s)
2. Choose a genetic marker (eg microsatellite, SNP) for linkage analysis
3. Genotype this marker in all individuals of the familie(s)
4. Identify informative meioses (R vs NR → between heterozygous GM and heterozygous disease locus)
  - Based on the phenotype you know the disease locus genotype (affected vs unaffected)
  - Is phase known?
5. Determine whether there is linkage between the GM locus and the disease locus
  - Determine recombination fraction  $\theta$

$$\log_{10} \left[ \frac{\text{Likelihood of linkage } (\theta)}{\text{Likelihood that loci are unlinked } \left(\theta = \frac{1}{2}\right)} \right] = \log_{10} \left[ \frac{L(\theta)}{L\left(\theta = \frac{1}{2}\right)} \right] = \log_{10} \left[ \frac{(1-\theta)^{NR} * \theta^R}{0.5^{(R+NR)}} \right] = \max$$

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6. Do we need more informative meioses / families?

# Linkage analysis: genetic markers

- Requirements
  - polymorphic
  - informative = high mean heterozygosity
- Types: RFLPs, microsatellites & SNPs
- Advantages
  - easy to detect
  - relatively inexpensive to test easily available material

# Linkage analysis – how?

1. Collect familie(s)
2. Choose a genetic marker (eg microsatellite, SNP) for linkage analysis
3. Genotype this marker in all individuals of the familie(s)
4. Identify informative meioses (R vs NR → between heterozygous GM and heterozygous disease locus)
  - Based on the phenotype you know the disease locus genotype (affected vs unaffected)
  - Is phase known?
5. Determine whether there is linkage between the GM locus and the disease locus
  - Determine recombination fraction  $\theta$

$$\log_{10} \left[ \frac{\text{Likelihood of linkage } (\theta)}{\text{Likelihood that loci are unlinked } \left(\theta = \frac{1}{2}\right)} \right] = \log_{10} \left[ \frac{L(\theta)}{L\left(\theta = \frac{1}{2}\right)} \right] = \log_{10} \left[ \frac{(1-\theta)^{NR} * \theta^R}{0.5^{(R+NR)}} \right] = \max$$

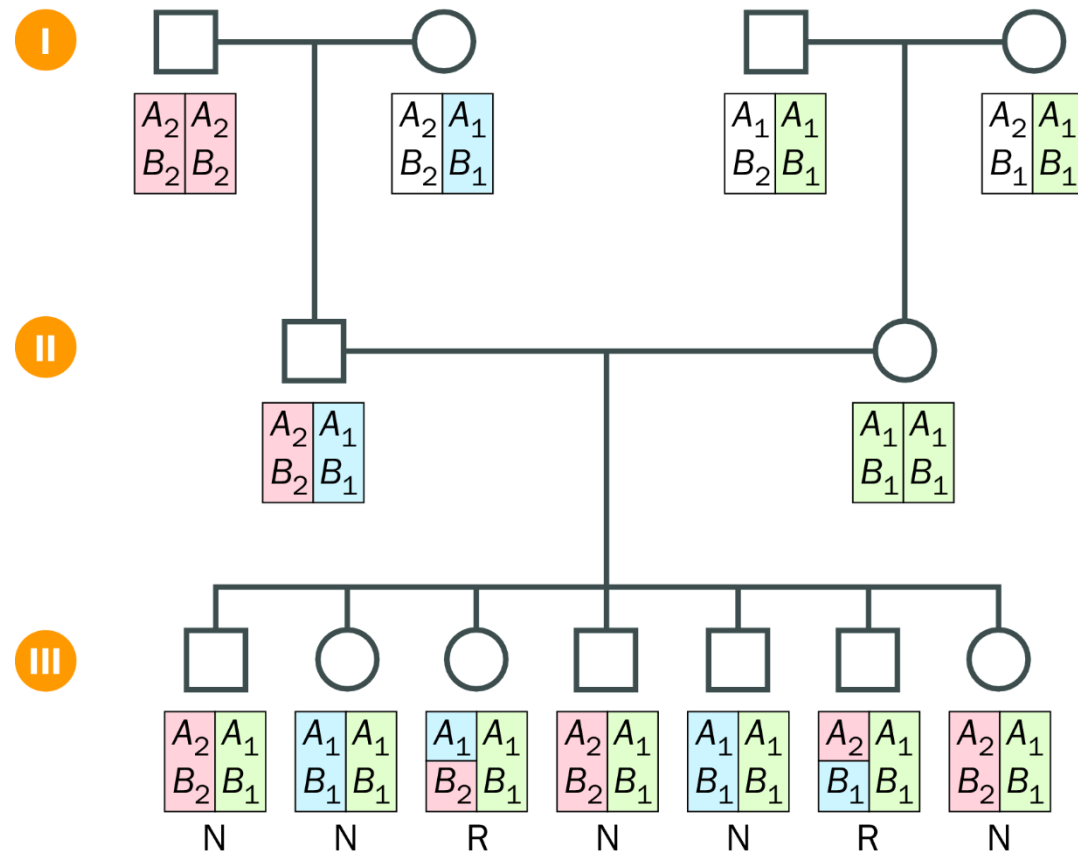
- Is this recombination significantly different from 0.5?  
(= null hypothesis; no linkage between GM and disease locus)

$$\log_{10} \left[ \frac{\text{Likelihood of linkage } (\theta)}{\text{Likelihood that loci are unlinked } \left(\theta = \frac{1}{2}\right)} \right] = \log_{10} \left[ \frac{L(\theta)}{L\left(\theta = \frac{1}{2}\right)} \right] = \log_{10} \left[ \frac{(1-\theta)^{NR} * \theta^R}{0.5^{(R+NR)}} \right] \geq 3 ?$$

6. Do we need more informative meioses / families?

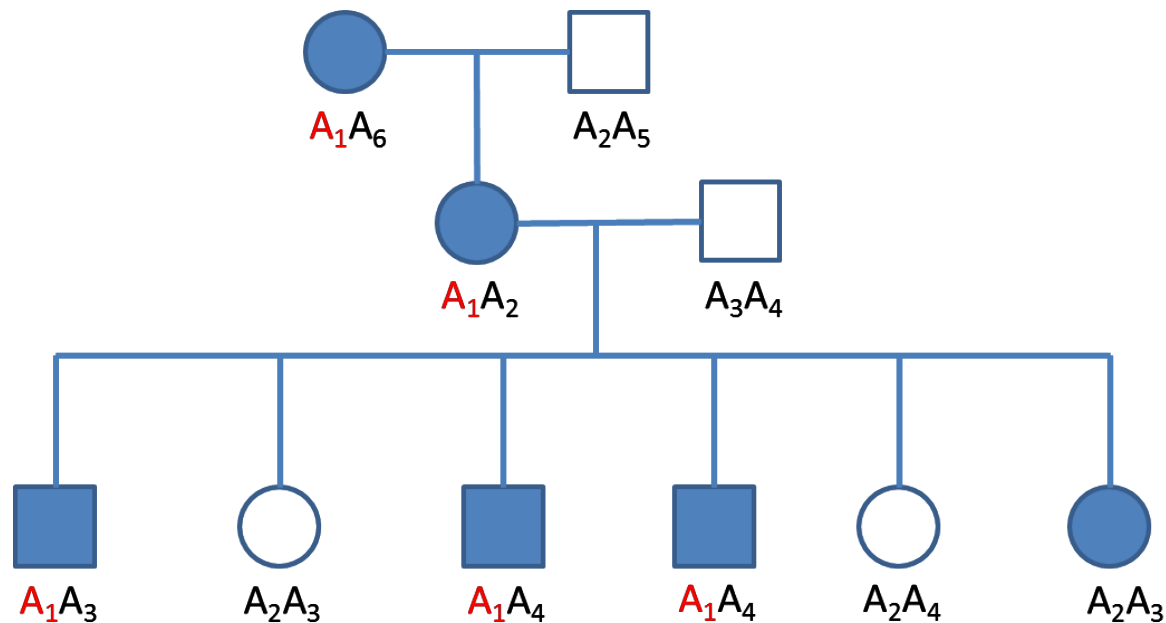


# Recombinants vs non-recombinants



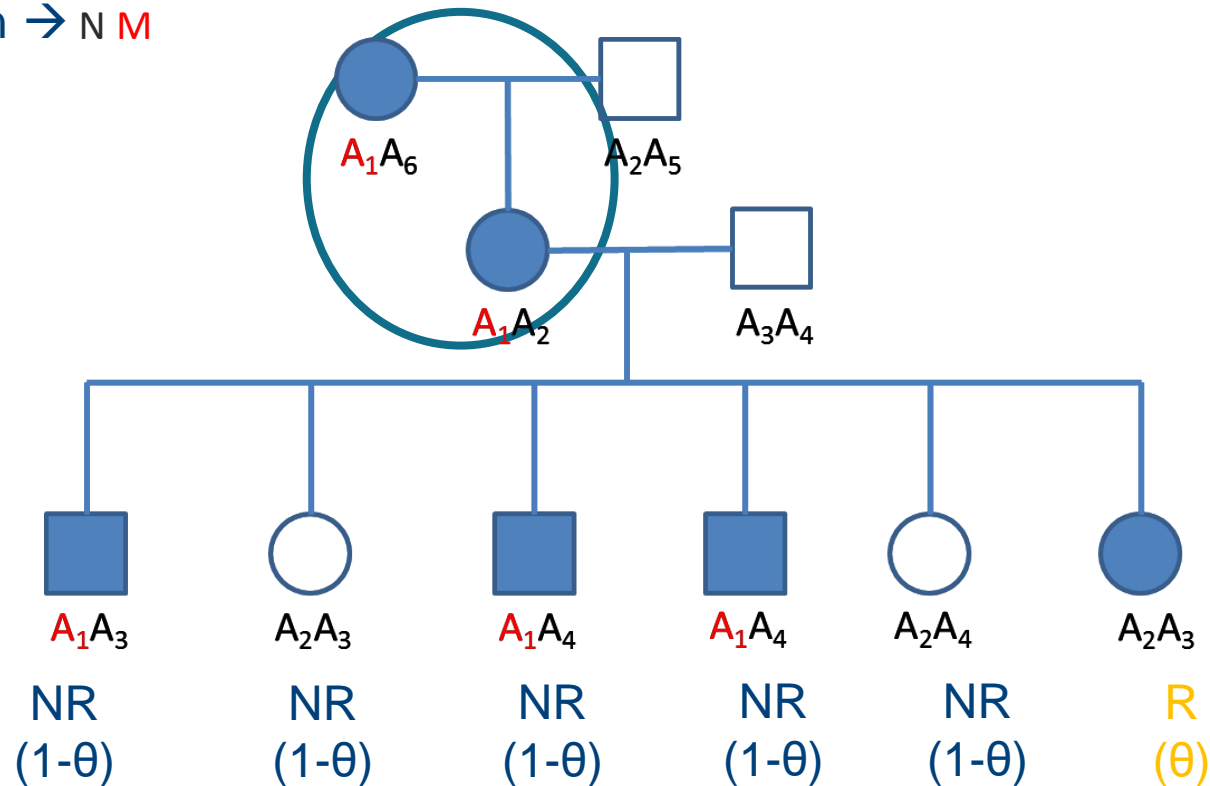
# Recombinants vs non-recombinants

Phase known?



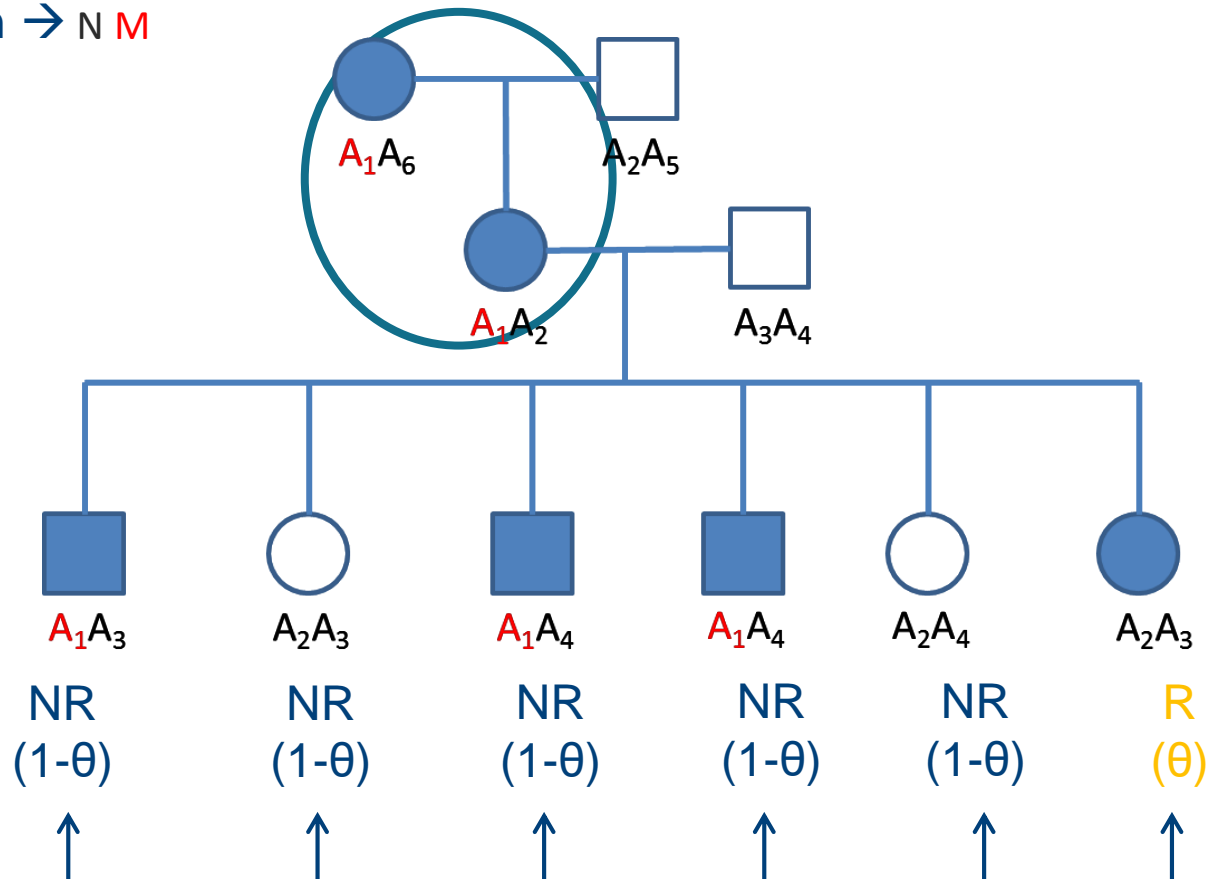
# Recombinants vs non-recombinants

Phase known  $\rightarrow$  N M



# Recombinants vs non-recombinants

Phase known  $\rightarrow$  N M

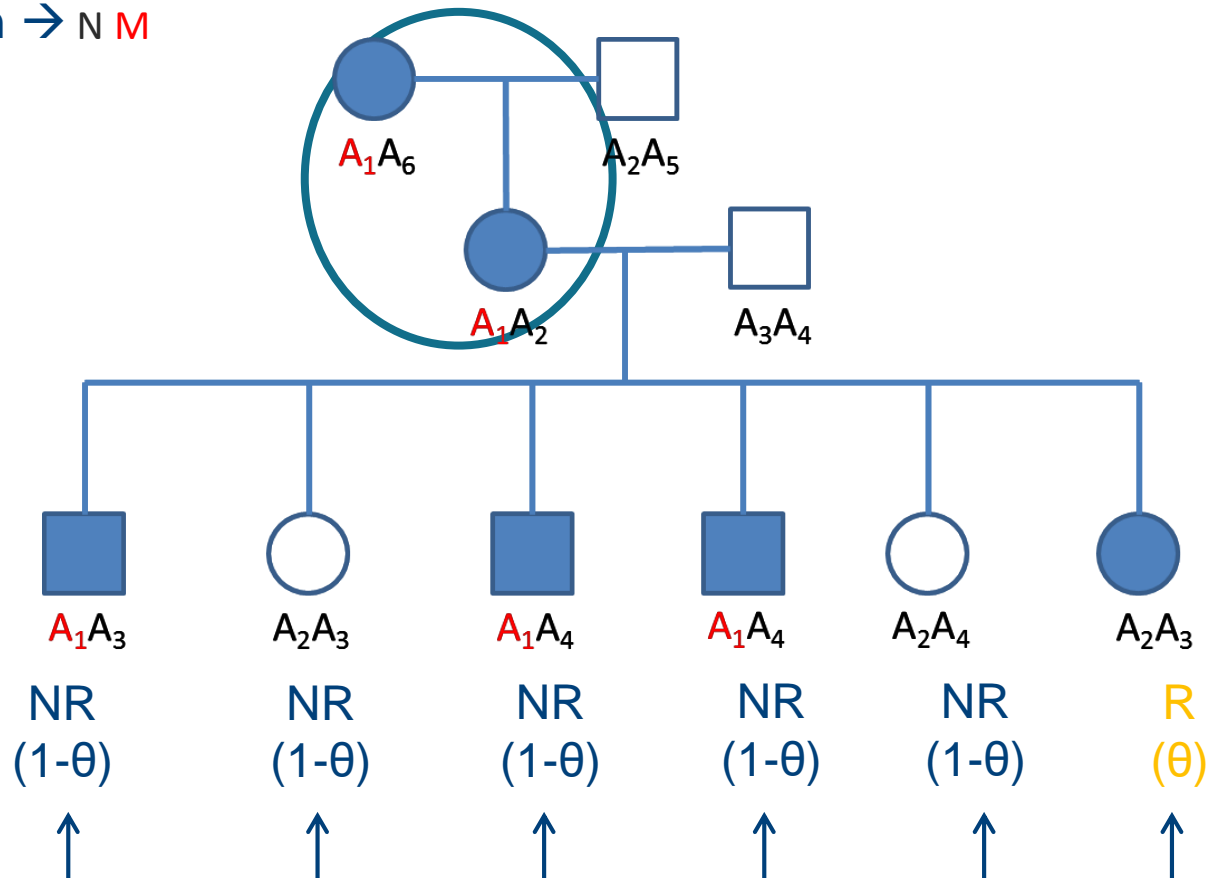


Chance for this observation when marker locus is **linked** with disease locus via  $\theta$ ?

$$L(\theta) = (1 - \theta)^5 * \theta^1$$

# Recombinants vs non-recombinants

Phase known  $\rightarrow$  N M



Chance for this observation when marker locus is **linked**/NOT linked with disease locus via  $\theta$ ?

$$L(\theta) = (1 - \theta)^5 * \theta^1$$


$$(1 - 0.5)^5 * 0.5 = 0.5^6$$


# Linkage analysis – LOD score

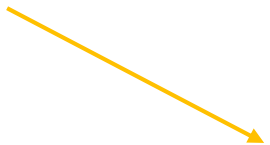
- $$\text{Odds} = \frac{\text{Likelihood of linkage } (\theta)}{\text{Likelihood that loci are unlinked } \left(\theta=\frac{1}{2}\right)} = \frac{L(\theta)}{L\left(\theta=\frac{1}{2}\right)} = \frac{(1-\theta)^5 * \theta^1}{0.5^6}$$
- $$\text{Logarithm of odds} = \text{LOD score } (Z) = \log_{10} \left[ \frac{L(\theta)}{L\left(\theta=\frac{1}{2}\right)} \right]$$

# Linkage analysis – LOD score

- $$\text{Odds} = \frac{\text{Likelihood of linkage } (\theta)}{\text{Likelihood that loci are unlinked } (\theta=\frac{1}{2})} = \frac{L(\theta)}{L(\theta=\frac{1}{2})} = \frac{(1-\theta)^5 * \theta^1}{0.5^6}$$

  $>1$

 What is most likely  $\theta$ ?
- $$\text{Logarithm of odds} = \text{LOD score } (Z) = \log_{10} \left[ \frac{L(\theta)}{L(\theta=\frac{1}{2})} \right]$$

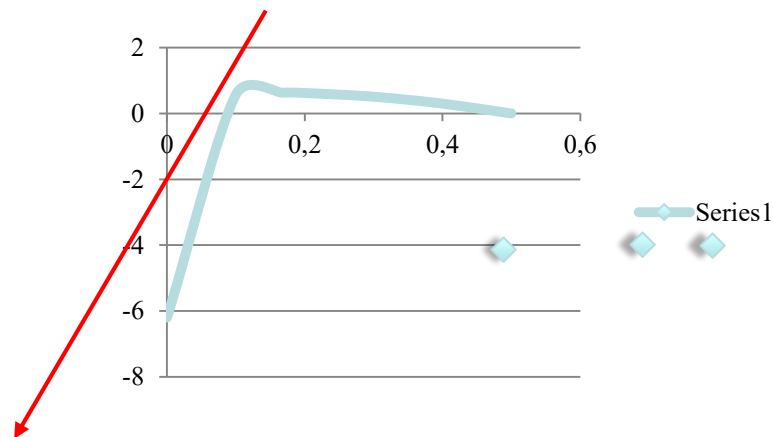
  $>0$

# Most likely $\theta$ ?

$$\log_{10} \left[ \frac{\theta^R \times (1-\theta)^{NR}}{0.5^{(R+NR)}} \right]$$

R = # rec. = 1  
NR = # non-rec. = 5


teta	0.00000001	0.1	0.16666667	0.2	0.3	0.4	0.5
lod score	-6.19382	0.57739252	0.63212249	0.6226599	0.50879143	0.29899622	0



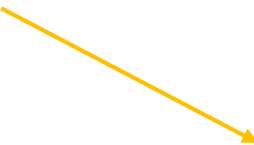
Is this significantly different from 0.5 ?



# Linkage analysis – LOD score

- $$\text{Odds} = \frac{\text{Likelihood of linkage } (\theta)}{\text{Likelihood that loci are unlinked } (\theta=\frac{1}{2})} = \frac{L(\theta)}{L(\theta=\frac{1}{2})} = \frac{(1-\theta)^5 * \theta^1}{0.5^6}$$


**>1**

- $$\text{Logarithm of odds} = \text{LOD score } (Z) = \log_{10} \left[ \frac{L(\theta)}{L(\theta=\frac{1}{2})} \right]$$


**>0 → ≥3 ?**

$Z=3.0$  threshold for accepting linkage with a 5% chance of a type1 error  
(falsely rejecting the null hypothesis)

Hypothesis	Loci are linked (recombination fraction = $\theta$ )	Loci are not linked (recombination fraction = 0.5)
Prior probability	1/50	49/50
Conditional likelihood: 1000:1 odds of linkage [lod score $Z(\theta) = 3.0$ ]	1000	1
Joint probability (prior $\times$ conditional)	20	$\sim 1$

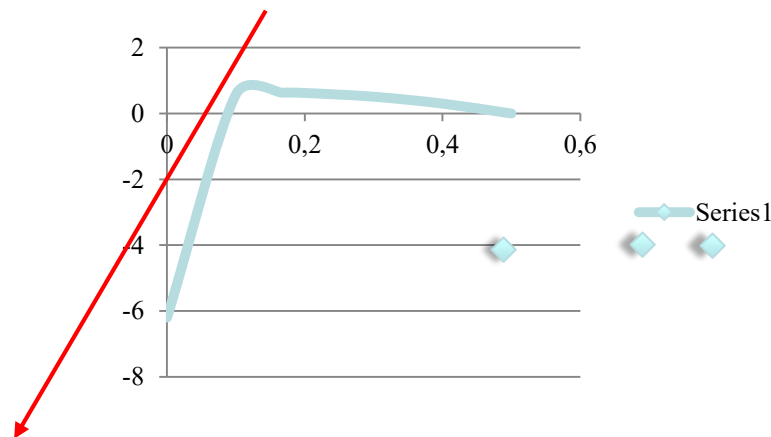
Box 14.3 Human Molecular Genetics, 4ed. (© Garland Science)

# Most likely $\theta$ ?

$$\log_{10} \left[ \frac{\theta^R \times (1-\theta)^{NR}}{0.5^{(R+NR)}} \right]$$

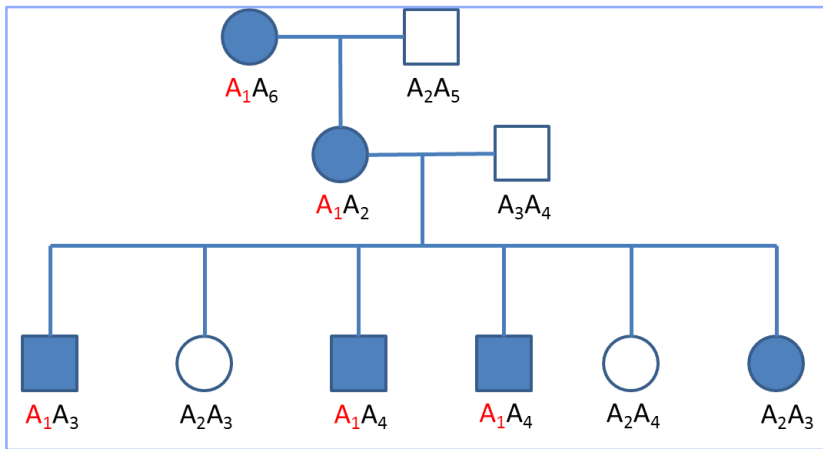
R = # rec. = 1  
NR = # non-rec. = 5

teta	0.00000001	0.1	0.16666667	0.2	0.3	0.4	0.5
lod score	-6.19382	0.57739252	0.63212249	0.6226599	0.50879143	0.29899622	0



Is this significantly different from 0.5 ?  $\rightarrow \geq 3$  ?

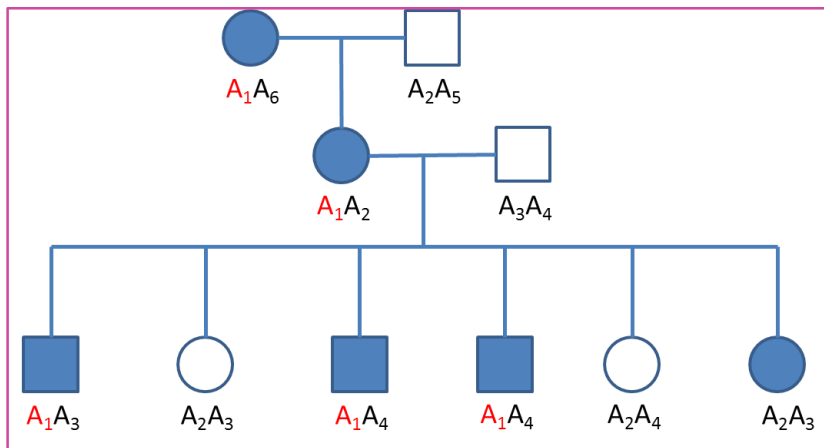
# More families...



$$\log_{10} \left[ \frac{\Theta^{(R1+R2)} \times (1-\Theta)^{(NR1+NR2)}}{0.5^{(R1+NR1)+(R2+NR2)}} \right]$$

**Family 1**  
 R1 = # rec.  
 NR1 = # non-rec.

**Family 2**  
 R2 = # rec.  
 NR2 = # non-rec.



$$\log_{10} \left[ \frac{\Theta^{R1} \times (1-\Theta)^{NR1}}{0.5^{(R1+NR1)}} \right]$$

$$+ \log_{10} \left[ \frac{\Theta^{R2} \times (1-\Theta)^{NR2}}{0.5^{(R2+NR2)}} \right]$$

---

SUM ≥ 3 ?

# Potential LOD score curves

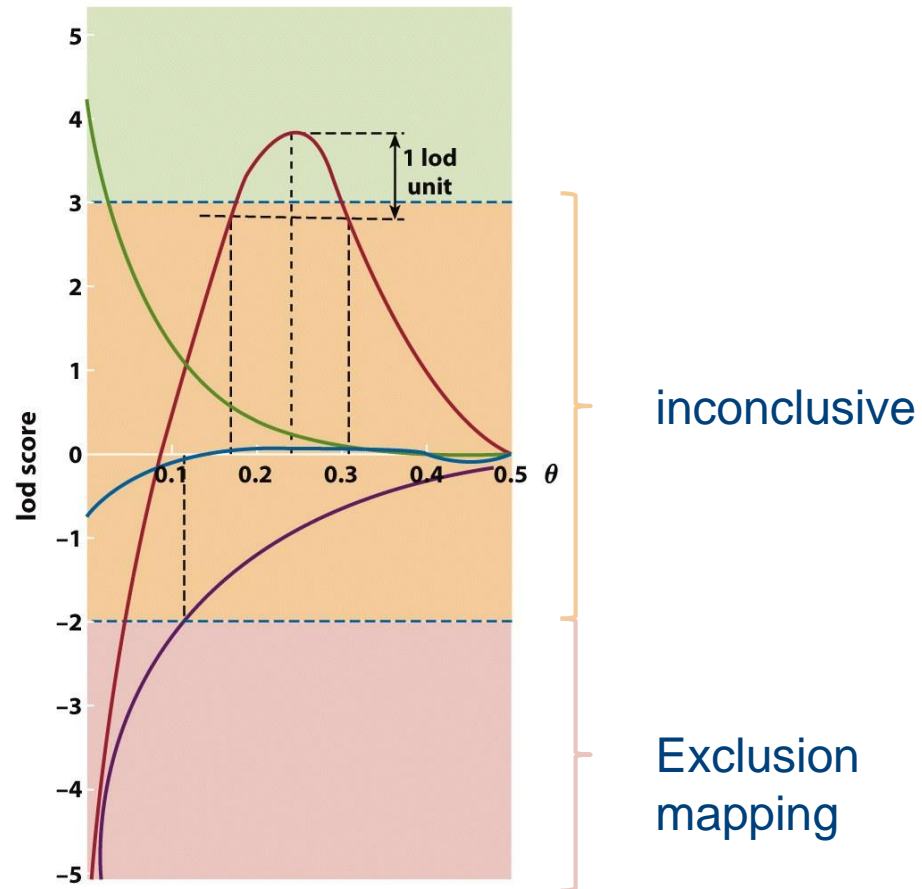
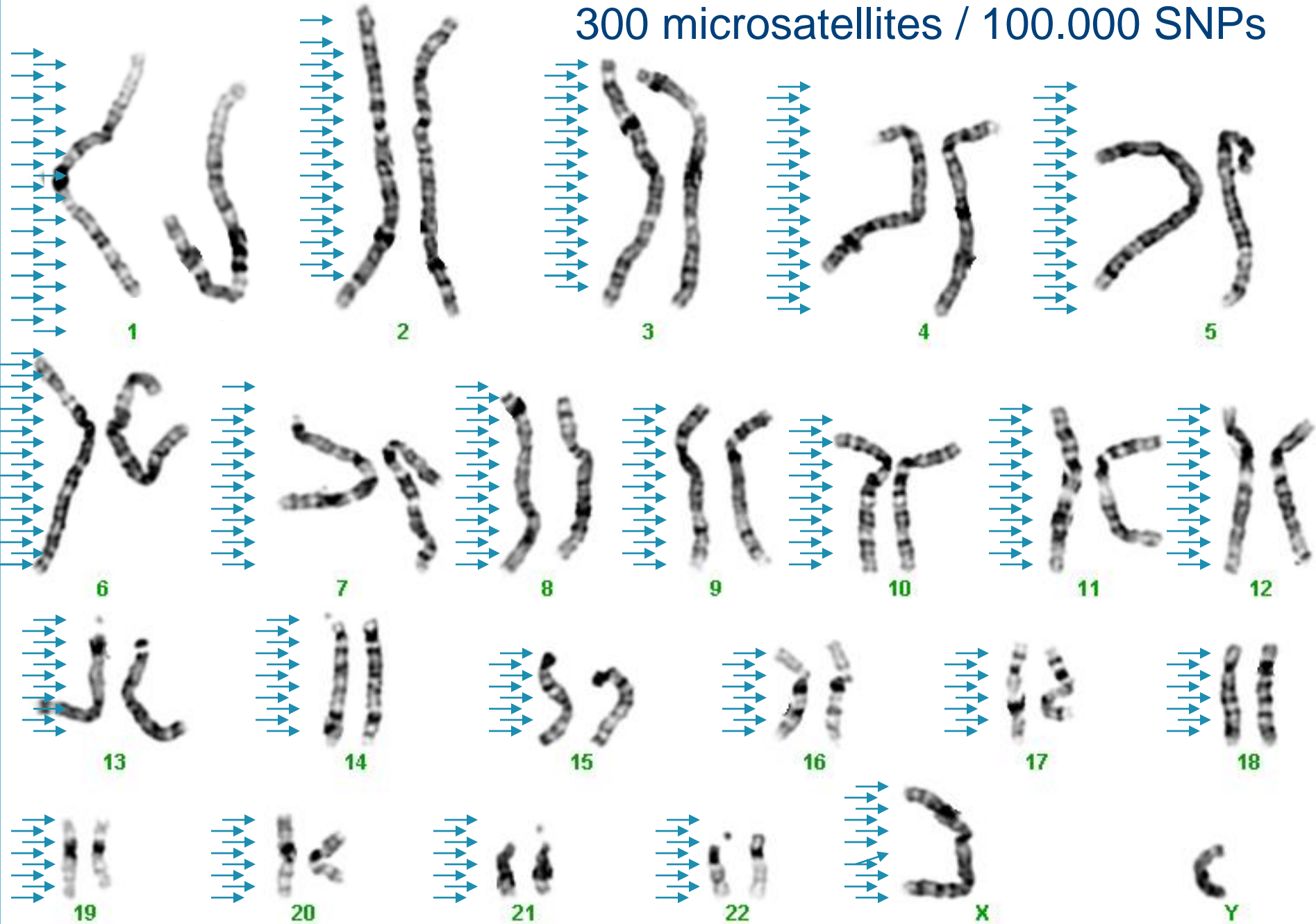
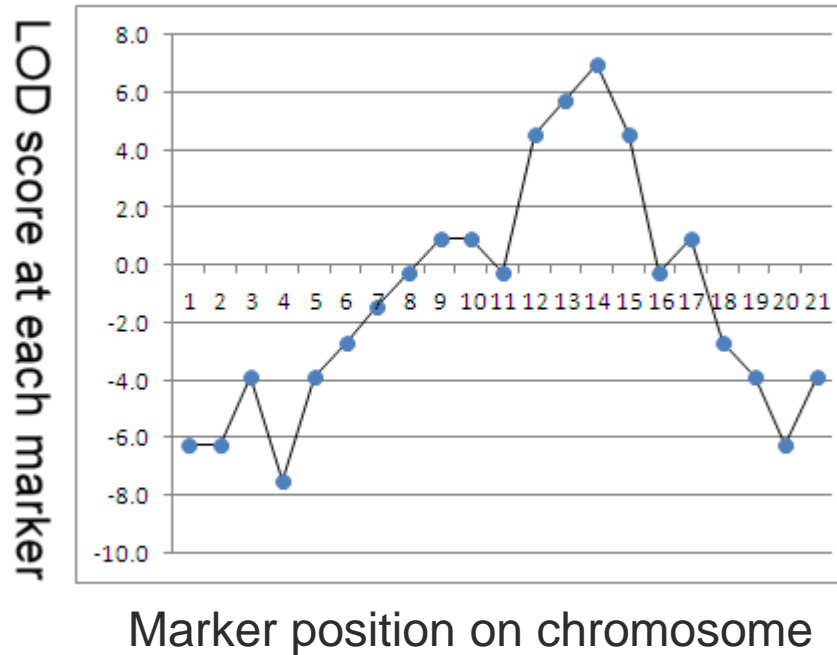


Figure 14.10 Human Molecular Genetics, 4ed. (© Garland Science)

300 microsatellites / 100.000 SNPs

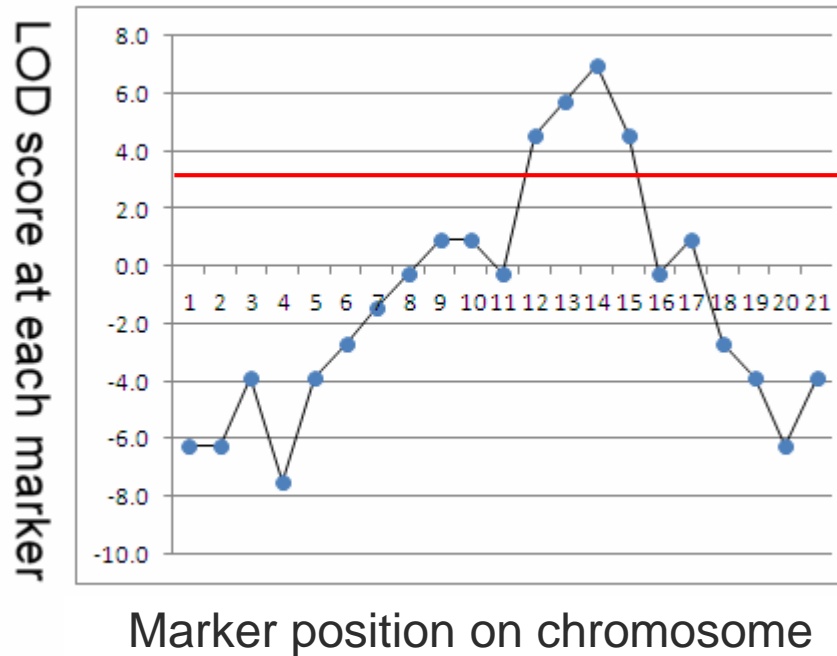


# LOD score - visualization



- $\theta$  between genetic markers & disease locus
  - LOD score plotted against chromosomal positions
  - highest peak = most likely locus

# LOD score - visualization



- $\theta$  between genetic markers & disease locus
  - LOD score plotted against chromosomal positions
  - highest peak = most likely locus

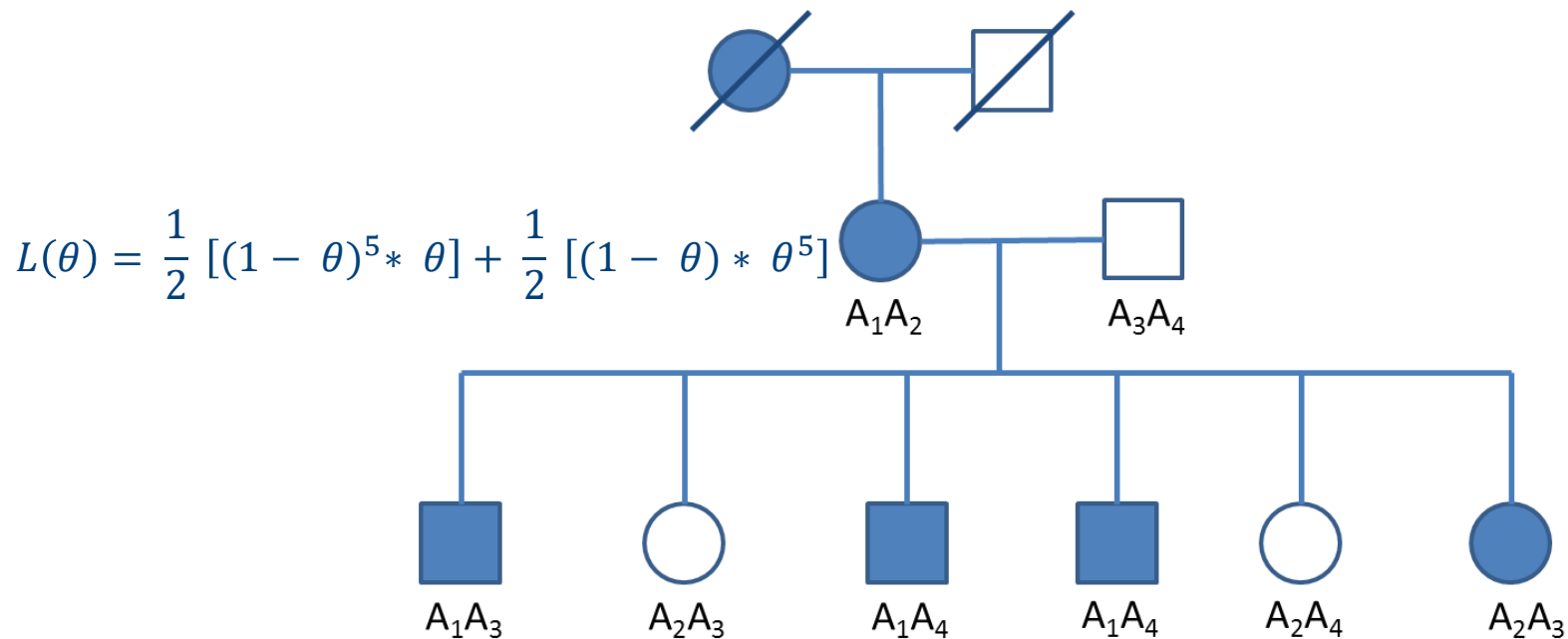
LOD score = 3

- $1 / 10^3$  chance that the observed concordance is due to chance



# Recombinants vs non-recombinants

Phase unknown



# Linkage analysis – how?

1. Collect familie(s)
2. Choose a genetic marker (eg microsatellite, SNP) for linkage analysis
3. Genotype this marker in all individuals of the familie(s)
4. Identify informative meioses (R vs NR → between heterozygous GM and heterozygous disease locus)
  - Based on the phenotype you know the disease locus genotype (affected vs unaffected)
  - Is phase known?
5. Determine whether there is linkage between the GM locus and the disease locus
  - Determine recombination fraction  $\theta$

$$\log_{10} \left[ \frac{\text{Likelihood of linkage } (\theta)}{\text{Likelihood that loci are unlinked } (\theta=\frac{1}{2})} \right] = \log_{10} \left[ \frac{L(\theta)}{L(\theta=\frac{1}{2})} \right] = \log_{10} \left[ \frac{(1-\theta)^{NR} * \theta^R}{0.5^{(R+NR)}} \right] = \max$$

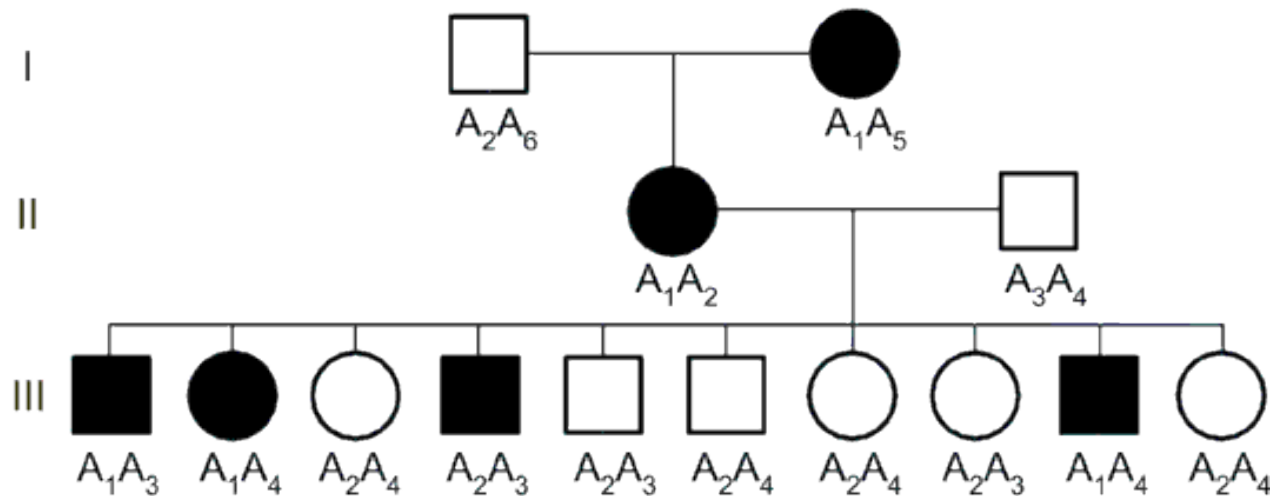
- Is this recombination significantly different from 0.5?  
(= null hypothesis; no linkage between GM and disease locus)

$$\log_{10} \left[ \frac{\text{Likelihood of linkage } (\theta)}{\text{Likelihood that loci are unlinked } (\theta=\frac{1}{2})} \right] = \log_{10} \left[ \frac{L(\theta)}{L(\theta=\frac{1}{2})} \right] = \log_{10} \left[ \frac{(1-\theta)^{NR} * \theta^R}{0.5^{(R+NR)}} \right] \geq 3 ?$$

6. Do we need more informative meioses / families?

# Linkage analysis – homework

## → assignment 2

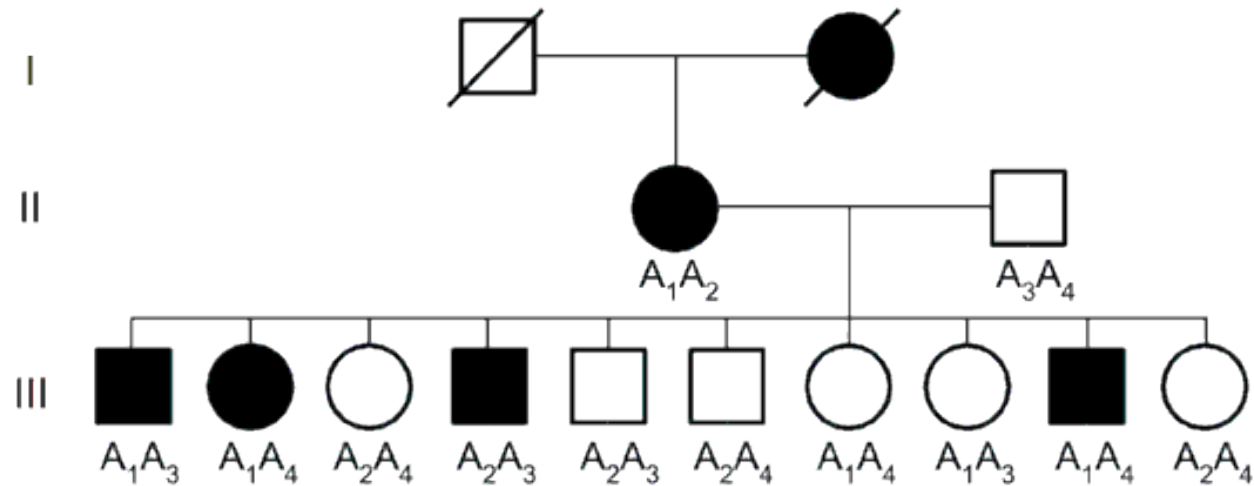


$\theta = ?$

LOD = ?

# Linkage analysis – homework

## → assignment 2

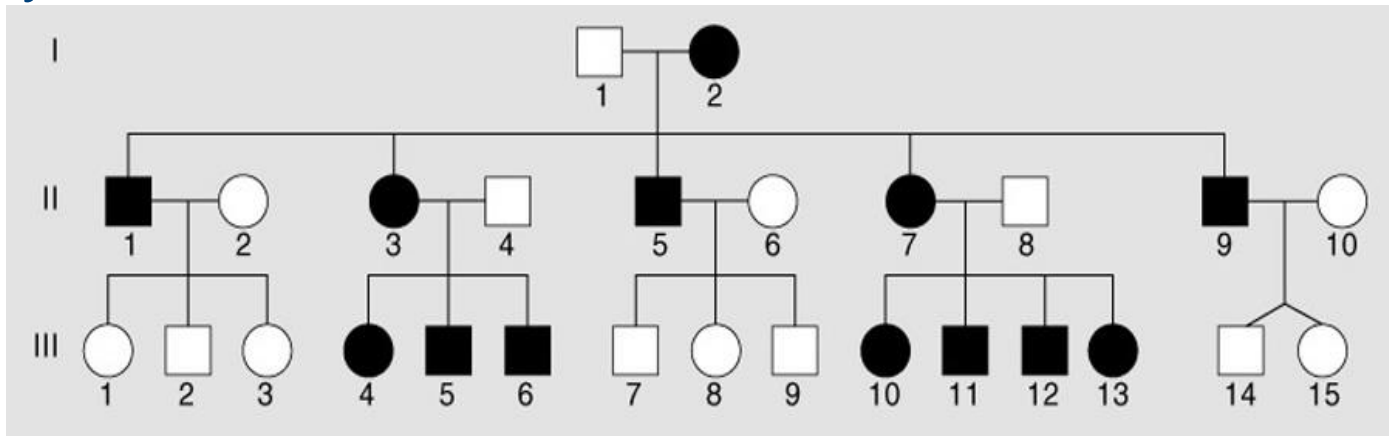


$\theta = ?$

LOD = ?

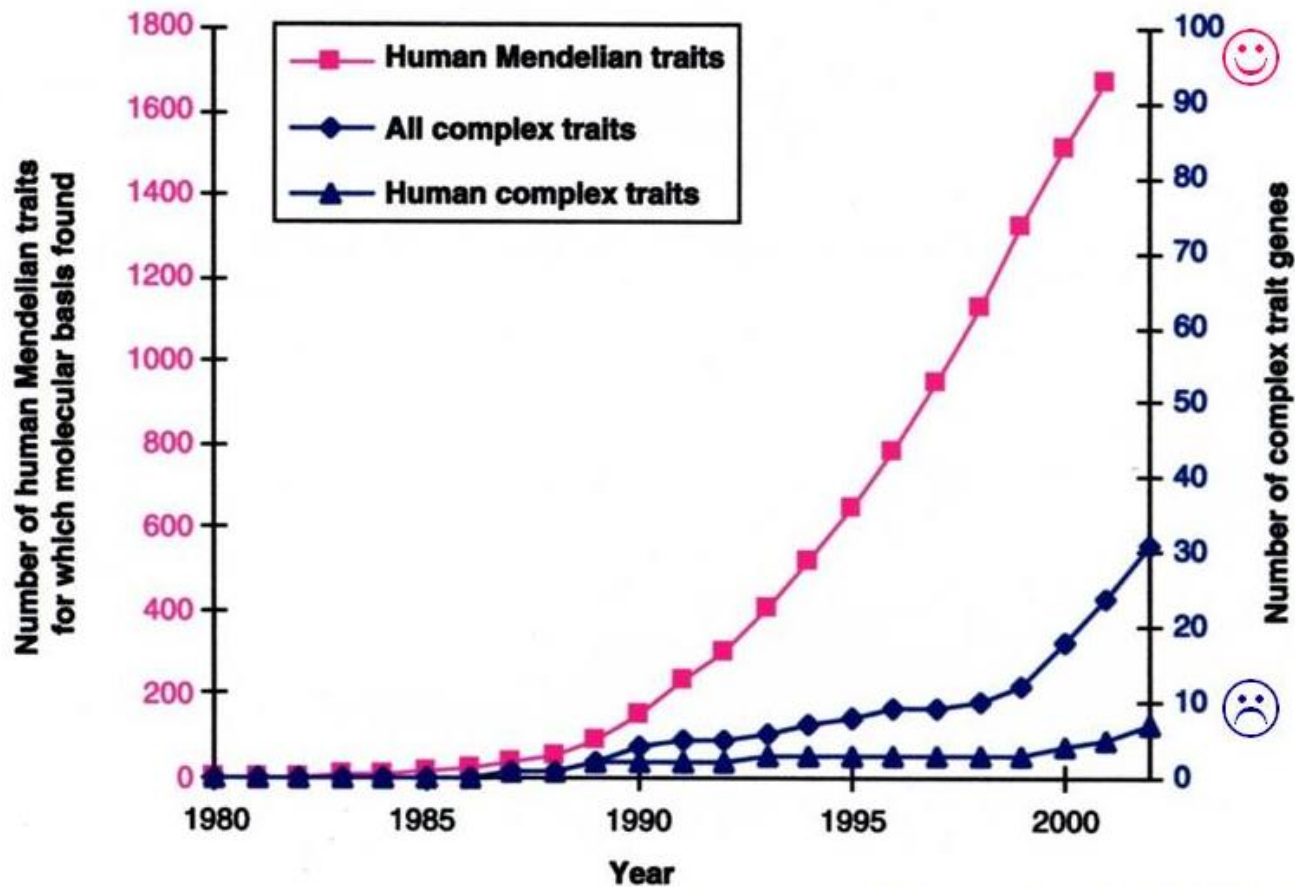
# Linkage analysis

- co-segregation of genetic marker(s) and disease in a family

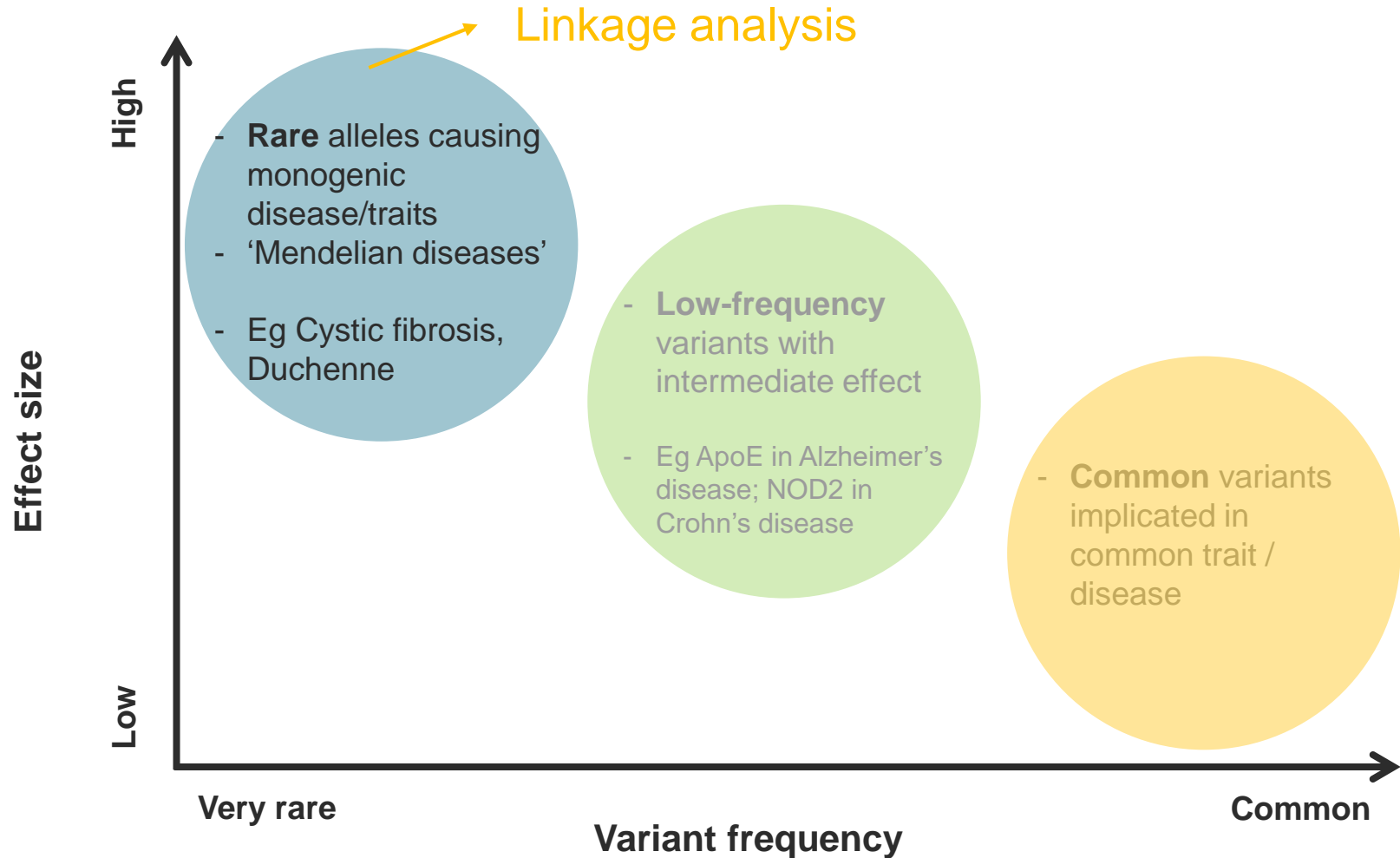


- Goal: identify chromosomal region with risk gene
- Limits :
  - good for detection of **highly penetrant** variant (ie extremely likely to cause the disease when present)
  - Hard to get big enough pedigrees with enough informative individuals

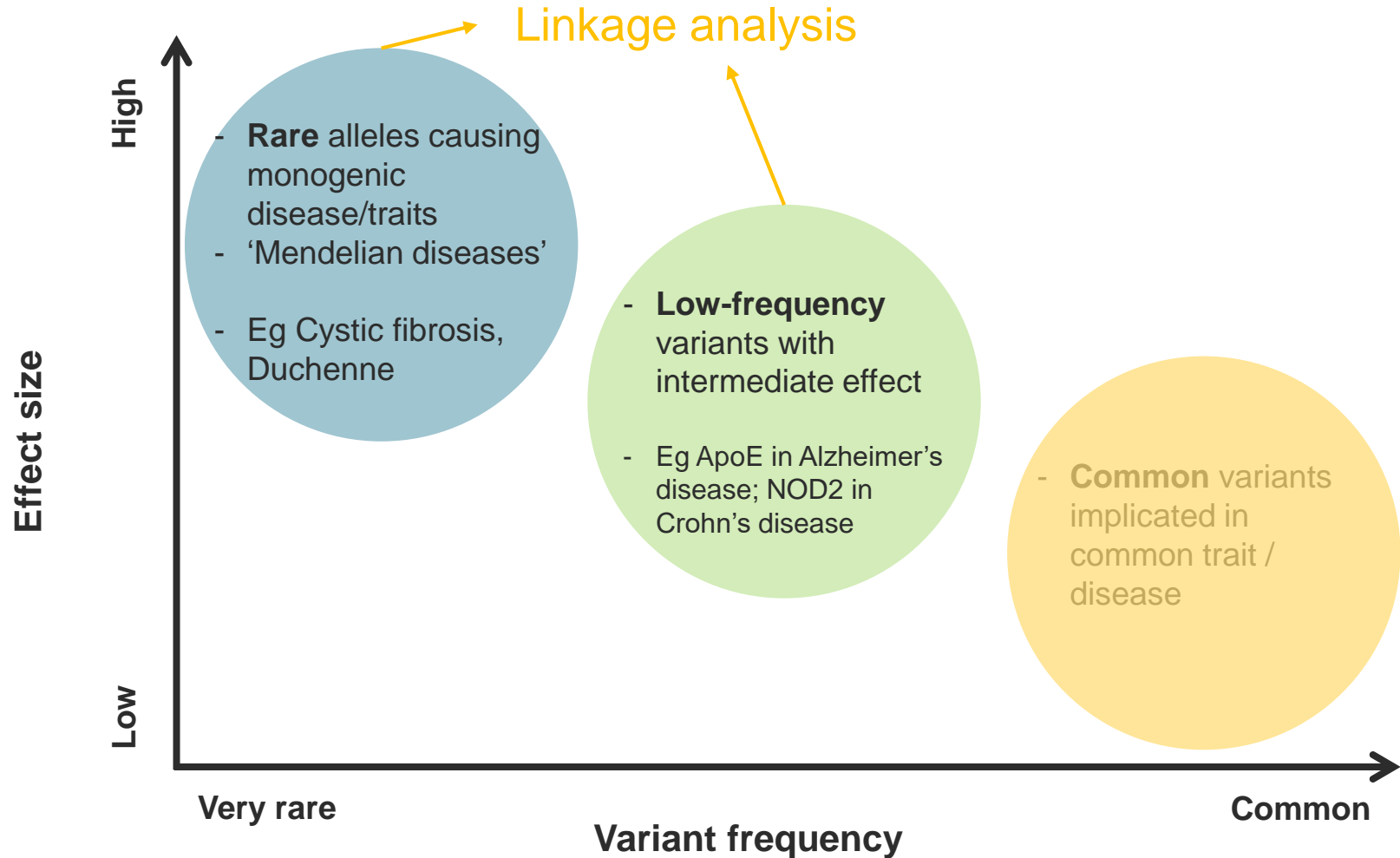
# Genetic successes in Mendelian >< complex disorders



# The genetic spectrum



# The genetic spectrum





# The genetic spectrum

